

# Spectroscopy of selected metal-containing diatomic molecules

by

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# Abstract

Fourier transform infrared emission spectra of MnH and MnD were observed in the ground  $X^7\Sigma^+$  electronic state. The vibration-rotation bands from  $v = 1 \rightarrow 0$  to  $v = 3 \rightarrow 2$  for MnH, and from  $v = 1 \rightarrow 0$  to  $v = 4 \rightarrow 3$  for MnD were recorded at an instrumental resolution of  $0.0085\text{ cm}^{-1}$ . Spectroscopic constants were determined for each vibrational level and equilibrium constants were found from a Dunham-type fit. The equilibrium vibrational constant  $\omega_e$  for MnH was found to be  $1546.84518(65)\text{ cm}^{-1}$ , the equilibrium rotational constant  $B_e$  was found to be  $5.6856789(103)\text{ cm}^{-1}$  and the equilibrium bond distance  $r_e$  was determined to be  $1.7308601(47)\text{ \AA}$ .

New high resolution emission spectra of CoH and CoD molecules have been recorded in the  $640\text{ nm}$  to  $3.5\text{ }\mu\text{m}$  region using a Fourier transform spectrometer. Many bands were observed for the  $A'^3\Phi - X^3\Phi$  electronic transition of CoH and CoD. In addition, a new [13.3]4 electronic state was found by observing the [13.3]4 –  $X^3\Phi_3$  and [13.3]4 –  $X^3\Phi_4$  transitions in the spectrum of CoD. Analysis of the transitions with  $\Delta\Omega = 0, \pm 1$  provided more accurate values of spin-orbit splittings between  $\Omega = 4$  and  $\Omega = 3$  components. The ground state for both molecules was fitted both to band and Dunham-type constants. The estimated band constants of the perturbed upper states were also obtained.

The emission spectrum of gas-phase YbO has been investigated using a Fourier transform spectrometer. A total of 8 red-degraded bands in the range  $9\,800 - 11\,300\text{ cm}^{-1}$  were recorded at a resolution of  $0.04\text{ cm}^{-1}$ . Because of the multiple isotopomers present in the spectra, only 3 bands were rotationally analyzed. Perturbations were identified in two of these bands and all 3 transitions were found to terminate at the  $X^1\Sigma^+$  ground electronic state. The electronic configurations that give rise to the observed states are discussed and molecular parameters for all of the analyzed bands are reported.

Electronic spectra of the previously unobserved EuH and EuD molecules were studied by means of Fourier transform spectroscopy and laser-induced fluorescence. The extreme complexity of these transitions made rotational assignments of EuH bands impossible. However, the spin-spin interaction constant,  $\lambda$ , and Fermi contact parameter,  $b_F$ , in the ground  $X^9\Sigma^-$  electronic state were estimated for the  $^{151}\text{EuH}$  and  $^{153}\text{EuH}$  isotopologues.

Electronic spectra of SmH, SmCl, TmH and ErF molecules were recorded for the first time using Fourier transform spectrometer. The poor signal to noise ratio of the observed bands coupled with their complexity prevented a rotational analysis. The electronic states that may be involved in the observed transitions are discussed.

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## Dedication

To my parents

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# Chapter 1

## Introduction and motivation

High resolution spectroscopy is one of the fundamental experimental tools of chemical physics. From the analysis of molecular spectra one can obtain detailed information about the bonding, structure, and interactions in the molecules as well as properties of their physical environment. This thesis concentrates on the spectroscopic studies of metal-containing diatomic molecules in the gas phase in order to gain a better understanding of their structural, electronic and bonding properties.

Metal-containing molecules are important in a variety of scientific areas such as chemical catalysis (including hydrogenation), metallurgy, astrophysics, high-density fuel research and even protein biology [1]. The study of the electronic structure of small molecules containing a metal atom is an interesting area of chemical physics, because these species can serve as models for more complicated systems.

### 1.1 Transition metal hydrides

The first two molecules described in this thesis are first row transition metal hydrides: MnH and CoH and their isotopologues. Diatomic molecules containing transition metal atoms have important applications. For example first row transition metal oxides such as TiO and VO are important in astrophysics because their spectra are used to classify cool stars [2]. Transition metal hydrides are also expected to be present in various stars and nebulae, and in the interstellar medium. Some of these hydrides have already been detected in the spectra of extraterrestrial objects. Lambert and Mallia [3] tentatively observed the NiH molecule in the spectra of sunspots. CrH was also observed in the spectra of sunspots [4], while

spectra of FeH [5, 6] and perhaps TiH [7] were identified in M-type stars. The spectrum of CoH is also expected to be found in sunspots, since the solar abundance of cobalt is just one order of magnitude less than that of chromium [8]. Transition metal monohydrides are also important because they represent the simplest metal-hydrogen bond, and their studies provide a starting point for research on gas-surface interactions and catalytic processes.

Although the electronic spectra of many first row transition metal hydrides have been known for decades not all of them have been fully interpreted. The reason is that the open  $d$ -shells of these metals give rise to a large number of low-lying excited electronic states with large spin and orbital angular momenta. These states lie close to each other, which results in perturbations of the rotational levels, making the spectra hard to assign. The complex symmetry of the electronic states (due to the metals' unpaired  $d$  electrons) also complicates the spectra. For example, the ground states of the molecules studied in this thesis are  $^7\Sigma^+$  for MnH, arising from the  $3d^54s$  configuration of  $\text{Mn}^+$  ion, and  $^3\Phi_i$  for CoH (see further discussion below). The most recent review of experimental data for the ground states of transition metal monohydrides was completed by Bernath in 2000 [9].

The electronic structure of the first row transition metal monohydrides can be explained using a simple qualitative valence molecular orbital diagram (Figure 1.1) [9]. The  $1\sigma$  orbital is always bonding and formed by the interaction of the ( $s + p$ )-metal hybrid orbital with the hydrogen  $1s$  orbital [10]. The  $2\sigma$  orbital is predominantly an ( $s - p$ )-metal non-bonding orbital which is located on the side of metal atom away from the partially negatively-charged hydrogen. The  $1\delta$ ,  $1\pi$  and  $3\sigma$  orbitals are nearly pure metal  $3d$  non-bonding orbitals. The ionicity of the ground states of metal hydrides is generally  $\text{M}^{\delta+}-\text{H}^{\delta-}$ . The ground states are derived by adding to the molecular orbitals of MH the valence electrons of the metal and hydrogen.

The MnH molecule has 8 valence electrons; they are distributed among the molecular orbitals to maximize the total spin, except for the bonding  $1\sigma$  orbital that has two electrons. The ground electron configuration of MnH is therefore  $1\sigma^22\sigma^13\sigma^11\delta^21\pi^2$  [11]. The  $1\sigma$  bonding orbital is a Mn  $4s-\text{H } 1s$  combination, the  $2\sigma$  non-bonding orbital is a Mn  $4s-4p$  hybrid orbital, while the  $1\delta$ ,  $1\pi$  and  $3\sigma$  orbitals are metal  $3d$  non-bonding orbitals. CoH molecule has two additional electrons (10 valence electrons) as compared to MnH; they are added to the low-lying  $2\sigma$  and  $1\delta$  orbitals, and the  $3\sigma$  electron shifts to the  $1\pi$  orbital. The ground  $^3\Phi_i$  electronic state of CoH is derived from the  $1\sigma^22\sigma^21\delta^31\pi^3$  configuration.

*Ab initio* calculations are in many ways ahead of the experiments, and large basis sets are available for transition metal atoms for performing such calculations.

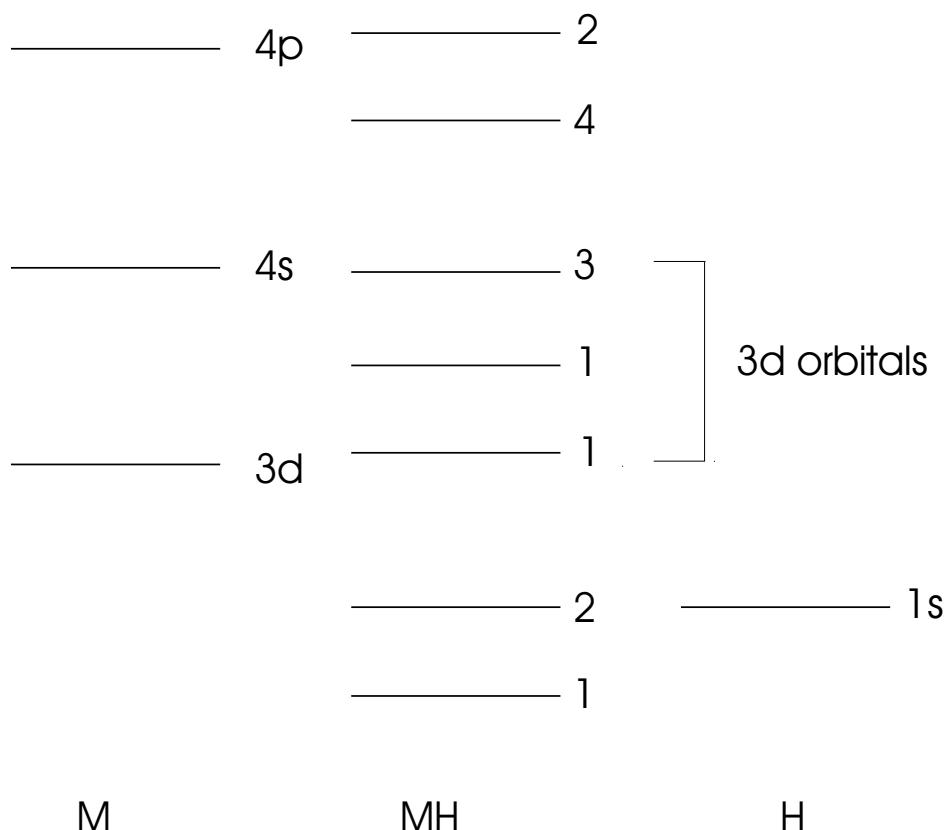


Figure 1.1: Molecular orbital diagram for the 3d-transition metal monohydrides.

The pioneering work to predict the properties of the low-lying electronic states of the transition metals are those of Chong *et al.* [12], for the first row (ScH to ZnH), and Langhoff *et al.* [13] and Balasubramanian [14], for the second row (YH to CdH). *Ab initio* calculations for the third row transition metal hydrides are more difficult because of the necessity to include the effects of spin-orbit coupling, but Balasubramanian has also completed calculations for 5d metal hydrides [14].

The literature overview of the spectroscopic work on MnH and CoH is given in Chapters 4 and 5.

## 1.2 Lanthanide-containing molecules

Studies of molecules that contain lanthanide metal atoms are motivated by their use in semiconductors [15, 16], magnetic [16, 17] and laser materials [16], hydrogen storage materials [18] and many other applications [16]. Astrophysical interest in these molecules has not developed yet, as the only lanthanide-containing molecule found in the spectra of astronomical objects is CeO, which was observed in the spectra of S stars by Wyckoff and Weninger [19]. However, the laboratory spectra of rare-earth metal-containing molecules, against which astrophysicists can compare their spectra, are limited, and some of the unidentified bands in the spectra of stars could be due to these molecules.

The experimental information for the lanthanide-containing molecules is limited for many reasons. The first obstacle is the price of the rare-earth metals (for instance the price of the Tm metal is about \$65 (US) per gram, depending on the supplier). Fortunately for the experiments in this thesis, we have been able to take advantage of the moderate prices provided to us by the HEFA Rare Earth Canada Company. Secondly, the high reactivity of the rare earth metals, together with their low vapor pressures at the temperatures that can be achieved by conventional methods, make the creation of these molecules in the gas phase a major challenge.

The difficulty in interpretation of the observed spectra is similar to that of spectra of molecules containing  $3d$  transition metal atoms. The lanthanide metal atoms and ions possess a large number of unpaired electrons in  $4f$  orbitals, which results in many low-lying electronic states with complex structure. The high density of states produces perturbations and band overlaps in the observed spectra. Additional obstacles that complicate the spectra are the relatively small rotational constants (due to heavy atoms of lanthanide elements), the large numbers of isotopes for many rare earth metals, and the hyperfine structure due to large nuclear spins of some of these isotopes.

The majority of the available spectroscopic studies of lanthanide-containing molecules in the gas phase concentrate on lanthanide oxides such as CeO [20], PrO [21], NdO [22, 23], SmO [24], EuO [25], GdO [26, 27], TbO [28], DyO [28], HoO [28, 29], ErO [30], YbO (see Chapter 6 and references therein) and LuO [31]. A new electronic emission spectrum of YbO is discussed in Chapter 6 of this thesis.

The lanthanide metal halides were studied less extensively, but experimental data on YbCl [32], YbF [33], DyF [34], HoF [35], HoCl [36] and CeF [37] are available. This thesis reports the first observations of the electronic spectra of ErF and SmCl (Chapter 8).

The lanthanide metal hydrides are studied the least and so far only experiments on YbH and LuH have been reported. The literature survey of the experimental and theoretical work on rare earth metal hydrides is given in Chapter 7. The spectra of EuH, SmH and TmH were observed in this work for the first time and these observations are reported in Chapters 7 and 8.

*Ab initio* calculations for lanthanide-containing molecules are very difficult because one has to account for relativistic and correlation effects. Nevertheless, pseudopotential or effective core potential approaches have recently been developed (see Ref. [38] and references therein). Density functional calculations had also been tried for the lanthanide oxides [39]. Semiempirical approaches and particularly ligand field theory (LFT) have proved to be useful in predicting the spectral properties of lanthanide oxides [40, 41] and halides [42]. This theory predicts the energy and ordering of molecular electronic states that arise from perturbation of the lanthanide ionic states by a negatively charged ligand.

One of the main goals of our experiments on lanthanide-containing molecules is to aid the development of the theoretical calculations for such molecules, and in particular to provide theoreticians with reference data for comparison with their calculations.

# Bibliography

- [1] L. Moran, K. Scrimgeour, H. Horton, R. Ochs, and J. Rawn, *Biochemistry*, Prentice-Hall, Engelwood Cliffs, NJ, 2nd edition, 1994.
- [2] N. M. White and R. F. Wing, *Astrophys. J.* **222**, 209 (1978).
- [3] D. L. Lambert and E. A. Mallia, *Mon. Not. R. Astron. Soc. London* **151**, 437 (1971).
- [4] O. Engvold, H. Wöhl, and J. W. Brault, *Astron. Astrophys. Supp. Series* **42**, 209 (1980).
- [5] B. Lindgren and G. Olofsson, *Astron. Astrophys.* **84**, 300 (1980).
- [6] P. K. Carroll, P. McCormack, and S. O'Connor, *Astrophys. J.* **208**, 903 (1976).
- [7] R. Yerle, *Astron. Astrophys.* **73**, 346 (1979).
- [8] S. P. Beaton, K. Evenson, and J. M. Brown, *J. Mol. Spectrosc.* **164**, 395 (1994).
- [9] P. Bernath, Transition metal monohydrides, in *Advances in Metal and Semiconductor Clusters*, vol. 5, edited by M. Duncan, Elsevier, 2000.
- [10] S. Walch and C. Bauschlicher Jr., *J. Chem. Phys.* **78**, 4597 (1983).
- [11] S. Langhoff, C. Bauschlicher Jr, and A. Rendell, *J. Mol. Spectrosc.* **138**, 108 (1989).
- [12] D. Chong, S. Langhoff, C. Bauschlicher Jr, S. Walch, and H. Partridge, *J. Chem. Phys.* **85**, 2850 (1986).
- [13] S. Langhoff, L. G. M. Pettersson, C. Bauschlicher, and H. Partridge, *J. Chem. Phys.* **86**, 268 (1987).

- [14] K. Balasubramanian, J. Chem. Phys. **93**, 8061 (1990).
- [15] P. Vaida and J. N. Daou, Phys. Rev. B **49**, 3275 (1994).
- [16] <http://www.americanelements.com>.
- [17] W. Bauhofer, W. Joss, R. K. Kremer, H. J. Mattausch, and A. Simon, J. Magn. Mater. **104**, 1243 (1992).
- [18] C. Rao and J. Gopalkrishnan, *New Directions in Solid State Chemistry*, CUP, London, 3rd edition, 1986.
- [19] S. Wyckoff and P. A. Wehinger, Astrophys. J. **212**, L139 (1977).
- [20] C. Linton et al., J. Mol. Spectrosc. **102**, 441 (1983).
- [21] M. Dulick and R. W. Field, J. Mol. Spectrosc. **113**, 105 (1985).
- [22] C. Linton et al., J. Mol. Spectrosc. **225**, 132 (2004).
- [23] C. Effantin, A. Bernard, P. Crozet, A. J. Ross, and J. D'Incan, J. Mol. Spectrosc. **231**, 154 (2005).
- [24] B. Guo and C. Linton, J. Mol. Spectrosc. **137**, 114 (1989).
- [25] S. McDonald, PhD thesis, MIT, Cambridge, MA, 1985.
- [26] P. Carrette, A. Hocquet, M. Douay, and B. Pinchemel, J. Mol. Spectrosc. **124**, 243 (1987).
- [27] L. A. Kaledin, M. Erickson, and M. C. Heaven, J. Mol. Spectrosc. **165**, 323 (1994).
- [28] L. A. Kaledin and E. A. Shenyavskaya, J. Mol. Spectrosc. **90**, 590 (1981).
- [29] Y. Liu, H. Schall, R. Field, and C. Linton, J. Mol. Spectrosc. **104**, 72 (1984).
- [30] L. A. Kaledin and E. A. Shenyavskaya, J. Mol. Spectrosc. **133**, 469 (1989).
- [31] A. Bernard and C. Effantin, Can. J. Phys. **64**, 246 (1986).
- [32] C. Linton and A. Adam, J. Mol. Spectrosc. **206**, 161 (2001).
- [33] K. Dunfield, C. Linton, T. E. Clarke, J. McBride, and A. G. Adam, J. Mol. Spectrosc. **174**, 433 (1995).

- [34] M. McCarthy, J. C. Bloch, R. W. Field, and L. A. Kaledin, *J. Mol. Spectrosc.* **179**, 253 (1996).
- [35] M. McCarthy, J. C. Bloch, R. W. Field, and L. A. Kaledin, *J. Mol. Spectrosc.* **154**, 417 (1996).
- [36] M. J. Dick and C. Linton, *J. Mol. Spectrosc.* **217**, 26 (2003).
- [37] M. McCarthy, J. C. Bloch, R. W. Field, and L. A. Kaledin, *J. Mol. Spectrosc.* **107**, 119 (1984).
- [38] M. Dolg and H. Stoll, *Electronic Structure Calculations for Molecules Containing Lanthanide Atoms*, volume 22, Elsevier, Amsterdam.
- [39] S. G. Wang, D. K. Pan, and W. Schwarz, *J. Chem. Phys.* **102**, 9296 (1995).
- [40] S. A. McDonald, S. Rice, R. Field, and C. Linton, *J. Chem. Phys.* **93**, 7676 (1990).
- [41] P. Carette and A. Hocquet, *J. Mol. Spectrosc.* **131**, 301 (1988).
- [42] A. L. Kaledin, M. C. Heaven, R. W. Field, and L. A. Kaledin, *J. Mol. Spectrosc.* **179**, 310 (1996).

# Chapter 2

## General theory

High resolution spectroscopy allows us to explore the processes inside the microscopic world of molecules by observing spacings between lines, their splittings and the deviations from periodic patterns. This chapter provides a brief explanation of the nature of such effects in diatomic molecules.

### 2.1 Born–Oppenheimer approximation

The solution of the Schrödinger equation  $\hat{H}\psi = E\psi$  with a nonrelativistic molecular Hamiltonian is a hard task, since this Hamiltonian is a combination of nuclear kinetic energy, electronic kinetic energy, nuclear-nuclear repulsion energy, electron-nuclear attraction energy and electron-electron repulsion energy [1]. The solution can be simplified by the separation of the electronic and nuclear motions by invoking the Born–Oppenheimer approximation [2]. The Coulombic forces acting on nuclei and electrons are the same order of magnitude, but the masses of electrons are much smaller, and therefore they move faster. The electronic motion can therefore be separated from the much slower nuclear (vibration-rotation) motion. The vibration and rotation parts of the nuclear motion can be further separated in a similar way. As a result the total wavefunction of a molecule can be broken into components, i.e.,  $\psi = \psi_{el}\psi_{vib}\psi_{rot}\dots$  as an approximation.

## 2.2 Rotational structure

In the simplest approximation, a diatomic molecule (AB) can be considered as a rigid rotor, consisting of two point masses (A and B) connected by a rigid massless bar [1, 3, 4]. The discrete rotational energy levels are given by

$$F(J) = BJ(J+1), \quad (2.1)$$

where

$$B[\text{cm}^{-1}] = \frac{h \times 10^{-2}}{8\pi^2 c I}, \quad (2.2)$$

with  $I = \mu r^2$ , where  $\mu$  is a reduced mass

$$\mu = \frac{m_A m_B}{m_A + m_B}. \quad (2.3)$$

and  $r$  is an internuclear separation.

The molecule, of course, is not completely rigid, and as it rotates the centrifugal forces cause the internuclear distance to elongate slightly. The rotational-level energy expression thus has to have terms that account for the effect of centrifugal forces

$$F(J) = BJ(J+1) - D[J(J+1)]^2 + H[J(J+1)]^3 + L[J(J+1)]^4 + \dots, \quad (2.4)$$

where  $D, H, L, \dots$  are centrifugal distortion constants [5]. The transitions between rotational levels of the same vibrational level (pure rotational spectra) can be observed in the microwave region of the spectrum; such transitions were not studied in this thesis.

## 2.3 Vibrational structure

The vibrational energy level expression can be written as [6]

$$G(v) = \omega_e(v + \frac{1}{2}) - \omega_e x_e(v + \frac{1}{2})^2 + \omega_e y_e(v + \frac{1}{2})^3 + \omega_e z_e(v + \frac{1}{2})^4 \dots, \quad (2.5)$$

where  $v$  is a vibrational quantum number, the  $\omega_e(v + \frac{1}{2})$  term reflects the harmonic oscillator part of the potential energy function and the other terms account for

the “anharmonicity” of real potentials. The value of the rotational constant  $B$  depends on the vibrational state of the molecule, since  $B \propto 1/r^2$ . The vibrational dependence of  $B$  can be modeled by the following expression [3]

$$B_v = B_e - \alpha_e(v + \frac{1}{2}) + \gamma_e(v + \frac{1}{2})^2 \dots, \quad (2.6)$$

where  $B_e$  is the equilibrium rotational constant and  $\alpha_e$  and  $\gamma_e$  are rotation-vibration interaction coefficients.

A popular expression for the energy levels of the vibrating rotor was introduced by Dunham [7] by using the first-order semi-classical quantization condition from WKB (Wentzel–Kramers–Brillouin) theory [8]

$$E(v, J) = \sum_{l,m} Y_{l,m}(v + \frac{1}{2})^l (J(J+1))^m. \quad (2.7)$$

The coefficients  $Y_{l,m}$  can be related to the conventional spectroscopic constants [3, 7]. For example  $Y_{10} \approx \omega_e$ ,  $Y_{01} \approx B_e$  and  $Y_{11} \approx \alpha_e$  [3].

The spectroscopic constants associated with vibration and rotation depend on the reduced mass; therefore, their values are different for different isotopologues of the same molecule. The isotopic dependence of the spectroscopic constants can be conveniently generalized for the Dunham  $Y_{l,m}$  constants as

$$Y_{l,m} \propto \mu^{-(l+2m)/2}. \quad (2.8)$$

Therefore, within the Born–Oppenheimer approximation, the parameters associated with different isotopologues are related as

$$Y_{l,m}^{(\alpha)} = Y_{l,m}^{(1)} \left( \frac{\mu_1}{\mu_\alpha} \right)^{m+l/2}, \quad (2.9)$$

where  $\mu_1$  is the reduced mass of the reference isotopologue and  $\mu_\alpha$  is the reduced mass of isotopologue- $\alpha$ . Equation (2.7) can be rewritten to express energy levels for any isotopologue through the Dunham  $Y_{l,m}$  constants of the reference isotopologue as

$$E^{(\alpha)}(v, J) = \sum_{l,m} Y_{l,m}^{(1)} \left( \frac{\mu_1}{\mu_\alpha} \right)^{m+l/2} (v + \frac{1}{2})^l (J(J+1))^m. \quad (2.10)$$

In the case of Born–Oppenheimer approximation breakdown, small correction terms [9–11] must be added to Eq. (2.10). In this thesis Le Roy’s formalism [11] was used to account for the breakdown of the Born–Oppenheimer approximation in CoH and MnH.

The rotation-vibrational transitions are usually observed in the infrared region of the spectrum. In this thesis we have studied infrared spectra of MnH and MnD.

## 2.4 Electronic spectroscopy of diatomic molecules

### 2.4.1 Angular momenta in diatomic molecules

To understand the electronic spectrum of diatomic molecules, it is important to consider their angular momenta and the interaction between these momenta.

If one excludes nuclear spin, the total angular momentum of the diatomic molecule  $\mathbf{J}$  is the vector sum of electron orbital  $\mathbf{L}$ , electron spin  $\mathbf{S}$ , and nuclear rotation  $\mathbf{R}$  angular momenta (Figure 2.1a). The angular momenta and their projections on the internuclear axis are very important parameters, and the notation is summarized in Table 2.1.

Table 2.1: Angular momenta in diatomic molecules.

| Angular momentum                   | Projection on molecular axis (units of $\hbar$ ) |
|------------------------------------|--|
| $\mathbf{J}$                       | $\Omega = \Lambda + \Sigma$                      |
| $\mathbf{L}$                       | $\Lambda$  |
| $\mathbf{S}$                       | $\Sigma$   |
| $\mathbf{R}$                       | —  |
| $\mathbf{N}=\mathbf{R}+\mathbf{L}$ | $\Lambda$  |

The  ${}^{2S+1}\Lambda_{\Omega}$  symbol is used to denote different electronic states. For electronic states with  $\Lambda > 0$  the circulation of electrons can be in a clockwise or counter-clockwise direction around the internuclear axis, which results in a double orbital degeneracy. This phenomena is usually called  $\Lambda$ -doubling. Analogously, for  $\Omega > 0$  there is an  $\Omega$ -doubling for which both values are represented by  $|\Omega|$  for each of the  $2S + 1$  spin components [1]. For the cases when  $S > |\Lambda| > 0$  the labeling of each spin component becomes difficult and,  $\Omega = |\Lambda| + \Sigma$  is used instead of  $\Omega = |\Lambda + \Sigma|$ .

### 2.4.2 Hund's coupling cases

The electronic spectra of molecules that do not have closed electron shells are usually quite complex because of the interaction of different angular momenta. In the absence of nuclear spin there are three “fine structure” interactions associated with the magnetic moments due to electrons, which are summarized in Table 2.2.

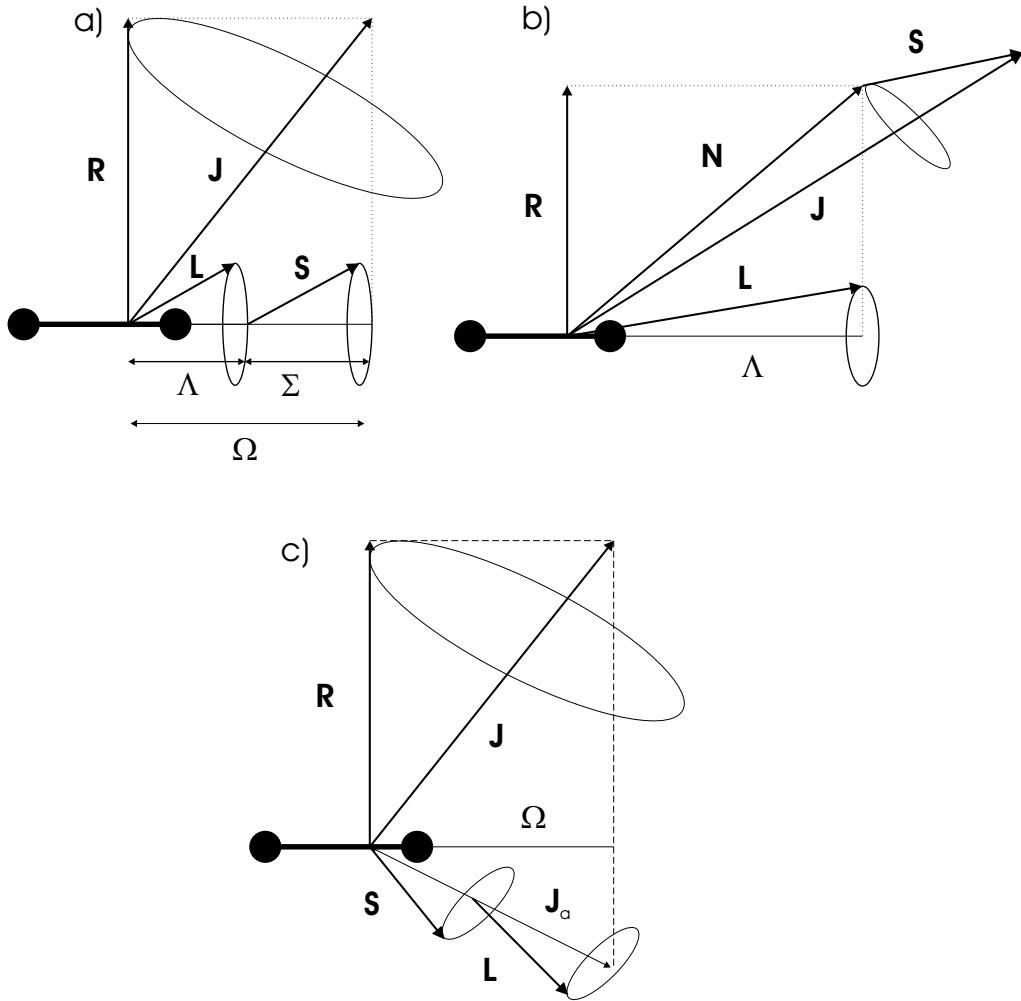


Figure 2.1: Hund's cases.

The effective Hamiltonian for a diatomic molecule can be therefore written as

$$\hat{H}_{\text{eff}} = \hat{H}_{\text{vib}} + \hat{H}_{\text{rot}} + \hat{H}_{\text{SO}} + \hat{H}_{\text{SR}} + \hat{H}_{\text{SS}} + \hat{H}_{\text{LD}}, \quad (2.11)$$

where

$$\hat{H}_{\text{SO}} = A \mathbf{L} \cdot \mathbf{S}, \quad (2.12)$$

$$\hat{H}_{\text{SR}} = \gamma \mathbf{N} \cdot \mathbf{S}, \quad (2.13)$$

Table 2.2: Coupling of angular momenta.

| Interaction term | Designation        | Description  |
|------------------|--------------------|--|
| <b>R·S</b>       | Spin-Rotation (SR) | Total electron spin interacting with the magnetic fields created by nuclear motion |
| <b>L·S</b>       | Spin-Orbit (SO)    | Electron spin interacting with the magnetic fields created by electron motion      |
| <b>S·S</b>       | Spin-Spin (SS)     | Interaction between magnetic moments of different unpaired electrons               |

$$\hat{H}_{\text{SS}} = \frac{2}{3}\lambda(3S_z^2 - \mathbf{S}^2), \quad (2.14)$$

and  $\hat{H}_{\text{LD}}$  describes the  $\Lambda$ -doubling interaction. The constants  $A, \gamma, \lambda$  and their physical interpretation (as well as that of  $\Lambda$ -doubling) are discussed in more detail in the following chapters and in Refs. [1, 6, 12–14].

As the appearance of the spectra depends strongly on the strength of spin-orbit coupling, it is convenient to introduce several idealized situations classified as Hund’s coupling schemes [15].

### Hund’s case (a)

The vector diagram of Hund’s case (a) is shown in Figure 1.1a. The electron orbital angular momentum  $\mathbf{L}$  is strongly coupled to the internuclear axis by electrostatic forces, and electron spin angular momentum  $\mathbf{S}$  is coupled to  $\mathbf{L}$  through strong spin orbit coupling. One can safely assume case (a) coupling whenever  $A \gg BJ$ , where  $A$  is the spin-orbit coupling constant. Obviously Hund’s case (a) approximation becomes less appropriate as  $J$  increases. The “good” quantum numbers in Hund’s case (a) are  $\Lambda, S, \Sigma, J$  and  $\Omega$ . In a pure case (a) there are  $2S + 1$  spin components, each with their own  $\Omega$ -value, and each of these spin components has a pattern of rotational energy levels given by  $B_{\Omega, \text{eff}}J(J + 1)$ , with the lowest level having  $J = \Omega$ . Each  $J$  is doubly degenerate (for  $\Omega > 0$ ), corresponding to  $e$  and  $f$  parities. Although  $\Lambda=0$  for  $\Sigma$  states, second order spin-orbit coupling can split a  $^{2S+1}\Sigma$  state

into  $S + 1$  spin components [5]. This situation is referred as Hund's coupling case (a') [16].

### Hund's case (b)

In the case when  $A \ll BJ$  the coupling of the electron spin to the internuclear axis is very weak and this situation is referred as Hund's case (b) (Figure (1.1b)). As it is illustrated in Figure 1.1b,  $\mathbf{L}$  (or its projection  $\Lambda$ ) is coupled to  $\mathbf{R}$  to form  $\mathbf{N}$ ;  $\mathbf{N}$  is then coupled with  $\mathbf{S}$  to form the total angular momentum  $\mathbf{J}$ . The “good” quantum numbers in Hund's case (b) are  $\Lambda, N, S$  and  $J$ . The energy of the rotational levels is given by  $BN(N + 1)$ , and each  $N$ -level is split into  $2(2S + 1)$  or  $2S + 1$  spin components for  $\Lambda \neq 0$  and  $\Lambda = 0$ , respectively. Electronic states obeying Hund's case (b) coupling are described in more detail later in the thesis for the  $X^7\Sigma^+$  state of MnH and the  $X^9\Sigma^-$  state of EuH.

Hund's cases (a) and (b) are extreme cases, and there are many examples of electronic states that do not obey either coupling approximation closely. These states can be described as intermediate coupling cases [6].

### Hund's case (c)

In electronic states that obey Hund's case (c) coupling, the spin-orbit coupling is so strong that  $A \gg \Delta E_{\text{states}}$ , where  $\Delta E_{\text{states}}$  is the separation between the electronic states. As shown in Figure 1.1c, the electron orbital angular momentum  $\mathbf{L}$  and electron spin  $\mathbf{S}$  couple to form  $J_a$  whose projection on the internuclear axis is  $\Omega$ .  $\mathbf{J}_a$  (or its projection  $\Omega$ ) is then coupled to  $\mathbf{R}$  to form the total angular momentum  $\mathbf{J}$ . The “good” quantum numbers in Hund's case (c) are therefore  $\Omega$  and  $J$ . The  $^{2S+1}\Lambda_\Omega$  spin components of a given  $^{2S+1}\Lambda$  term can be considered as independent electronic states, because these components are usually a mixture of many  $^{2S+1}\Lambda_\Omega$  basis functions coming from different electronic states. The spectroscopic constants for different  $\Omega$  components of the same  $^{2S+1}\Lambda$  term can be quite different, as we shall see for the electronic states of CoH. In fact, because of the aforementioned mixing of basis functions, the  $^{2S+1}\Lambda_\Omega$  notation is not very appropriate for Hund's case (c) and the notation suggested by Linton *et al.* [17] is commonly used. In this notation states are labeled by  $[T_0]\Omega$ , where  $[T_0]$  is the energy of the state in thousands of wavenumbers.

Just as in case (a), the rotational levels have relative energies  $BJ(J + 1)$  which are doubled for  $\Omega \neq 0$ .

### Hund's cases ( $a_{\beta J}$ ) and ( $b_{\beta J}$ )

If nuclear spin is present in at least one of the atoms, then one has to consider its coupling with other angular momenta in the molecule, and Hund's cases (*a*) and (*b*) are divided into various sub-classifications. In this thesis we encounter only Hund's cases ( $a_{\beta J}$ ) and ( $b_{\beta J}$ ). In both cases, the nuclear spin **I** couples with total angular momentum **J** to produce **F**. The subscript  $\beta$  implies that this quantization occurs only in the laboratory system of coordinates, and hyperfine components are expected to form a Landé-type pattern [18]; i.e., the spacing between them is proportional to the larger value of  $F$ .

#### 2.4.3 Parity

It should be noted that the meaning of parity in molecular spectroscopy is slightly different from the one given in physics textbooks. The concept of parity as it applies to molecular spectroscopy is well explained in Refs. [1, 14]. In this thesis, the term parity usually refers to rotationless *e* and *f* parities.

All rovibronic energy levels can be divided into two types by applying the inversion operator  $\hat{E}^*$ , which inverts the laboratory coordinates of all electrons and nuclei:

$$\hat{E}^*\psi = \hat{E}^*(\psi_{\text{el}}\psi_{\text{vib}}\psi_{\text{rot}}) = (\pm)\psi. \quad (2.15)$$

All  $(+)\psi$  energy states have positive total parity, while  $(-\psi)$  energy states have negative total parity. Of course, the effects of  $\hat{E}^*$  on the electronic, vibrational and electronic parts of the wavefunction need to be determined individually [1].  $\hat{E}^*$  is a symmetry operator, because all of the relative distances between particles are preserved.

The total parity alternates with  $J$  and it is useful to factor out this alternation by introducing rotationless *e* and *f* parities

$$\hat{E}^*\psi = +(-1)^J\psi, \quad (2.16)$$

$$\hat{E}^*\psi = -(-1)^J\psi. \quad (2.17)$$

Rotationless parity is more convenient to use as, for example all rotational energy levels of a  ${}^1\Sigma^-$  state have *f* parity, while the sign of their total parity alternates with  $J$ .

#### 2.4.4 Transitions between electronic states

Transitions between different electronic states of the molecule can be observed at a great range of frequencies, depending on the energy separation between these states. In this thesis, the electronic transitions of CoH, YbO, EuH, ErF, SmH, TmH and SmCl molecules are reported in Chapters 5, 6, 7 and 8.

# Bibliography

- [1] P. F. Bernath, *Spectra of Atoms and Molecules*, Oxford University Press, New York, 2nd edition, 2005.
- [2] M. Born and J. R. Oppenheimer, Ann. Phys. **84**, 457 (1927).
- [3] C. H. Townes and A. L. Schawlow, *Microwave Spectroscopy*, Dover, New York, 1975.
- [4] W. Gordy and R. L. Cook, *Microwave Molecular Spectroscopy*, Interscience, New York, 1970.
- [5] P. F. Bernath, *Spectra of Atoms and Molecules*, Oxford University Press, Oxford, 1995.
- [6] G. Herzberg, *Spectra of Diatomic Molecules*, Van Nostrand, New York, 1950.
- [7] J. L. Dunham, Phys. Rev. **41**, 721 (1932).
- [8] J. L. Dunham, Phys. Rev. **41**, 713 (1932).
- [9] A. H. M. Ross, R. S. Eng, and H. Kildal, Opt. Comm. **12**, 433 (1974).
- [10] J. K. G. Watson, J. Mol. Spectrosc. **80**, 411 (1980).
- [11] R. J. Le Roy, J. Mol. Spectrosc. **194**, 189 (1999).
- [12] J. M. Hollas, *Modern Spectroscopy*, John Wiley & Sons, Chichester, England, 2nd edition, 1996.
- [13] J. M. Brown and A. Carrington, *Rotational Spectroscopy of Diatomic Molecules*, Cambridge University Press, Cambridge, U.K., 2003.
- [14] H. Lefebvre-Brion and R. W. Field, *Perturbations in the Spectra of Diatomic Molecules*, Academic Press, New York, 1986.

- [15] F. Hund, Handbuch der Physik **24**, 561 (1933).
- [16] I. Kopp and J. T. Hougen, Can. J. Phys. **45**, 2581 (1967).
- [17] C. Linton et al., J. Mol. Spectrosc. **102**, 441 (1983).
- [18] T. M. Dunn, Nuclear hyperfine structure in the electronic spectra of diatomic molecules, in *Molecular Spectroscopy- Modern Research*, edited by K. N. Rao and C. W. Mathews, pages 231–257, Academic Press, New York, 1978.

# Chapter 3

## Experimental

### 3.1 Fourier transform emission spectroscopy

#### 3.1.1 Emission spectroscopy vs absorption spectroscopy

The majority of the experiments reported in this thesis were carried out in emission, and were recorded using a Bruker IFS 120HR Fourier transform spectrometer. The vibrational (infrared) and electronic (in the near infrared and visible parts of the spectrum) transitions were studied for different metal-containing diatomic molecules.

It is well known that emission spectroscopy is more sensitive than the absorption spectroscopy in the visible and ultraviolet regions. This is due to the fact that absorption spectroscopy requires intense broad band background radiation which introduces noise [1].

The advantages in the infrared regions are not that obvious. Our experiments on the metal containing molecules in the gas phase required the heating of the metal to produce the metal vapor. This heating results also in background black-body radiation, even for emission experiments. Moreover, the Einstein  $A$  coefficient which determines the emission rate of photons is proportional to  $\nu^3$ , and is therefore much smaller for the vibrational transitions than for electronic transitions [1]. Nevertheless, the emission experiments in the IR region proved to be very effective partly due to the fact that these experiments do not require high concentrations of the gas phase molecules (or very long absorption paths), unlike absorption experiments. In Ref. [2] the infrared spectrum of BaH was recorded both in emission

and absorption. Those experiments demonstrated that in that particular case the emission measurement was 20 times more sensitive with all conditions being equal.

### 3.1.2 Fourier transform spectroscopy

Modern Fourier transform spectrometers employ the Michelson interferometer first proposed by Albert Michelson in 1891 [3]. A schematic diagram of a Michelson interferometer is shown in Figure 3.1.

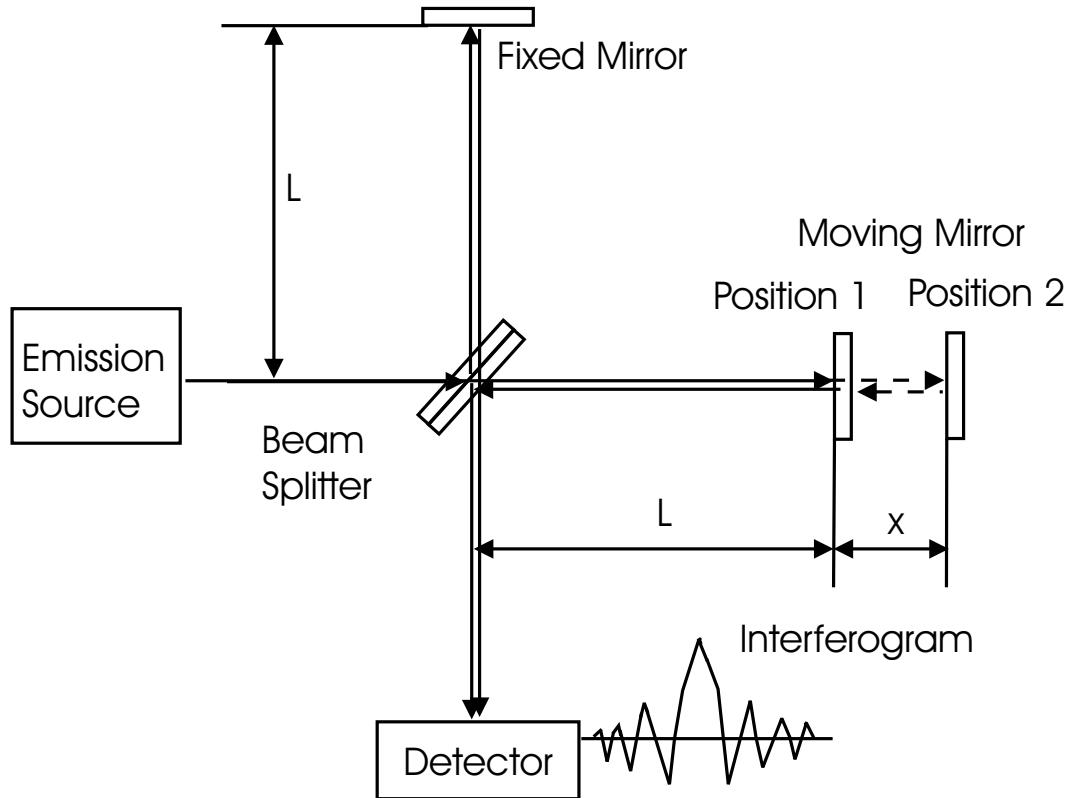


Figure 3.1: The schematic diagram of a Michelson interferometer. This figure is taken from Ref. [4].

When electromagnetic radiation from the source reaches the beamsplitter it splits into two beams. One beam is transmitted in the original direction while the other is reflected in the perpendicular direction. Both beams are reflected back from two mirrors and recombine at the detector after passing through the beamsplitter

again. The two components of the recombined beam interfere with each other in a way that depends on the difference in the distances of the mirrors from the beamsplitter (optical path difference). For that purpose one of the mirrors is held fixed while the other one is moved to change the optical path difference between two beams. Although the optical design of our Bruker IFS 120 HR Fourier transform spectrometer is more sophisticated than that of classical Michelson interferometer, the general concept remains the same.

If the light source is monochromatic, then the relationship between the intensity of the interferogram  $I(x)$  as a function of the optical path difference  $x$  between the two beams, and spectral intensity  $B(\bar{\nu})$  as a function of wavenumber  $\bar{\nu}$  is given by [5]

$$I(x) = B(\bar{\nu})[1 + \cos(2\pi\bar{\nu}x)] \quad (3.1)$$

When the source contains more than one frequency the intensity of interferogram is given by [5]

$$I(x) = \int_{-\infty}^{+\infty} B(\bar{\nu})[1 + \cos(2\pi\bar{\nu}x)]d\bar{\nu}. \quad (3.2)$$

This integral contains a mean intensity of the interferogram ( $\int_{-\infty}^{+\infty} B(\bar{\nu})d\bar{\nu}$ ) and a so-called ac component

$$I(x) = \int_{-\infty}^{+\infty} B(\bar{\nu})\cos(2\pi\bar{\nu}x)d\bar{\nu}, \quad (3.3)$$

which can be generalized as

$$I(x) = \int_{-\infty}^{+\infty} B(\bar{\nu})\exp(2\pi i\bar{\nu}x)d\bar{\nu}. \quad (3.4)$$

The spectral distribution  $B(\bar{\nu})$  can be obtained by the complex Fourier transform of the interferogram  $I(x)$  as

$$B(\bar{\nu}) = \int_{-\infty}^{+\infty} I(x)\exp(-2\pi i\bar{\nu}x)dx. \quad (3.5)$$

Since real spectrometers can produce only finite optical path differences, the spectra have a finite resolution. The maximum optical path difference ( $OPD_{\max}$ ) of our Bruker IFS 120 HR FTS is about 5 m, which gives the highest resolution  $\Delta\bar{\nu}_{\max}$  of  $\sim 0.002 \text{ cm}^{-1}$ , since  $\Delta\bar{\nu}_{\max} \approx 1/OPD_{\max}$ .

Another factor that has to be taken into account is a finite size of the entrance aperture of the spectrometer. The aperture introduces oblique rays in the nominally parallel beam, which results in circular fringes in the plane of the detector. Ideally, the detector should sample only the central fringe, because if the other interference rings fall on the detector the resolution is degraded. One therefore has a dilemma between choosing a large aperture to increase the light intensity at the detector, or choosing a smaller aperture to increase the resolution. In practice, the aperture is chosen to select as much as possible of the central region of the “bull’s eye” pattern of interferogram. The following expression gives the maximum achievable resolution at the chosen aperture diameter  $d$

$$\Delta\bar{\nu} = \frac{\bar{\nu}_{\max}d^2}{8F^2}, \quad (3.6)$$

where  $\bar{\nu}_{\max}$  is the maximum wavenumber for which the interference is constructive over the OPD for a given aperture diameter and  $F$  is the focal length of the collimating mirror ( $F = 418$  mm in our FTS). For example, for a resolution of  $0.02 \text{ cm}^{-1}$  at  $5000 \text{ cm}^{-1}$  the maximum aperture has a diameter of 2.4 mm, while for  $0.002 \text{ cm}^{-1}$  the maximum aperture is 0.75 mm. In our high-temperature experiments Doppler broadening was significant (as was pressure broadening for the experiments in the King furnace) and it was not necessary to use the maximum possible instrumental resolution. This allowed us to use larger diameters of the aperture to let more photons into the spectrometer.

Fourier transform spectrometers have two main advantages in comparison with grating spectrometers.

### (1) Throughput Advantage (Jacquinot Advantage)

The optical throughput (also known as étendue) is equal to the product of the area  $A$  of the instrument aperture and the solid angle  $\Omega$  subtended by the collimator. For the same spectral resolution, the circular aperture of an FTS has a larger area than that of the slit of a dispersive spectrometer; therefore the product  $A\Omega$  is larger and the signal intensity is higher [5].

### (2) Multiplex Advantage (Fellgett Advantage)

The total flux in the input beam falls on the detector of the FTS to give a large total signal, while in a grating spectrometer each frequency is dispersed (small signal falls on the detector) and scanned separately. The Fellgett advantage, however, applies only if the dominant source of noise is due to the detector or background radiation, which remains constant regardless of the level of signal entering the spectrometer.

### (3) Precision Advantage

All modern FTSs have a built-in single mode laser (usually He-Ne) to control the mirror motion and to provide a convenient internal wavenumber standard.

The sensitivity of FTSs is however worse than that of diode lasers used for spectroscopic measurements in the infrared region. Nevertheless, an FTS is often the preferred instrument even in the infrared, because diode lasers have gaps in their tunable range and they do not have inherent means of calibration.

## 3.2 Emission sources

Three types of emission sources were used to generate the gas-phase molecules studied in this thesis. The choice of one source over another depends on the molecule that one wants to study. The main factors that have to be taken into account before choosing an experimental cell are the metal vapor pressures at the temperatures achievable in these sources, the reactivity of the metals and the oxidant gases with the experimental environment, and the stability of the created molecules under the experimental conditions. The temperature dependence of the vapor pressures of the metals studied in this thesis, calculated using interpolation equations from Ref. [6], is shown in Figure 3.2.

### 3.2.1 Broida oven

A flow system known as a Broida oven was introduced by West *et al.* [7] as a source for production of gas-phase diatomic metal oxides and halides. Broida ovens have been widely used by spectroscopists for many years in optical emission (chemiluminescence) and laser-induced fluorescence (LIF) experiments (see for example Ref. [8] - [12]).

The designs of this source vary slightly in different research groups, but the general idea remains the same. Figure 3.3 presents a schematic diagram of the Broida oven used in optical emission experiments in the Bernath laboratory.

About 5 g of metal sample is placed in an alumina ( $\text{Al}_2\text{O}_3$ ) crucible which is surrounded by a tungsten heating basket. The current flowing through the basket is increased slowly over the period of 1-2 hours to a maximum value determined by the vapor pressure of the metal. Typically, few mTorr of metal vapor is adequate, and excessive metal vapor pressure will cause deposits that block the cone at the top of the crucible. An inert carrier gas (normally argon) is introduced through a small

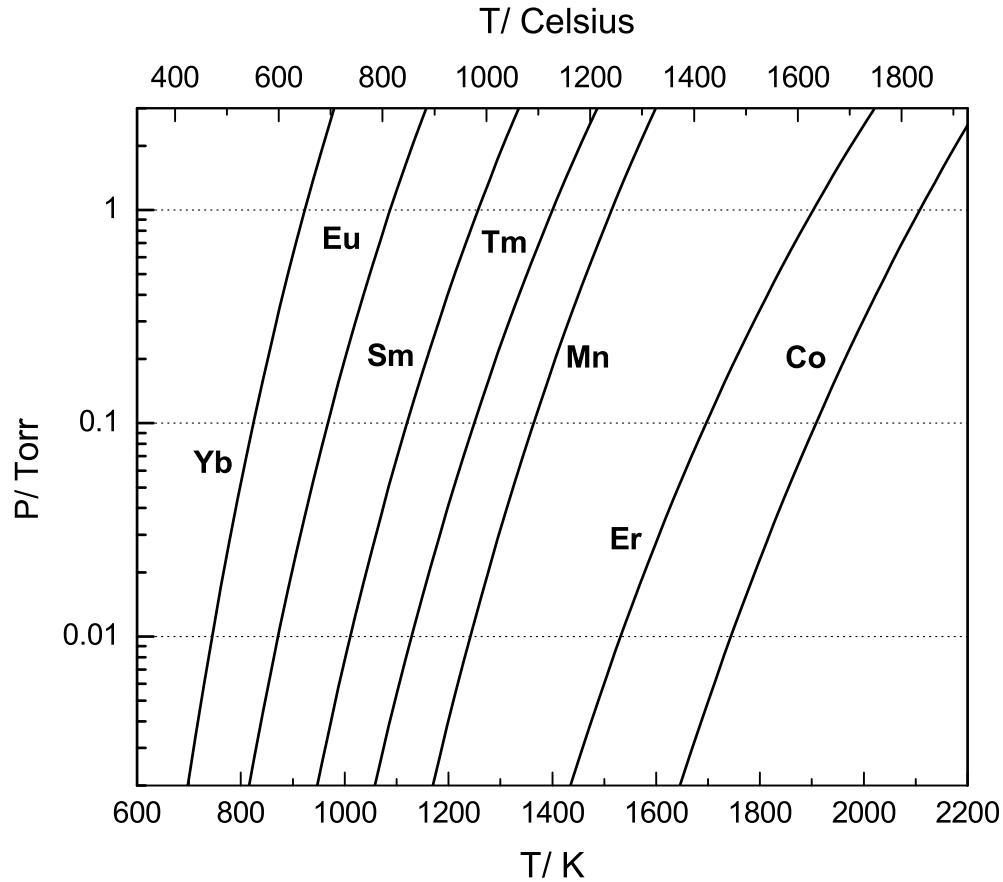


Figure 3.2: Selected metal vapor pressures as a function of temperature. Calculated using equations from Ref. [6].

stainless steel ring at the top of crucible just below the cone. The vaporized metal is carried out of the crucible by this inert gas through the stainless steel conical chimney. The chimney is about 5 mm in diameter at the top, and it reduces the cross sectional area of the flow. The tip of the chimney is surrounded by another ring through which an oxidant gas flows. The typical oxidant gases are: a)  $\text{N}_2\text{O}$  for production of metal oxides, b)  $\text{SF}_6$  for metal fluorides, and c)  $\text{HCl}$  or  $\text{CH}_3\text{Cl}$  for metal chlorides. The heating system is placed inside a water-cooled stainless steel chamber which is constantly pumped while the inert gas pressure is usually kept at

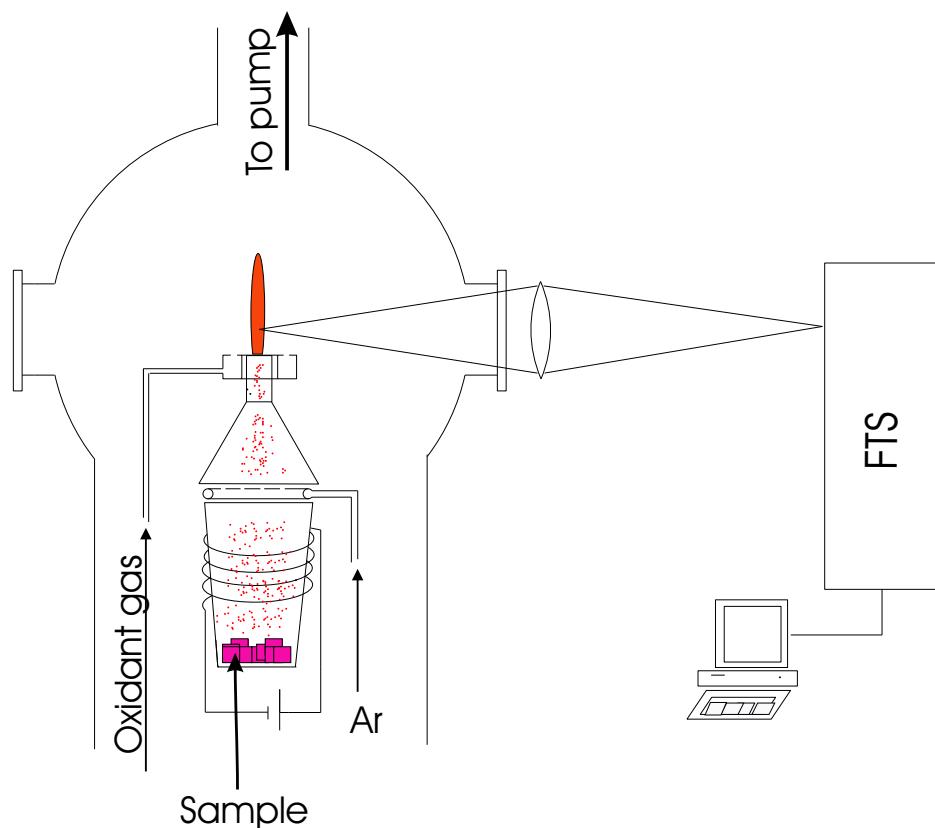


Figure 3.3: A schematic of the Broida oven at the University of Waterloo.

2-10 Torr and oxidant gas at  $\sim$ 0.1 Torr. To avoid contamination of the pump oil with dust particles, a large diameter automobile air filter is used.

In order to prevent the escape of heat from the system, a cylindrical alumina heat shield is usually placed around the crucible (not shown on Figure 3.3). The space between the crucible and the heat shield is filled with zirconia or other fibrous ceramic materials. Care has to be taken because some ceramic materials become conductive at high temperatures and need to be isolated from the tungsten basket.

The diatomic molecules formed at the exit of the chimney usually produce a bright chemiluminescent flame. The shape and color of the flame depends on the metal and the oxidant gas as well as on the pressures of the carrier gas and oxidant. In the emission experiments carried out in this work, the flame was imaged onto the entrance aperture of the FTS, and emission spectra were recorded.

Although the Broida oven is one of the most widely used sources for produc-

tion of metal-containing diatomics for spectroscopic experiments, it has some disadvantages: a) the chemiluminescence is not very bright, which result in a poor signal-to-noise ratio in emission experiments; b) the operating temperatures are typically  $\leq 1500^{\circ}\text{C}$  (nevertheless some modifications can be made to achieve higher temperatures [7], [13]); c) it is best for experiments with metal oxides and halides.

### 3.2.2 The high temperature furnace/electrical discharge emission source

A combination of an electrical discharge with a high temperature furnace has proved to be an excellent emission source for the electronic and infrared spectroscopy of diatomic [14–17] and triatomic [18, 20] metal hydrides. A schematic diagram of the source is depicted in Figure 3.4.

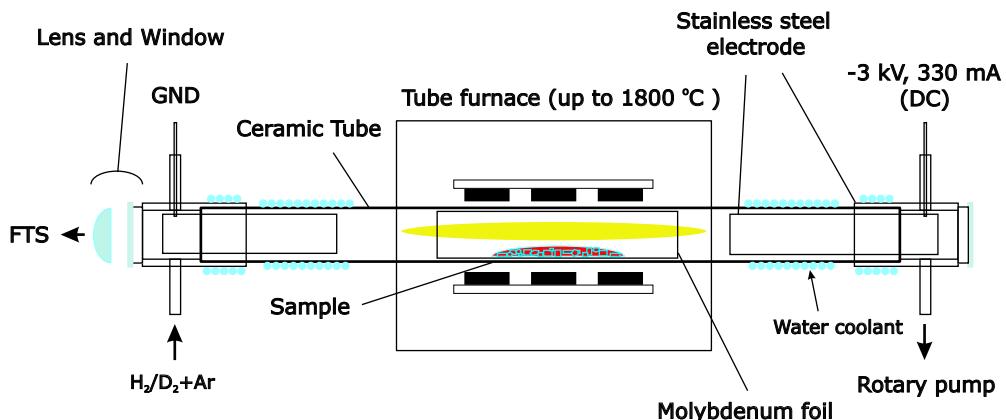


Figure 3.4: An illustration of the emission source that combines a dc discharge and a high temperature furnace.

The following procedure is used in our experiments. First, a sample of metal, 20–50 g, is placed in the center of the alumina ( $\text{Al}_2\text{O}_3$ ) or mullite ( $2\text{Al}_2\text{O}_3 \cdot 2\text{SiO}_2$ ) tube, and is then heated by the CM Rapid Temp furnace. In the case of rare earth metals, the hot part of the tube is wrapped inside with molybdenum foil to prevent the reaction between the metal and the ceramic. The furnace can be heated to temperatures  $\leq 1800^{\circ}\text{C}$ , depending on the experiment. Normally the temperature is chosen to achieve about 1 Torr of the metal vapor pressure. The heating rate was usually  $250^{\circ}\text{C}$  per hour, to avoid thermal shock of the alumina ceramic.

An electrical discharge (3 kV, 333 mA) was then applied between two cylindrical stainless steel electrodes inside the water-cooled ends of the tube. A mixture of Ar and H<sub>2</sub> gases flows slowly over the sample, typically at 3-12 Torr of total pressure, with the H<sub>2</sub> pressure being just 2% of the total. The high temperature together with a DC discharge not only facilitates the production of the molecules in the gas phase, but also populates excited vibrational levels and excited electronic states. Electronic transitions appear in the visible or near infrared parts of the spectral range, while transitions between vibrational levels of the same electronic state can be observed in the infrared region. The tube is sealed with windows made from different materials depending on the spectral range of interest. The emission from the tube is focused on the entrance aperture of the Fourier transform spectrometer by a lens made from the same material as the windows.

One of the disadvantages of this method is the reaction of the alumina (or mullite) with some of the metals at high temperatures. This sometimes results in deformation or even breaking of the tubes. Although there are some methods to avoid direct contact of the metal and the ceramic, i.e., carbon liners, tantalum or carbon boats, damage of the tubes sometimes occurs anyway. Unlike the Broida oven source, there are numerous impurities that can be seen in emission spectra produced in the discharge/furnace source. The most common impurities are AlH (with alumina tubes) and SiO (with mullite tubes). It is interesting that during an attempt to produce the infrared spectrum of scandium monohydride (ScH), a very intense spectrum of AlH was observed. The signal was in fact of the same quality as in the experiment that was aimed directly at observing the spectrum of AlH [21]. This was probably because Sc atoms were “replacing” the Al atoms in the walls of the tube.

Another disadvantage of the furnace/discharge source is that experiments to make molecules other than hydrides are difficult. This is mostly because the electrodes at the ends of the tube become contaminated rapidly and the discharge becomes very unstable.

### 3.2.3 The King furnace

One of the oldest tools for gas phase spectroscopy of atoms and molecules is a King furnace (a graphite tube furnace) originally introduced by Arthur King in 1908 [22]. The design of the King furnace at the University of Waterloo is depicted in Figure 3.5.

The furnace shell is a water jacket made from anodized aluminum. The end bulkheads were originally made from nickel-plated aluminum, but we had to replace

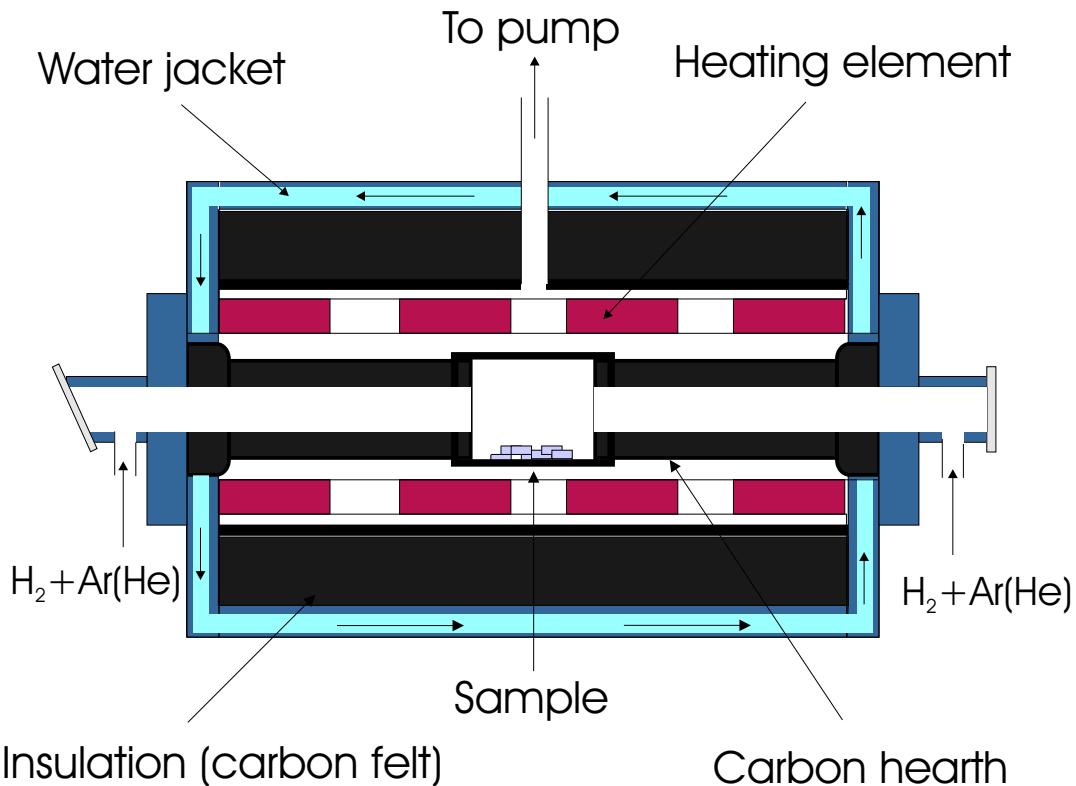


Figure 3.5: A schematic of the King furnace at the University of Waterloo.

them with new stainless steel bulkheads because the internal cooling water passages were clogged with deposits. Everything inside the outer shell is made of carbon. The active part of the furnace is a graphite heating element through which currents up to 65 A can flow. Thermal insulation between the heating element and the furnace shell is provided by carbon felt which is retained by a graphite radiation shield. Two carbon hearths (tubes) are inserted into each end of the furnace coaxial to the heating element. The graphite holder containing the metal sample connects the two hearths. The temperatures inside the furnace can reach 2700°C, depending on the operating gas and the current applied.

The heating process was started with about 100 Torr of operating gas. Hydrogen, helium and argon gases were used for the experiments in this thesis. It was found that when doing experiments on metal hydrides, the use of pure hydrogen does not yield intense spectra due to the relatively low temperature. This is due to the fact that at temperatures greater than 2250°C molecular hydrogen dissociates

to atomic hydrogen, which is an endothermic reaction. The addition of argon gas helps significantly in achieving higher temperatures (up to 2800°C), but at high temperatures the argon gas proved to be harmful to the heating element. Helium gas yields a smaller increase in temperature, but it does not harm the heating element. In the experiments with metal fluorides, chlorides and sulfides, the furnace was heated with helium gas, and after the maximum temperature was achieved CF<sub>4</sub>, HCl or CS<sub>2</sub> gases, respectively, were added. When the spectra were recorded the total pressure in the furnace was held at ~200 Torr. The emission from the furnace was imaged onto the entrance aperture of the FTS with a lens.

It was found that the lanthanide metals are very reactive with the carbon environment of the King furnace. Some of the damage can be avoided by wrapping the inside of the sample holder first with tantalum and then with tungsten foils. However, the metal vapor can penetrate almost everywhere inside the furnace, causing severe damage to the heating element and radiation shield.

### 3.3 Laser ablation/molecular beam apparatus

The sub-Doppler spectrum of EuH was recorded in the laser ablation/molecular beam apparatus at the Arizona State University in the laboratory of Prof. T. C. Steimle. A brief description of this apparatus is given in section 7.2.2 of this thesis.

# Bibliography

- [1] P. Bernath, Chem. Soc. Rev **25**, 111 (1996).
- [2] K. Walker, H. Hedderich, and P. Bernath, Mol. Phys. **78**, 577 (1993).
- [3] A. Michelson, Phil. Mag. **31**, 256 (1891).
- [4] G. Li, PhD thesis, University of Waterloo, Waterloo, ON, 2003.
- [5] S. P. Davis, M. C. Abrams, and J. W. Brault, *Fourier Transform Spectrometry*, Academic Press, New York, 2001.
- [6] O. Knacke, O. Kubaschewski, and K. Hesselmann, *Thermo-chemical Properties of Inorganic Substances*, volume 51, Springer-Verlag Berlin, Heidelberg, 2nd edition, 1991.
- [7] J. West, R. Bradford, J. D. Eversole, and C. Jones, Rev. Sci. Instr. **46**, 164 (1975).
- [8] T. Melville, I. Gordon, K. Tereszchuk, J. Coxon, and P. Bernath, J. Mol. Spectrosc. **218**, 235 (2003).
- [9] H. Li, R. Skelton, C. Fosca, B. Pinchemel, and P. Bernath, J. Mol. Spectrosc. **203**, 188 (2000).
- [10] S. A. McDonald, S. Rice, R. Field, and C. Linton, J. Chem. Phys. **93**, 7676 (1990).
- [11] P. Carrette, A. Hocquet, M. Douay, and B. Pinchemel, J. Mol. Spectrosc. **124**, 243 (1987).
- [12] M. J. Dick and C. Linton, J. Mol. Spectrosc. **217**, 26 (2003).
- [13] P. Sheridan, PhD thesis, University of Arizona, Tucson, AZ, 2003.

- [14] A. Shayesteh, D. Appadoo, I. Gordon, R. LeRoy, and P. Bernath, *J. Chem. Phys.* **120**, 10002 (2004).
- [15] A. Shayesteh, K. Walker, I. Gordon, D. Appadoo, and P. Bernath, *J. Mol. Struct.* **695**, 23 (2004).
- [16] S. Yu et al., *J. Mol. Spectrosc.* **229**, 257 (2005).
- [17] I. E. Gordon, A. Shayesteh, D. Appadoo, K. Walker, and P. Bernath, *J. Mol. Spectrosc.* **229**, 269 (2005).
- [18] P. Bernath, A. Shayesteh, and K. Tereszchuk, *Science* **297**, 1323 (2002).
- [19] A. Shayesteh, D. Appadoo, I. Gordon, and P. Bernath, *J. Chem. Phys.* **119**, 7785 (2003).
- [20] A. Shayesteh, D. Appadoo, I. Gordon, and P. Bernath, *J. Am. Chem. Soc.* **126**, 14356 (2004).
- [21] J. White, M. Dulick, and P. Bernath, *J. Chem. Phys.* **99**, 8371.
- [22] A. S. King, *Astrophys. J.* **28**, 300 (1908).

# Chapter 4

## Infrared emission spectra of MnH and MnD

### 4.1 Introduction

The search for infrared spectra of gas phase metal dihydride molecules using Fourier transform emission spectroscopy is a continuing project in the Bernath laboratory. So far we have been able to detect spectra of BeH<sub>2</sub> [1, 2], MgH<sub>2</sub> [3], ZnH<sub>2</sub> [4–6], HgH<sub>2</sub> and CdH<sub>2</sub> [6]. Similar experiments on MnH<sub>2</sub> were of particular interest, because early spectroscopic studies [7, 8] suggested a bent structure for MnH<sub>2</sub>, whereas theory predicts a linear geometry [9–11]. The most recent experimental work on MnH<sub>2</sub> also favors a linear structure [12]. Unfortunately, we were not able to find the spectrum of manganese dihydride in our experiments. In our paper on CaH and SrH [13], we discuss the factors that promote the production of gaseous metal dihydrides. Nevertheless high quality spectra of manganese monohydride and monodeuteride were obtained in the course of our experiments, and we present the results in this chapter.

Molecules containing transition metal atoms are of interest to scientists, including spectroscopists. Apart from astrophysical interest, research on metal hydrides contributes to understanding of such topics as hydrogenation catalysis and the formation of the metal-hydrogen bond. Transition metal atoms have partially filled *d*-subshells, resulting in numerous low-lying electronic states that readily interact with each other. Manganese is an unusual transition element because it has a half-filled 3*d*-subshell, and therefore manganese-containing molecules possess only a few low-lying electronic states. Manganese has high spin coupling that leads to

high-multiplicity electronic states. Spectra of molecules with electronic states of high multiplicity are very complex, and are a challenge to analyze.

Manganese hydride is one of the most extensively studied high-spin molecules. The MnH  $A^7\Pi-X^7\Sigma^+$  electronic transition alone has been the subject of more than a dozen experimental and theoretical papers. The first observation and identification of this spectrum was carried out by Heimer in 1936 [14]. Between 1942 and 1957, Nevin and co-workers recorded and rotationally analyzed the 0-0 and 0-1 bands of the  $A^7\Pi-X^7\Sigma^+$  transition (near 568 and 624 nm) for MnH and MnD. This extensive work was published in six papers over a 15 year period [15–20]. The  $A-X$  0-0 band was revisited 50 years later by Varberg *et al.* [21–23] using laser excitation spectroscopy. Theye extended Nevin’s rotational analysis to the lowest  $J$  values for every spin component, and studied the nuclear hyperfine interaction.

The first observation of transitions involving quintet states of MnH was in 1938 by Pearse and Gaydon [24]. Balfour *et al.* recorded a number of quintet bands using a Fourier transform spectrometer. They rotationally analyzed the  $c^5\Sigma^+-a^5\Sigma^+$  0-0 and 1-1 bands near 846 nm, the  $b^5\Pi-a^5\Sigma^+$  0-0 band at 1060 nm [25], the  $d^5\Pi_i-a^5\Sigma^+$  0-0, 1-1 and 2-2 bands at 480 nm, and the  $e^5\Sigma^+-a^5\Sigma^+$  0-0 band at 450 nm [26, 27]. Some of the corresponding MnD bands were also presented in these papers.

The ground  $X^7\Sigma^+$  electronic state of MnH was probed by means of electron spin resonance (ESR) [7] and electron-nuclear double resonance (ENDOR) spectroscopy [28, 29]. Later Urban and Jones observed an infrared spectrum of MnH [30] and MnD [31] using a diode laser spectrometer. They recorded vibrational bands  $v=1\leftarrow 0$  to  $v=3\leftarrow 2$  with a nominal accuracy of  $0.001\text{ cm}^{-1}$ . Urban and Jones [30, 31] determined equilibrium constants for both molecules and carried out a combined isotopologue fit to determine mass-independent parameters. Unfortunately, semiconductor diode lasers have certain limitations (mainly due to gaps in the tuning curve), which do not allow coverage of the whole spectral range. As a result, only relatively few infrared lines have been measured; for example only seven R-lines, that are all spin components of a single R(5) transition, were obtained for the fundamental band of MnH.

Theoretical studies of MnH began with work of Kovács and Pacher [32–34], who derived a molecular Hamiltonian for  $A^7\Pi$  and  $X^7\Sigma^+$  states. *Ab initio* calculations on MnH by Das [35], Walch and Bauschlicher [36] and Chong *et al.* [37] were performed for the ground  $X^7\Sigma^+$  state. Bagus and Schaefer [38] investigated both the  $A^7\Pi$  and  $X^7\Sigma^+$  states, but in the absence of electron correlation. *Ab initio* calculations by Langhoff *et al.* [39] included all quintet and septet states below  $30\,000\text{ cm}^{-1}$ . The most recent *ab initio* calculations for the ground state were carried out by Harrison [40].

In this chapter, we report new infrared emission spectra of MnH and MnD recorded with a Fourier transform spectrometer. The vibrational bands  $v = 1 \rightarrow 0$  to  $v = 3 \rightarrow 2$  for MnH and  $v = 1 \rightarrow 0$  to  $v = 4 \rightarrow 3$  for MnD were observed. Analyses of the new spectra have provided improved ground state molecular constants for MnH and MnD.

## 4.2 Experimental

The same emission source that has proved to be very effective in providing spectra of other metal hydrides in our laboratory [4, 13, 41] was used for MnH and MnD. About 40 g of manganese metal was heated to 1200°C in a sealed and evacuated alumina tube by a CM Rapid Temp furnace. This produced approximately 1 Torr pressure of manganese vapor. A mixture of hydrogen (or deuterium) and argon gases was introduced into the tube and an electrical discharge (3 kV, 333 mA) was applied between two cylindrical stainless steel electrodes inside the ends of the tube. The total pressure inside the system was maintained at about 3.5 Torr, with hydrogen gas being approximately 10 % of the total. Emission from the tube was focused onto the entrance aperture of a Bruker IFS 120 HR Fourier transform spectrometer. The windows at the ends of the tube and the lens were made from BaF<sub>2</sub>. The infrared spectra of MnH/D were recorded between 800 and 1700 cm<sup>-1</sup> at a resolution of 0.0085 cm<sup>-1</sup> using a KBr beamsplitter and a liquid nitrogen-cooled HgCdTe (MCT) detector. A 1670 cm<sup>-1</sup> red pass filter was used to limit the emission to the desired spectral range. The spectra contained MnH/D emission lines, as well as blackbody emission from the hot tube, and absorption lines from atmospheric water vapor, as one can see for the spectrum of MnH in Figure 4.1. Four hundred scans were co-added for each molecule in order to improve the signal-to-noise ratio.

## 4.3 Results and discussion

The recorded infrared emission spectrum of MnH/D contained vibration-rotation bands in the ground electronic  $^7\Sigma^+$  state. The lines from  $v = 1 \rightarrow 0$  to  $v = 3 \rightarrow 2$  for MnH and the lines from  $v = 1 \rightarrow 0$  to  $v = 4 \rightarrow 3$  transitions for MnD were found and analyzed. An overview spectrum of MnD is shown on Fig. 4.2. In order to display the bands more clearly, the baseline was corrected by eliminating blackbody emission profile using the Bruker OPUS program.

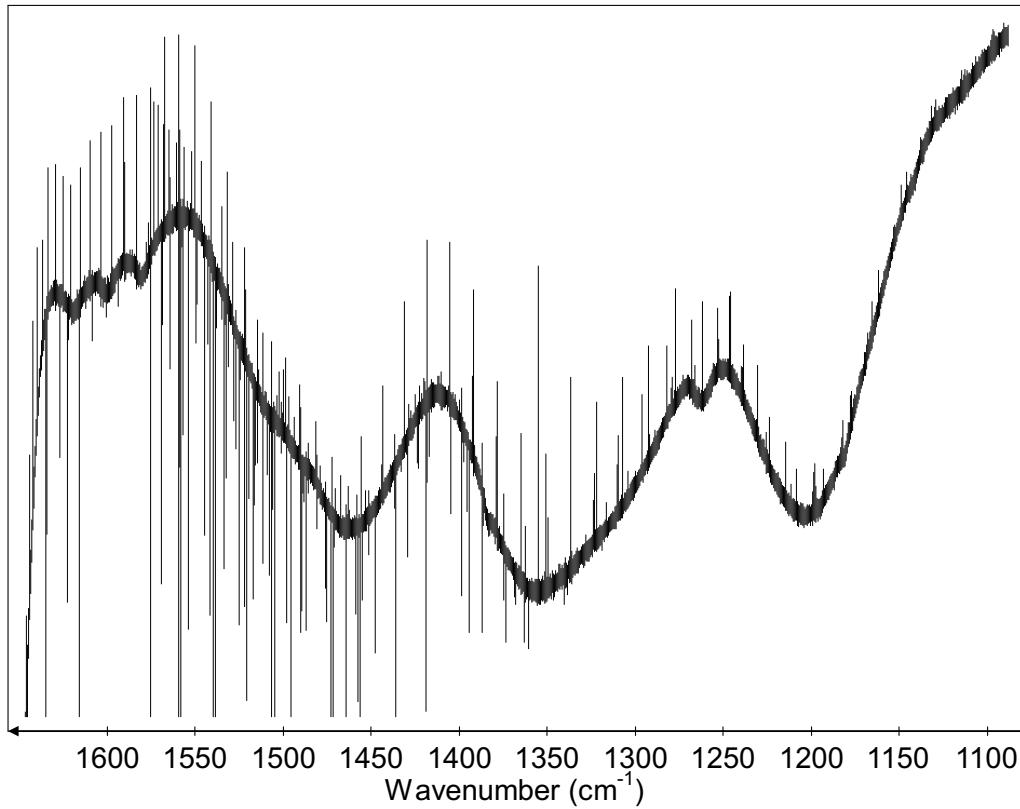


Figure 4.1: An overview of the infrared emission spectrum of MnH.

The  $X^7\Sigma^+$  state of MnH obeys Hund's case (b) coupling, so each rotational level ( $N$ ) is split into seven spin components (for  $N \geq 3$ ) labeled by  $J$  with  $\mathbf{J}=\mathbf{N}+\mathbf{S}$ , where  $\mathbf{J}$  is the total angular momentum,  $\mathbf{N}$  is rotational angular momentum and  $\mathbf{S}$  is the total electron spin. The fine structure splitting of  $N = 0$  to 3 rotational levels is shown in Figure 4.3. An example showing seven spin components for R(5) and P(7) lines of the fundamental band of MnH are displayed in Fig. 4.4. It is fortunate that manganese has just one isotope (<sup>55</sup>Mn with  $I = 5/2$ ), otherwise the spectrum would be more complicated due to line overlaps. The spacing between the spin components in the R branches decreases with increasing  $N$ , causing transitions with  $N > 20$  of fundamental band to be observed as single broad lines. This blending is observed to occur at lower  $N$  values as the vibrational quantum number increases. On one hand it is a disadvantage, since unblended lines are more desirable for analysis, but on the other hand, the intensity of blended lines is usually higher, allowing the measurement of the  $v = 4 \rightarrow 3$  transition in MnD for which only single R-lines

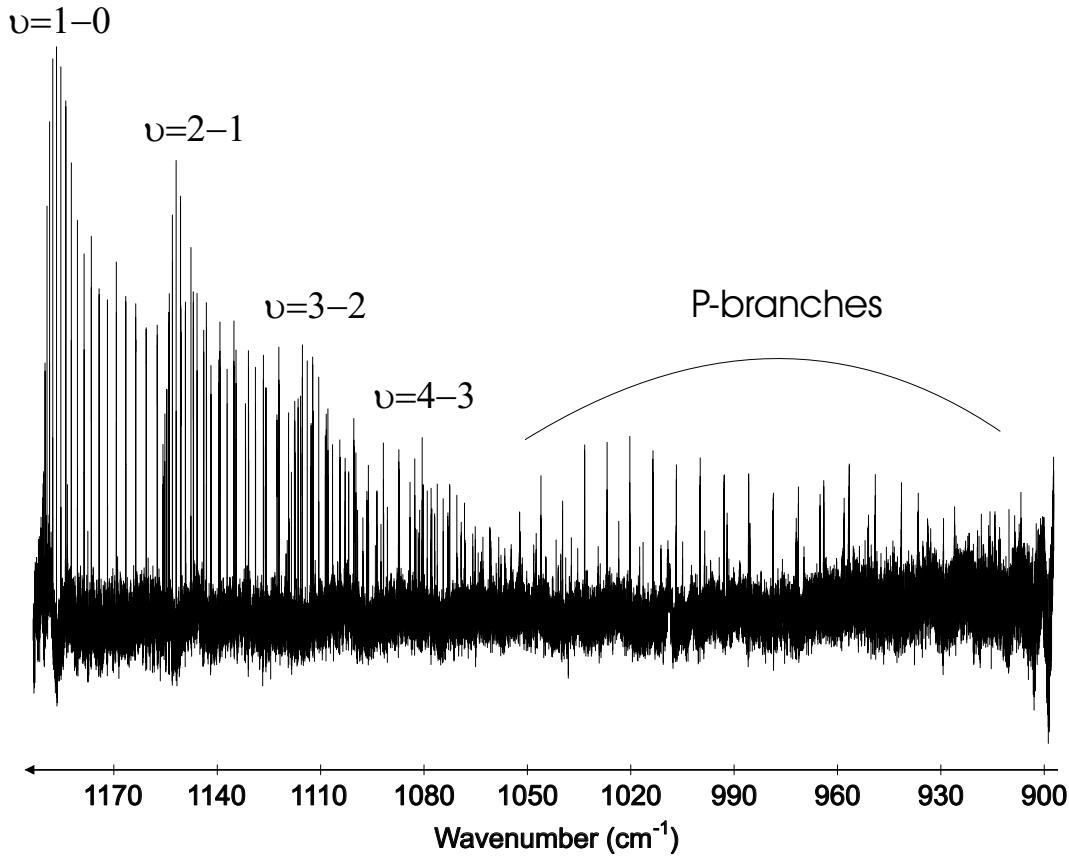


Figure 4.2: An overview of the infrared emission spectrum of MnD after baseline correction.

were observed without any trace of corresponding P-lines. The intensities of the spin components of each rotational line both in the P- and R-branches increase from  $J = N - 3$  to  $J = N + 3$ , as shown in Figure 4.4 for R(5) and P(7) transitions of the fundamental band. These line intensities have the classic pattern given by coupling of two angular momenta such as  $\mathbf{L}$  and  $\mathbf{S}$  to give  $\mathbf{J}$  for atoms [42]. Urban and Jones [30] observed deviations from this expected intensity pattern. In the present FT spectrum, however, this intensity pattern seems to be consistent throughout the spectrum with the exception of a few lines that are overlapped with water absorption lines or atomic emission lines. As an illustration, the lines in Fig. 4.4 were chosen to be the same as the ones shown by Urban and Jones [30]. In our spectrum we were also able to observe a few satellite lines (transitions across spin components) at low  $N$  values.

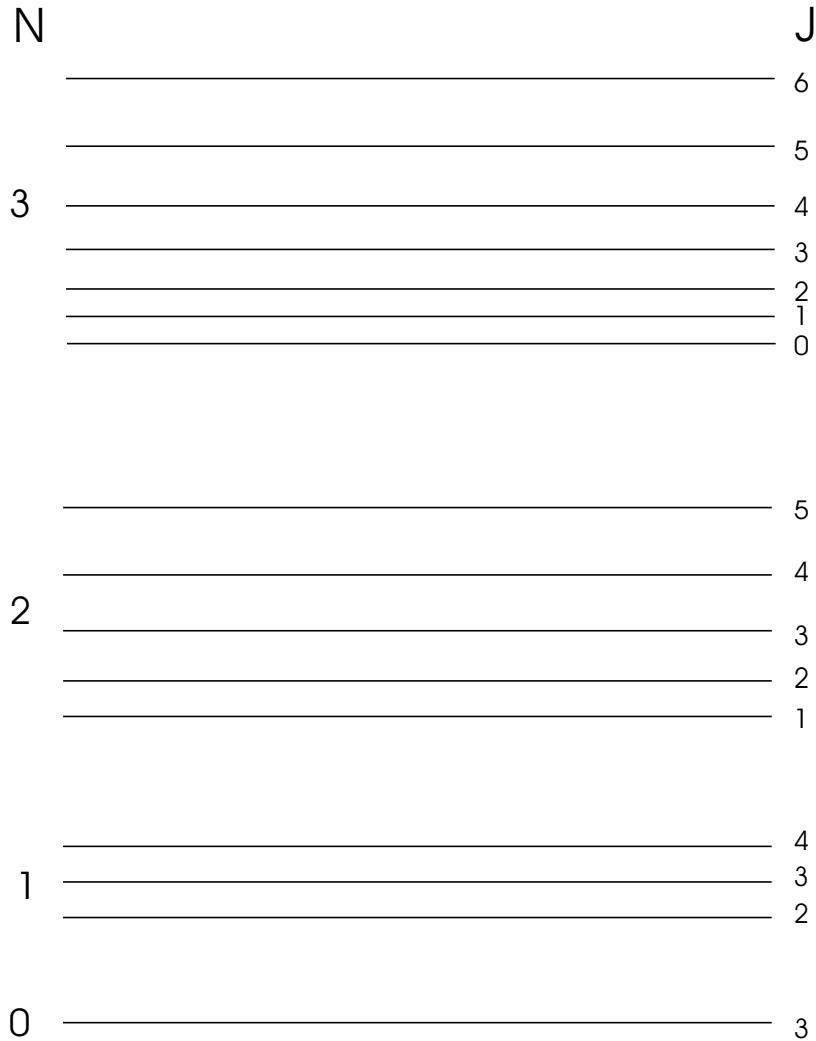


Figure 4.3: Fine structure of the low rotational levels of the  $X^7\Sigma^+$  state of MnH.

A zero filling factor of 8 was used during the Fourier transformation to improve data reduction. Zero filling in the interferogram interpolates the spectrum by increasing the number of sampling points. The line positions were determined using the program WSpectra written by M. Carleer. The MnH/D spectra were calibrated using the line positions of the previous diode laser infrared measurements [30, 31]. The effect of blending at higher  $N$  values forced us to assign an experimental uncertainty ranging from  $0.001 \text{ cm}^{-1}$  for strong unblended lines to  $0.003 \text{ cm}^{-1}$  for completely blended lines (i.e., lines corresponding to seven spin

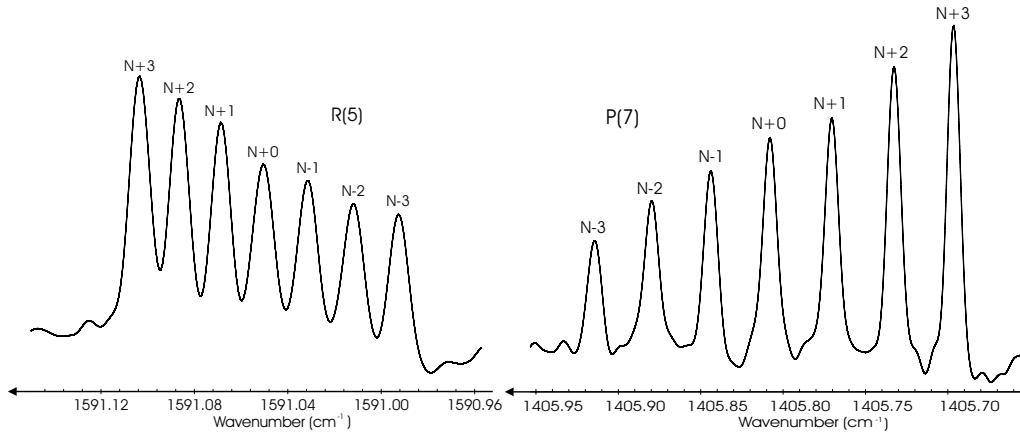


Figure 4.4: Example of spin-splitting in MnH lines: R(5) and P(7) transitions of the fundamental band. The intensities of the spin components of each rotational line both in the P- and R-branches increase from  $J = N - 3$  to  $J = N + 3$ . The spin components are labeled by  $J$  values.

components blended into one feature) for MnH, and 0.001 to 0.005  $\text{cm}^{-1}$  for MnD. For the blended lines, the same line position was used for all seven spin-components but with different uncertainties. This procedure proved to be more effective than assigning a blended line to a single transition. The bands were picked out and assigned using a color Loomis-Wood program. Assignments were made for the fundamental band up to  $N''=27$  for MnH, for the  $v=2 \rightarrow 1$  transition up to  $N''=24$  and for the  $v=3 \rightarrow 2$  transition up to  $N''=21$ . The corresponding bands of MnD were assigned up to  $N''=37$ ,  $N''=36$  and  $N''=33$  respectively, while the weak R-branch of the  $v=4 \rightarrow 3$  transition of MnD was followed up to  $N''=29$ . In total, 874 MnH lines and 953 MnD lines were assigned.

The high multiplicity septet ground state of MnH caused some difficulties at the beginning in the fitting of the experimental data. Urban and Jones [30, 31] fitted their data using expressions similar to the Dunham expansion for spin-rotation and spin-spin interactions, along with a regular Dunham expression for the ro-vibrational energy levels. In this way they were able to determine equilibrium constants for MnH and MnD.

Instead we chose to update our existing fitting program by inclusion of a Hamiltonian matrix for  ${}^7\Sigma^+$  states. We derived a matrix using Hund case (a) basis functions, similar to that of Ref. [23], but with the addition of the  $H$  and  $L$  centrifugal distortion constants required for fitting data with higher  $N$  values. It should be noted that there is a small typographical error in Table II of Ref. [23]: a part of the  $\langle 3|2 \rangle$  element should be  $-2D(x-1)$  instead of  $-2D(2x-2)$ . The updated Hamiltonian matrix for a  ${}^7\Sigma^+$  electronic state is given in Table 4.1. However, it turned to be very tedious to update the existing code to perform Dunham-type fits for MnH and MnD. It was therefore decided to employ Pickett's program SPFIT [43], which is widely used to fit microwave spectra.

SPFIT was used to carry out a Dunham-type fit to obtain equilibrium parameters for MnH and MnD using transitions up to  $v = 3 \rightarrow 2$ . The  $v = 4 \rightarrow 3$  band of MnD was excluded because almost all of the observed lines were blended and the inclusion of these transitions led to an unsatisfactory fit. In this Dunham-type fit, each parameter  $X$  was assumed to have the usual vibrational dependence,

$$X_{ij} = X_{0j} + X_{1j}(v + \frac{1}{2}) + X_{2j}(v + \frac{1}{2})^2 + \dots \quad (4.1)$$

indicated by first index for each parameter. The second index for each parameter indicates the order of the rotational dependence. The calculated equilibrium constants are provided in Table 4.2 for MnH and Table 4.3 for MnD. Then a fit was carried out with SPFIT to determine band constants and the results are presented in Table 4.4 for MnH and Table 4.5 for MnD. This time the  $v=4 \rightarrow 3$  band was included for MnD in the fit with spin-spin and spin-rotation constants fixed to the values calculated using equilibrium constants from Table 4.3.

No higher order parameters such as  $\theta$  and  $\gamma_s$  were required to obtain a good fit. The diode laser lines of Urban and Jones [30, 31] were included in the fits; this was particularly helpful in the case of MnD since the diode laser spectrum was recorded at higher resolution than our Fourier transform measurements and some lines that were blended in our spectrum were resolved. The corresponding lines in our spectrum were given lower weight. It appears that the P(17) lines of the fundamental band in Ref. [30] are mistyped. Tables 4.2 and 4.3 list constants obtained by Urban and Jones [30, 31] for comparison.

Table 4.1:  $^7\Sigma^+$  Hamiltonian matrix (Hund's case (a) basis),  $x = J(J+1)$ .

|       | $ 3>$  | $ 2>$  | $ 1>$   | $ 0>$   |
|-------|--|--|---|---|
| $ 3>$ | $10\lambda + 15\theta - 3\gamma + 90\gamma_s + (B + 10\lambda_D - 6\gamma_D)(x - 6) - D(x^2 - 6x) + H(x^3 - 48x + 72) + L(x^4 + 12x^3 - 96x^2 - 168x + 576)$ | $-(6(x-6))^{1/2}[B - \frac{1}{2}\gamma - 10\gamma_s + 5\lambda_D - \gamma_D(\frac{1}{2}x + 5) - 2D(x-1) + H(3x^2 + 10x - 28) + 4L(x^3 + 13x^2 + 4x + 50)]$                     | $(15(x-2)(x-6))^{1/2}(-\gamma_D - 2D + 2H(3x + 8) + 2L(6x^2 + 60x + 52 \mp 12x))$   | $-(15(x-2)x(x-6))^{1/2}(4H + 16L(x + 5))$   |
| $ 2>$ |  | $-35\theta - 8\gamma - 60\gamma_s + B(x+4) - D(x^2 + 24x - 40) - 4\gamma_D(4x + 1) + H(x^3 + 60x^2 + 72x - 368) + L(x^4 + 112x^3 + 904x^2 - 1008x - 2464 \mp (120x^2 - 240x))$ | $-(10(x-2))^{1/2}[B - \frac{1}{2}\gamma - 3\lambda_D - \gamma_D(\frac{1}{2}x + 13) - D(2x + 14) + H(3x^2 + 70x + 100 \mp 12x) + 4L(x^3 + 49x^2 + 296x + 158 \mp (12x^2 + 108x))]$   | $(15x(x-2))^{1/2}(-2\gamma_D - 4D + 2H(6x + 52) + 2L(12x^2 + 288x + 824))$  |
| $ 1>$ | Symmetric  |  | $-6\lambda + 5\theta - 11\gamma - 30\gamma_s + (B - 6\lambda_D)(x + 10) - D(x^2 + 42x + 80 \mp 12x) - 2\gamma_D(11x + 50 \mp 3x) + H(x^3 + 96x^2 + 864x + 520 \mp (36x^2 + 384x)) + L(x^4 + 172x^3 + 3664x^2 + 1288x + 3200 \mp (72x^3 + 2064x^2 + 7728x))$ | $-(24x)^{1/2}[B - \frac{1}{2}\gamma + 5\gamma_s - \gamma_D(\frac{1}{2}x + 17) - 7\lambda_D - D(2x + 22) + H(3x^2 + 100x + 344) + L(4x^3 + 268x^2 + 2792x + 4648)]$                  |
| $ 0>$ |  |  |   | $-8\lambda + 30\theta - 12\gamma + (B - 8\lambda_D)(x + 12) - D(x^2 + 48x + 144) - 24\gamma_D(x + 6) + H(x^3 + 108x^2 + 1248x - 1728) + L(x^4 + 192x^3 - 4944x^2 - 24960x + 20736)$ |

Table 4.2: Equilibrium constants (in  $\text{cm}^{-1}$ ) for MnH. Numbers in parentheses represent one standard deviation in units of the last digit.

| Constant             | This work      | Ref. [37]                 |
|----------------------|----------------|---------------------------|
| $Y_{1,0}$            | 1546.84518(65) | 1546.8536(15)             |
| $Y_{2,0}$            | -27.59744(39)  | -27.60280(91)             |
| $Y_{3,0}$            | -0.309037(67)  | -0.30822(15)              |
| $Y_{0,1}$            | 5.6856789(103) | 5.685795(37)              |
| $Y_{1,1}$            | -0.1602038(70) | -0.160488(22)             |
| $10^4 Y_{2,1}$       | -1.200(40)     | 0.405(91)                 |
| $10^4 Y_{3,1}$       | -3.0252(72)    | -3.255(13)                |
| $10^4 Y_{0,2}$       | -3.05384(58)   | -3.0630(30)               |
| $10^6 Y_{1,2}$       | 1.397(22)      | 2.983(68)                 |
| $10^7 Y_{2,2}$       | -2.823(83)     | -12.01(16)                |
| $10^7 Y_{3,2}$       | -1.225(16)     | -                         |
| $10^9 Y_{0,3}$       | 9.4670(128)    | 8.68(60)                  |
| $10^9 Y_{1,3}$       | -1.551(48)     | -                         |
| $10^{12} Y_{0,4}$    | 1.360(89)      | -                         |
| $10^{13} Y_{1,4}$    | 9.16(39)       | -                         |
| $10^2 \gamma_{0,1}$  | 3.1749(35)     | 3.2055(83)                |
| $10^4 \gamma_{1,1}$  | -7.698(54)     | -8.32(13)                 |
| $10^5 \gamma_{2,1}$  | -4.100(101)    | -3.40(33)                 |
| $10^6 \gamma_{0,2}$  | -6.763(53)     | -7.54(21)                 |
| $10^7 \gamma_{1,2}$  | -2.554(98)     | -                         |
| $10^3 \lambda_{0,0}$ | -3.758(92)     | -3.35(12) <sup>a)</sup>   |
| $10^4 \lambda_{1,0}$ | -2.623(117)    | -                         |
| $10^6 \lambda_{0,1}$ | -5.39(43)      | -0.0195(27) <sup>a)</sup> |

<sup>a)</sup> Calculated from values of  $\varepsilon_{0,1}$  and  $\varepsilon_{1,1}$  listed in Ref. [30].

A few lines for certain low  $N$  values could not be fitted within the experimental uncertainty. This can be attributed to the internal hyperfine perturbations discussed by Varberg *et al.* [23]. Therefore, a larger uncertainty was assigned to those

Table 4.3: Equilibrium constants for MnD and Born–Oppenheimer breakdown parameters estimated using Eq. 4.2 (in  $\text{cm}^{-1}$ ). Numbers in parentheses represent one standard deviation in units of the last digit.

| Constant             | This work      | Ref. [38]               | Calculated <sup>a)</sup> | $\delta_{l,m}^H$              |
|----------------------|----------------|-------------------------|--------------------------|-------------------------------|
| $Y_{1,0}$            | 1104.65312(51) | 1104.65225(93)          | 1104.0017                | $\delta_{1,0}^H$ 1.8268       |
| $Y_{2,0}$            | -14.22657(31)  | -14.22656(54)           | -14.05771                | $\delta_{2,0}^H$ -0.6635      |
| $Y_{3,0}$            | -0.085848(52)  | -0.085813(90)           | -0.112351                | $\delta_{3,0}^H$ 0.14591      |
| $Y_{0,1}$            | 2.8987214 (57) | 2.898685(12)            | 2.8961972                | $\delta_{0,1}^H$ 0.009919     |
| $Y_{1,1}$            | -0.0581028(33) | -0.0580972(79)          | -0.0582427               | $\delta_{1,1}^H$ -0.159557    |
| $10^4 Y_{2,1}$       | -1.065(20)     | -0.943(31)              | -0.3115                  | $10^4 \delta_{2,1}^H$ -5.8150 |
| $10^4 Y_{3,1}$       | -0.4500(35)    | -0.4784(44)             | -0.5602                  | $10^4 \delta_{3,1}^H$ 1.1914  |
| $10^4 Y_{0,2}$       | -0.796939(190) | -0.79584(54)            | -0.79239                 | $10^4 \delta_{0,2}^H$ 0.03511 |
| $10^6 Y_{1,2}$       | 0.2543(41)     | 0.201(21)               | 0.259                    | $10^6 \delta_{1,2}^H$ -0.048  |
| $10^7 Y_{2,2}$       | -0.521(22)     | -0.897(40)              | -0.373                   | $10^7 \delta_{2,2}^H$ -2.239  |
| $10^7 Y_{3,2}$       | -0.0870(38)    | -                       | -0.1156                  | $10^7 \delta_{3,2}^H$ 0.6059  |
| $10^9 Y_{0,3}$       | 1.5713(197)    | 1.58(12)                | 1.2513                   | $10^9 \delta_{0,3}^H$ 4.8464  |
| $10^9 Y_{1,3}$       | -0.0957(30)    | -                       | -0.1463                  | $10^9 \delta_{1,3}^H$ 1.0738  |
| $10^2 \gamma_{0,1}$  | 1.6234(30)     | 1.6388(67)              | 1.6172                   |                               |
| $10^4 \gamma_{1,1}$  | -3.026(37)     | -2.954(76)              | -2.799                   |                               |
| $10^5 \gamma_{2,1}$  | -0.831(99)     | -                       | -1.06                    |                               |
| $10^6 \gamma_{0,2}$  | -1.968(39)     | -2.19(13)               | -1.755                   |                               |
| $10^3 \lambda_{0,0}$ | -1.823(55)     | -1.44(21) <sup>b)</sup> | -3.758                   |                               |
| $10^4 \lambda_{1,0}$ | -1.17(11)      | -1.33(19) <sup>b)</sup> | -1.87                    |                               |

<sup>a)</sup>Calculated from MnH constants from Table 4.2 using Eq. 4.1.

<sup>b)</sup> Calculated from values of  $\alpha_{0,1}$  and  $\alpha_{1,1}$  listed in Ref. [31].

lines. This problem affected most of the observed satellite lines as well, which is particularly disadvantageous since these lines are very useful in determining better values for the spin-spin constants. Line lists for MnH and MnD spectra are given in Appendix A. Input and output files of SPFIT program are available on ScienceDirect ([www.sciencedirect.com](http://www.sciencedirect.com)) and as part of the Ohio State University

Table 4.4: Spectroscopic constants (in  $\text{cm}^{-1}$ ) for the  $X^7\Sigma^+$  ground state of MnH. Numbers in parentheses represent one standard deviation in units of the last digit.

| Constant            | $v=0$         | $0^a)$       | 1               | 2              | 3              |
|---------------------|---------------|--------------|-----------------|----------------|----------------|
| $T_v$               | 0             | -            | 1490.644889(21) | 2923.31542(34) | 4296.15620(55) |
| $B_v$               | 5.6055050(96) | 5.605746(71) | 5.4441092(96)   | 5.2797006(106) | 5.1104876(160) |
| $10^4 D_v$          | 3.04743(57)   | 3.0413(61)   | 3.04512(62)     | 3.05665(76)    | 3.08943(128)   |
| $10^9 H_v$          | 8.639(131)    | -            | 7.532(152)      | 5.926(196)     | 3.38(39)       |
| $10^{12} L_v$       | 1.861(96)     | -            | 2.473(122)      | 3.324(174)     | 5.12(39)       |
| $\gamma_v$          | 0.031349( 36) | 0.030341(82) | 0.030497(37)    | 0.029559(38)   | 0.028548(38)   |
| $10^6 \gamma_{Dv}$  | -6.902(58)    | -11.0(12)    | -7.159(64)      | -7.399(71)     | -7.681(80)     |
| $\lambda_v$         | -0.004020(92) | -0.00325(10) | -0.004230(92)   | -0.004462(95)  | -0.004778(103) |
| $10^6 \lambda_{Dv}$ | -5.20(46)     | 0.0 (fixed)  | -5.22(49)       | -5.40(55)      | -5.32(60)      |

<sup>a)</sup> Constants for  $v=0$  from Ref. [23].

Table 4.5: Spectroscopic constants (in  $\text{cm}^{-1}$ ) for the  $X^7\Sigma^+$  ground state of MnD. Numbers in parentheses represent one standard deviation in units of the last digit.

| Constant           | $v=0$          | 1                | 2                | 3              | 4                       |
|--------------------|----------------|------------------|------------------|----------------|-------------------------|
| $T_v$              | 0              | 1075.920727(133) | 2122.616176(206) | 3139.57067(27) | 4126.0780(25)           |
| $B_v$              | 2.8696280(55)  | 2.8111700(52)    | 2.7520865(50)    | 2.6921167(51)  | 2.6310263(193)          |
| $10^5 D_v$         | 7.95559(189)   | 7.94459(167)     | 7.94981(155)     | 7.97910(153)   | 8.0685(42)              |
| $10^9 H_v$         | 1.5025(191)    | 1.4147(160)      | 1.3148(139)      | 1.2189(126)    | 1.295(27)               |
| $\gamma_v$         | 0.0164400(181) | 0.0161162(173)   | 0.0157850(166)   | 0.0154373(161) | 0.014704 <sup>a)</sup>  |
| $10^6 \gamma_{Dv}$ | -2.418(34)     | -2.410(31)       | -2.396(28)       | -2.403(25)     | -1.97 <sup>a)</sup>     |
| $\lambda_v$        | -0.001637(58)  | -0.001698(58)    | -0.001855(58)    | -0.002005(57)  | -0.002350 <sup>a)</sup> |

<sup>a)</sup> Fixed to the values calculated from Table 4.3 using Eq. 4.1

Molecular Spectroscopy Archives ([http://msa.lib.ohio-state.edu/jmsa\\_hp.htm](http://msa.lib.ohio-state.edu/jmsa_hp.htm)) as supplementary data for Ref. [44].

The Dunham constants of MnH and MnD display evidence for the breakdown of the Born–Oppenheimer approximation. In order to demonstrate this, MnD equilibrium constants were calculated from those of MnH using the reduced mass relationship:

$$Y_{l,m}^{\text{MnD}} = Y_{l,m}^{\text{MnH}} \left( \frac{\mu_{\text{MnH}}}{\mu_{\text{MnD}}} \right)^{(l+2m)/2}. \quad (4.2)$$

Calculated MnD constants are shown in Table 4.3. There is a significant difference between the constants obtained from the fit of the experimental data and the ones calculated from the MnH constants. The Born–Oppenheimer breakdown constants were estimated using Le Roy’s formalism [45]:

$$Y_{l,m}^{\text{MnD}} = \left\{ Y_{l,m}^{\text{MnH}} + \frac{M_D - M_H}{M_D} \delta_{l,m}^H \right\} \left( \frac{\mu_{\text{MnH}}}{\mu_{\text{MnD}}} \right)^{(l+2m)/2}. \quad (4.3)$$

The estimated Born–Oppenheimer breakdown constants ( $\delta_{l,m}^H$ ) obtained are also given in Table 4.3.

The fit of the new and extensive dataset has provided an improved set of constants for the ground states of MnH and MnD, and allowed us to determine higher-order expansion constants in the Dunham-type fit. The equilibrium bond distance was determined to be 1.7308601(47) Å for MnH, based on the value of  $B_e$  calculated in the fit. Our spectroscopic constants for  $v=0$  can also be compared with those of Varberg *et al.* [21] in Table 4.4. Of the series of spin-orbit parameters  $A$ ,  $\lambda$ ,  $\eta$ ,  $\theta$  (corresponding to first through fourth order in perturbation theory) only  $\lambda$  was required. For  $\Sigma$  states the constants  $A$  and  $\eta$  are zero. Varberg *et al.* [23] determined a value for  $\theta$  and for  $\gamma_s$  (a cross-term between spin-rotation and spin-spin terms) that we find unnecessary. We find that the Born–Oppenheimer breakdown correction parameters ( $\delta_{l,m}^H$ ) are relatively large, as is usually the case for metal hydrides [41].

One of the most prominent features that distinguish manganese hydride from other transition metal hydrides is a very small spin-spin interaction constant  $\lambda_e = -0.003758(92) \text{ cm}^{-1}$ . As discussed by Varberg *et al.* [23], the spin-spin interaction in the ground state of manganese hydride is a sum of the first order electron spin-spin interaction and the second order spin-orbit interaction with other states, with the latter usually dominating in other metal hydrides. The selection rules for the second order spin-orbit interaction are  $\Delta S=0,\pm 1$ ;  $\Sigma^\pm \sim \Sigma^\mp$ ;  $\Delta \Omega=0$ , hence among states known from experiment, only the  $b^5\Pi_i$  (lying at  $11\,000 \text{ cm}^{-1}$ ),  $d^5\Pi_i$  (at  $23\,000 \text{ cm}^{-1}$ )

and  $A^7\Pi_r$  (at 18 000 cm<sup>-1</sup>) states can be involved in this second order interaction. Since  $b^5\Pi_i$  arises from the  $3d^6$  electron configuration, it therefore does not interact with the  $3d^5$  ground  $^7\Sigma^+$  electronic state. The  $d^5\Pi_i$  state arises from the  $3d^5$  electron configuration, but it lies far from the ground state. This leaves the  $A^7\Pi_r$  state as the dominant perturber. The second order spin-orbit interaction between  $A^7\Pi_r$  and  $X^7\Sigma^+$  states can be expressed as [46]:

$$\lambda = \frac{|\langle A^7\Pi | \hat{H}_{SO} | X^7\Sigma^+ \rangle|^2}{E(X^7\Sigma^+) - E(A^7\Pi)} \quad (4.4)$$

The denominator of Eq. (4.4) is large (18 000 cm<sup>-1</sup>) and the numerator is relatively small, as discussed in the MnF case [46], which leads to the small value of  $\lambda$ .

The spin-rotation constant  $\gamma$  is an order of magnitude larger than  $\lambda$ , and this leads to the simple appearance of the rotational lines (Fig. 4.4). The seven spin components for each  $N$  appear in order of increasing  $J$ .

Surprisingly, no microwave experiments have been carried out yet on MnH. The rotational spectra will be complex because of fine and hyperfine structure. Every rotational level will be split into  $(2S+1)(2I_{\text{Mn}}+1)(2I_{\text{H}}+1)=84$  energy levels, where  $I_{\text{Mn}}=5/2$  and  $I_{\text{H}}=1/2$ . This will lead to many lines, overlapped due to the fact that spin-spin interaction in MnH is fairly small, as observed for the similar spectrum of MnF [46].

## 4.4 Conclusions

New infrared emission spectra of manganese hydride and deuteride were recorded at high resolution using a Fourier transform spectrometer. Improved sets of band constants and equilibrium parameters for the ground  $^7\Sigma^+$  state of MnH and MnD were determined. The Born–Oppenheimer breakdown constants ( $\delta_{l,m}^H$ ) were estimated. Our search for the manganese dihydride molecule in the gas phase was not successful.

# Bibliography

- [1] P. Bernath, A. Shayesteh, and K. Tereszchuk, *Science* **297**, 1323 (2002).
- [2] A. Shayesteh, K. Tereszchuk, R. Colin, and P. Bernath, *J. Chem. Phys.* **118**, 3622 (2003).
- [3] A. Shayesteh, D. Appadoo, I. Gordon, and P. Bernath, *J. Chem. Phys.* **119**, 7785 (2003).
- [4] A. Shayesteh, D. Appadoo, I. Gordon, and P. Bernath, *J. Am. Chem. Soc.* **126**, 14356 (2004).
- [5] A. Shayesteh, D. Appadoo, I. Gordon, and P. Bernath, *Phys. Chem. Chem. Phys.* **7**, 3132 (2005).
- [6] A. Shayesteh, S. Yu, and P. Bernath, *Chemistry - A European Journal* **11**, 4709 (2005).
- [7] R. Van Zee, T. DeVore, J. Willkerson, and W. Weltner Jr., *J. Chem. Phys.* **69**, 1869 (1978).
- [8] R. Van Zee, C. M. Brown, and W. Weltner Jr., *Chem. Phys. Lett.* **64**, 325 (1979).
- [9] J. Demuynck and H. Schaefer, *J. Chem. Phys.* **72**, 72 (1980).
- [10] J. A. Platts, *J. Mol. Struct. (Theochem)* **545**, 111 (2001).
- [11] N. Balabanov and J. Boggs, *J. Phys. Chem.* **106**, 6839 (2002).
- [12] X. Wang and L. Andrews, *J. Phys. Chem.* **107**, 4081 (2003).
- [13] A. Shayesteh, K. Walker, I. Gordon, D. Appadoo, and P. Bernath, *J. Mol. Struct.* **695**, 23 (2004).

- [14] T. Heimer, *Naturwiss.* **24**, 521 (1936).
- [15] T. Nevin, *Proc. R. Irish Acad.* **48**, 1 (1942).
- [16] T. Nevin, *Proc. R. Irish Acad.* **50**, 123 (1945).
- [17] T. Nevin, M. Conway, and M. Cranley, *Proc. Roy. Soc. (London) A* **65**, 115 (1952).
- [18] T. Nevin and P. G. Doyle, *Proc. R. Irish Acad.* **52**, 35 (1948).
- [19] T. Nevin and D. V. Stevens, *Proc. R. Irish Acad.* **55**, 109 (1953).
- [20] W. Hayes, P. McCarvill, and T. Nevin, *Proc. Roy. Soc. (London) A* **70**, 904 (1957).
- [21] T. Varberg, R. Field, and A. Merer, *J. Chem. Phys.* **92**, 7123 (1990).
- [22] T. Varberg, R. Field, and A. Merer, *J. Chem. Phys.* **95**, 1563 (1991).
- [23] T. Varberg, J. A. Gray, R. Field, and A. Merer, *J. Mol. Spectrosc.* **156**, 296 (1992).
- [24] R. Pearse and A. Gaydon, *Proc. Phys. Soc. (London)* **50**, 201 (1938).
- [25] W. Balfour, O. Launila, and L. Klynning, *Mol. Phys.* **69**, 443 (1990).
- [26] W. Balfour, *J. Chem. Phys.* **88**, 5242 (1988).
- [27] W. Balfour, B. Lindgren, O. Launila, S. O'Connor, and E. Cusack, *J. Mol. Spectrosc.* **154**, 177 (1992).
- [28] R. Van Zee, D. Garland, and W. Weltner Jr, *J. Chem. Phys.* **84**, 5968 (1986).
- [29] R. Van Zee, D. Garland, and W. Weltner Jr, *J. Chem. Phys.* **85**, 3237 (1986).
- [30] R.-D. Urban and H. Jones, *Chem. Phys. Lett.* **163**, 34 (1989).
- [31] R.-D. Urban and H. Jones, *Chem. Phys. Lett.* **178**, 295 (1991).
- [32] I. Kovács and O. Scari, *Acta Phys. Acad. Sci. Hung.* **9**, 423 (1959).
- [33] P. Pacher, *Acta Phys. Acad. Sci. Hung.* **35**, 73 (1974).
- [34] I. Kovács and P. Pacher, *J. Phys. B* **35**, 796 (1975).

- [35] G. Das, J. Chem. Phys. **74**, 5766 (1981).
- [36] S. Walch and C. Bauschlicher Jr., J. Chem. Phys. **78**, 4597 (1983).
- [37] D. Chong, S. Langhoff, C. Bauschlicher Jr, S. Walch, and H. Partridge, J. Chem. Phys. **85**, 2850 (1986).
- [38] P. Bagus and H. Schaefer III, J. Chem. Phys. **58**, 1844 (1973).
- [39] S. Langhoff, C. Bauschlicher, and A. Rendell, J. Mol. Spectrosc. **138**, 108 (1989).
- [40] J. Harrison, Chem. Rev. **100**, 679 (2000).
- [41] A. Shayesteh, D. Appadoo, I. Gordon, R. LeRoy, and P. Bernath, J. Chem. Phys. **120**, 10002 (2004).
- [42] E. U. Condon and G. Shortley, *The Theory of Atomic Spectra*, Cambridge University Press, Cambridge, England, 1951.
- [43] H. M. Pickett, J. Mol. Spectrosc. **148**, 371 (1991).
- [44] I. E. Gordon, A. Shayesteh, D. Appadoo, K. Walker, and P. Bernath, J. Mol. Spectrosc. **229**, 269 (2005).
- [45] R. J. Le Roy, J. Mol. Spectrosc. **194**, 189 (1999).
- [46] P. Sheridan and L. Ziurys, Chem. Phys. Lett. **380**, 632 (2003).

# Chapter 5

## Electronic emission spectra of CoH and CoD

### 5.1 Introduction

Molecules containing  $3d$ -transition metal atoms usually have many low-lying electronic states with complex structure due to the open  $d$ -shells. As a result the electronic spectra are complicated because of the perturbations caused by interactions of close-lying electronic states. Spectra of the cobalt-containing molecules (including cobalt monohydride) are a perfect example of such complexity.

The first observation of the electronic spectra of CoH was reported by Heimer in 1937 [1]. The spectra were recorded in emission from a King furnace (carbon tube furnace), and Heimer was able to assign two of the observed bands (at 420.3 and 449.2 nm) as the (1,0) and (0,0) bands of the  $A^3\Phi_4 \rightarrow X^3\Phi_4$  transition. Despite a suggestion in Ref. [2] (based on the electronic configuration proposed in Ref. [1]) that the ground electronic state of CoH should be a  ${}^1\Gamma$  state, it was proved in subsequent work that it is in fact a  ${}^3\Phi$  state. Klynning and co-workers [3–6] significantly extended Heimer’s results for the  $A - X$  transition by recording the (1,1) band of CoH and several bands of the corresponding system of CoD. In these experiments they were also able to observe the (0,0) transition between  $\Omega'' = \Omega' = 3$  spin components for CoH and the analogous (0,0) and (1,0) bands of CoD. However, only one parity component of the  $\Omega = 3$  transitions was observed for CoH. Smith [7] was also able to see some of these transitions in absorption behind reflected shock waves.

Later, Varberg *et al.* [8, 9] recorded several new bands via laser excitation spec-

troscopy. Two of the analyzed  $\Omega' = 4 - X^3\Phi_4$  transitions were later identified by Barnes *et al.* [10] as (3,0) and (4,0) bands of the  $A'^3\Phi_4 - X^3\Phi_4$  electronic transition. Varberg *et al.* [8] had also observed resolved fluorescence from an excited [16.0]3 state, which enabled them to find a new electronic state (presumably  ${}^3\Delta_3$ ) lying  $2469 \text{ cm}^{-1}$  above  $X^3\Phi_4$ , as well as to determine spin-orbit splitting between the  $\Omega'' = 4$  and 3 spin components as  $728(\pm 3) \text{ cm}^{-1}$ . A little later, Barnes *et al.* [10] carried out laser excitation experiments on CoH and CoD generated in a laser ablation/molecular beam source, and recorded the (0,0) to (5,0) bands of the  $A'^3\Phi_4 - X^3\Phi_4$  electronic transition. The (0,0) bands were recorded at high resolution and a hyperfine analysis was carried out for both molecules. The electron configuration of the  $A'^3\Phi$  state was found to be  $(7\sigma)^1(3d\delta)^3(3d\pi)^3(8\sigma)^1$ . In addition, Barnes *et al.* carried out resolved fluorescence experiments and determined the spin-orbit splitting in the ground state of the CoD molecule.

The  $A'^3\Phi - X^3\Phi$  transition in CoH was also studied by Ram *et al.* [11] in emission using Fourier transform spectrometer. For the  $A'^3\Phi_4 - X^3\Phi_4$  electronic transition the (0,0) and (0,1) bands were observed, while the (0,0) band was observed for the  $A'^3\Phi_3 - X^3\Phi_3$  transition, although one of its parity components was missing as it had been in Ref. [6]. Photoelectron spectroscopy of  $\text{CoH}^-$  [12] showed the existence of an excited electronic state of quintet multiplicity lying 0.8 eV above the ground state of CoH. The ground  $X^3\Phi$  electronic state of CoH was studied by laser magnetic resonance (LMR). Lipus *et al.* [13] reported the infrared spectrum of the fundamental band of the  $X^3\Phi_4$  substate, and Beaton *et al.* [14, 15] carried out far-infrared LMR experiments to perform a hyperfine analysis of the  $X^3\Phi_4$  and  $X^3\Phi_3$  substates.

The first theoretical work on CoH was reported by Chong *et al.* [16], in which some spectroscopic parameters for the ground  $X^3\Phi$  state have been predicted using the modified coupled pair functional (MCPF) method. Anglada *et al.* [17] carried out calculations mainly for the low-lying electronic states of  $\text{CoH}^+$ , but the ionization potential for the  $X^3\Phi$  state of CoH was also calculated. A set of very thorough *ab initio* calculations was performed by Freindorf *et al.* [18] in which 30 electronic states of singlet, triplet and quintet multiplicity below 4 eV were studied. The latest theoretical work was reported by Barone and Adamo [19], who calculated some properties of CoH and other first-row transition metal hydrides in order to test a new density functional method. Theoretical calculations on the CoH molecule are also currently in progress in the group of Hirano [20].

None of the aforementioned experimental studies were able to locate the  $\Omega = 2$  spin component for the ground state or for any of the observed excited electronic states. Also  $\Delta\Omega = \pm 1$  transitions were not observed at high resolution, and there

was not enough vibrational data to allow a combined-isotopologue fit of data for CoH and CoD. It was therefore decided to revisit the  $A'{}^3\Phi - X{}^3\Phi$  system in order to obtain the missing information.

In this thesis, the analysis of numerous bands of CoH and CoD in the near infrared region is reported. This work significantly extends the available vibrational and rotational information for the  $A'{}^3\Phi$  and  $X{}^3\Phi$  electronic states, allowing us to perform Dunham-type and combined isotopologue fits. The  $\Delta\Omega = -1$  transition was also observed and analyzed for the CoH molecule. In addition, new [13.3]4 –  $X{}^3\Phi_3$  and [13.3]4 –  $X{}^3\Phi_4$  transitions were observed for the CoD molecule.

## 5.2 Experimental details

About 40 g of cobalt metal was heated in the King furnace to a temperature of  $\sim 2600^\circ\text{C}$  with a mixture of hydrogen (or deuterium) and helium gases flowing slowly through the system. The total pressure inside the furnace was kept between 150 and 200 Torr. It was found that the use of argon instead of helium allows higher temperatures to be achieved, but can be harmful to the carbon heating element. A BaF<sub>2</sub> lens was employed to image emission from the King furnace onto the entrance aperture of a Bruker IFS 120 HR Fourier transform spectrometer. The CoH/D emission spectra were recorded in two parts. The region 8 000 – 15 700 cm<sup>-1</sup> was recorded using a silicon photodiode detector, a quartz beamsplitter and a 640 nm red pass optical filter that blocked the signal from the He-Ne laser of the spectrometer. The region 1 800 – 10 000 cm<sup>-1</sup> was recorded using a CaF<sub>2</sub> beamsplitter and an InSb detector cooled with liquid nitrogen. A total of 100 – 200 scans (depending on the experiment) were co-added at a resolution of 0.05 cm<sup>-1</sup> in order to obtain a good signal-to-noise ratio (S/N). An overview spectrum of CoD in the near infrared region is shown on Fig. 5.1. In order to display the bands more clearly, the baseline was corrected by eliminating the blackbody emission profile using the Bruker OPUS program.

Line positions were measured using a Windows-based program called WSpectra, written by M. Carleer (Université Libre de Bruxelles). The width of the individual lines in different bands vary from 0.05 to 0.8 cm<sup>-1</sup>. Apart from Doppler and pressure broadening, the lines are broadened by unresolved hyperfine and  $\Omega$ -doubling splittings. Significant broadening due to hyperfine structure (<sup>59</sup>Co has large nuclear spin  $I = \frac{7}{2}$  and a large magnetic moment,  $\mu = 4.627$  nuclear magnetons) is present not only in the lower  $J$  lines, but also for some higher  $J$  lines of the transitions terminating on the  $\Omega=3$  component of the ground  $X{}^3\Phi$  state (see discussion).

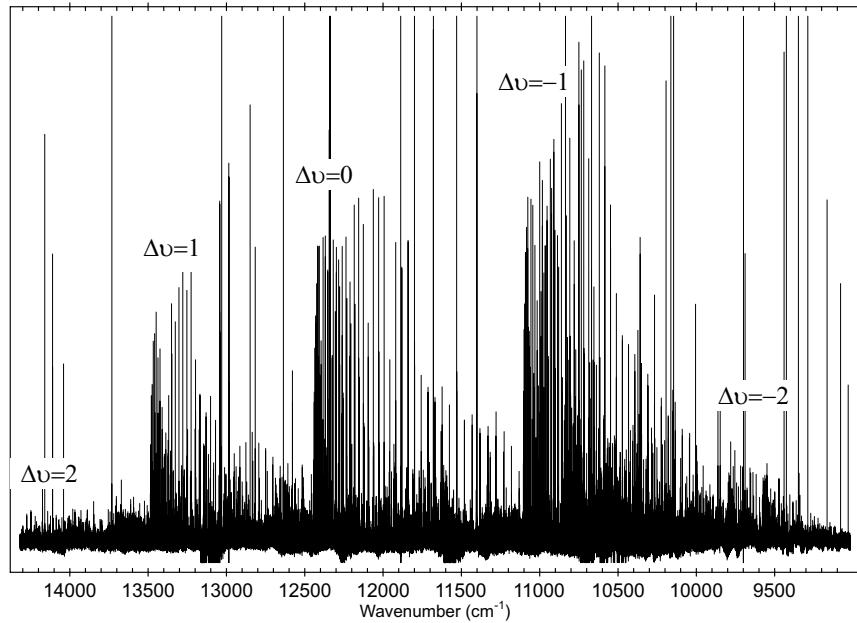


Figure 5.1: An overview spectrum of CoD after baseline correction.

The CoH spectrum in the  $8\,000 - 15\,700\text{ cm}^{-1}$  region was calibrated using lines reprinted in Ref. [11]. The corresponding spectrum of CoD was calibrated using lines common to the spectra of both molecules. The infrared part of the spectrum was calibrated using lines of HF impurity [21]. The accuracy of the measured lines is estimated to vary from  $\pm 0.002\text{ cm}^{-1}$  to  $\pm 0.01\text{ cm}^{-1}$ , depending on the S/N ratio.

### 5.3 Observations and analysis

For the  $A'^3\Phi_4 \rightarrow X^3\Phi_4$  transition of CoH, the (2,0), (1,0), (0,0), (0,1) and (1,2) bands were assigned. For the  $v'' = 0$  level the lines were followed up to  $J_e'' = 26$  for the  $e$ -parity component and  $J_f'' = 33$  for the  $f$ -parity component, for  $v'' = 1$  up to  $J_e'' = 26$  and  $J_f'' = 31$ , and for  $v'' = 2$  up to  $J_e'' = 21$  and  $J_f'' = 18$ . For the corresponding transition of CoD the (2,0), (1,0), (2,1), (0,0), (0,1), (1,2), (2,3), (0,2) and (1,3) bands were analyzed. Assignments were made up to  $J_e'' = J_f'' = 37$  for  $v'' = 0$  and 1, up to  $J_e'' = J_f'' = 22$  for  $v'' = 2$ , and up to  $J_e'' = J_f'' = 16$  for  $v'' = 3$ . For the  $A'^3\Phi_3 \rightarrow X^3\Phi_3$  transitions of both CoH and CoD and for the [13.3]4 →  $X^3\Phi_3$  and [13.3]4 →  $X^3\Phi_4$  transitions of CoD only the (0,0) bands were observed. The

(0,0) and (0,1) bands were analyzed for the  $A'^3\Phi_3 \rightarrow X^3\Phi_4$  transition of CoH. For the  $\Omega'' = 3$  component lines were found corresponding to  $J$ 's up to  $J_e'' = 16$  and  $J_f'' = 23$  for CoH and up to  $J_e'' = J_f'' = 21$  for CoD.

In all transitions with  $\Delta\Omega=0$ ,  $P$  and  $R$  branches appear to have similar relative intensities while  $Q$  branches disappear rapidly with increasing  $J$ . In the [13.3]4  $\rightarrow X^3\Phi_4$  transition in CoD the lines start to appear only from  $J=13$ , and the  $Q$  branch was not observed. The [13.3]4  $\rightarrow X^3\Phi_3$  transition has a  $P$  branch much weaker than  $R$  and  $Q$  branches. In addition, the overall intensity of this band is weaker than that of the [13.3]4  $\rightarrow X^3\Phi_4$  transition. These observations led us to the conclusion that  $\Omega'$  is equal to 4.

The  $A'^3\Phi_3 \rightarrow X^3\Phi_4$  transition of CoH has strong  $R$  and  $Q$  branches, but the  $P$  branch is so weak that we were able to assign only two  $P$ -lines. This is not consistent with a pattern one would expect for a transition with  $\Delta\Omega = -1$  where the  $P$  branch should be stronger than  $R$ , but strong interactions between close-lying states in CoH may be responsible for the deviations in the intensity pattern. Most of the recorded bands are severely perturbed, especially the ones from the [13.3]4 state in CoD. The assignments of the lines were made by the application of combination differences starting from the ground state values for CoD and CoH known from the previous experimental papers [4, 11]. We were unable to find transitions to the  $\Omega'' = 2$  component of the ground state, probably because it is extremely perturbed as suggested in Ref. [11]. There are many unassigned lines in the spectra of both molecules. The most intense unassigned bands are in the  $7500 - 8500 \text{ cm}^{-1}$  region; it is unclear what states are involved in these transitions, but certainly they are not known states. Figure 5.2 shows these unassigned bands for CoH.

Because the spectroscopic constants for  $\Omega = 3$  and  $\Omega=4$  spin components in the ground and in the excited electronic states are quite different, it was decided to use empirical Hund's case (*c*) expressions when fitting the data. We have performed band constant and Dunham-type fits for CoH and CoD separately and then a combined isotopologue fit, using the DParfit 3.3 program [22]. An experimental uncertainty of  $\pm 0.007 \text{ cm}^{-1}$  was assigned to most of the lines. The data of Heimer [1], and Klynning and Kronekvist [4, 5] were included in our fit in order to obtain a consistent set of spectroscopic constants. However, some published lines were not included in the fit because of discrepancies in the combination differences.

For the band-constant fits, we first fitted the severely perturbed upper states to individual term values, while the ground state was fitted with the following Hund's case (*c*) expression:

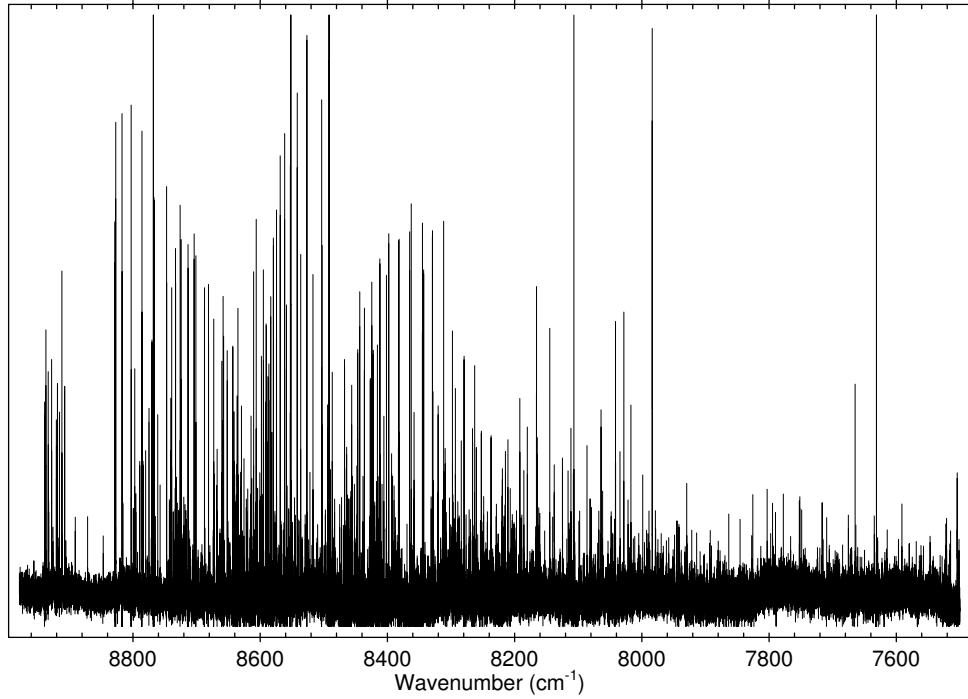


Figure 5.2: Unassigned bands of CoH at  $8000\text{ cm}^{-1}$ .

$$\begin{aligned} F_v(J) = & T_v + B_v[J(J+1) - \Omega^2] - D_v[J(J+1) - \Omega^2]^2 + H_v[J(J+1) - \Omega^2]^3 \\ & + L_v[J(J+1) - \Omega^2]^4 \pm \frac{1}{2}[J(J+1)]^\Omega \sum_{m=\Omega} q_m [J(J+1) - \Omega^2]^{m-\Omega}. \end{aligned} \quad (5.1)$$

The last term in this equation reflects the fact that the  $\Omega$ -doubling splitting increases as  $\sim J^{2\Omega}$  [23]. In particular, it implies that if  $\Omega = 3$  then the leading  $\Omega$ -doubling splitting term is  $q_H[J(J+1)]^3$ , while if  $\Omega = 4$  it would be  $q_L[J(J+1)]^4$ . The summation in Eq. 5.1 starts from the leading term and the upper limit is determined by the quality of the fit, i.e., there is no necessity to add more  $\Omega$ -doubling splitting terms if the quality of the fit is good. Note that following the common practice the  $m$ -subscript in  $q$  is replaced by the label for the mechanical rotational constant of the same order of  $J(J+1)$ .

It is interesting to observe the effect of using an  $\Omega$ -doubling constant of the incorrect order on the quality of the fit. The quality of the fit of  $N$  data  $y_{\text{obs}}(i)$  with associated uncertainties  $u(i)$  is indicated by the value of the dimensionless root mean square deviation (DRMSD),

$$\text{DRMSD} \equiv \left\{ \frac{1}{N} \sum_{i=1}^N \left[ \frac{y_{\text{calc}}(i) - y_{\text{obs}}(i)}{u(i)} \right]^2 \right\}^{1/2}, \quad (5.2)$$

in which  $y_{\text{calc}}(i)$  is the value of datum- $i$  calculated from the model. For illustrative purposes the (0,0) band of  $A'^3\Phi_4 \rightarrow X^3\Phi_4$  transition of CoH was fitted using Eq. 5.1 with only a single  $\Omega$ -doubling constant but of different orders (the number of rotational constants was the same). Fig. 5.3 shows the dependence of DRMSD on the order of the  $\Omega$ -doubling constant used, and it is clear that the best fit corresponds to the use of a  $q_L$  constant. This shows that the dependence of the DRMSD on the leading  $\Omega$ -doubling constant can be a useful tool in assigning new electronic transitions in order to determine the  $\Omega$  values of the states involved.

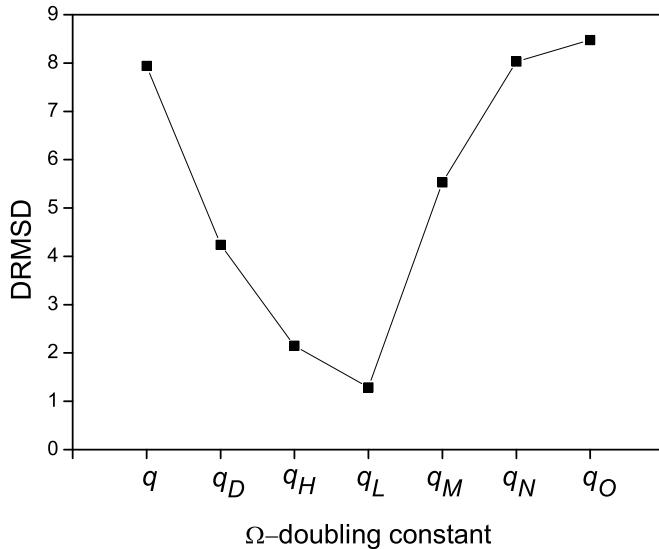


Figure 5.3: The dependence of DRMSD as defined in Eq. 5.2 on the lower state  $\Omega$ -doubling constant used to fit (0,0) band of  $A'^3\Phi_4 \rightarrow X^3\Phi_4$  transition of CoH.

The  $v = 1$  vibrational level of the  $X^3\Phi_4$  sub-state appears to be slightly perturbed between  $J'' = 13$  and  $J'' = 21$ , so the corresponding lines were fitted with larger uncertainties assigned to them. Despite the fact that the  $v = 2$  state fits well, it is probably slightly perturbed as well because the values of the constants do not follow the trend established by  $v = 0$  and  $v = 1$ .

The results of the band-constant fits for CoH and CoD are presented in Table 5.1. The modified output files of DParfit 3.3 containing line positions are given in Appendix B.

The ground state constants obtained (Table 5.1) were then held fixed, while the upper states were fitted using Eq. 5.1. Since all upper states are perturbed, we employed Watson’s “robust” fit method [24] which iteratively minimizes the contribution to the fit from the lines with large discrepancies from the model. This approach worked fairly well for CoD, but required some “manual” help for the CoH, i.e., some lines had to be assigned larger uncertainties before performing the fit. The constants for the upper states are listed in Tables 5.2 and 5.3. One can immediately note the large difference between  $B$ -values for the  $A'^3\Phi_4$  and  $A'^3\Phi_3$  spin components. This means that the  $\Omega$ -components of the excited state are mixed with the sub-states of other electronic states and the use of Hund’s case (*c*) expressions is justified.

The CoH molecule was used as a reference isotopologue for the combined-isotopologue fit of the data involving  $X^3\Phi_4$  state. The fit was carried out using following expression

$$\begin{aligned} E^\alpha(v, J) = & \sum_{m=0} \sum_{l=0} \left\{ Y_{l,m}^{(\text{CoH})} + \frac{\Delta M_H^{(\alpha)}}{M_H^{(\alpha)}} \delta_{l,m}^H \right\} (\mu_{\text{CoH}}/\mu_\alpha)^{m+l/2} \\ & \times (v + \frac{1}{2})^l [J(J+1) - \Omega^2]^m \\ & \pm \frac{1}{2} [J(J+1)]^\Omega \sum_{m=\Omega} \sum_{l=0} q_{l,m}^{(\text{CoH})} (\mu_{\text{CoH}}/\mu_\alpha)^{\Omega+m+l/2} \\ & \times (v + \frac{1}{2})^l [J(J+1) - \Omega^2]^{m-\Omega}, \end{aligned} \quad (5.3)$$

in which  $\alpha$  labels to a particular isotopologue and  $\Delta M_A^{(\alpha)}$  is the difference between the atomic mass of atom  $A$  in isotopologue- $\alpha$  and in the reference isotopologue. The Born–Oppenheimer breakdown terms are represented using the formalism of Ref. [25]. The severely perturbed upper states were fitted to individual term values. The results of this fit are presented in Table 5.4. A large number (8) of Born–Oppenheimer breakdown correction parameters ( $\delta_{l,m}^H$ ) was required, and their values are relatively large, which is usually the case for metal hydrides [26]. This fit was also carried out using “robust” routine because of the perturbations in CoH.

A Dunham-type fit was also carried out using Eq. 5.3 for each molecule separately, because the  $X^3\Phi_4$  state of the CoH molecule is slightly perturbed for  $v=1$

Table 5.1: Spectroscopic constants (in  $\text{cm}^{-1}$ ) for the  $X^3\Phi_4$  and  $X^3\Phi_3$  states of CoH and CoD. The numbers in parentheses are 95% confidence limit (approximately two standard deviations, in units of the last significant digit quoted).

| $v$             | $T_v$          | $B_v$         | $-10^4 D_v$   | $10^9 H_v$   | $10^{11} L_v$ | $10^8 q_H$  | $10^{11} q_L$ | $10^{14} q_M$ |
|-----------------|----------------|---------------|---------------|--------------|---------------|-------------|---------------|---------------|
| CoH $X^3\Phi_4$ |                |               |               |              |               |             |               |               |
| 0               | 0.0            | 7.136591(160) | -4.0096(93)   | 8.4(2.1)     | -1.34(12)     | ...         | -1.167(100)   | -8.7(1.5)     |
| 1               | 1855.3720(64)  | 6.925110(180) | -4.0672(97)   | 33.8(2.0)    | -3.47(14)     | ...         | 2.37(97)      | -5.09(13)     |
| 2               | 3641.603(95)   | 6.71168(38)   | -3.948(42)    | 61.(18)      | -18.7(2.6)    | ...         | 1.3(1.3)      | 31.(41)       |
| CoH $X^3\Phi_3$ |                |               |               |              |               |             |               |               |
| 0               | 675.564(14)    | 7.27614(21)   | -5.3253(79)   | -8.6290(130) | ...           | -169.32(25) |               |               |
| CoD $X^3\Phi_4$ |                |               |               |              |               |             |               |               |
| 0               | 0.0            | 3.719474(59)  | -1.11330(110) | 1.65(53)     | ...           | ...         | -0.00900(110) |               |
| 1               | 1338.0940(40)  | 3.641032(64)  | -1.10797(120) | 1.68(61)     | ...           | ...         | -0.01870(120) |               |
| 2               | 2640.9270(52)  | 3.56283(16)   | -1.08400(180) | ...          | ...           | ...         | -0.170(55)    |               |
| 3               | 3908.6000(120) | 3.48426(20)   | -1.0690(72)   | ...          | ...           | ...         | -0.30(37)     |               |
| CoD $X^3\Phi_3$ |                |               |               |              |               |             |               |               |
| 0               | 669.045(50)    | 3.75536(54)   | -1.1792(230)  | -7.9(4.0)    | -3.56(27)     | -0.437(110) | 8.20(26)      |               |

Table 5.2: Spectroscopic constants (in  $\text{cm}^{-1}$ ) for the excited states of CoH. Uncertainties are defined as in Table 5.1.

| $v$                | $T_v$          | $B_v$        | $-10^4 D_v$  | $10^7 H_v$ | $10^9 L_v$ | $10^8 q_H$ | $10^{10} q_L$ | $10^{13} q_M$ |
|--------------------|----------------|--------------|--------------|------------|------------|------------|---------------|---------------|
| CoH $A'^3\Phi_4$   |                |              |              |            |            |            |               |               |
| 0                  | 12358.4390(85) | 5.47693(69)  | 4.28(14)     | 1.760(73)  | ...        | ...        | 1.003(39)     | -8.30(35)     |
| 1                  | 13796.574(13)  | 5.28919(190) | 3.68(66)     | 9.33(75)   | 6.20(24)   | ...        | 5.32(55)      | -3.10(28)     |
| 2                  | 15136.047(150) | 5.1564(40)   | -8.43(33)    | 6.04(85)   | ...        | ...        | 4.72(99)      | -2.010(53)    |
| CoH $A'^3\Phi_3$   |                |              |              |            |            |            |               |               |
| 0                  | 12644.977(18)  | 6.36226(49)  | -10.6810(43) | 8.26(11)   | ...        | -5.380(68) | 1.580(32)     |               |
| CoH $A'^3\Phi_4^a$ |                |              |              |            |            |            |               |               |
| 0                  | 22243.210(43)  | 6.5197(14)   | -5.260(74)   | -3.5(1.6)  | ...        | ...        | -6.(2)        |               |

<sup>a</sup> These constants are calculated using the line lists from Ref. [1].

Table 5.3: Spectroscopic constants (in  $\text{cm}^{-1}$ ) for the excited states of CoD. Uncertainties are defined as in Table 5.1.

| $v$               | $T_v$           | $B_v$        | $-10^4 D_v$  | $10^7 H_v$  | $10^9 L_v$  | $10^8 q_H$ | $10^{10} q_L$ | $10^{13} q_M$ |
|-------------------|-----------------|--------------|--------------|-------------|-------------|------------|---------------|---------------|
| CoD $A^3\Phi_4$   |                 |              |              |             |             |            |               |               |
| 0                 | 12415.6620(37)  | 2.935920(64) | -0.3863(270) | -0.2731(40) | 0.01240(18) | ...        | 0.01547(83)   | -0.0082(69)   |
| 1                 | 13460.6260(100) | 2.90166(53)  | 6.89(73)     | -5.37(30)   | 1.230(38)   | ...        | -0.942(110)   | -3.40(31)     |
| 2                 | 14459.2060(81)  | 2.87454(27)  | 0.469(31)    | 2.100(90)   | ...         | ...        | 0.0           | ...           |
| CoD $A^3\Phi_3$   |                 |              |              |             |             |            |               |               |
| 0                 | 12687.207(250)  | 3.22093(54)  | -8.166(38)   | 20.44(11)   | -1.900(110) | 4.07(45)   | -2.00(12)     |               |
| 0                 | 13293.008(160)  | 3.6180(15)   | -14.833(48)  | 13.951(69)  | -0.5988(39) | ...        | -1.6909(15)   | 2.640(22)     |
| CoD $A^3\Phi_4^a$ |                 |              |              |             |             |            |               |               |
| 0                 | 22267.480(18)   | 3.34007(46)  | -1.076(29)   | -0.520(61)  | 0.0460(40)  | ...        | -0.0130(12)   |               |
| 1                 | 23383.261(22)   | 3.23602(67)  | -0.776(58)   | -2.06(19)   | 0.240(20)   | ...        | 1.824(11)     | -3.90(21)     |
| 2                 | 24433.450(86)   | 3.1212(51)   | -2.010(97)   | 15.(10)     | ...         | ...        | -1.10(52)     |               |
| CoD $A^3\Phi_3^a$ |                 |              |              |             |             |            |               |               |
| 0                 | 22598.221(19)   | 3.37874(38)  | -1.291(18)   | 5.0(2.1)    | ...         | 1.23(21)   | -0.760(36)    |               |
| 1                 | 23708.644(25)   | 3.27127(64)  | -1.208(41)   | -2.10(68)   | ...         | -1.60(11)  |               |               |

<sup>a</sup> These constants are calculated using the line lists from Refs. [4] and [5].

Table 5.4: Dunham-type parameters and Born-Oppenheimer breakdown parameters (in  $\text{cm}^{-1}$ ) for the  $X^3\Phi_4$  state of CoH determined from the combined-isotopologue analysis. Uncertainties are defined as in Table 5.1.

| constant                     | CoH                           | CoD                          |
|------------------------------|-------------------------------|------------------------------|
| $\tilde{T}_{v=-1/2}$         | 953.730825                    | 682.294956                   |
| $Y_{1,0}$                    | 1924.8598(230)                | 1373.4397(140)               |
| $Y_{2,0}$                    | -34.8214(150)                 | -17.7087(73)                 |
| $10^2 \times Y_{3,0}$        | 5.02(32)                      | 1.821(120)                   |
| $Y_{0,1}$                    | 7.242385(74)                  | 3.758673(73)                 |
| $Y_{1,1}$                    | -0.212336(270)                | -0.078031(82)                |
| $10^4 \times Y_{2,1}$        | 2.87(99)                      | -0.67(26)                    |
| $10^4 \times Y_{0,2}$        | -3.9856(83)                   | -1.1132(23)                  |
| $10^6 \times Y_{1,2}$        | 0.210(94)                     | -2.11(21)                    |
| $10^6 \times Y_{2,2}$        | -2.11(25)                     | 0.656(66)                    |
| $10^8 \times Y_{0,3}$        | -0.672(170)                   | 0.188(24)                    |
| $10^8 \times Y_{1,3}$        | 2.188(130)                    | 0.2055(120)                  |
| $10^{13} \times Y_{0,4}$     | -0.10(13)                     | -0.67(89)                    |
| $10^{11} \times Y_{1,4}$     | -1.910(100)                   | -0.0913(49)                  |
| $q_{0,4}$                    | $-0.56(11) \times 10^{-11}$   | $-2.36(47) \times 10^{-15}$  |
| $q_{1,4}$                    | $-3.278(180) \times 10^{-11}$ | $-1.220(67) \times 10^{-16}$ |
| $q_{2,4}$                    | $3.370(70) \times 10^{-11}$   | $1.107(23) \times 10^{-18}$  |
| $q_{0,5}$                    | $1.440(130) \times 10^{-14}$  | $4.18(39) \times 10^{-24}$   |
| $q_{1,5}$                    | $-4.120(98) \times 10^{-14}$  | $-1.054(25) \times 10^{-27}$ |
| $\delta_{1,0}^H$             | 1.273(32)                     |                              |
| $10^3 \times \delta_{2,0}^H$ | 0.310(130)                    |                              |
| $10^1 \times \delta_{0,1}^H$ | 2.90555(34)                   |                              |
| $10^3 \times \delta_{1,1}^H$ | -5.36(47)                     |                              |
| $10^3 \times \delta_{2,1}^H$ | -1.10(23)                     |                              |
| $10^5 \times \delta_{0,2}^H$ | -6.303(110)                   |                              |
| $10^5 \times \delta_{1,2}^H$ | -2.330(150)                   |                              |
| $10^5 \times \delta_{2,2}^H$ | 1.420(97)                     |                              |
| $10^8 \times \delta_{0,3}^H$ | 4.200(100)                    |                              |

and 2, and it definitely affects the combined-isotopologue fit. The results of the Dunham-type fits are presented in Table 5.4. The equilibrium bond lengths ( $r_e$ ) for CoH and CoD were found to be 1.532731(27) Å and 1.517506(13) Å, respectively. The difference between  $r_e$  values of the two isotopologues is about 1%, which is

Table 5.5: Dunham-type parameters for the  $X^3\Phi_4$  state of CoH and CoD, all in  $\text{cm}^{-1}$ . Uncertainties are defined as in Table 5.1.

| Constant                 | CoH           | CoD            |
|--------------------------|---------------|----------------|
| $\tilde{T}_{v=-1/2}$     | 953.6188875   | 682.303188     |
| $Y_{1,0}$                | 1924.5256(21) | 1373.4556(150) |
| $Y_{2,0}$                | -34.5757(76)  | -17.7063(86)   |
| $10^2 \times Y_{3,0}$    | ...           | 1.570(140)     |
| $Y_{0,1}$                | 7.24175(26)   | 3.758823(69)   |
| $10 \times Y_{1,1}$      | -2.0984(42)   | -0.78765(52)   |
| $10^3 \times Y_{2,1}$    | -0.851(160)   | 0.1480(120)    |
| $10^4 \times Y_{0,2}$    | -3.9069(140)  | -1.11661(120)  |
| $10^5 \times Y_{1,2}$    | -2.618(210)   | 0.0625(69)     |
| $10^5 \times Y_{2,2}$    | 1.045(79)     | ...            |
| $10^8 \times Y_{0,3}$    | -2.287(30)    | 0.168(63)      |
| $10^8 \times Y_{1,3}$    | 7.697(35)     | -0.0030(39)    |
| $10^8 \times Y_{2,3}$    | -2.640(120)   | ...            |
| $10^{12} \times Y_{0,4}$ | -3.8(2.2)     | ...            |
| $10^{11} \times Y_{1,4}$ | -2.03(15)     | ...            |
| $10^{11} \times q_{0,4}$ | 0.349(170)    | 0.0039(11)     |
| $10^{11} \times q_{1,4}$ | -5.118(24)    | -0.00970(57)   |
| $10^{11} \times q_{2,4}$ | -4.300(93)    | ...            |
| $10^{14} \times q_{0,5}$ | 1.14(21)      | ...            |
| $10^{14} \times q_{1,5}$ | -4.130(150)   | ...            |
| $dd$                     | 1.058         | 1.040          |

due to the breakdown of the Born–Oppenheimer approximation and to the effect of perturbations.

## 5.4 Discussion

When comparing our spectroscopic constants with those derived in previous experimental work [1, 3–11], one has to be very cautious because of the different energy level expressions used. For instance, band origins for the excited  $A'^3\Phi_4$  state reported by Barnes *et al.* [10] and Ram *et al.* [11] differ by as much as  $\sim 30 \text{ cm}^{-1}$ . However, this is merely because Ram *et al.* [11] did not include the term  $\Omega^2$  in the rotational angular momentum factor  $[J(J+1) - \Omega^2]$  in their versions of Eq. 5.1.

One can compare values of the spin-orbit splitting in the ground state obtained in this work with values determined in the laser experiments [8, 10]. If one considers the ground-state term values of CoH calculated using constants from Table 5.1, the difference between the energy levels  $J = 4$  in  $\Omega = 3$  and  $J = 4$  in  $\Omega = 4$  is found to be  $726.996 \text{ cm}^{-1}$ , which is in excellent agreement with the value of  $728 (\pm 3) \text{ cm}^{-1}$  reported in Ref. [8]. However for CoD our difference between  $J = 4$  in  $\Omega = 3$  and  $J = 4$  in  $\Omega = 4$  levels is found to be  $695.464 \text{ cm}^{-1}$ , which is significantly different from the value of  $729 (\pm 2) \text{ cm}^{-1}$  reported by Barnes *et al.* [10]. The reason for this discrepancy is not yet understood.

The fact that only one parity component of the  $X^3\Phi_3$  state of the CoH molecule is perturbed leads to the assumption that the perturbing state has only one parity component. *Ab initio* calculations [18] predict a  $^3\Sigma^-$  state  $0.14 \text{ eV}$  above the ground electronic state. This state has a  $0^+$  spin component of *e*-parity and we believe that despite the difference in  $\Omega$ -values, it is a perturber of the  $X^3\Phi_3$  state. That means that the perturbed levels belong to the *e*-parity component, and this makes it possible to assign the parities of all observed energy levels in the ground and excited electronic states. The tentative parity assignment of the levels given in Ref. [11] has to be changed to satisfy the arguments above. Also, one can assume that the  $0^+$  spin component of the  $^3\Sigma^-$  is located  $\sim 700 \text{ cm}^{-1}$  above the  $X^3\Phi_4$  state. Nevertheless, it should be noted that since the *e* and *f* levels of the same  $J$  of the  $\Omega=1$  component of the  $^3\Sigma^-$  state are widely separated, one of these components could also be responsible for perturbing only one parity component of the  $X^3\Phi_3$  sub-state.

The anomalous broadening of the high- $J$  lines of the transitions terminating on the  $X^3\Phi_3$  state that was observed in this work was also noticed by Klynnings and Kronekvist [5] in the  $A^3\Phi_3$ -  $X^3\Phi_3$  transition of CoH. They suggested that it may be caused by predissociation of the upper state. However, the experiments in Ref. [5] were done in absorption, and since we are observing the same broadening in emission it is unlikely that it is caused by predissociation. More likely, this broadening is evidence for hyperfine perturbations which were also observed in the  $X^3\Phi_3$  state of the CoCl molecule by Flory *et al.* [27]. In the case of CoCl it was suggested that these perturbations are caused by second-order spin-orbit mixing with a nearby isoconfigurational  $^1\Phi_3$  state, but theoretical predictions [18] suggest that for the CoH molecule  $^1\Phi$  state is located  $2.60 \text{ eV}$  above the ground state; therefore, that state can not be responsible for the hyperfine perturbations.

The [13.3]4 state of CoD observed in this work is most probably a  $^1\Gamma_4$  state, as it is the only state within  $5000 \text{ cm}^{-1}$  that has an  $\Omega=4$  spin component, according to theory [18]. Fig. 5.4 illustrates electronic states of CoH molecule observed in all

previous optical experiments [1, 3–11] and this work. The transitions observed in this work are marked with arrows. The [15.5]3, [16.0]3 and [16.6]3 states observed in Ref. [9] are probably higher vibrational levels of the  $A'^3\Phi_3$  and  $^1\Gamma_3$  states.

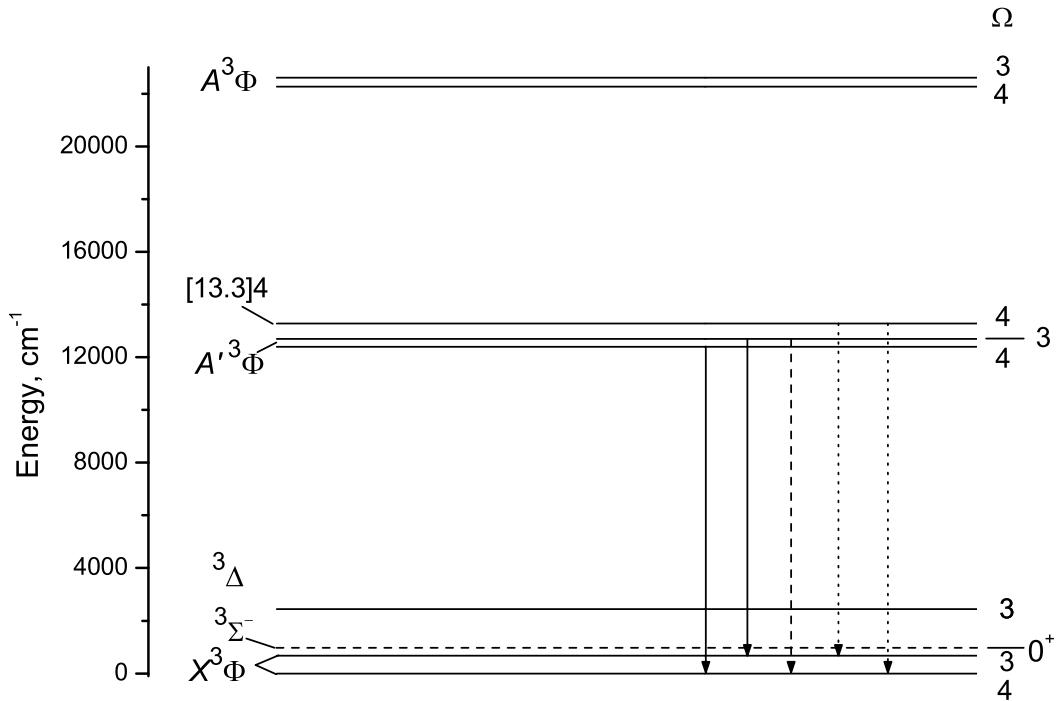


Figure 5.4: An energy level diagram showing the electronic states found in the Refs. [1, 3–11] and this work. The transitions observed in this work are marked with arrows. The solid arrows correspond to transitions observed for both CoH and CoD, dash arrows-only for CoH and dot arrows-only for CoD.

## 5.5 Conclusions

The Fourier transform emission spectra of CoH and CoD have been investigated in the near infrared region. A detailed analysis of bands of the  $A'^3\Phi \rightarrow X^3\Phi$  tran-

sitions in both molecules has provided an improved set of ground state band and Dunham-type constants for the  $\Omega=4$  component. A combined-isotopologue fit was also performed for the  $X^3\Phi_4$  spin component. The global fit of all transitions (including those from the previous optical experiments) has provided more precise values for the spin-orbit splittings between  $\Omega=4$  and  $\Omega=3$  in the ground and excited electronic states. We find no trace of any spin components with  $\Omega=2$ . This is probably due to the fact that these sub-states are more perturbed than those with higher  $\Omega$ -values because there are more possible perturbers available (according to the *ab initio* calculations [18]).

# Bibliography

- [1] A. Heimer, Z. Physik **104**, 448 (1937).
- [2] G. Herzberg, *Spectra of Diatomic Molecules*, Van Nostrand, New York, 1950.
- [3] L. Klynning and H. Neuhaus, Z. Naturforsch. **18**, 1142 (1963).
- [4] L. Klynning and M. Kroneqvist, Physica Scripta **6**, 61 (1972).
- [5] L. Klynning and M. Kroneqvist, Physica Scripta **7**, 72 (1973).
- [6] L. Klynning and M. Kroneqvist, Physica Scripta **24**, 21 (1981).
- [7] R. E. Smith, Proc. Roy. Soc. (London) A **322**, 113 (1973).
- [8] T. D. Varberg, E. J. Hill, and R. W. Field, J. Mol. Spectrosc. **138**, 630 (1989).
- [9] T. D. Varberg, PhD thesis, MIT, Cambridge, MA, 1992.
- [10] M. Barnes, A. J. Merer, and G. F. Metha, J. Mol. Spectrosc. **173**, 100 (1995).
- [11] R. S. Ram, P. F. Bernath, and S. P. Davis, J. Mol. Spectrosc. **175**, 1 (1996).
- [12] A. E. S. Miller, C. S. Feigerle, and W. C. Lineberger, J. Chem. Phys. **87**, 1549 (1987).
- [13] K. Lipus, T. Nelis, E. Bachem, and W. Urban, Mol. Phys. **68**, 1171 (1989).
- [14] S. A. Beaton, K. M. Evenson, T. Nelis, and J. M. Brown, J. Chem. Phys. **89**, 4446 (1988).
- [15] S. A. Beaton, K. M. Evenson, and J. M. Brown, J. Mol. Spectrosc. **164**, 395 (1994).

- [16] D. Chong, S. Langhoff, C. Bauschlicher Jr, S. Walch, and H. Partridge, J. Chem. Phys. **85**, 2850 (1986).
- [17] J. Anglada, P. J. Bruna, and F. Grein, J. Chem. Phys. **92**, 6732 (1990).
- [18] M. Freindorf, C. M. Marian, and B. A. Hess, J. Chem. Phys. **99**, 1215 (1993).
- [19] V. Barone and C. Adamo, Int. J. Quant. Chem. **61**, 443 (1997).
- [20] T. Hirano, private communication.
- [21] R. B. Le Blanc, J. B. White, and P. F. Bernath, J. Mol. Spectrosc. **164**, 574 (1994).
- [22] R. J. L. Roy, *DParFit 3.3: A Computer Program for Fitting Multi-Isotopologue Diatomic Molecule Spectra*, University of Waterloo Chemical Physics Research Report CP-660 (2005). <http://leroy.uwaterloo.ca>.
- [23] J. M. Brown and A. Carrington, *Rotational Spectroscopy of Diatomic Molecules*, Cambridge University Press, Cambridge, U.K., 2003.
- [24] J. K. G. Watson, J. Mol. Spectrosc. **219**, 326 (2003).
- [25] R. J. Le Roy, J. Mol. Spectrosc. **194**, 189 (1999).
- [26] A. Shayesteh, D. Appadoo, I. Gordon, R. LeRoy, and P. Bernath, J. Chem. Phys. **120**, 10002 (2004).
- [27] M. Flory, D. T. Halfen, and L. M. Ziurys, J. Chem. Phys. **121**, 8385 (2004).

# Chapter 6

## Fourier transform spectroscopy of ytterbium monoxide

### 6.1 Introduction

A considerable interest in lanthanide-containing molecules has arisen during past two decades [1]. For diatomic molecules, the lanthanide monoxides were studied most extensively, both theoretically and experimentally. The spectra are difficult to interpret because of the huge number of electronic states arising from open  $4f$  configurations. Moreover, large spin-orbit coupling effects split and mix the various spin components that arise from the numerous  $^{2S+1}\Lambda$  terms. The only remaining good quantum numbers are thus  $J$  and  $\Omega$ , in the absence of nuclear spin. *Ab initio* calculations thus need to include relativistic effects before any meaningful comparison with experiment can be made.

The first experimental work on YbO, apart from band head positions found in the Vatican plates [2], was by Linton *et al.* [3]. They recorded a number of visible bands by laser excitation spectroscopy and examined some of the low-lying states by dispersing the laser-induced fluorescence. The ground state of YbO was found to be  $X^1\Sigma^+$ , arising from the  $4f^{14} \text{Yb}^{2+}$  configuration, as predicted from a ligand-field calculation [3, 4] on  $\text{Yb}^{2+}\text{O}^{2-}$ . Such a closed-shell ground state was unusual because all lanthanide oxides except EuO and YbO have ground states that arise from  $M^{2+} 4f^n 6s^1$  configurations rather than  $4f^{n+1}$  configurations [4, 5]. The extra stability of the half-filled  $4f^7 \text{Eu}^{2+}$  and the filled  $4f^{14} \text{Yb}^{2+}$  leads to  $X^8\Sigma^-$  and  $X^1\Sigma^+$  ground states, respectively, for EuO and YbO.

The combination of ligand field theory [4, 5] and laser spectroscopy [3, 6] has led

to a rather satisfactory picture of the first few low-lying electronic states of YbO. In spite of a large number of papers [7–14], *ab initio* calculations do not predict a  $X^1\Sigma^+$  ground state but rather a  $0^-$  ground state that correlates with the  $4f^{13}6s^1$  configuration of  $\text{Yb}^{2+}$ . Experimentally, this  $0^-$  state is found at just  $910\text{ cm}^{-1}$  above the  $X^1\Sigma^+$  state [6], so it is not surprising that calculations have difficulty obtaining the correct energy ordering. There is also substantial configuration mixing between the  $4f^{13}1\sigma^22\sigma^21\pi^43\sigma^1$  and  $4f^{14}1\sigma^22\sigma^21\pi^4$  configurations (i.e.,  $4f^{13}6s^1$  and  $4f^{14}$  on  $\text{Yb}^{2+}$ ) in the ground state, as deduced from the dipole moment of  $5.89\text{ D}$  [15]. The most recent experimental work was the detection of the infrared vibrational fundamentals of both YbO and  $\text{YbO}^+$  in an argon matrix [16]. The excited states of YbO seen in the visible bands are ascribed to states correlating with the  $4f^{13}5d^1$  and  $4f^{13}6p^1$  configurations of  $\text{Yb}^{2+}$ , as well as to charge transfer states associated with  $\text{Yb}^+\text{O}^-$  [6]. The details are uncertain, however, and it would be helpful to locate additional transitions in the near infrared region where the density of states is lower. We, therefore, report the observation of 8 new bands near 1 micron. A rotational analysis was possible for 3 of these bands.

## 6.2 Experimental Arrangement

Gas-phase YbO was generated in a Broida-type oven [17] by the reaction of ytterbium metal vapor with  $\text{N}_2\text{O}$ . About 10 g of ytterbium metal was resistively heated in an alumina crucible with a current of about 45 A. A flow of argon gas carried the Yb metal vapor from the crucible to the reaction region where it was mixed with the oxidant gas. The partial pressures of the argon and nitrous oxide were adjusted to optimize the reddish chemiluminescent flame. Total pressures in the oven were approximately 6 – 8 Torr, with the oxidant gas making up a small fraction of this total. Little can be said about the exact chemistry inside the flame, but the mechanism of reaction is straightforward. The  $\text{N}_2\text{-O}$  bond dissociation energy is 70 kcal/mole, while the dissociation energy of YbO is  $\sim$ 100 kcal/mole [18] and the exothermic reaction proceeds quite readily. For the reaction of  $\text{N}_2\text{O}$  with ytterbium metal  $\Delta H = -30\text{ kcal/mole}$  [19]. The energy released is available to cause excited electronic states to be populated, and is responsible for the observed chemiluminescence.

The chemiluminescence from the flame was imaged onto the entrance aperture of a Bruker IFS 120 HR Fourier transform spectrometer. The YbO emission spectrum was recorded in the range  $9\,000$ - $12\,000\text{ cm}^{-1}$  using a silicon photodiode detector. An 800 nm red pass filter was used to eliminate the signal from the He-Ne laser of the spectrometer. To obtain a good signal-to-noise ratio (S/N), a total of 50

scans were co-added at a resolution of  $0.04\text{ cm}^{-1}$ . Line positions were measured using a Windows-based program called WSpectra, written by Dr. Michel Carleer (Laboratoire Chimie Physique Moléculaire, Université Libre de Bruxelles, Belgium). A zero filling factor of 4 was used to generate enough points for good data reduction, and Voigt lineshape functions were fitted to the observed rotational lines. For calibration, argon atomic lines were recorded from an argon pen lamp immediately after the experiment and compared to the list of Norlén [20]. The accuracy of measurements in similar previous work of this nature is typically  $0.005\text{ cm}^{-1}$  (or better) for strong, unblended lines.

## 6.3 Results and Discussion

An overview of YbO chemiluminescence spectrum obtained in the present work is displayed in Figure 6.1. A total of 8 red-degraded bands were identified in the  $9800 - 11300\text{ cm}^{-1}$  region . However due to the presence of several isotopomers, as well as perturbations in some of the bands, only 3 were rotationally analyzed. The bandhead positions of all the observed bands are listed in Table 1, along with the band origins for the 3 analyzed systems.

Table 6.1: Observed YbO bandhead positions ( $\text{cm}^{-1}$ ).

| Bandhead | Type    | Band origin | Note      |
|----------|---------|-------------|-----------|
| 9888.40  | R-head  | —           | —         |
| 10200.28 | R-head? | —           | —         |
| 10256.08 | Q-head  | 10256.11    | System 1  |
| 10537.02 | R-head  | —           | —         |
| 10862.66 | R-head  | —           | —         |
| 10963.13 | R-head  | —           | perturbed |
| 10992.03 | R-head  | 10943.04    | System 2  |
| 11200.26 | R-head  | 11196.90    | System 3  |

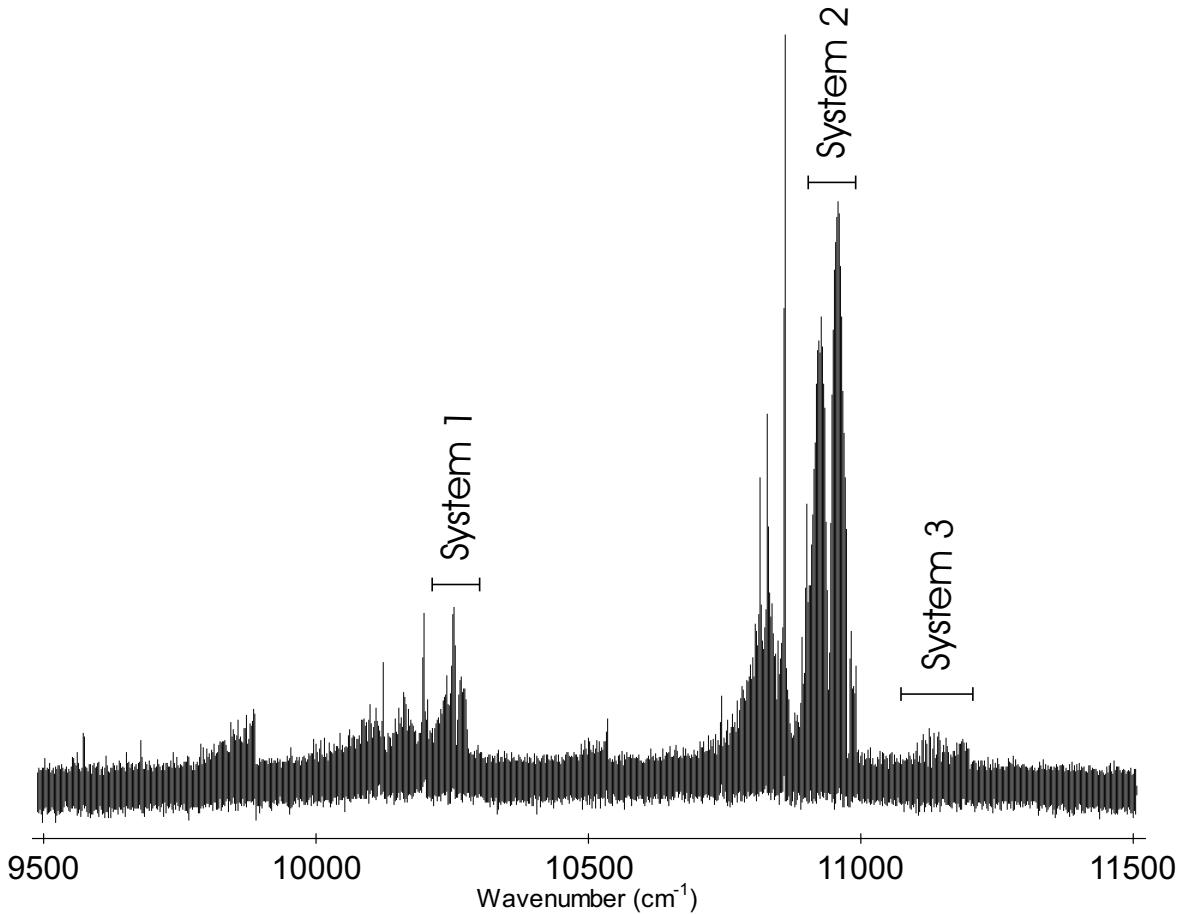


Figure 6.1: An overview of the emission spectrum of YbO.

Once the spectrum was recorded and measured, preliminary assignments of the rotational numbering were achieved by using graphical methods [21]. Since the splitting of the spectral lines due to the different isotopes was not resolved the analysis (by convention) was assumed to be for the principal isotopologue (<sup>174</sup>YbO). In addition, for systems 1 and 2 it was possible to observe the “first lines” of the bands, which confirmed our initial rotational assignments. System 1 has a simple P-Q-R branch structure, which is typical for a  $^1\Pi - ^1\Sigma$  transition, while systems 2 and 3 possess only P- and R-branches, indicative of a  $^1\Sigma - ^1\Sigma$  transition. The data for system 3 and the combined data for the systems 1 and 2 were then employed in least-squares fits that contained the usual analytical expressions for  $^1\Sigma^+$  and  $^1\Pi$  states.

$$F_v(J) = \nu_0 + BJ(J+1) - D[J(J+1)]^2 + H[J(J+1)]^3 \quad (6.1)$$

$$\begin{aligned} F_v(J) = & \nu_0 + BJ(J+1) - D[J(J+1)]^2 + H[J(J+1)]^3 \\ & \pm \frac{1}{2}\{qJ(J+1) + q_D[J(J+1)]^2\}. \end{aligned} \quad (6.2)$$

For the lower states, the fitted parameters were the rotational parameters  $B$  and  $D$ , and for upper states: the band origin,  $\nu_0$ , rotational parameters  $B, D$  and  $H$ , and the lambda-doubling parameters,  $q$  and  $q_D$  for system 1.

*System 1:*  $\nu_0 = 10\,256 \text{ cm}^{-1}$

As mentioned above, this band has a simple P-Q-R branch structure, and no perturbations were identified in the observed  $J$ -range ( $1 \leq J \leq 50$ ). In total, more than 100 lines were assigned for this band. By comparing combination differences for the lower state to those from the work of Linton *et al.* [3], it was determined that this band connects to the  $X^1\Sigma^+ v=0$  level.

*System 2:*  $\nu_0 = 10\,943 \text{ cm}^{-1}$

System 2 has the best S/N of all of the observed bands, and the first lines of this system were easily identified. Furthermore, a strong perturbation was immediately obvious in the spectrum at high- $J$  (see Figure 6.2). The perturbation appears to be a classic level crossing, although attempts to assign the more severely perturbed lines were met with frustration. The shifts in the line positions indicate that the perturber's origin lies at higher energy, but the identity of the perturbing state is unknown. Assignments were made for both branches up to  $J' = 55$  and it is believed the perturbation occurs at  $J' \geq 56$ .

Because we were unable to completely assign the perturbation, the perturbed lines were omitted from the data set in order to obtain a satisfactory fit. The lower state of this band was found to be the  $X^1\Sigma^+ v=0$  level.

*System 3:*  $\nu_0 = 11\,197 \text{ cm}^{-1}$

Of the 3 analyzed bands, system 3 had the poorest S/N, and we were only able to assign about 60 lines to  $^{174}\text{YbO}$ . Least-squares fitting of the data revealed a perturbation at high- $J$ , occurring at  $J' \geq 44$ . As with system 2, the more severely perturbed lines were omitted from the final least-squares fits. It should be noted that the perturbation found in this band is not due to system 1, that is, they are

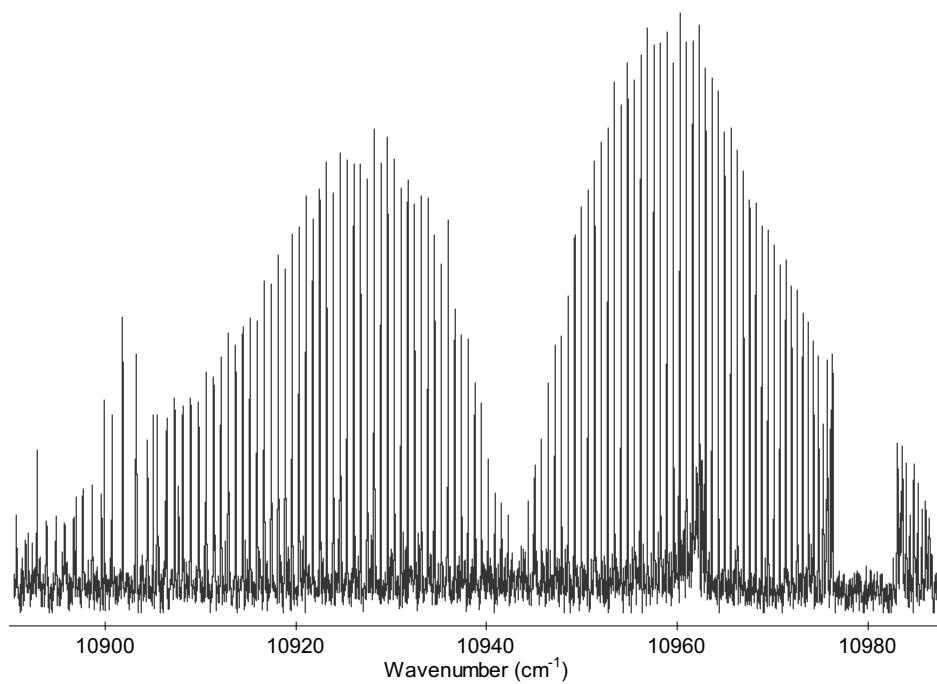


Figure 6.2: The observed YbO chemiluminescence spectrum of the strongest band with a perturbation clearly visible in the R-branch near  $10980\text{ cm}^{-1}$ .

not the same perturbation. The lower state of this band was determined to be the  $X^1\Sigma^+$   $v=1$  level located  $683.107\text{ cm}^{-1}$  above  $v=0$  [3].

The molecular parameters for all 3 of the bands analyzed in the present work are summarized in Table 2. A complete list of the line positions used in the fits, as well as residuals between the measured lines and those calculated using the parameters in Table 2, is available in Appendix C. Our ground state rotational constants are in agreement with those of Linton *et al.* [3].

The standard deviations of the fits were on the order of  $0.005\text{ cm}^{-1}$ , indicating that the deviations between the calculated and measured line positions were consistent, on average, with the estimated measurement precision.

The results from the study of YbO by McDonald *et al.* [6], which includes laser-induced fluorescence results and ligand field predictions, can shed some light on the transitions observed in the present study. In their work, McDonald *et al.* showed that the ground state of YbO arises primarily from the  $\text{Yb}^{2+}(4f^{14})\text{O}^{2-}$  electronic

Table 6.2: Molecular parameters ( $\text{cm}^{-1}$ ) for the observed  $^{174}\text{YbO}$  bands.

| Parameter    | System 1       | System 2            | System 3            |
|--------------|----------------|---------------------|---------------------|
| $v_0$        | 10256.1246(19) | 10943.0413(20)      | 11196.9197(30)      |
| $B'$         | 0.346383(30)   | 0.350130(30)        | 0.310778(47)        |
| $10^7 D'$    | 4.99(12)       | 4.27(15)            | 2.31(27)            |
| $10^{11} H'$ | -1.53(17)      | -6.71(36)           | -22.84(81)          |
| $10^4 q'$    | -9.516 (4)     | -                   | -                   |
| $10^8 q_D'$  | 4.59 (21)      | -                   | -                   |
| $B''$        | 0.350326(27)   |                     | 0.346116(48)        |
| $10^7 D''$   |                | 3.91(9)             | 4.45(23)            |
| Lower state  |                | $X^1\Sigma^+ v = 0$ | $X^1\Sigma^+ v = 1$ |

configuration. In addition, they investigated the manifold of electronic states arising from the  $\text{Yb}^{2+}(4f^{13}6s)\text{O}^{2-}$  configuration. Based on the magnitude of the rotational constant,  $B$ , for the upper state of system 3 from the present work, it seems unlikely that it arises from the  $f^{13}s$  configuration, since all of the observed  $f^{13}s$  states in the work of McDonald *et al.* have  $B \approx 0.35 \text{ cm}^{-1}$ . Also noted by those authors is the fact that all states with  $f^{13}s$  electronic configurations have a vibrational spacing of about  $830 \text{ cm}^{-1}$ . In the present work, unfortunately, we have observed only one vibrational level, and therefore could not determine a vibrational spacing for any of the observed states. At this point it is unclear what type of electronic configuration would give rise to a rotational parameter with a value similar to that observed for the upper state of system 3 ( $B' \approx 0.31 \text{ cm}^{-1}$ ,  $r \sim 1.92 \text{ \AA}$ ). Unlike system 3, both systems 1 and 2 have  $B' \approx 0.35 \text{ cm}^{-1}$  ( $r \sim 1.81 \text{ \AA}$ ), so it is plausible that these upper states could arise primarily from the  $\text{Yb}^{2+}(f^{13}s)\text{O}^{2-}$  electronic configuration. Interestingly, the ligand-field fit of the low-lying states in  $\text{YbO}$  by McDonald *et al.* [6] predicts that an electronic state with  $\Omega = 0^+$  will lie at  $11981 \text{ cm}^{-1}$  and one with  $\Omega = 1$  at  $11675 \text{ cm}^{-1}$ . These calculated states are close to the states observed in the present work in which system 2 ( $\Omega = 0^+$ ) lies at about  $11000 \text{ cm}^{-1}$  and system 1 ( $\Omega = 1$ ) at about  $10250 \text{ cm}^{-1}$ .

After our work was completed we learned of an unpublished ligand field calculation for  $\text{YbO}$  that uses relativistic atomic wavefunctions [22]. The use of relativistic

wavefunctions rather than the usual non-relativistic electronic wavefunctions cause small shifts in the YbO energy levels. For example the  $\Omega = 0^+$  and 1 states from the  $\text{Yb}^{2+}(f^{13}s)\text{O}^{2-}$  configuration predicted by McDonald *et al.* [6] shift from  $11\,981\text{ cm}^{-1}$  and  $11\,675\text{ cm}^{-1}$  to  $11\,884\text{ cm}^{-1}$  and  $11\,708\text{ cm}^{-1}$ , respectively.

Kaledin *et al.*'s calculations [22] show that the states arising from the  $\text{Yb}^{2+}(f^{13}p)\text{O}^{2-}$  and  $\text{Yb}^{2+}(f^{13}d)\text{O}^{2-}$  configurations lie too high in energy to be responsible for any of our new states, although the integer charge model may not be very reliable for these configurations. However, the singly charged configurations  $\text{Yb}^{1+}(f^{14}s)\text{O}^{1-}(p^5)$  and  $\text{Yb}^{1+}(f^{13}s^2)\text{O}^{1-}(p^5)$  give rise to a number of electronic states in the  $10\,000\text{-}13\,000\text{ cm}^{-1}$  region. In particular, the  $\text{Yb}^{1+}(f^{14}s)\text{O}^{1-}(p^5)$  configuration has a  $[12.3]1$  ( $A'^1\Pi_1$ ) state at  $12\,283\text{ cm}^{-1}$ ,  $[12.0]0$  ( $a^3\Pi_0$ ) at  $12\,026\text{ cm}^{-1}$  and  $[11.9]1$  ( $a^3\Pi_1$ ) at  $11\,950\text{ cm}^{-1}$ , while the  $\text{Yb}^{1+}(f^{13}s^2)\text{O}^{1-}(p^5)$  configuration has states with  $\Omega = 2,1,1,0,0$  (probably  ${}^3\Pi$  and  ${}^1\Pi$  states) around  $12\,565\text{ cm}^{-1}$ . The square bracket notation corresponds to  $[\text{T}_0]\Omega$ , and the  $A'$  and  $a$  notation is based on a comparison with CaO [22]. The upper state of system 3 probably originates from one of the singly charged  $\text{Yb}^+$  configurations, and the  $A'^1\Pi$  state at  $12\,283\text{ cm}^{-1}$  is a plausible match. Note, however, that the  $A^1\Sigma^+$  state of YbO with  $r = 2.062\text{ \AA}$  is attributed to the same  $\text{Yb}^{1+}(f^{14}s)\text{O}^{1-}(p^5)$  configuration as the  $A'^1\Pi$  state, and hence should have the same bond length, while the observed  $r$  value for the upper state of system 3 is only  $1.92\text{ \AA}$ .

In conclusion, we have made the first observation of several electronic transitions in the near-infrared spectrum of YbO using Fourier transform emission spectroscopy. A rotational analysis of three transitions identified the lower states as the ground electronic state of YbO. While two of the upper states involved in the transitions appear to arise primarily from the  $f^{13}s$  electronic configuration, it is unclear which configuration gives rise to the third observed state. Additional calculations, both ligand field and *ab initio*, are required to provide more information about low-lying states. Experimental work for transitions in infrared region will be very helpful as well.

# Bibliography

- [1] M. Dolg and H. Stoll, *Electronic Structure Calculations for Molecules Containing Lanthanide Atoms*, volume 22, Elsevier, Amsterdam.
- [2] A. Gatterer, J. Junkes, E. Salpeter, and B. Rosen, *Molecular Spectra of Metallic Oxides*, Specola Vaticana, Vatican City, 1957.
- [3] C. Linton et al., *J. Mol. Spectrosc.* **101**, 332 (1983).
- [4] M. Dulick, E. Murad, and R. Barrow, *J. Chem. Phys.* **85**, 385 (1986).
- [5] P. Carette and A. Hocquet, *J. Mol. Spectrosc.* **131**, 301 (1988).
- [6] S. A. McDonald, S. Rice, R. Field, and C. Linton, *J. Chem. Phys.* **93**, 7676 (1990).
- [7] M. Dolg and H. Stoll, *Theor. Chem. Acta* **75**, 369 (1989).
- [8] M. Dolg, H.-J. Flad, H. Stoll, and H. Preuss, *J. Chem. Phys.* **97**, 1162 (1992).
- [9] M. Dolg, H. Stoll, and H. Preuss, *Theor. Chem. Acta* **85**, 441 (1993).
- [10] S. G. Wang and W. Schwarz, *J. Phys. Chem.* **99**, 11687 (1995).
- [11] S. G. Wang, D. K. Pan, and W. Schwarz, *J. Chem. Phys.* **102**, 9296 (1995).
- [12] W. Liu, G. Hong, D. Dai, L. Li, and M. Dolg, *Theor. Chem. Acc.* **96**, 75 (1997).
- [13] W. Liu, M. Dolg, and L. Li, *J. Chem. Phys.* **108**, 2886 (1998).
- [14] X. Cao, W. Liu, and M. Dolg, *Science in China (Series B)* **31**, 6 (2001).
- [15] T. C. Steimle, D. M. Goodridge, and C. Linton, *J. Chem. Phys.* **107**, 3723 (1997).

- [16] S. Willson and L. Andrews, J. Phys. Chem. **103**, 6972 (1999).
- [17] J. West, R. Bradford, J. D. Eversole, and C. Jones, Rev. Sci. Instr. **46**, 164 (1975).
- [18] C. B. Cosmovici et al., Chem. Phys. Lett. **47**, 241.
- [19] S. McDonald, PhD thesis, MIT, Cambridge, MA, 1985.
- [20] G. Norlén, Physica Scripta **8**, 249.
- [21] G. Herzberg, *Spectra of Diatomic Molecules*, Van Nostrand, New York, 1950.
- [22] L. Kaledin, M. Heaven, and R. W. Field, unpublished manuscript.

# Chapter 7

## Electronic spectra of europium monohydride

### 7.1 Introduction

The lanthanide hydrides have attracted recently much interest because of their use in semiconducting and magnetic materials [1, 2]. Lanthanide metals are also being considered as hydrogen storage materials [3]. It is therefore important to study small lanthanide hydrides in order to extend our knowledge of the hydrogen chemistry of these compounds.

Unfortunately, spectroscopic experiments with rare-earth metals are difficult. Apart from the fact that lanthanides are expensive, they are also very reactive, and it is hard to control the chemistry during an experiment. Gas-phase experiments are also difficult due to the low vapor pressures of most of these metals at the temperatures that can be achieved by conventional methods. When the experiments are successful, the interpretation of the obtained spectra is also difficult. The main reason is that the partially filled  $4f$  orbitals of lanthanide metal atoms result in many low-lying molecular electronic states with complex structures. The great number of these states results in band overlaps in electronic spectra in addition to perturbations caused by interactions between the states. *Ab initio* calculations are not straightforward, because of the necessity of including relativistic and electron correlation effects when dealing with the atoms of heavy rare earth elements.

So far, the only lanthanide metal hydrides that have been studied in the gas phase are YbH and LuH [4–11]. Matrix isolation experiments were carried out by Willson and Andrews [12], who studied the vibrational fundamentals of several

lanthanide metal polyhydrides as well as of NdH, CeH and TbH. In the experiments with europium metal, only EuH<sub>2</sub> and EuH<sub>3</sub> molecules were observed.

The first theoretical investigation of rare earth hydrides was carried out by Pyykkö [13] who estimated some spectroscopic parameters of LuH and TmH using Hartree-Fock (HF) and Dirac-Hartree-Fock (DHF) calculations. A series of pseudopotential calculations on rare earth oxides, hydrides and halides were reported by Dolg and co-workers [14–17]. Most of these calculations were performed with nonrelativistic pseudopotentials, but for some molecules (including EuH), quasirelativistic pseudopotentials were used as well. Dolg and Stoll summarized the results of all calculations on lanthanide monohydrides in Table 15 of Ref. [16]. The calculated parameters for the ground electronic state of EuH range from 1.55 to 1.82 eV for dissociation energies, from 2.150 to 2.235 Å for bond lengths and from 1102 to 1215 cm<sup>-1</sup> for the vibrational frequencies ( $\omega_e$ ), depending on the basis sets and pseudopotentials that were used. In Ref. [17] the molecular constants of selected lanthanide compounds (including EuH) have been calculated using relativistic small core pseudopotentials and optimized valence basis sets. All available theoretical calculations on EuH are limited to the ground electronic state. The lack of experimental and theoretical data forces us to use experiments and ligand field theory calculations on related molecules such as GdO [18–20] and EuF [18, 21] as a guide. New *ab initio* calculations on EuH by Yang and Pitzer are in progress at the Ohio State University [22].

In our work the EuH molecular spectrum was observed for the first time.

## 7.2 Experimental

### 7.2.1 Fourier transform spectra of EuH and EuD

The first set of experiments on EuH and EuD was carried out at the University of Waterloo. An emission source described in section 3.2.2 was used to generate an electronic spectrum. The inside of the alumina tube was wrapped with molybdenum foil to prevent the reaction between the metal and ceramic. The tube furnace was heated to 750°C and a mixture of Ar (~13 Torr) and H<sub>2</sub> or D<sub>2</sub> (~2 Torr) gases flowed slowly over the metal. The melting point of Eu is 1150°C so during our experiment the metal was in the solid phase. An electrical discharge (3 kV, 333 mA) was applied between two cylindrical stainless steel electrodes inside the ends of the tube. The argon pressure had to be much higher than in other experiments on metal hydrides carried out in our laboratory [23–25]. In this experiment as well as in

experiments with other rare earth metals, the metal surface absorbed hydrogen gas, presumably forming solid EuH<sub>2</sub>. For europium, the hydrogen absorption occurred at all temperatures but after some time the pressure inside the system stabilized probably after saturation of the metal surface with hydrogen. Nevertheless, the pressure in the system would occasionally increase suddenly, presumably because of a rapid release of hydrogen from the europium sample. The chemistry of this process was unfortunately beyond our control. After the experiment with hydrogen gas, deuterium gas was used the following day, but for the first two hours only EuH emission lines were observed, due to the fact that a considerable amount of hydrogen was still trapped in the metal from the previous experiment. Only after four hours of heating was the EuH signal completely replaced by that of EuD. It is worth noting that the Eu metal did not melt during the experiment, so the vapor was subliming from the surface.

Emission from the tube was focused onto the entrance aperture of a Bruker IFS 120 HR Fourier transform spectrometer. The windows at the ends of the tube and the lens were made from BaF<sub>2</sub>. The EuH emission spectrum was recorded in the 10 000–18 000 cm<sup>-1</sup> region using a silicon photodiode detector, quartz beamsplitter and 550 nm red-pass filter. The EuD spectrum was recorded in the 8 000 – 16 000 cm<sup>-1</sup> region. A total of 100 scans for both molecules were co-added at a resolution of 0.04 cm<sup>-1</sup> in order to obtain a good signal-to-noise ratio. Overview spectra of EuD and EuH are shown in Fig. 7.1. The dense features in the spectrum are molecular emission lines, while sparse and intense lines are europium and argon atomic emission lines.

Line positions were measured using a Windows-based program called WSpectra, written by M. Carleer (Université Libre de Bruxelles). The spectrometer was not under vacuum and the “air-to-vacuum” wavenumber correction [26] had to be made before the lines were calibrated against argon atomic lines present in the spectrum [27]. There are many bands present in the spectrum, as can be seen from Fig. 7.1. This results in line overlaps which make assignment of the lines difficult. Therefore it was decided to record a “cold” spectrum (when molecules are at ∼ 5 K) of EuH in order to populate only the first few rotational levels, which will result in less lines in the electronic spectrum and simplify the line assignment.

### 7.2.2 Laser ablation/molecular beam experiment

The sub-Doppler spectrum of EuH was recorded in the laser ablation/molecular beam apparatus at the Arizona State University in the laboratory of Prof. T. C. Steimle. A europium metal rod (approximately 1" long and 0.25" in diameter) was

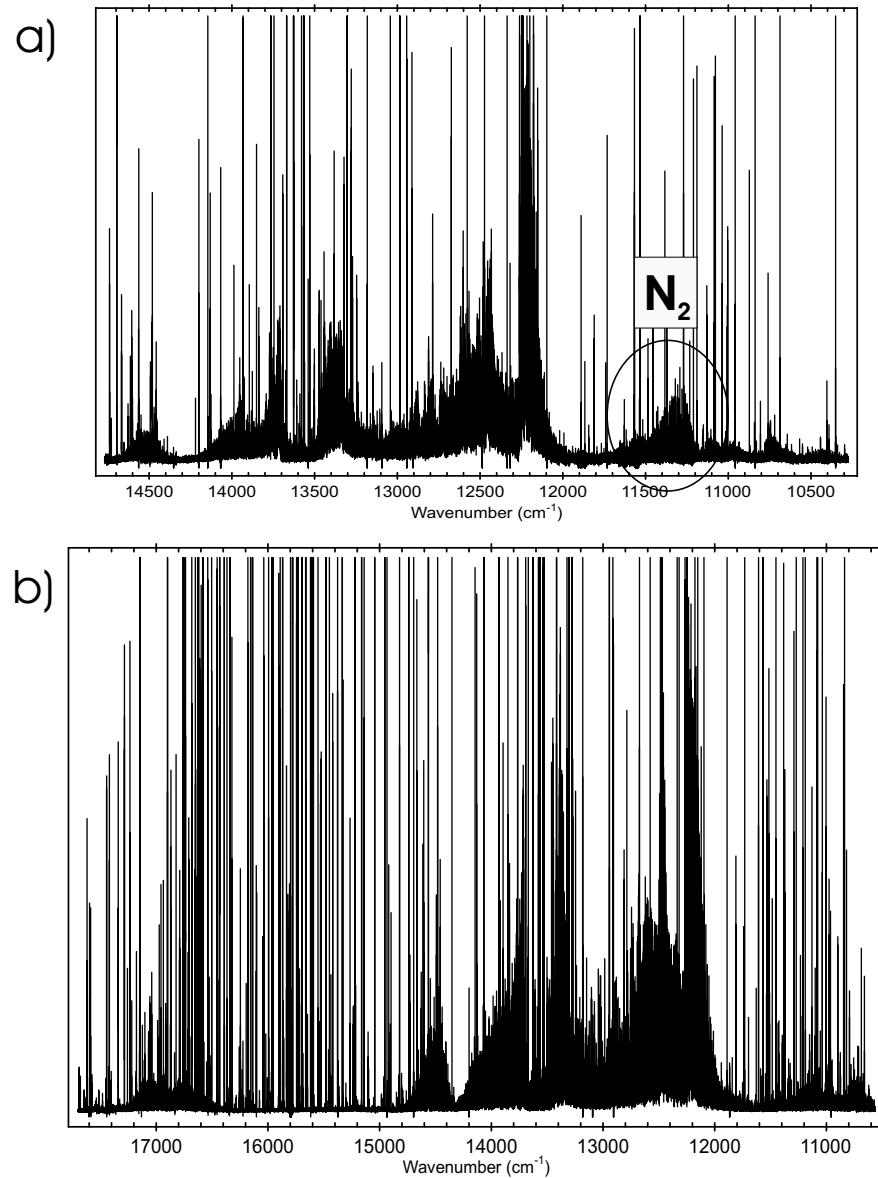


Figure 7.1: An overview of the FT spectrum of a) EuD and b) EuH. The dense features in the spectrum are molecular emission lines, while sparse and intense lines are europium and argon atomic lines. Note that the wavenumber ranges covered in EuD and EuH experiments are different (see text for details).

ablated by the third harmonic (355 nm) of a Q-switched Nd:YAG laser operating at approximately 10 mJ/pulse with a 20 Hz frequency of the pulses. In order to

obtain stable shot-to-shot production of the metal vapor and to extend the life time of the sample, the rod was rotated and translated during the experiment. A quartz lens of 0.5 m focal length was used to focus the laser pulses onto the Eu sample. A solenoid pulsed valve was used to introduce the mixture of He and H<sub>2</sub> gases. After trying different proportions of gases in the mixture and different total backing pressures, it was found that a 50:50 mixture at  $\sim$ 2300 kPa yields the best signal. As an alternative to helium, argon gas was used as well but the signal was much weaker. The created EuH molecules were skimmed about 15 cm downstream by a 5 mm diameter “skimmer” that separates source and detection chambers operated at approximately  $5 \times 10^{-5}$  Torr and  $1 \times 10^{-6}$  Torr pressures, respectively.

The dye laser radiation intersected the molecular beam at a right angle 10 cm downstream from the skimmer. A lens assembly was used to collect and collimate the resulting total laser-induced fluorescence through the band-pass filter, which minimized the background light associated with the ablation plasma. The cooled photomultiplier tube (PMT) detector was placed perpendicular to both the molecular beam and the probe laser. The signal from the PMT was processed using gated, single-photon-counting techniques.

First we made a number of survey scans ( $> 100 \text{ cm}^{-1}$ ) of the 13 000 – 18 000  $\text{cm}^{-1}$  region. For that purpose a Ti:Sapphire laser and a continuous wave, linear dye laser (operating with different dyes) were employed. This was done in an attempt to cover the range of the FT spectrum. Only the band at  $\sim$ 17 000  $\text{cm}^{-1}$  was found in these low resolution LIF scans. The bandwidth of the linear dye laser is approximately 5 GHz. A commercial wavemeter accurate to  $\pm 0.01 \text{ cm}^{-1}$  was employed for the wavelength calibration. An overview of the survey scan of this band is shown on Figure 7.2. As can be seen, this band has several intense features in a somewhat periodic pattern. It was decided to perform high resolution scans of these strong features.

Unfortunately, the condition of the rod could not allow a high resolution scan of the entire 16 980 – 17 125  $\text{cm}^{-1}$  region. The narrow scans ( $< 2 \text{ cm}^{-1}$ ) were carried out using a stabilized single mode, continuous wave ring dye laser. The bandwidth of this laser system was approximately 1 MHz. An absorption spectrum of a heated gaseous I<sub>2</sub> cell was recorded simultaneously with EuH laser induced fluorescence spectrum for wavelength calibration [28, 29] in narrow scans. An example of the “raw” high resolution scan is shown in Figure 7.3. The regions of the spectrum covered by the series of narrow scans are listed in Table 7.1.

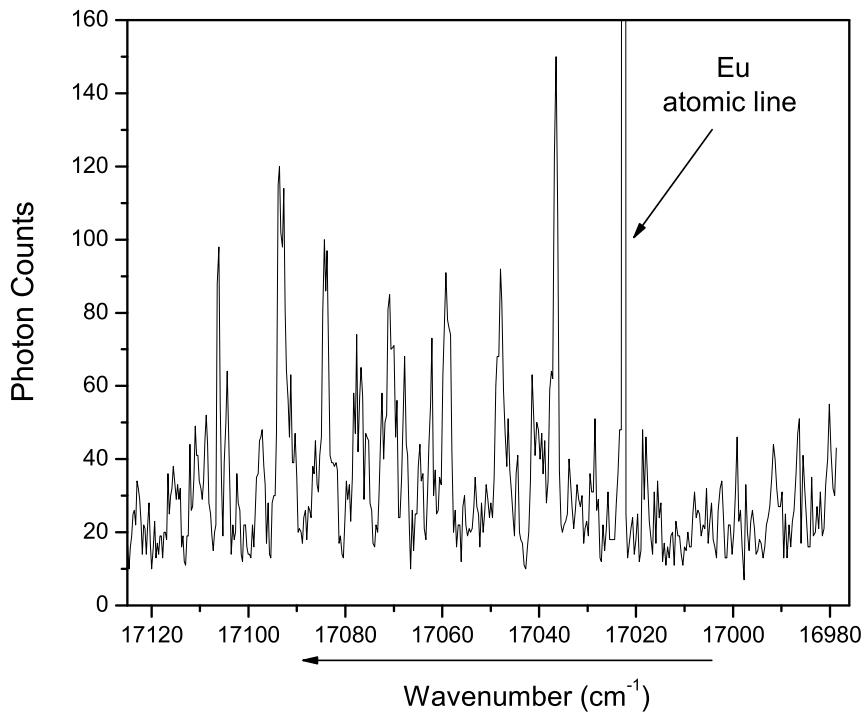


Figure 7.2: A survey laser excitation scan of the  $16\,975\text{--}17\,125\,\text{cm}^{-1}$

## 7.3 Results and Discussion

### 7.3.1 Electronic states of EuH

The lack of available theoretical calculations, especially for excited electronic states, makes the interpretation of the EuH emission spectrum very difficult. In order to understand the electronic spectrum of EuH, we need to make some assumptions and educated guesses based on ligand field theory (LFT) and papers on EuF [18, 21] and GdO [18–20].

The ground-state atomic electron configuration is assumed to be  $\text{Eu}^+\{4f^76s^1\}\text{H}^-$ . There are 8 unpaired electrons with parallel spins in the lowest energy configuration, which gives rise to a  ${}^9\Sigma^-$  state [30]. In first excited electronic state, the spin of the  $s$ -electron flips to give a  ${}^7\Sigma^-$  state. The next electronic configuration would be  $4f^75d^1$ , which gives rise to nonet and septet  $\Sigma^-$ ,  $\Pi$  and  $\Delta$  states, and the nearby

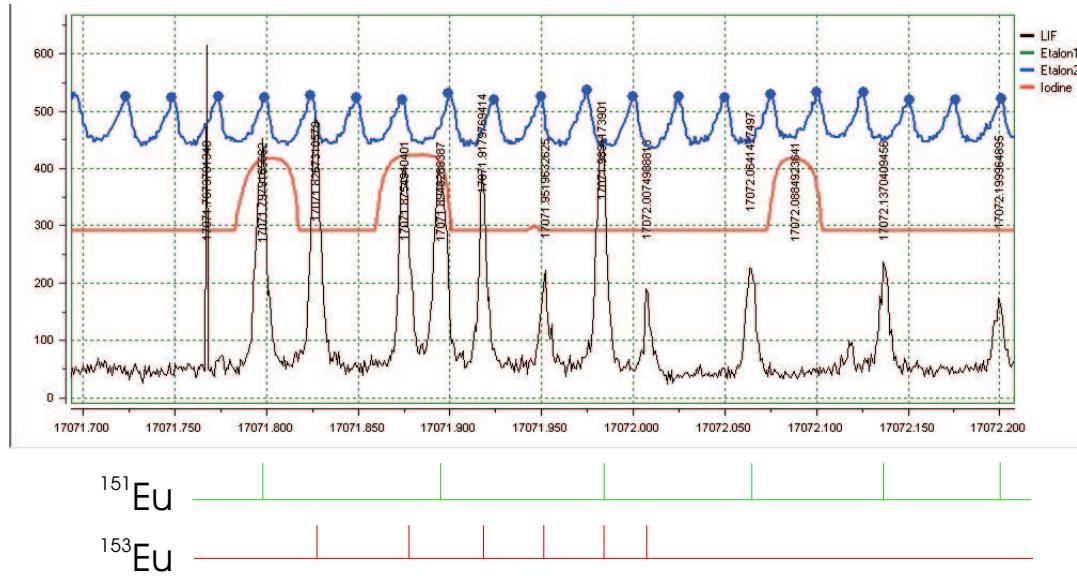


Figure 7.3: An example of “raw” high resolution LIF scan. Hyperfine and isotope splittings in EuH can be easily seen in the lower panel of this figure. The top panel are the fringes of an etalon and the middle panel is the spectrum of  $I_2$  used for calibration.

$4f^76p^1$  configuration gives rise to the  $^7\Sigma^-$ ,  $^7\Pi$ ,  $^9\Sigma^-$  and  $^9\Pi$  states. Other possible excited electronic configurations are  $f^6s^2$ ,  $f^6s^1d^1$ , etc., which will give rise to numerous additional states. The absolute and relative positions of these states are hard to determine based on the simple LFT model. The main difficulty is that LFT is probably not a reliable model for the prediction of energy levels because EuH is not ionic. Some LFT predictions can be taken from Table 1 of Ref. [21], in which the results of LFT calculations for the low-lying states of EuF are listed. The  $^7\Sigma^-$  state of EuF is predicted to lie  $1420\text{ cm}^{-1}$  above the ground electronic state. Therefore, it was assumed initially that the majority of the observed transitions are from the excited  $^7\Sigma^-$ ,  $^9\Sigma^-$  and  $^9\Pi$  states to the ground  $X\ ^9\Sigma^-$  state.

It is believed that the spin-spin interaction in the ground state is small and that this state obeys Hund’s case (b) coupling. This is based on the fact that the spin-spin interaction is a sum of the first order electron spin-spin interaction and the second-order spin-orbit interaction with other states, with the latter usually dominating in heavy molecules [31]. The selection rules for the second order spin-orbit interaction are  $\Delta S=0,\pm 1$ ;  $\Sigma^\pm \sim \Sigma^\mp$ ;  $\Delta \Omega=0$ . Of the low-lying states, the best

Table 7.1: The regions covered by high-resolution scans (in  $\text{cm}^{-1}$ )

| Start    | End      |
|----------|----------|
| 16982.7  | 16984.7  |
| 16986    | 16986.31 |
| 17012.5  | 17013.5  |
| 17037.6  | 17038.7  |
| 17040.2  | 17041.7  |
| 17051.05 | 17053.1  |
| 17060.45 | 17063.1  |
| 17067.29 | 17067.95 |
| 17070.25 | 17073.4  |
| 17082.9  | 17084.85 |
| 17091.97 | 17092.9  |
| 17094.3  | 17095.2  |
| 17105.3  | 17105.6  |
| 17108.8  | 17109.1  |
| 17112.3  | 17113.14 |

candidates for such an interaction with the ground state are  ${}^9\Pi$  and  ${}^7\Pi$  states arising from  $4f^75d^1$  and  $4f^75p^1$  configurations. According to the LFT predictions for EuF [21], the states arising from these configurations are located  $\sim 16\,200$  and  $\sim 18\,900 \text{ cm}^{-1}$ , above the ground  $X\ {}^9\Sigma^-$  electronic state, respectively; hence the interaction with these states is small. A similar situation was discussed in Chapter 4 in the case of  $X\ {}^7\Sigma^+$  state of MnH. Notice that the ground state atomic configuration of MnH is  $\text{Mn}^+\{3d^54s^1\}\text{H}^-$ , and so MnH is the transition metal analog of EuH. Also, according to Ref. [20] the value of spin-spin interaction constant  $\lambda$  of EuF was determined to be  $-0.13 \text{ cm}^{-1}$  for an excited  ${}^7\Sigma^-$  state, while the value for ground state was “very much” smaller (the exact value could not be determined from the available spectra).

In the Hund’s case (b) coupling scheme, each rotational level ( $N$ ) is split into nine spin components (for  $N>4$ ) labeled by  $J$ , with  $\mathbf{J}=\mathbf{N}+\mathbf{S}$ , where  $\mathbf{J}$  is the total angular momentum,  $\mathbf{N}$  is rotational angular momentum and  $\mathbf{S}$  is the total electron spin. The excited septet and nonet states most probably obey Hund’s case (a) (or (a') for  $\Sigma$  states) coupling which spin “uncouples” to Hund’s case (b) at higher  $J$ -values, just like the  $A{}^7\Pi$  state of MnH [32]. At low  $J$  values the excited states of EuH will therefore be split into  $2S+1$  well-separated spin components for non- $\Sigma$

states and into  $S+1$  components for  $\Sigma$  states. That means that for lower  $J$ -values the excited  ${}^9\Sigma^-$  state will be split into 5 relatively isolated spin components with  $\Omega=0^-$ , 1, 2, 3 and 4. The 4 last components ( $\Omega > 0$ ) will have both  $e$  and  $f$  parity levels.

### 7.3.2 FT spectra of EuH/D

Guided by these ideas when scrutinizing the FT spectrum of EuH (Fig. 7.1b), it was noted that the band at  $14\,500\text{ cm}^{-1}$  (by coincidence this band is also the only band with a clear rotational structure, not overlapped by other bands) has the general appearance one would expect for  ${}^9\Sigma^- - {}^9\Sigma^-$  transition, because it has 5 band heads (corresponding to 5  $\Omega$ -values). The spectrum of this band is shown in Figure 7.4.

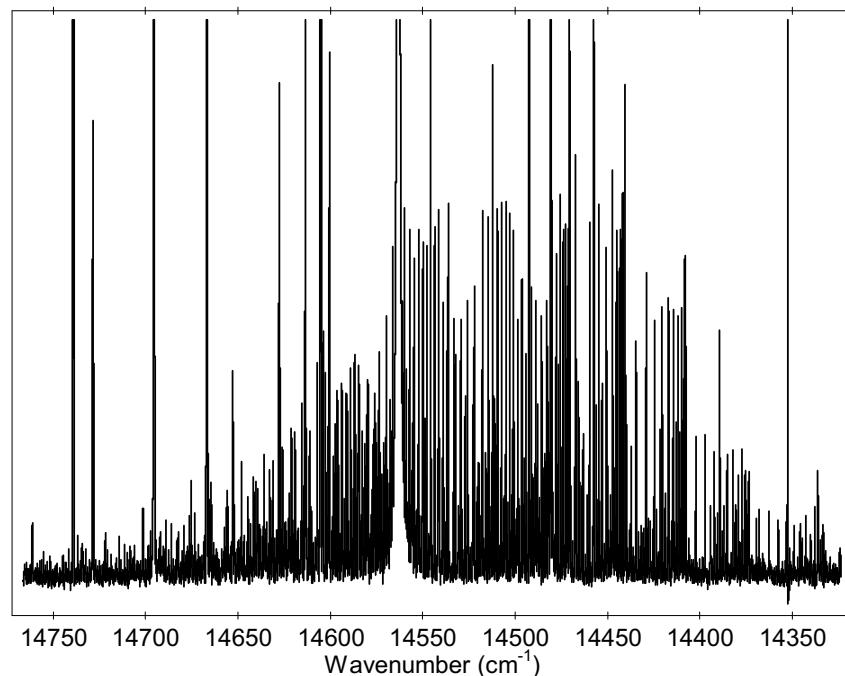


Figure 7.4: The  $14\,500\text{ cm}^{-1}$  transition of EuH observed by FT emission spectroscopy.

However, we have failed to assign this band because the branches are perturbed and exhibit behavior typical for transitions involving states with spin uncoupling,

i.e., the spacing between the lines can increase and then decrease in the same branch [32].

### 7.3.3 The “cold” spectrum of EuH

Our failure to assign the FT spectrum of EuH, led us to record the sub-Doppler spectrum at Arizona State University. It was somewhat surprising that only the band at  $\sim 17\,000 \text{ cm}^{-1}$  was seen with the laser ablation-molecular beam spectrometer. This implies that all other transitions in the FT spectrum (Fig. 7.1b) are not to the ground electronic state. The corresponding transition (at  $\sim 17\,000 \text{ cm}^{-1}$ ) was also observed for the EuF molecule [33], and most probably is a  ${}^9\Sigma^- - X{}^9\Sigma^-$  or a  ${}^9\Pi - X{}^9\Sigma^-$  transition.

When using the  $\text{H}_2\text{-He}$  gas mixture in the apparatus at the Arizona State University, an increase in the percentage of hydrogen leads to an increase in rotational temperature. Therefore the use of a 50:50 mixture of He and  $\text{H}_2$  not only increases the production efficiency but unfortunately also increases the rotational temperature. This temperature is estimated to be 70 K by analogy with an experiment on CaH performed under similar conditions [34], while the desired rotational temperature was about 10 K. It is interesting to estimate the population distribution in the rotational levels at these temperatures. For that purpose the  $X{}^9\Sigma^-$  ground state term values  $E(J)$  were calculated using the SPCAT program [35]. The rotational constant  $B$  was taken to be  $5.33 \text{ cm}^{-1}$ , the spin-spin interaction constant  $\lambda=0.022 \text{ cm}^{-1}$  and spin-rotation interaction constant  $\gamma=0$ . Then the rotational partition function was calculated using the following equation:

$$q_r = \sum_J (2J+1)e^{-\frac{E(J)}{kT}}, \quad (7.1)$$

in which  $k$  is the Boltzmann constant and the summation was taken over all  $J$  values corresponding to  $N$  having values from 0 to 7 (the population of the  $J$  levels corresponding to  $N > 7$  is negligible). Now the population of every  $N$  level can be calculated as

$$p(N) = \sum_J p(J), \quad (7.2)$$

where  $p(J)$  is a population of a particular  $J$  level given by

$$p(J) = (2J + 1) \frac{e^{-\frac{E(J)}{kT}}}{q_r}. \quad (7.3)$$

Note that the summation in Eq. (7.2) is over the  $J$  values corresponding to a particular  $N$ .

The distribution of population calculated using Eq. (7.1-7.3) for 10 and 70 K is shown on Figure 7.5. As can be seen from the picture the  $N=0$  to 6 levels have sufficient population at 70 K to contribute to the spectrum. Since the ground state obeys Hund's case (b) these levels are split into 4 to 9  $J$  values.

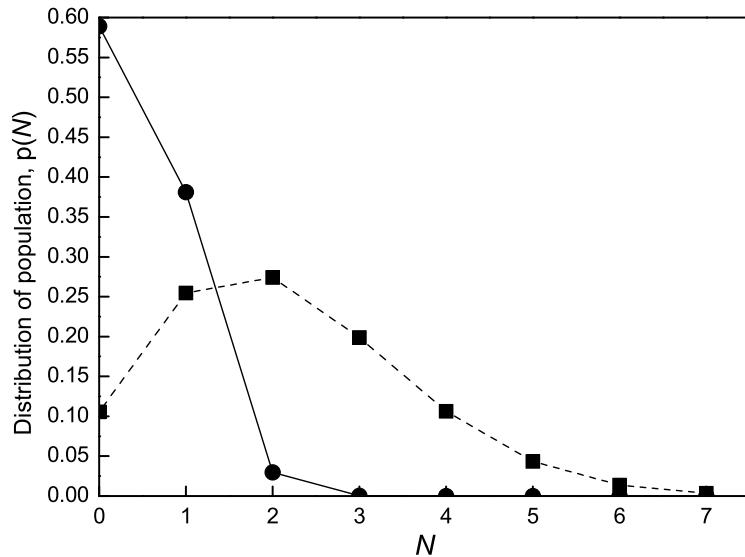


Figure 7.5: Distribution of population for the rotational temperature of 10 K (solid line) and 70 K (dashed line).

When considering our scan regions reported in Table 7.1, one must keep in mind that the isotope and hyperfine splittings are present at high resolution. Europium has two stable isotopes of similar abundance. Both isotopes have nuclear spins of  $\frac{5}{2}$  and large nuclear magnetic moments. Table 7.2 provides nuclear data for isotopes of europium [36].

Table 7.2: The Eu data from the Ref. [36].

| Isotope           | Abundance (%) | Nuclear spin, $I$ | Nuclear magnetic moment, $\mu/\text{nuclear magnetons}$ | magnetic moment, Q/fm <sup>2</sup> | Quadrupole |
|-------------------|---------------|-------------------|---|------------------------------------|------------|
| <sup>151</sup> Eu | 47.8          | 5/2               | +3.4718   | +116                               |            |
| <sup>153</sup> Eu | 52.2          | 5/2               | +1.5331   | +294                               |            |

The nuclear spin of the H atom is  $\frac{1}{2}$  but because the proton spin contribution to the hyperfine splitting is much smaller than that from the europium we can completely resolve only the Eu hyperfine splitting. We expect that the  $X^9\Sigma^-$  state obeys Hund's case ( $b_{\beta J}$ ) coupling [37], because it is a most common case for this type of molecules. For Hund's case ( $b_{\beta J}$ ) coupling in addition to  $\mathbf{J}=\mathbf{N}+\mathbf{S}$  coupling there is also a coupling of total angular momentum with nuclear spin:  $\mathbf{F}=\mathbf{J}+\mathbf{I}$ . For the ground  $X^9\Sigma^-$  state, each  $N$  level is split into  $2S+1=9$  components (for  $N>4$ ) and each  $J$  level is further split into  $2I+1=6$  hyperfine components for each isotope. There are thus a total of  $54\times 2=108$  levels for each  $N$  counting each isotope separately. The upper state most probably follows Hund's case ( $a_{\beta}$ ) coupling [37]. For both upper and lower states the  $J = 0$  level splits into 3 hyperfine components (for each isotope),  $J = 1$  into 4,  $J = 2$  into 5 and  $J \geq 3$  splits into 6 hyperfine components. The rotational selection rule for the electronic transition in this case will be  $\Delta J = 0, \pm 1$ . The selection rule for the transitions between upper and lower hyperfine levels is  $\Delta F = 0, \pm 1$  with spectral lines with  $\Delta J = \Delta F$  being the strongest. For higher  $J$  values only transitions with  $\Delta J = \Delta F$  can be observed. As an example, hyperfine transitions from the  $J' = 8$  level in the upper state to the  $J'' = 9$  component for  $N'' = 5$  rotational level of the ground state are shown in Figure 7.6. It follows from the figure that the transitions involving higher  $J$  values will appear in the spectrum with 6 hyperfine lines for each isotope (therefore 12 lines in total). The transition shown in Figure 7.3 is a clear illustration of these predictions as it is split into 12 hyperfine lines.

The lines in Fig. 7.3 appear in a “flag” or Landé pattern [38]. Before assigning the lines it is useful to consider the form of hyperfine interactions in the  ${}^9\Sigma^-$  state. The hyperfine Hamiltonian for this state can be written as:

$$H_{hfs} = b_F \mathbf{I} \cdot \mathbf{S} + c(I_z S_z - \frac{1}{3} \mathbf{I} \cdot \mathbf{S}), \quad (7.4)$$

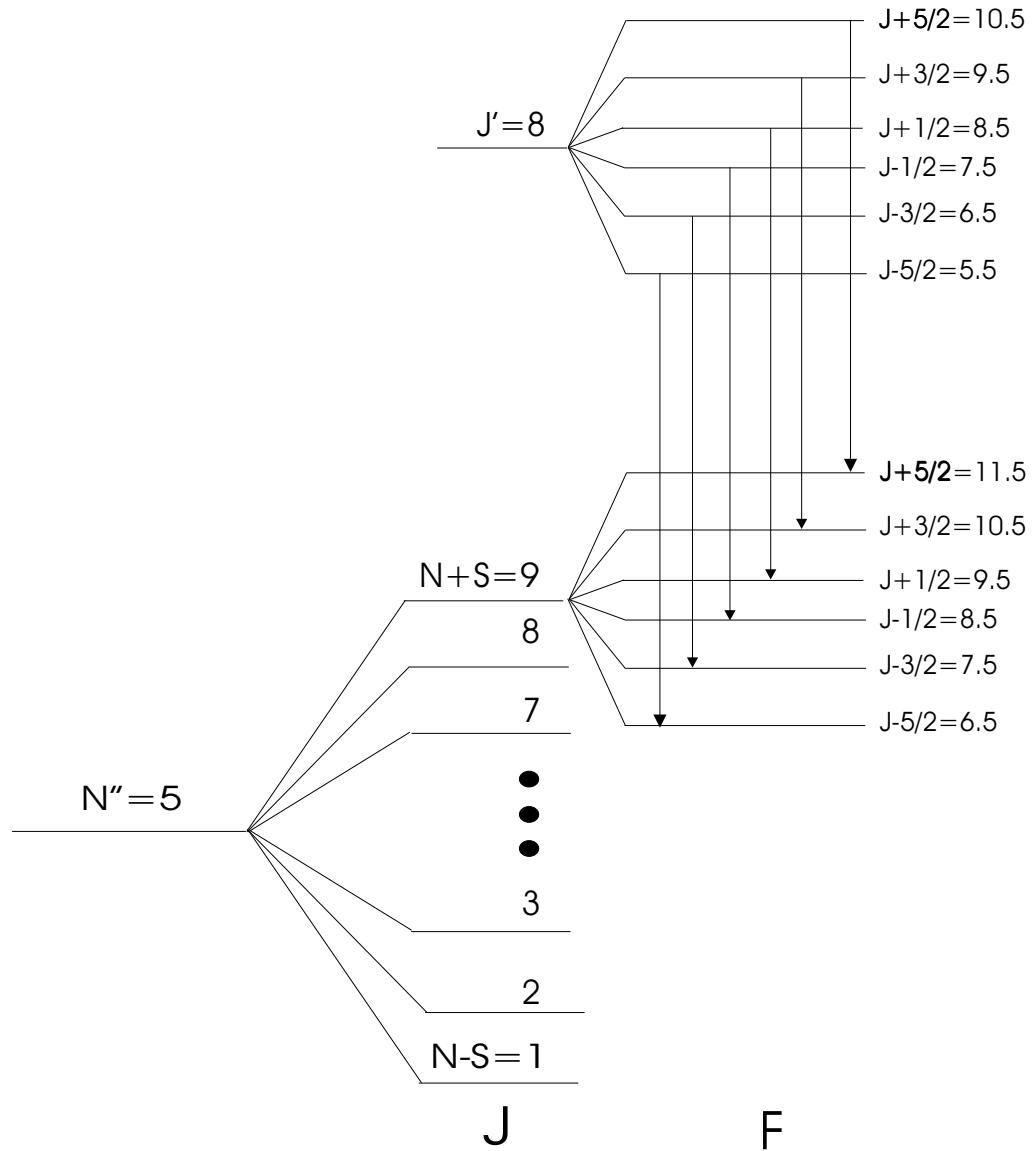


Figure 7.6: An example of the transitions between hyperfine levels in excited and ground electronic states.

where  $b_F$  is the Fermi contact parameter defined by

$$b_F = \frac{1}{hc} \frac{8\pi}{3} g \mu_B g_N \mu_N \sum_i | \langle \psi_i(r_i = 0) \rangle |^2 \quad (7.5)$$

and the dipolar parameter  $c$  by

$$c = \frac{1}{hc} \frac{3}{2} g \mu_B g_N \mu_N \sum_i \langle (3\cos^2 \theta_i - 1) r_i^{-3} \rangle. \quad (7.6)$$

The expressions (7.5) and (7.6) are written in wavenumbers and  $\mu_B$  and  $\mu_N$  are the Bohr and nuclear magnetons,  $g$  and  $g_N$  are the electron and nuclear spin  $g$ -factors and  $(r_i, \theta_i)$  are the spherical polar coordinates of the electron  $i$ , defined with respect to the Eu nucleus. The angle brackets imply the expectation value and the summations are over the unpaired electrons. The Fermi contact parameter basically describes the contribution of any  $s$ -electron density at the nucleus to the hyperfine interactions. Eq. (7.5) implies that  $b_F'' \gg b_F'$  for EuH since the ground state arises from an  $f^7s^1$  configuration while the upper state is caused by  $f^7d^1$  or  $f^7p^1$  configurations. The difference in  $b_F$  values for the two isotopes of europium arise from the difference in  $g_N$  values. For  $^{151}\text{Eu}$   $g_N = \frac{\mu_I}{I} = 1.38872$  and for  $^{153}\text{Eu}$   $g_N = \frac{\mu_I}{I} = 0.61324$  and the ratio between the  $b_F$  values for  $^{151}\text{Eu}$  and  $^{153}\text{Eu}$  will be equal to 2.2646. In the spectrum the spacing between hyperfine lines of  $^{151}\text{EuH}$  isotopologue will be a factor of  $\sim 2.2646$  larger than that of  $^{153}\text{EuH}$ . This fact helps significantly in assigning the lines in hyperfine multiplets as can be seen in Fig. 7.3 (the isotope assignment is at the bottom of the Fig. 7.3). Notice that the  $f^7s^1$  ground state configuration has a mainly spherical electron distribution so  $c''$  is very small but  $c'$  can be significantly larger.

The diagonal matrix element of the Fermi contact interaction was derived by Varberg *et al.* [39] using the formulas of Ref. [40] as

$$\langle \Lambda NSJIF | b_F \mathbf{I} \cdot \mathbf{S} | \Lambda NSJIF \rangle = -b_F \left[ \frac{N(N+1) - S(S+1) - J(J+1)}{4J(J+1)} \right] \times [F(F+1) - I(I+1) - J(J+1)]. \quad (7.7)$$

This equation was derived for a  $^7\Sigma^+$  state but it is also correct for a  $^9\Sigma^-$  state.

It is clear that the hyperfine energies depend on which spin component they belong to (for simplicity we will denote  $N+S$  (where  $S=4$ ) electron spin components as  $F_1$ ,  $N+S-1$  as  $F_2, \dots, N-S$  as  $F_9$ ). Nevertheless in order to make  $J$ -assignments of the lines we will temporarily neglect this dependence. For that matter one can imagine that we are dealing with atomic rather than molecular lines and use the energy expression for atomic nuclear magnetic interaction

$$W_F = \frac{1}{2} A_F [F(F+1) - I(I+1) - J(J+1)], \quad (7.8)$$

and in our case  $A_F$  is proportional to the  $b_F$  value (as it follows from comparison of Eq. (7.7) and (7.8)).

The difference between two adjacent hyperfine levels (and hence the difference between adjacent hyperfine lines in the spectrum) will therefore be

$$\Delta W_F = A_F(F+1) \quad (7.9)$$

as long as the dominant hyperfine parameter is  $b''_F$ . Eq. (7.9) implies that one can take the differences between adjacent hyperfine lines in each transition and assign different  $F$  values to them until the plot  $\Delta W_F$  vs  $F+1$  yields a straight line going through the origin with a slope equal to  $A_F$ . This way the  $J''$  and  $F''$ -assignments can be made. Figure 7.7 shows such a plot for both isotopologues of EuH using one of the lines observed at  $\sim 17108 \text{ cm}^{-1}$  as an example.

The ratio between extracted from the two slopes  $A_F$  values has to correspond roughly to the expected ratio of 2.265. The lines that we were able to assign in this way are listed in Table 7.3. The first column of this table corresponds to the range in which the lines are observed, then  $A_F$  values for both isotopologues are followed by their ratio and tentative  $J$ -assignment based on the method described above. As can be seen from the table, some of the lines do not have the same  $J$ -assignment for the two isotopologues. These deviations may be caused by electric quadrupole interactions or (and) hyperfine perturbations.

If one takes the electric quadrupole interaction into account Eq. (7.4) changes to

$$H_{hfs} = b_F \mathbf{I} \cdot \mathbf{S} + c(I_z S_z - \frac{1}{3} \mathbf{I} \cdot \mathbf{S}) + \frac{e^2 Q q (3I_z^2 - I(I+1))}{4I(2I-1)}, \quad (7.10)$$

in which

$$e^2 Q q = -\frac{e^2 Q}{hc} \sum_i \langle (3\cos^2 \theta_i - 1) r_i^{-3} \rangle. \quad (7.11)$$

Table 7.3: The assigned lines, and some parameters associated with them. See text for details.

| Region            | $A_F^{151}$ | $A_F^{153}$ | $\frac{A_F^{151}}{A_F^{153}}$ | $J^{151}$ | $J^{153}$ | $\Delta W^{151}$ | $\Delta W^{153}$ | $\frac{\Delta W^{151}}{\Delta W^{153}}$ |
|-------------------|-------------|-------------|-------------------------------|-----------|-----------|------------------|------------------|---|
| 16983.1-16982.7   | 0.0072      | 0.0071      | 10                            | 4         | 0.3808    | 0.1606           | 2.37             |   |
| 16983.3-16983.8   | 0.0095      | 0.0088      | 9                             | 4         | 0.4489    | 0.1973           | 2.27             |   |
| 16986.03-16986.3  | 0.0051      | 0.0044      | 10                            | 5         | 0.2708    | 0.1201           | 2.25             |   |
| 17012.6-17013.33  | 0.0185      | 0.0081      | 2.28                          | 5         | 0.5032    | 0.2246           | 2.24             |   |
| 17037.89-17038.3  | 0.0078      | 0.0073      | 9                             | 4         | 0.3698    | 0.1657           | 2.23             |   |
| 17052.1-17052.6   | 0.0263      | 0.0118      | 2.23                          | 3         | 0.4524    | 0.2026           | 2.23             |   |
| 17062.4-17062.93  | 0.0212      | 0.0093      | 2.28                          | 4         | 0.4787    | 0.2142           | 2.25             |   |
| 17067.29-17067.75 | 0.0164      | 0.0074      | 2.22                          | 5         | 0.4537    | 0.1998           | 2.27             |   |
| 17071.15-17071.59 | 0.0265      | 0.0108      | 2.45                          | 3         | 0.4362    | 0.1875           | 2.32             |   |
| 17072.0-17072.83  | 0.0106      | 0.0049      | 2.16                          | 7         | 0.4020    | 0.1808           | 2.22             |   |
| 17083.4-17083.73  | 0.0074      | 0.0078      | 8                             | 3         | 0.3174    | 0.1387           | 2.28             |   |
| 17084.0-17084.6   | 0.0216      | 0.0096      | 2.25                          | 4         | 0.4857    | 0.2146           | 2.26             |   |
| 17108.45-17108.91 | 0.0167      | 0.0078      | 2.14                          | 4         | 0.4522    | 0.2061           | 2.19             |   |
| 17108.61-17109.1  | 0.0168      | 0.0078      | 2.15                          | 5         | 0.4620    | 0.2067           | 2.23             |   |

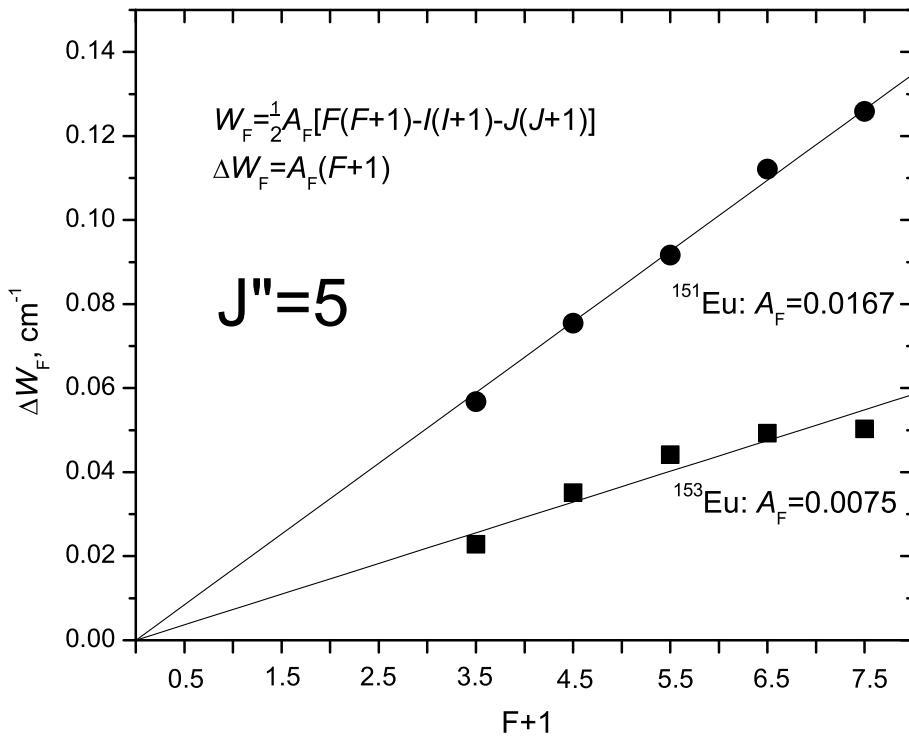


Figure 7.7: An example of the graphical method for making the  $J''$  assignments in the observed transitions. See text for details.

In Eq. (7.11)  $q$  is the gradient of the electric field acting at the nucleus that is trying to orient the nucleus. Unlike magnetic hyperfine interactions which arise only from the unpaired electrons, the electric quadrupole interaction arises from *all* valence electrons. Therefore the contribution of the quadrupole interaction from the excited electronic state should be bigger than that in the more spherical ground state. Electric quadrupole hyperfine structure is definitely not negligible in our spectrum since for some of the lines the deviation from the Landé pattern is clearly larger in  $^{153}\text{Eu}$  lines which is consistent with the fact that the  $^{153}\text{Eu}$  nucleus has a larger quadrupole moment (see Table 7.2).

The effect of hyperfine perturbations is also easily observable in our spectrum. These perturbations occur due to the fact that at low  $N$  values the fine structure

splitting between spin components of each  $N$  in the ground  ${}^9\Sigma^-$  state is comparable to the size of the hyperfine splitting. That implies that for the same  $N$  level the hyperfine levels with the same  $F$  value but from different spin components could be located close to each other and cause perturbations. The selection rule for these perturbations is  $\Delta F=0$ . The  $F = J + I$  hyperfine level of each spin component can be perturbed only from above since no levels with the same  $F$  value exist in the spin components that lie lower in energy. The analogous hyperfine perturbations were observed in the  $X{}^7\Sigma^-$  state of MnH by Varberg *et al.* [39].

Table 7.4: Overall widths of magnetic hyperfine energy multiplets of  ${}^9\Sigma^-$  state for Hund's case ( $b_{\beta J}$ ) coupling. See text for details.

|   |
|---|
| $\Delta W(F_1) = \frac{4Ib_F(2N+9)}{(N+4)}$             |
| $\Delta W(F_2) = \frac{Ib_F(3N+16)(2N+7)}{(N+4)(N+3)}$  |
| $\Delta W(F_3) = \frac{Ib_F(2N+13)(2N+5)}{(N+2)(N+3)}$  |
| $\Delta W(F_4) = \frac{Ib_F(N+11)(2N+3)}{(N+1)(N+2)}$   |
| $\Delta W(F_5) = \frac{10Ib_F(2N+1)}{N(N+1)}$           |
| $\Delta W(F_6) = -\frac{Ib_F(N-10)(2N-1)}{N(N-1)}$      |
| $\Delta W(F_7) = -\frac{Ib_F(2N-11)(2N-3)}{(N-1)(N-2)}$ |
| $\Delta W(F_8) = -\frac{Ib_F(3N-13)(2N-5)}{(N-3)(N-2)}$ |
| $\Delta W(F_9) = -\frac{4Ib_F(2N-7)}{(N-3)}$            |

The overall width  $\Delta W$  of the hyperfine multiplet due to the europium Fermi

contact interaction is defined as the energy difference between the  $F = J + I$  and  $F = J - I$  levels and depends on the spin component. The overall hyperfine widths for all nine spin components were derived using Eq. (7.7) and are listed in Table 7.4. The negative signs in front of the expressions for the widths of  $F_6$  to  $F_9$  spin components indicates that after the  $N$  value exceeds a certain number the hyperfine pattern is reversed. For the  $F_6$  component it will happen at  $N > 10$ , for the  $F_7$  at  $N > 5$ , for the  $F_8$  at  $N > 4$  and for the  $F_9$  at  $N > 3$ . Considering that in our spectrum we are populating only  $N = 0$  to 6 rotational levels, theoretically we should expect to see inverted patterns only for the  $F_7$ ,  $F_8$  and  $F_9$  spin components. However, we were unable to find any inverted patterns in the scanned spectral ranges.

The widths of the hyperfine multiplets for both isotopologues and their ratios for every assigned line are also listed in Table 7.3. Since the ratios between widths in almost all cases are close to the expected values, it was decided to attempt to get a rough estimate of the  $b_F$  values. For that purpose we took the lines that seemed to be least perturbed and had consistent  $J$  assignments based on the graphical method described above for both isotopologues, and applied to them all equations from Table 7.4 changing values of  $N$  so all spin components will yield consistent  $J$  values. For example if the line at  $\sim 17084 \text{ cm}^{-1}$  is assigned to have  $J'' = 4$  then the  $F_1$  component would have  $N = 0$ ,  $F_2$  would have  $N = 1, \dots, F_9$  would have  $N = 5$ . Then we calculate  $b_F$  values using equations from the Table 7.4 for all lines and after that look for a number that would be roughly the same for every line. The average of these roughly matching numbers was taken as a  $b_F$  value. This procedure also provides  $N''$  and more reliable  $J''$  and  $F''$  assignments of the observed lines, which are given in Table 7.5 together with approximate  $J'$  values. For some of the lines, the results are ambiguous and their assignments are not listed.

As one can see from Table 7.5 both transitions at  $17108 \text{ cm}^{-1}$  terminate at the  $N''=1$  rotational level of the ground state but at two different spin components ( $F_1$ ,  $J = 5$  and  $F_2$ ,  $J = 4$ ). Both of these transitions are most probably from the same upper state  $J'$ -level and the lines appear close to each other because of the small magnitude of the spin-spin interaction constant  $\lambda$  in the ground electronic state. The upper state  $J$  value could be 4 or 5 but since we do not observe a transition to the  $N'' = 1$ ,  $J'' = 3$  level around  $17108 \text{ cm}^{-1}$ ,  $J'$  is most certainly equal to 5. This information is sufficient to determine the values for the Fermi contact interaction ( $b_F$ ) and spin-spin interaction ( $\lambda$ ) parameters. A fit was performed using the SPFIT program [35] with the hyperfine parameters of the upper state assumed to be negligible. However, one has to keep in mind that despite the fact that  $b''_F \gg b'_F$ , the magnetic dipolar and electric quadrupole interactions in the

upper state could be significant. Nevertheless all 12 lines for both isotopologues fit very well with the quadrupole interaction neglected in both states. From this fit we found that for  $^{151}\text{EuH}$   $\lambda'' = 0.0224(21) \text{ cm}^{-1}$  and  $b''_F = 0.020930(190) \text{ cm}^{-1}$ , whilst for  $^{153}\text{EuH}$   $\lambda'' = 0.0232(21) \text{ cm}^{-1}$  and  $b''_F = 0.009477(191) \text{ cm}^{-1}$ . The ratio between  $b''_F$  values for 2 isotopologues is 2.21 which is a little different from the expected ratio of 2.265. This deviation may be due to the fact that we neglected the quadrupole interaction parameters in our fit (particularly for  $^{153}\text{EuH}$ , which is consistent with the fact that  $^{153}\text{Eu}$  has a larger  $Q$  value in Table 7.2). The  $\lambda''$  values for  $^{151}\text{EuH}$  and  $^{153}\text{EuH}$  are the same within the estimated uncertainty as expected because this parameter does not depend on the reduced mass. Other lines from Table 7.5 were fitted separately and these fits yield the same (within calculated uncertainty)  $b''_F$  values as from the fit of lines at  $17108 \text{ cm}^{-1}$ . Unfortunately a global fit of all lines in Table 7.5 was not possible since it was difficult to make an unambiguous assignment of the upper state quantum numbers for these transitions based on the available information, and the difficulty in fitting Hund's case (a)-case (b) transitions with the SPFIT program.

Table 7.5: Assignment of some of the transitions observed in the high-resolution LIF scans. The values of  $J'$  for some of the lines are not clear but the most probable assignment is given in bold font.

| $J'$      | $F'$ | $N''$ | $J''$ | $F''$ | Wavenumber ( $^{151}\text{Eu}$ ) | Wavenumber ( $^{153}\text{Eu}$ ) |
|-----------|------|-------|-------|-------|----------------------------------|----------------------------------|
| 5         | 7.5  | 1     | 4     | 6.5   | 17108.4563                       | 17108.4912                       |
| 5         | 6.5  | 1     | 4     | 5.5   | 17108.5875                       | 17108.5415                       |
| 5         | 5.5  | 1     | 4     | 4.5   | 17108.6979                       | 17108.5908                       |
| 5         | 4.5  | 1     | 4     | 3.5   | 17108.7862                       | 17108.6394                       |
| 5         | 3.5  | 1     | 4     | 2.5   | 17108.8590                       | 17108.6701                       |
| 5         | 2.5  | 1     | 4     | 1.5   | 17108.9085                       | 17108.6979                       |
| 5         | 7.5  | 1     | 5     | 7.5   | 17108.6121                       | 17108.6529                       |
| 5         | 6.5  | 1     | 5     | 6.5   | 17108.7379                       | 17108.7118                       |
| 5         | 5.5  | 1     | 5     | 5.5   | 17108.8501                       | 17108.7608                       |
| 5         | 4.5  | 1     | 5     | 4.5   | 17108.9418                       | 17108.7992                       |
| 5         | 3.5  | 1     | 5     | 3.5   | 17109.0172                       | 17108.8319                       |
| 5         | 2.5  | 1     | 5     | 2.5   | 17109.0740                       | 17108.8590                       |
| 3, 4 or 5 | -    | 0     | 4     | 6.5   | 17084.0731                       | 17084.0932                       |
| 3, 4 or 5 | -    | 0     | 4     | 5.5   | 17084.2118                       | 17084.1561                       |
| 3, 4 or 5 | -    | 0     | 4     | 4.5   | 17084.3320                       | 17084.2117                       |

Table 7.5: Assignment of some of the transitions observed in the high-resolution LIF scans. The values of  $J'$  for some of the lines are not clear but the most probable assignment is given in bold font.

| $J'$             | $F'$ | $N''$ | $J''$ | $F''$ | Wavenumber ( $^{151}\text{Eu}$ ) | Wavenumber ( $^{153}\text{Eu}$ ) |
|------------------|------|-------|-------|-------|----------------------------------|----------------------------------|
| 3, <b>4 or 5</b> | -    | 0     | 4     | 3.5   | 17084.4297                       | 17084.2509                       |
| 3, <b>4 or 5</b> | -    | 0     | 4     | 2.5   | 17084.5045                       | 17084.2861                       |
| 3, <b>4 or 5</b> | -    | 0     | 4     | 1.5   | 17084.5588                       | 17084.3078                       |
| 3, <b>4 or 5</b> | -    | 1     | 4     | 6.5   | 17067.2922                       | 17067.3341                       |
| 3, <b>4 or 5</b> | -    | 1     | 4     | 5.5   | 17067.4162                       | 17067.3950                       |
| 3, <b>4 or 5</b> | -    | 1     | 4     | 4.5   | 17067.5224                       | 17067.4433                       |
| 3, <b>4 or 5</b> | -    | 1     | 4     | 3.5   | 17067.6108                       | 17067.4814                       |
| 3, <b>4 or 5</b> | -    | 1     | 4     | 2.5   | 17067.6832                       | 17067.5116                       |
| 3, <b>4 or 5</b> | -    | 1     | 4     | 1.5   | 17067.7459                       | 17067.5339                       |
| <b>3, 4 or 5</b> | -    | 0     | 4     | 6.5   | 17062.4600                       | 17062.5071                       |
| <b>3, 4 or 5</b> | -    | 0     | 4     | 5.5   | 17062.5967                       | 17062.5613                       |
| <b>3, 4 or 5</b> | -    | 0     | 4     | 4.5   | 17062.7112                       | 17062.6144                       |
| <b>3, 4 or 5</b> | -    | 0     | 4     | 3.5   | 17062.8079                       | 17062.6596                       |
| <b>3, 4 or 5</b> | -    | 0     | 4     | 2.5   | 17062.8838                       | 17062.6941                       |
| <b>3, 4 or 5</b> | -    | 0     | 4     | 1.5   | 17062.9387                       | 17062.7213                       |
| 3 or <b>4</b>    | -    | 1     | 3     | 5.5   | 17052.0923                       | 17052.1289                       |
| 3 or <b>4</b>    | -    | 1     | 3     | 4.5   | 17052.2384                       | 17052.1978                       |
| 3 or <b>4</b>    | -    | 1     | 3     | 3.5   | 17052.3580                       | 17052.2526                       |
| 3 or <b>4</b>    | -    | 1     | 3     | 2.5   | 17052.4531                       | 17052.2866                       |
| 3 or <b>4</b>    | -    | 1     | 3     | 1.5   | 17052.5150                       | 17052.3140                       |
| 3 or <b>4</b>    | -    | 1     | 3     | 0.5   | 17052.5447                       | 17052.3314                       |
| 3 or <b>4</b>    | -    | 2     | 3     | 5.5   | 17037.8903                       | 17037.9108                       |
| 3 or <b>4</b>    | -    | 2     | 3     | 4.5   | 17037.9764                       | 17037.9592                       |
| 3 or <b>4</b>    | -    | 2     | 3     | 3.5   | 17038.0568                       | 17037.9969                       |
| 3 or <b>4</b>    | -    | 2     | 3     | 2.5   | 17038.1339                       | 17038.0322                       |
| 3 or <b>4</b>    | -    | 2     | 3     | 1.5   | 17038.2027                       | 17038.0568                       |
| 3 or <b>4</b>    | -    | 2     | 3     | 0.5   | 17038.2601                       | 17038.0765                       |
| <b>3 or 4</b>    | -    | 1     | 4     | 6.5   | 16983.3335                       | 16983.3704                       |
| <b>3 or 4</b>    | -    | 1     | 4     | 5.5   | 16983.4452                       | 16983.4303                       |
| <b>3 or 4</b>    | -    | 1     | 4     | 4.5   | 16983.5453                       | 16983.4777                       |
| <b>3 or 4</b>    | -    | 1     | 4     | 3.5   | 16983.6320                       | 16983.5159                       |
| <b>3 or 4</b>    | -    | 1     | 4     | 2.5   | 16983.7112                       | 16983.5453                       |

Table 7.5: Assignment of some of the transitions observed in the high-resolution LIF scans. The values of  $J'$  for some of the lines are not clear but the most probable assignment is given in bold font.

| $J'$          | $F'$ | $N''$ | $J''$ | $F''$ | Wavenumber ( $^{151}\text{Eu}$ ) | Wavenumber ( $^{153}\text{Eu}$ ) |
|---------------|------|-------|-------|-------|----------------------------------|----------------------------------|
| <b>3 or 4</b> | -    | 1     | 4     | 1.5   | 16983.7824                       | 16983.5677                       |
| <b>3 or 4</b> | -    | 2     | 3     | 5.5   | 16982.7053                       | 16982.7334                       |
| <b>3 or 4</b> | -    | 2     | 3     | 4.5   | 16982.7929                       | 16982.7786                       |
| <b>3 or 4</b> | -    | 2     | 3     | 3.5   | 16982.8774                       | 16982.8179                       |
| <b>3 or 4</b> | -    | 2     | 3     | 2.5   | 16982.9512                       | 16982.8487                       |
| <b>3 or 4</b> | -    | 2     | 3     | 1.5   | 16983.0212                       | 16982.8740                       |
| <b>3 or 4</b> | -    | 2     | 3     | 0.5   | 16983.0861                       | 16982.8989                       |

It is interesting to compare the molecular Fermi contact interaction parameters to those of the free  $\text{Eu}^+$  ion. The values for both isotopes are taken from Ref. [41] where for the  $^{151}\text{Eu}^+$  ion the coupling constant for the magnetic-dipole interaction ( $A$ ) was found to be  $0.0514 \text{ cm}^{-1}$  and for the  $^{153}\text{Eu}^+$  ion it was found to be  $0.0228 \text{ cm}^{-1}$ . The value of  $A$  is a sum of the isotropic constant  $A_{\text{iso}}$  (which is analogous to molecular  $b_F$ ) and the dipolar hyperfine interaction  $A_{\text{dip}}$  [42]. The  $A_{\text{dip}}$  value is expected to be very small for the ground configuration of  $\text{Eu}^+$  and one can assume that  $A \approx A_{\text{iso}}$ . Therefore the ratio between molecular and ionic Fermi contact interaction parameters is 0.41 for both isotopologues or in other words the ground state configuration has 41%  $6s$  character, which is reasonable considering that the electric field of the  $\text{H}^-$  ion in the molecule polarizes the  $\text{Eu}^+$  ion.

One can speculate about the values of the  $B$  rotational constant based on the available information. As can be seen from the Table 7.5 there are lines at  $17108 \text{ cm}^{-1}$  and  $16983 \text{ cm}^{-1}$  that have common lower state level ( $N'' = 1, J'' = 4$ ). If one assumes that the upper state levels of these transitions are  $J' = 5$  and  $J' = 3$  of the same  $\Omega$ -component then the  $B'$  value can be estimated to be  $\sim 6.94 \text{ cm}^{-1}$ . Based on that value we can predict that the  $J' = 4$  to  $N'' = 1, J'' = 4$  transition will be at  $\sim 17038.5 \text{ cm}^{-1}$  and there are indeed a number of lines in that area, but they are in a congested region, making their assignment difficult.

Finally a low resolution dispersed-fluorescence experiment enabled us to determine the vibrational spacing between the  $v''=0$  and  $v''=1$  levels in the ground state as  $1145(\pm 5) \text{ cm}^{-1}$ .

## 7.4 Conclusions and future work

We have recorded FT and LIF spectra of the EuH molecule. In the FT spectrum we have observed many transitions in the  $10\,000 - 18\,000\text{ cm}^{-1}$  region. The lack of any information about the electronic states of EuH together with the perturbations, band overlaps and other difficulties in the spectrum make the assignment difficult. The “cold” spectrum of EuH recorded in the laser ablation/molecular beam setup showed that in the FT spectrum only the transition at  $\sim 17\,000\text{ cm}^{-1}$  terminates at the ground  $X\ ^9\Sigma^-$  electronic state. Unfortunately we were unable to perform a continuous high resolution scan of this band because it spreads over a  $\sim 100\text{ cm}^{-1}$  region, and the condition of the Eu rod did not allow coverage of such a wide region. Instead we have recorded only the most intense features at high resolution. This enabled us to extract some information about the spectroscopic parameters of the ground and excited states in this transition, but still more information is required to obtain a full analysis. Therefore it is necessary to record a high resolution LIF spectrum of this band: however, the price of Eu metal is very high and it is important to have more information about the electronic states involved. In other words, reliable *ab initio* calculations are needed before experiments on the EuH molecule can be resumed.

# Bibliography

- [1] P. Vaida and J. N. Daou, Phys. Rev. B **49**, 3275 (1994).
- [2] W. Bauhofer, W. Joss, R. K. Kremer, H. J. Mattausch, and A. Simon, J. Magn. Mater. **104**, 1243 (1992).
- [3] C. Rao and J. Gopalkrishnan, *New Directions in Solid State Chemistry*, CUP, London, 3rd edition, 1986.
- [4] L. Hagland, I. Kopp, and N. Åslund, Arkiv för Fysik **32**, 321 (1966).
- [5] I. Kopp, L. Hagland, and B. Rydh, Can. J. Phys. **53**, 2242 (1975).
- [6] A. Bahmaier, R.-D. Urban, and H. Jones, Chem. Phys. Lett. **195**, 609 (1992).
- [7] C. Effantin and J. D'Incan, Can. J. Phys. **51**, 1394 (1973).
- [8] J. D'Incan, C. Effantin, and R. Bacis, Can. J. Phys. **50**, 1810 (1972).
- [9] C. Effantin and J. D'Incan, Can. J. Phys. **52**, 523 (1974).
- [10] J. D'Incan, C. Effantin, and R. Bacis, Can. J. Phys. **55**, 1654 (1977).
- [11] J. D'Incan, C. Effantin, and R. Bacis, J. Phys. B **5**, L187 (1972).
- [12] S. P. Willson and L. Andrews, J. Chem. Phys. **104**, 1640 (2000).
- [13] P. Pyykkö, Physica Scripta **20**, 647 (1979).
- [14] M. Dolg and H. Stoll, Theor. Chem. Acta **75**, 369 (1989).
- [15] M. Dolg, H. Stoll, and H. Preuss, Chem. Phys. **165**, 321 (1992).
- [16] M. Dolg and H. Stoll, *Electronic Structure Calculations for Molecules Containing Lanthanide Atoms*, volume 22, Elsevier, Amsterdam.

- [17] X. Cao, W. Liu, and M. Dolg, *Science in China (Series B)* **31**, 6 (2001).
- [18] Y. N. Dmitriev et al., *Acta Physics Hungarica* **61**, 51 (1987).
- [19] P. Carrette, A. Hocquet, M. Douay, and B. Pinchemel, *J. Mol. Spectrosc.* **124**, 243 (1987).
- [20] L. A. Kaledin, M. Erickson, and M. C. Heaven, *J. Mol. Spectrosc.* **165**, 323 (1994).
- [21] A. L. Kaledin, M. C. Heaven, R. W. Field, and L. A. Kaledin, *J. Mol. Spectrosc.* **179**, 310 (1996).
- [22] T. Yang and R. Pitzer, private communication.
- [23] A. Shayesteh, D. Appadoo, I. Gordon, R. LeRoy, and P. Bernath, *J. Chem. Phys.* **120**, 10002 (2004).
- [24] A. Shayesteh, K. Walker, I. Gordon, D. Appadoo, and P. Bernath, *J. Mol. Struct.* **695**, 23 (2004).
- [25] I. E. Gordon, A. Shayesteh, D. Appadoo, K. Walker, and P. Bernath, *J. Mol. Spectrosc.* **229**, 269 (2005).
- [26] B. Elden, *Metrologia* **2**, 71.
- [27] W. Whaling, W. Anderson, M. Carle, J. Brault, and H. Zarem, *J. Res. Natl. Inst. Stand. Technol.* **107**, 149.
- [28] S. Gerstenkorn and P. Luc, *Atlas du spectre d'absorption de la molécule de diode*, Editions du C. N. R. S., Paris, 1978.
- [29] S. Gerstenkorn, P. Luc, and R. Vetter, *Rev. Phys. Appl.* **16**, 529 (1981).
- [30] E. Wigner and E. E. Witmer, *Z. Physik* **51**, 859 (1928).
- [31] H. Lefebvre-Brion and R. W. Field, *Perturbations in the Spectra of Diatomic Molecules*, Academic Press, New York, 1986.
- [32] T. Varberg, J. A. Gray, R. Field, and A. Merer, *J. Mol. Spectrosc.* **156**, 296 (1992).
- [33] M. J. Dick, J.-G. Wang, J. Tang, and P. F. Bernath, Laser spectroscopy of europium monofluoride, in *59<sup>th</sup> Ohio State University International Symposium on Molecular Spectroscopy*, page TB04, Columbus, Ohio, 2004.

- [34] T. C. Steimle, J. Gengler, and J. Chen, *Can. J. Chem.* **82**, 779 (2004).
- [35] H. M. Pickett, *J. Mol. Spectrosc.* **148**, 371 (1991).
- [36] I. Mills, T. Cvitaš, K. Homann, N. Kallay, and K. Kuchitsu, *Quantities, Units and Symbols in Physical Chemistry*, Blackwell Science, Oxford, 2nd edition, 1993.
- [37] C. H. Townes and A. L. Schawlow, *Microwave Spectroscopy*, Dover, New York, 1975.
- [38] T. M. Dunn, Nuclear hyperfine structure in the electronic spectra of diatomic molecules, in *Molecular Spectroscopy- Modern Research*, edited by K. N. Rao and C. W. Mathews, pages 231–257, Academic Press, New York, 1978.
- [39] T. Varberg, R. Field, and A. Merer, *J. Chem. Phys.* **95**, 1563 (1991).
- [40] C. Ryzlewicz, H.-U. Schutze-Pahlmann, J. Hoeft, and T. Torring, *Chem. Phys.* **71**, 389 (1982).
- [41] O. Becker, K. Enders, G. Werth, and J. Dembczynski, *Phys. Rev. A* **48**, 3546 (1993).
- [42] W. Weltner, *Magnetic atoms and molecules*, Van Nostrand Reinhold, New York, 1983.

# Chapter 8

## First observations of the gas-phase spectra of SmH, SmCl, TmH and ErF

### 8.1 Samarium monohydride

The gas phase SmH molecule was generated in the high temperature furnace/electrical discharge emission source described in section 3.2.2. The inside of the alumina tube was wrapped with molybdenum foil to prevent the reaction between the metal and ceramic. The tube furnace was heated to 950°C and a mixture of Ar ( $\sim$ 5 Torr) and H<sub>2</sub> (or D<sub>2</sub> for SmD) ( $\sim$ 2 Torr) gases flowed slowly over the metal. The melting point of samarium metal is 1072°C so during our experiment the metal was in the solid phase. The surface of samarium metal was absorbing hydrogen just as in experiments with europium metal (see Chapter 7). An electrical discharge (3 kV, 333 mA) was applied between two cylindrical stainless steel electrodes inside the ends of the tube. Emission from the tube was focused onto the entrance aperture of a Bruker IFS HR 120 Fourier transform spectrometer. The windows at the ends of the tube and the lens were made from BaF<sub>2</sub>. The SmH emission spectrum was recorded in the 8 000-15 800 cm<sup>-1</sup> region using a silicon photodiode detector, CaF<sub>2</sub> beamsplitter and 640 nm red-pass filter. The molecular emission was observed in the 11 000 cm<sup>-1</sup> region (see Fig 8.1). The observed bandheads are at 10575.03 cm<sup>-1</sup> (red degraded), 10620.11 cm<sup>-1</sup> (red degraded) and 10700.42 cm<sup>-1</sup> (blue degraded). A total of 180 scans for both molecules were co-added at a resolution of 0.04 cm<sup>-1</sup> in order to obtain a good signal-to-noise ratio. The observed lines (or at least the strongest lines) appear to belong to two different bands (further referred

to as the red system and the blue system). Line positions were measured using a Windows-based program called WSpectra, written by M. Carleer (Université Libre de Bruxelles). The spectrometer was not under vacuum and the “air-to-vacuum” wavenumber correction [1] had to be made before the lines were calibrated against argon atomic lines present in the spectrum [2].

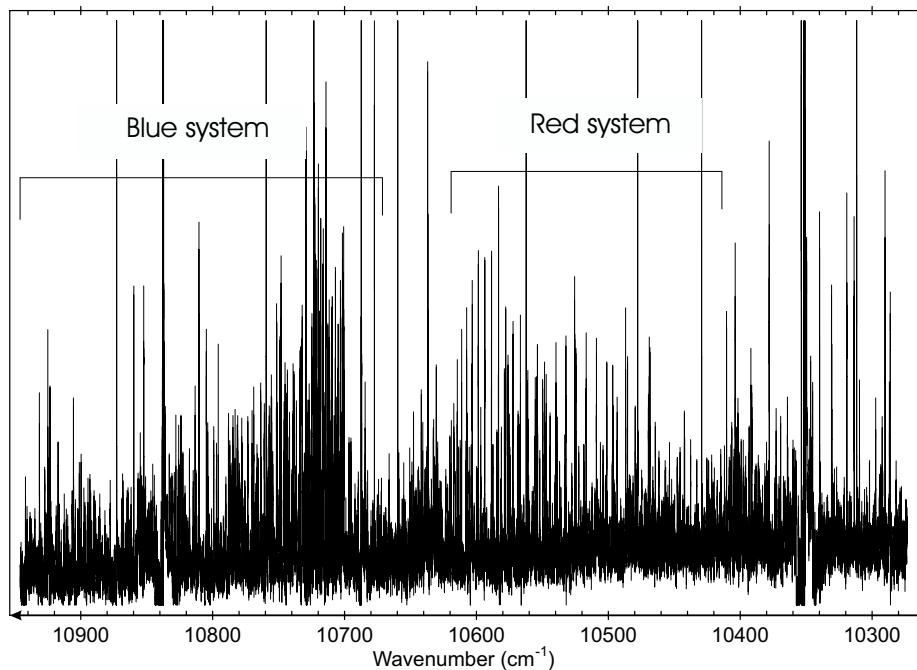


Figure 8.1: An overview of the SmH electronic transitions.

In order to analyze the recorded spectrum of SmH it is necessary to consider what electronic states may be involved in the observed transitions. The ground state configuration of the  $\text{Sm}^+$  ion is  $4f^66s^1$  [3]. The lowest lying state of this configuration is an  ${}^8F$  [4], where spins of all seven unpaired electrons are parallel. This ionic state gives rise to  ${}^8\Phi$ ,  ${}^8\Delta$ ,  ${}^8\Pi$  and  ${}^8\Sigma^+$  molecular electronic states. When the spin of  $s$  electron flips ( ${}^6F$  state) the resultant molecular states will be  ${}^6\Phi$ ,  ${}^6\Delta$ ,  ${}^6\Pi$  and  ${}^6\Sigma^+$ . It is hard to determine the relative positions of these states and it is convenient to consider separate  $\Omega$ -components in the frame of ligand field theory (LFT). As it was mentioned earlier ligand field theory does not apply very well to lanthanide hydrides because hydrogen can not be considered as a point charge, nevertheless LFT can provide qualitative information about the low-lying states of SmH. The  ${}^8F$  term has  ${}^8F_{1/2}$ ,  ${}^8F_{3/2}$ ,  ${}^8F_{5/2}$ ,  ${}^8F_{7/2}$ ,  ${}^8F_{9/2}$ ,  ${}^8F_{11/2}$  and  ${}^8F_{13/2}$   $J$ -components, with

the  $^8F_{1/2}$  state being lowest in energy because the  $f$  shell is less than half-filled. Each of these states is split into several doubly degenerate  $\Omega$ -components by the presence of the negatively charged ligand (hydrogen anion), for example, the  $^8F_{13/2}$  state is split into  $\Omega$ -components with  $\Omega = 1/2, 3/2, 5/2, 7/2, 9/2, 11/2$  and  $13/2$ . In total there will be 28 degenerate states arising from the ionic  $^8F$  state with one of the  $\Omega = 1/2$  states being the ground state. The first excited configuration of  $\text{Sm}^+$  is  $4f^56s^2$  with the  $^6H$  term being the lowest arising from this configuration. This state has six  $J$ -components with  $^6H_{5/2}$  lying lowest in energy. The ligand field splits  $^6H_{5/2}$  into  $\Omega = 1/2, 3/2$  and  $5/2$  components. Kaledin *et al.* [3] calculated that for the  $\text{SmF}$  molecule the lowest  $\Omega = 1/2$  state is located  $9800 \text{ cm}^{-1}$  above the ground state, which is close to the region where we observe  $\text{SmH}$  bands. Ren *et al.* [5] calculated the ligand field splittings of the  $^6H$  state for  $\text{SmF}$  using density functional theory.

The red system appears to have strong  $R$  and  $Q$  branches, but we were unable to find the  $P$  branch because of the great congestion of lines. This intensity pattern points to a  $\Delta\Omega = +1$  transition and the excited state could be an  $\Omega = 3/2$  state, arising from the  $4f^56s^2$  configuration, and the transition could connect to the ground  $\Omega = 1/2$  state. The blue system has only an obvious strong  $P$  branch with a head, this transition may be from the  $\Omega' = 1/2$  state, arising from the  $4f^56s^2$  configuration to the first  $\Omega'' = 3/2$  state arising from the ground  $4f^66s^1$  configuration. Unfortunately we were not able to perform rotational assignment of these bands due to their relatively poor signal to noise ratio.

## 8.2 Samarium monochloride

The spectrum of  $\text{SmCl}$  was recorded in the same experimental setup as  $\text{SmH}$ , but using  $\text{CH}_3\text{Cl}$  gas instead of  $\text{H}_2$ . The observed bands are so dense that even at an instrumental resolution of  $0.04 \text{ cm}^{-1}$  the rotational structure was not resolved. In addition the signal to noise ratio of these bands is poor. The bandhead positions are  $11\,129.6 \text{ cm}^{-1}$ ,  $11\,512.7 \text{ cm}^{-1}$ ,  $11\,688.0 \text{ cm}^{-1}$  and  $11\,710.9 \text{ cm}^{-1}$ . The observed bandheads (see Figure 8.2) are in reasonable agreement with the prediction from Ref. [3] for  $\text{SmCl}$  that an  $\Omega' = 1/2$  state of the  $4f^56s^2$  configuration lies  $12\,200 \text{ cm}^{-1}$  above the ground state.

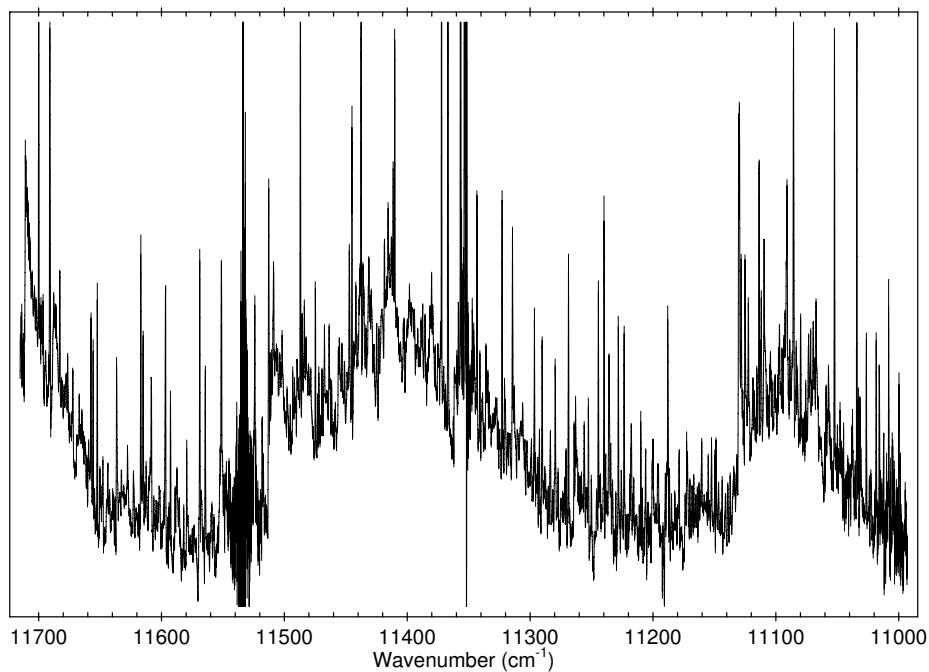


Figure 8.2: Observed bands of SmCl. The bands in this figure are actually recorded at  $0.2\text{ cm}^{-1}$  resolution as the bands can be seen more clearly at lower resolution.

### 8.3 Thulium monohydride

About 20 g of thulium metal was heated in the King furnace (carbon tube furnace), described in the section 3.2.3, to a temperature of  $\sim 2000^\circ\text{C}$  with a mixture of hydrogen (or deuterium) and helium gases flowing slowly through the system. The inside of the carbon sample holder was wrapped with tantalum and tungsten foils. The total pressure inside the furnace was kept at  $\sim 120$  Torr. A  $\text{BaF}_2$  lens was employed to image emission from the King furnace onto the entrance aperture of a Bruker IFS 120 HR Fourier transform spectrometer. The TmH emission spectrum was recorded in the  $8\,000 - 15\,800\text{ cm}^{-1}$  region using a silicon photodiode detector,  $\text{CaF}_2$  beamsplitter and 640 nm red-pass filter. The TmH bands were found at  $14\,000 - 15\,000\text{ cm}^{-1}$  region (see Figure 8.3). The bands are very weak and have a complicated structure leading to failure of the rotational assignment. Nevertheless one can speculate about the electronic states involved in this spectrum.

In his Dirac-Fock one-center expansion calculations Pyykkö [6] assumed that the ground state electron configuration of TmH is  $4f^{14}[(6s + 6p + 6d)\sigma]^2$ , but he

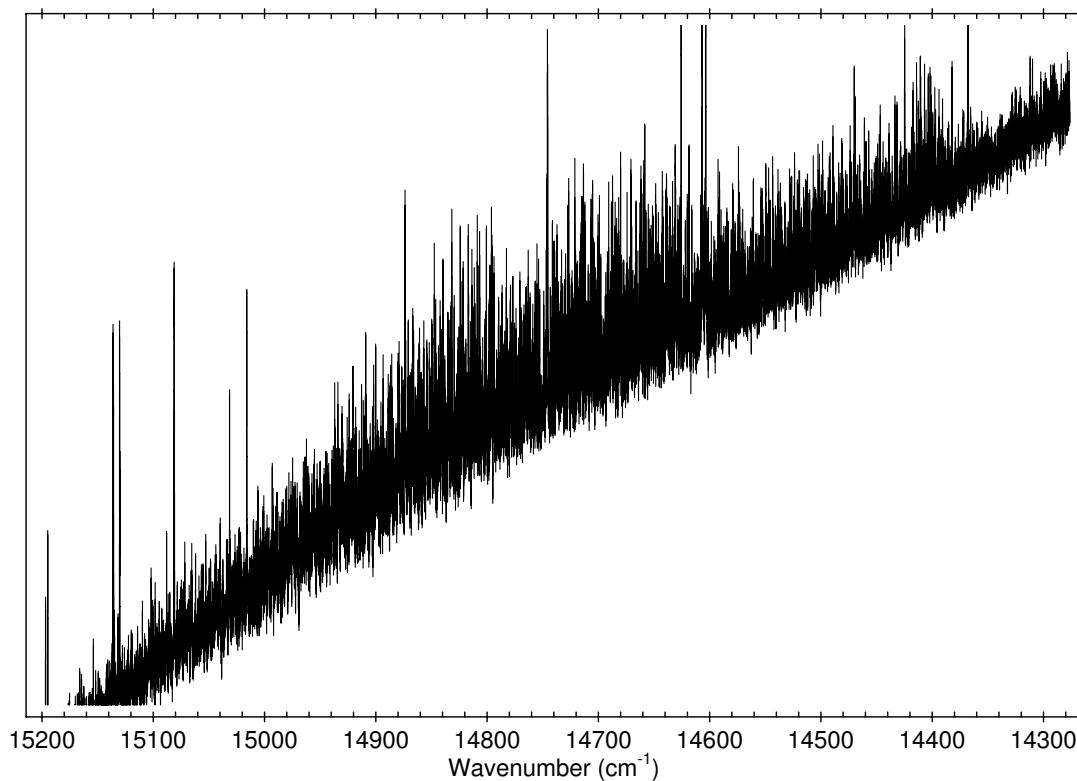


Figure 8.3: TmH electronic transition observed in emission from the King furnace.

admitted that it may not be a realistic choice. The ground configuration of the  $\text{Er}^+$  ion is  $4f^{12}6s^2$  [3] with the lowest electronic state being  ${}^3\text{H}_6$ . This  ${}^3\text{H}_6$  state is split by the ligand field into 7 spin components with  $\Omega = 0^+$  component being the ground state of the TmH. The excited state of the observed transition is probably arising from the  $4f^{12}6s^16p^1$  configuration. LFT calculations [3] place the first  $\Omega = 0$  component of this configuration for TmF at  $16\,800\text{ cm}^{-1}$ .

## 8.4 Erbium monofluoride

The spectrum of ErF was generated in the King furnace (carbon tube furnace) described in the section 3.2.3. The erbium metal sample (about 40 g) was heated in the furnace to a temperature of  $\sim 2200^\circ\text{C}$  with a mixture of  $\text{SF}_6$  and helium gases flowing slowly through the system. The inside of the carbon sample holder

was wrapped with tantalum and tungsten foils. The total pressure was maintained at  $\sim 150$  Torr. Emission from the tube was imaged onto the entrance aperture of a Bruker IFS 120 HR Fourier transform spectrometer. The windows that sealed the furnace and the lens were made from  $\text{BaF}_2$ . First a survey scan was performed in the visible and the near infrared parts of the spectrum. We have found two  $\text{ErF}$  bands near  $17500 \text{ cm}^{-1}$ . A 550 nm band pass filter was then used to eliminate the contribution of strong black body radiation in order to improve the signal to noise ratio of the molecular lines. One difficulty arose during the experiment in that the emission and absorption lines were “competing” in the spectrum and it was hard to optimize either one. The emission spectrum of  $\text{ErF}$  is shown in Fig. 8.4. Ten scans were recorded at  $0.2 \text{ cm}^{-1}$  resolution. Unfortunately at the moment when a higher resolution scan was planned to start, the furnace carbon heating element was permanently damaged by the  $\text{Er}$  metal, which also destroyed the foils and carbon holder. After that experience we abandoned the experiments with rare earth metals in the King furnace as they proved to be expensive and dangerous.

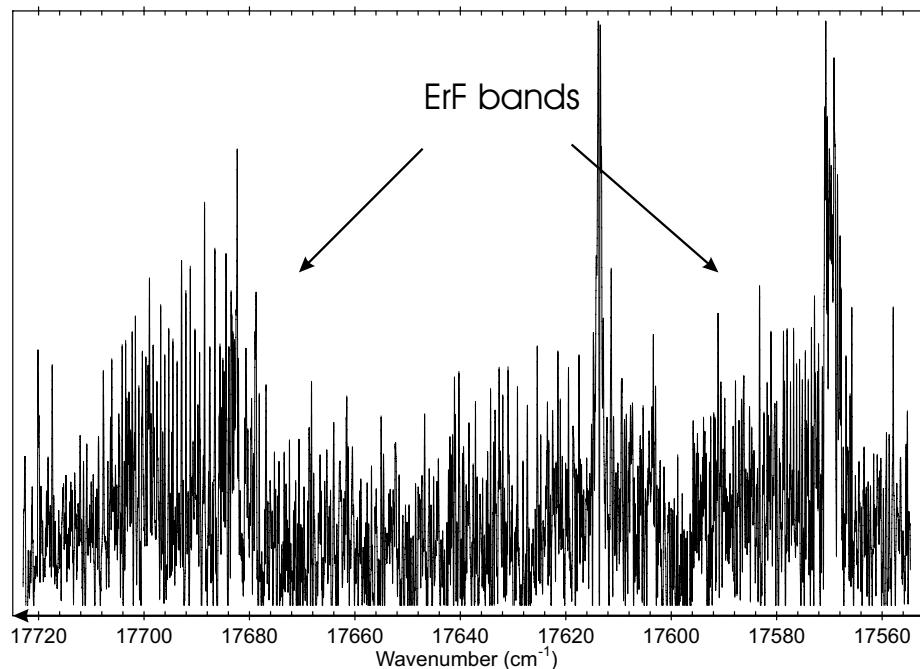


Figure 8.4:  $\text{ErF}$  electronic transitions.

The two bands of  $\text{ErF}$  in Fig. 8.4 are therefore recorded at low resolution and poor signal to noise ratio. The bandhead positions are  $17567.8 \text{ cm}^{-1}$  and  $17682.3$

$\text{cm}^{-1}$ . Although a rotational analysis is not possible in these circumstances some conclusions can be made about the nature of the observed transitions. The ground configuration of the  $\text{Er}^+$  ion is  $4f^{11}6s^2$  [3] with the lowest electronic state being  ${}^4\text{I}_{15/2}$ . The ligand field splits this state into 8 components with  $\Omega=1/2$  to  $\Omega=15/2$ . The  $\Omega=1/2$  component of this state is the ground state of  $\text{ErF}$ . It is worth noting that in the theoretical work of Lesar *et al.* [7] the authors calculate spectroscopic parameters for erbium and thulium fluorides. They give the ground state of  $\text{ErF}$  as a  ${}^1\Sigma_g$  state (Table 1 of Ref. [7]), which is probably a typographical error. Kaledin *et al.* [3] predict the  $\Omega=1/2$  state of the excited  $4f^{11}6s^16p^1$  configuration to be at  $16\,700 \text{ cm}^{-1}$  above the ground electronic state. We observe transitions at  $17\,550 - 17\,720 \text{ cm}^{-1}$  region, which is close to that prediction.

As it was mentioned above it is hazardous to resume experiments with  $\text{ErF}$  in the King furnace, but the observed spectrum can be revisited using the molecular beam apparatus as we did for the  $\text{EuH}$  molecule at Arizona State University (see Chapter 7). The metal fluorides usually yield stronger signals in laser ablation experiments than hydrides and the probability of a successful experiment is high.

## 8.5 Conclusions

The emission spectra presented in this chapter represent preliminary observations of transitions of  $\text{SmH}$ ,  $\text{SmCl}$ ,  $\text{TmH}$  and  $\text{ErF}$ . These spectra can serve as guides to more detailed spectroscopic studies of these molecules. For example, our spectrum of  $\text{ErF}$  can be used to plan molecular beam experiments using laser-induced fluorescence detection.

In this thesis spectra of different metal-containing diatomic molecules were studied. Analysis of new high resolution infrared emission spectra of  $\text{MnH}$  and  $\text{MnD}$  recorded with a Fourier transform spectrometer have extended earlier data and have given improved spectroscopic constants. Analysis of the electronic emission spectra of  $\text{CoH}$  and  $\text{CoD}$  have provided significantly improved spectroscopic constants for the ground and excited electronic states. In addition, a new electronic state of  $\text{CoD}$  ([13.3]4) has been found in these experiments. Three new near-infrared transitions of  $\text{YbO}$  are reported in this work, and their rotational analyses were carried out. Extensive work on the  $\text{EuH}$  molecule has given some insights concerning the electronic structure. Although some spectroscopic parameters were estimated for  $\text{EuH}$ , there is considerable scope for further work.

# Bibliography

- [1] B. Elden, *Metrologia* **2**, 71.
- [2] W. Whaling, W. Anderson, M. Carle, J. Brault, and H. Zarem, *J. Res. Natl. Inst. Stand. Technol.* **107**, 149.
- [3] A. L. Kaledin, M. C. Heaven, R. W. Field, and L. A. Kaledin, *J. Mol. Spectrosc.* **179**, 310 (1996).
- [4] W. C. Martin, R. Zalubas, and L. Hagan, *Atomic Energy Levels—The Rare Earth Elements*, US Government Printing Office, Washington, 1978.
- [5] J. Ren, M.-H. Whangbo, D. Dai, and L. Li, *J. Chem. Phys.* **108**, 8479 (1998).
- [6] P. Pyykkö, *Physica Scripta* **20**, 647 (1979).
- [7] A. Lesar, G. Muri, and M. Hodošček, *J. Phys. Chem.* **102**, 1170 (1998).

# APPENDIX

# Appendix A

## Line lists for MnH and MnD

Line lists for MnH and MnD, together with uncertainties assigned to these lines, calculated lines and differences between calculated and observed wavenumbers. The calculated lines in these tables were obtained from the band constant fits.

### A.1 Line list for MnH

Table A.1: Line list for MnH.

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 1    | 1    | 4    | 0     | 0     | 3     | 1501.6312 | 1501.6327  | -0.0015  | 0.001       |
| 0    | 1    | 3    | 1     | 0     | 4     | 1479.3361 | 1479.3343  | 0.0019   | 0.001       |
| 2    | 1    | 4    | 1     | 0     | 3     | 1512.1517 | 1512.1569  | -0.0052  | 1           |
| 2    | 1    | 5    | 1     | 0     | 4     | 1512.1843 | 1512.1826  | 0.0018   | 0.002       |
| 1    | 1    | 4    | 2     | 0     | 5     | 1467.8079 | 1467.8115  | -0.0036  | 10          |
| 1    | 1    | 3    | 2     | 0     | 4     | 1467.8476 | 1467.8408  | 0.0068   | 10          |
| 1    | 1    | 2    | 2     | 0     | 3     | 1467.9142 | 1467.9151  | -0.0009  | 0.001       |
| 3    | 1    | 2    | 2     | 0     | 1     | 1522.2613 | 1522.2696  | -0.0082  | 10          |
| 3    | 1    | 3    | 2     | 0     | 2     | 1522.2956 | 1522.3021  | -0.0064  | 10          |
| 3    | 1    | 4    | 2     | 0     | 3     | 1522.3343 | 1522.3376  | -0.0033  | 10          |
| 3    | 1    | 5    | 2     | 0     | 4     | 1522.3718 | 1522.3717  | 0.0001   | 0.002       |
| 3    | 1    | 6    | 2     | 0     | 5     | 1522.3984 | 1522.3977  | 0.0007   | 0.002       |
| 2    | 1    | 5    | 3     | 0     | 6     | 1455.9748 | 1455.9773  | -0.0025  | 0.005       |
| 2    | 1    | 4    | 3     | 0     | 5     | 1456.0077 | 1456.0091  | -0.0014  | 0.005       |
| 2    | 1    | 3    | 3     | 0     | 4     | 1456.0550 | 1456.0511  | 0.0039   | 0.005       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 2    | 1    | 2    | 3     | 0     | 3     | 1456.0976 | 1456.0945  | 0.0031   | 0.005       |
| 2    | 1    | 1    | 3     | 0     | 2     | 1456.1311 | 1456.1337  | -0.0026  | 0.001       |
| 4    | 1    | 1    | 3     | 0     | 0     | 1532.0992 | 1532.1023  | -0.0031  | 0.005       |
| 4    | 1    | 2    | 3     | 0     | 1     | 1532.1235 | 1532.1275  | -0.0040  | 0.005       |
| 4    | 1    | 3    | 3     | 0     | 2     | 1532.1509 | 1532.1548  | -0.0039  | 0.005       |
| 4    | 1    | 4    | 3     | 0     | 3     | 1532.1812 | 1532.1840  | -0.0028  | 0.005       |
| 4    | 1    | 5    | 3     | 0     | 4     | 1532.2148 | 1532.2141  | 0.0008   | 0.001       |
| 4    | 1    | 6    | 3     | 0     | 5     | 1532.2437 | 1532.2432  | 0.0005   | 0.001       |
| 4    | 1    | 7    | 3     | 0     | 6     | 1532.2691 | 1532.2688  | 0.0003   | 0.001       |
| 3    | 1    | 6    | 4     | 0     | 7     | 1443.8396 | 1443.8414  | -0.0018  | 0.005       |
| 3    | 1    | 5    | 4     | 0     | 6     | 1443.8724 | 1443.8748  | -0.0024  | 0.005       |
| 3    | 1    | 4    | 4     | 0     | 5     | 1443.9140 | 1443.9128  | 0.0012   | 0.005       |
| 3    | 1    | 3    | 4     | 0     | 4     | 1443.9524 | 1443.9517  | 0.0007   | 0.005       |
| 3    | 1    | 2    | 4     | 0     | 3     | 1443.9907 | 1443.9887  | 0.0020   | 0.005       |
| 3    | 1    | 1    | 4     | 0     | 2     | 1444.0246 | 1444.0222  | 0.0025   | 0.005       |
| 3    | 1    | 0    | 4     | 0     | 1     | 1444.0491 | 1444.0512  | -0.0021  | 0.005       |
| 5    | 1    | 2    | 4     | 0     | 1     | 1541.6338 | 1541.6296  | 0.0042   | 0.001       |
| 5    | 1    | 3    | 4     | 0     | 2     | 1541.6512 | 1541.6551  | -0.0039  | 0.001       |
| 5    | 1    | 4    | 4     | 0     | 3     | 1541.6799 | 1541.6816  | -0.0017  | 0.001       |
| 5    | 1    | 5    | 4     | 0     | 4     | 1541.7085 | 1541.7088  | -0.0003  | 0.001       |
| 5    | 1    | 6    | 4     | 0     | 5     | 1541.7374 | 1541.7364  | 0.0010   | 0.001       |
| 5    | 1    | 7    | 4     | 0     | 6     | 1541.7636 | 1541.7632  | 0.0004   | 0.001       |
| 5    | 1    | 8    | 4     | 0     | 7     | 1541.7877 | 1541.7881  | -0.0004  | 0.001       |
| 4    | 1    | 7    | 5     | 0     | 8     | 1431.4102 | 1431.4117  | -0.0015  | 0.005       |
| 4    | 1    | 6    | 5     | 0     | 7     | 1431.4447 | 1431.4462  | -0.0015  | 0.005       |
| 4    | 1    | 5    | 5     | 0     | 6     | 1431.4830 | 1431.4833  | -0.0003  | 0.005       |
| 4    | 1    | 4    | 5     | 0     | 5     | 1431.5211 | 1431.5211  | 0.0001   | 0.005       |
| 4    | 1    | 3    | 5     | 0     | 4     | 1431.5577 | 1431.5576  | 0.0001   | 0.005       |
| 4    | 1    | 2    | 5     | 0     | 3     | 1431.5936 | 1431.5920  | 0.0016   | 0.005       |
| 4    | 1    | 1    | 5     | 0     | 2     | 1431.6232 | 1431.6234  | -0.0002  | 0.005       |
| 6    | 1    | 3    | 5     | 0     | 2     | 1550.7958 | 1550.7971  | -0.0013  | 0.001       |
| 6    | 1    | 4    | 5     | 0     | 3     | 1550.8210 | 1550.8221  | -0.0011  | 0.001       |
| 6    | 1    | 5    | 5     | 0     | 4     | 1550.8476 | 1550.8475  | 0.0001   | 0.001       |
| 6    | 1    | 6    | 5     | 0     | 5     | 1550.8744 | 1550.8732  | 0.0012   | 0.001       |
| 6    | 1    | 7    | 5     | 0     | 6     | 1550.9003 | 1550.8990  | 0.0013   | 0.001       |
| 6    | 1    | 8    | 5     | 0     | 7     | 1550.9245 | 1550.9242  | 0.0003   | 0.001       |
| 6    | 1    | 9    | 5     | 0     | 8     | 1550.9479 | 1550.9482  | -0.0003  | 0.005       |
| 5    | 1    | 8    | 6     | 0     | 9     | 1418.6947 | 1418.6955  | -0.0008  | 0.005       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 5    | 1    | 7    | 6     | 0     | 8     | 1418.7301 | 1418.7310  | -0.0009  | 0.001       |
| 5    | 1    | 5    | 6     | 0     | 6     | 1418.8053 | 1418.8056  | -0.0003  | 0.001       |
| 5    | 1    | 4    | 6     | 0     | 5     | 1418.8416 | 1418.8422  | -0.0006  | 0.001       |
| 5    | 1    | 3    | 6     | 0     | 4     | 1418.8772 | 1418.8772  | 0.0000   | 0.001       |
| 5    | 1    | 2    | 6     | 0     | 3     | 1418.9103 | 1418.9100  | 0.0003   | 0.001       |
| 7    | 1    | 4    | 6     | 0     | 3     | 1559.5977 | 1559.5981  | -0.0004  | 0.001       |
| 7    | 1    | 5    | 6     | 0     | 4     | 1559.6224 | 1559.6222  | 0.0002   | 0.001       |
| 7    | 1    | 6    | 6     | 0     | 5     | 1559.6473 | 1559.6465  | 0.0008   | 0.001       |
| 7    | 1    | 7    | 6     | 0     | 6     | 1559.6711 | 1559.6708  | 0.0003   | 0.001       |
| 7    | 1    | 8    | 6     | 0     | 7     | 1559.6978 | 1559.6951  | 0.0027   | 0.001       |
| 7    | 1    | 9    | 6     | 0     | 8     | 1559.7190 | 1559.7189  | 0.0001   | 0.001       |
| 7    | 1    | 10   | 6     | 0     | 9     | 1559.7411 | 1559.7418  | -0.0007  | 0.001       |
| 6    | 1    | 9    | 7     | 0     | 10    | 1405.7000 | 1405.7003  | -0.0003  | 0.002       |
| 6    | 1    | 8    | 7     | 0     | 9     | 1405.7361 | 1405.7366  | -0.0005  | 0.002       |
| 6    | 1    | 7    | 7     | 0     | 8     | 1405.7739 | 1405.7740  | -0.0001  | 0.002       |
| 6    | 1    | 6    | 7     | 0     | 7     | 1405.8114 | 1405.8115  | -0.0001  | 0.002       |
| 6    | 1    | 5    | 7     | 0     | 6     | 1405.8473 | 1405.8484  | -0.0011  | 0.002       |
| 6    | 1    | 4    | 7     | 0     | 5     | 1405.8831 | 1405.8840  | -0.0009  | 0.002       |
| 6    | 1    | 3    | 7     | 0     | 4     | 1405.9178 | 1405.9178  | 0.0000   | 0.002       |
| 8    | 1    | 5    | 7     | 0     | 4     | 1568.0257 | 1568.0256  | 0.0001   | 0.001       |
| 8    | 1    | 6    | 7     | 0     | 5     | 1568.0489 | 1568.0487  | 0.0003   | 0.001       |
| 8    | 1    | 7    | 7     | 0     | 6     | 1568.0727 | 1568.0717  | 0.0010   | 0.001       |
| 8    | 1    | 8    | 7     | 0     | 7     | 1568.0957 | 1568.0947  | 0.0010   | 0.001       |
| 8    | 1    | 9    | 7     | 0     | 8     | 1568.1186 | 1568.1176  | 0.0011   | 0.001       |
| 8    | 1    | 10   | 7     | 0     | 9     | 1568.1399 | 1568.1400  | -0.0001  | 0.001       |
| 8    | 1    | 11   | 7     | 0     | 10    | 1568.1609 | 1568.1618  | -0.0009  | 0.001       |
| 7    | 1    | 10   | 8     | 0     | 11    | 1392.4333 | 1392.4333  | 0.0000   | 0.002       |
| 7    | 1    | 9    | 8     | 0     | 10    | 1392.4700 | 1392.4702  | -0.0002  | 0.002       |
| 7    | 1    | 8    | 8     | 0     | 9     | 1392.5084 | 1392.5080  | 0.0004   | 0.002       |
| 7    | 1    | 7    | 8     | 0     | 8     | 1392.5459 | 1392.5458  | 0.0001   | 0.002       |
| 7    | 1    | 6    | 8     | 0     | 7     | 1392.5826 | 1392.5831  | -0.0005  | 0.002       |
| 7    | 1    | 5    | 8     | 0     | 6     | 1392.6189 | 1392.6192  | -0.0003  | 0.002       |
| 7    | 1    | 4    | 8     | 0     | 5     | 1392.6539 | 1392.6538  | 0.0001   | 0.002       |
| 9    | 1    | 6    | 8     | 0     | 5     | 1576.0732 | 1576.0726  | 0.0007   | 0.001       |
| 9    | 1    | 7    | 8     | 0     | 6     | 1576.0949 | 1576.0944  | 0.0005   | 0.001       |
| 9    | 1    | 8    | 8     | 0     | 7     | 1576.1171 | 1576.1162  | 0.0009   | 0.001       |
| 9    | 1    | 9    | 8     | 0     | 8     | 1576.1389 | 1576.1379  | 0.0011   | 0.001       |
| 9    | 1    | 10   | 8     | 0     | 9     | 1576.1600 | 1576.1593  | 0.0007   | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 9    | 1    | 11   | 8     | 0     | 10    | 1576.1600 | 1576.1804  | -0.0204  | 1           |
| 9    | 1    | 12   | 8     | 0     | 11    | 1576.1998 | 1576.2010  | -0.0012  | 0.002       |
| 8    | 1    | 11   | 9     | 0     | 12    | 1378.9017 | 1378.9015  | 0.0002   | 0.002       |
| 8    | 1    | 10   | 9     | 0     | 11    | 1378.9392 | 1378.9392  | 0.0000   | 0.002       |
| 8    | 1    | 9    | 9     | 0     | 10    | 1378.9779 | 1378.9774  | 0.0005   | 0.002       |
| 8    | 1    | 8    | 9     | 0     | 9     | 1379.0157 | 1379.0155  | 0.0002   | 0.002       |
| 8    | 1    | 7    | 9     | 0     | 8     | 1379.0528 | 1379.0531  | -0.0003  | 0.002       |
| 8    | 1    | 6    | 9     | 0     | 7     | 1379.0894 | 1379.0898  | -0.0004  | 0.002       |
| 8    | 1    | 5    | 9     | 0     | 6     | 1379.1251 | 1379.1251  | 0.0000   | 0.002       |
| 10   | 1    | 7    | 9     | 0     | 6     | 1583.7323 | 1583.7319  | 0.0004   | 0.001       |
| 10   | 1    | 8    | 9     | 0     | 7     | 1583.7528 | 1583.7525  | 0.0003   | 0.001       |
| 10   | 1    | 9    | 9     | 0     | 8     | 1583.7735 | 1583.7729  | 0.0006   | 0.001       |
| 10   | 1    | 10   | 9     | 0     | 9     | 1583.7941 | 1583.7932  | 0.0009   | 0.001       |
| 10   | 1    | 11   | 9     | 0     | 10    | 1583.8138 | 1583.8132  | 0.0006   | 0.001       |
| 10   | 1    | 12   | 9     | 0     | 11    | 1583.8326 | 1583.8330  | -0.0004  | 0.001       |
| 10   | 1    | 13   | 9     | 0     | 12    | 1583.8513 | 1583.8523  | -0.0010  | 0.001       |
| 9    | 1    | 12   | 10    | 0     | 13    | 1365.1126 | 1365.1122  | 0.0005   | 0.002       |
| 9    | 1    | 11   | 10    | 0     | 12    | 1365.1508 | 1365.1504  | 0.0004   | 0.002       |
| 9    | 1    | 10   | 10    | 0     | 11    | 1365.1900 | 1365.1891  | 0.0009   | 0.002       |
| 9    | 1    | 9    | 10    | 0     | 10    | 1365.2283 | 1365.2276  | 0.0007   | 0.002       |
| 9    | 1    | 8    | 10    | 0     | 9     | 1365.2658 | 1365.2656  | 0.0002   | 0.002       |
| 9    | 1    | 7    | 10    | 0     | 8     | 1365.3025 | 1365.3027  | -0.0002  | 0.002       |
| 9    | 1    | 6    | 10    | 0     | 7     | 1365.3387 | 1365.3387  | 0.0000   | 0.002       |
| 11   | 1    | 8    | 10    | 0     | 7     | 1590.9965 | 1590.9965  | 0.0000   | 0.001       |
| 11   | 1    | 9    | 10    | 0     | 8     | 1591.0158 | 1591.0158  | 0.0000   | 0.001       |
| 11   | 1    | 10   | 10    | 0     | 9     | 1591.0353 | 1591.0349  | 0.0004   | 0.001       |
| 11   | 1    | 11   | 10    | 0     | 10    | 1591.0543 | 1591.0537  | 0.0006   | 0.001       |
| 11   | 1    | 12   | 10    | 0     | 11    | 1591.0725 | 1591.0723  | 0.0002   | 0.001       |
| 11   | 1    | 13   | 10    | 0     | 12    | 1591.0904 | 1591.0906  | -0.0002  | 0.001       |
| 11   | 1    | 14   | 10    | 0     | 13    | 1591.1074 | 1591.1086  | -0.0012  | 0.001       |
| 10   | 1    | 13   | 11    | 0     | 14    | 1351.0729 | 1351.0722  | 0.0007   | 0.002       |
| 10   | 1    | 12   | 11    | 0     | 13    | 1351.1116 | 1351.1110  | 0.0006   | 0.002       |
| 10   | 1    | 11   | 11    | 0     | 12    | 1351.1511 | 1351.1501  | 0.0010   | 0.002       |
| 10   | 1    | 10   | 11    | 0     | 11    | 1351.1899 | 1351.1890  | 0.0009   | 0.002       |
| 10   | 1    | 9    | 11    | 0     | 10    | 1351.2275 | 1351.2274  | 0.0001   | 0.002       |
| 10   | 1    | 8    | 11    | 0     | 9     | 1351.2650 | 1351.2650  | 0.0000   | 0.002       |
| 10   | 1    | 7    | 11    | 0     | 8     | 1351.3017 | 1351.3015  | 0.0002   | 0.002       |
| 12   | 1    | 9    | 11    | 0     | 8     | 1597.8591 | 1597.8595  | -0.0004  | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 12   | 1    | 10   | 11    | 0     | 9     | 1597.8772 | 1597.8774  | -0.0002  | 0.001       |
| 12   | 1    | 11   | 11    | 0     | 10    | 1597.8954 | 1597.8950  | 0.0004   | 0.001       |
| 12   | 1    | 12   | 11    | 0     | 11    | 1597.9133 | 1597.9124  | 0.0009   | 0.001       |
| 12   | 1    | 13   | 11    | 0     | 12    | 1597.9299 | 1597.9295  | 0.0004   | 0.001       |
| 12   | 1    | 14   | 11    | 0     | 13    | 1597.9459 | 1597.9463  | -0.0004  | 0.001       |
| 12   | 1    | 15   | 11    | 0     | 14    | 1597.9617 | 1597.9629  | -0.0012  | 0.002       |
| 11   | 1    | 14   | 12    | 0     | 15    | 1336.7892 | 1336.7884  | 0.0008   | 0.001       |
| 11   | 1    | 13   | 12    | 0     | 14    | 1336.8283 | 1336.8278  | 0.0005   | 0.001       |
| 11   | 1    | 12   | 12    | 0     | 13    | 1336.8686 | 1336.8673  | 0.0013   | 0.001       |
| 11   | 1    | 11   | 12    | 0     | 12    | 1336.9069 | 1336.9066  | 0.0003   | 0.001       |
| 11   | 1    | 10   | 12    | 0     | 11    | 1336.9448 | 1336.9454  | -0.0006  | 0.001       |
| 11   | 1    | 9    | 12    | 0     | 10    | 1336.9826 | 1336.9834  | -0.0008  | 0.001       |
| 11   | 1    | 8    | 12    | 0     | 9     | 1337.0199 | 1337.0205  | -0.0006  | 0.001       |
| 13   | 1    | 10   | 12    | 0     | 9     | 1604.3139 | 1604.3139  | 0.0000   | 0.001       |
| 13   | 1    | 11   | 12    | 0     | 10    | 1604.3298 | 1604.3303  | -0.0005  | 0.001       |
| 13   | 1    | 12   | 12    | 0     | 11    | 1604.3465 | 1604.3464  | 0.0001   | 0.001       |
| 13   | 1    | 13   | 12    | 0     | 12    | 1604.3629 | 1604.3622  | 0.0007   | 0.001       |
| 13   | 1    | 14   | 12    | 0     | 13    | 1604.3783 | 1604.3778  | 0.0005   | 0.001       |
| 13   | 1    | 15   | 12    | 0     | 14    | 1604.3929 | 1604.3932  | -0.0003  | 0.001       |
| 13   | 1    | 16   | 12    | 0     | 15    | 1604.4071 | 1604.4082  | -0.0011  | 0.001       |
| 12   | 1    | 15   | 13    | 0     | 16    | 1322.2684 | 1322.2677  | 0.0007   | 0.001       |
| 12   | 1    | 14   | 13    | 0     | 15    | 1322.3082 | 1322.3076  | 0.0006   | 0.001       |
| 12   | 1    | 13   | 13    | 0     | 14    | 1322.3487 | 1322.3476  | 0.0011   | 0.001       |
| 12   | 1    | 12   | 13    | 0     | 13    | 1322.3883 | 1322.3872  | 0.0011   | 0.001       |
| 12   | 1    | 11   | 13    | 0     | 12    | 1322.4265 | 1322.4264  | 0.0001   | 0.001       |
| 12   | 1    | 10   | 13    | 0     | 11    | 1322.4648 | 1322.4648  | 0.0000   | 0.001       |
| 12   | 1    | 9    | 13    | 0     | 10    | 1322.5027 | 1322.5023  | 0.0004   | 0.001       |
| 14   | 1    | 11   | 13    | 0     | 10    | 1610.3523 | 1610.3527  | -0.0004  | 0.001       |
| 14   | 1    | 12   | 13    | 0     | 11    | 1610.3673 | 1610.3676  | -0.0003  | 0.001       |
| 14   | 1    | 13   | 13    | 0     | 12    | 1610.3826 | 1610.3821  | 0.0005   | 0.001       |
| 14   | 1    | 14   | 13    | 0     | 13    | 1610.3973 | 1610.3964  | 0.0009   | 0.001       |
| 14   | 1    | 15   | 13    | 0     | 14    | 1610.4113 | 1610.4104  | 0.0009   | 0.001       |
| 14   | 1    | 16   | 13    | 0     | 15    | 1610.4244 | 1610.4242  | 0.0002   | 0.001       |
| 14   | 1    | 17   | 13    | 0     | 16    | 1610.4373 | 1610.4377  | -0.0004  | 0.001       |
| 13   | 1    | 16   | 14    | 0     | 17    | 1307.5173 | 1307.5166  | 0.0007   | 0.001       |
| 13   | 1    | 15   | 14    | 0     | 16    | 1307.5575 | 1307.5570  | 0.0005   | 0.001       |
| 13   | 1    | 14   | 14    | 0     | 15    | 1307.5983 | 1307.5974  | 0.0009   | 0.001       |
| 13   | 1    | 13   | 14    | 0     | 14    | 1307.6381 | 1307.6374  | 0.0007   | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 13   | 1    | 12   | 14    | 0     | 13    | 1307.6772 | 1307.6770  | 0.0003   | 0.001       |
| 13   | 1    | 11   | 14    | 0     | 12    | 1307.7156 | 1307.7158  | -0.0002  | 0.001       |
| 13   | 1    | 10   | 14    | 0     | 11    | 1307.7536 | 1307.7537  | -0.0001  | 0.001       |
| 15   | 1    | 12   | 14    | 0     | 11    | 1615.9688 | 1615.9692  | -0.0004  | 0.001       |
| 15   | 1    | 13   | 14    | 0     | 12    | 1615.9824 | 1615.9825  | -0.0001  | 0.001       |
| 15   | 1    | 14   | 14    | 0     | 13    | 1615.9965 | 1615.9954  | 0.0011   | 0.002       |
| 15   | 1    | 15   | 14    | 0     | 14    | 1616.0094 | 1616.0080  | 0.0014   | 0.002       |
| 15   | 1    | 16   | 14    | 0     | 15    | 1616.0220 | 1616.0204  | 0.0016   | 0.002       |
| 15   | 1    | 17   | 14    | 0     | 16    | 1616.0338 | 1616.0325  | 0.0013   | 0.001       |
| 15   | 1    | 18   | 14    | 0     | 17    | 1616.0444 | 1616.0444  | 0.0000   | 0.001       |
| 14   | 1    | 17   | 15    | 0     | 18    | 1292.5421 | 1292.5416  | 0.0005   | 0.001       |
| 14   | 1    | 16   | 15    | 0     | 17    | 1292.5828 | 1292.5825  | 0.0003   | 0.001       |
| 14   | 1    | 15   | 15    | 0     | 16    | 1292.6238 | 1292.6233  | 0.0005   | 0.001       |
| 14   | 1    | 14   | 15    | 0     | 15    | 1292.6644 | 1292.6637  | 0.0007   | 0.001       |
| 14   | 1    | 13   | 15    | 0     | 14    | 1292.7038 | 1292.7036  | 0.0002   | 0.001       |
| 14   | 1    | 12   | 15    | 0     | 13    | 1292.7424 | 1292.7427  | -0.0003  | 0.001       |
| 14   | 1    | 11   | 15    | 0     | 12    | 1292.7809 | 1292.7811  | -0.0002  | 0.001       |
| 16   | 1    | 13   | 15    | 0     | 12    | 1621.1569 | 1621.1566  | 0.0003   | 0.002       |
| 16   | 1    | 14   | 15    | 0     | 13    | 1621.1693 | 1621.1682  | 0.0011   | 0.002       |
| 16   | 1    | 15   | 15    | 0     | 14    | 1621.1813 | 1621.1794  | 0.0019   | 0.002       |
| 16   | 1    | 16   | 15    | 0     | 15    | 1621.1927 | 1621.1903  | 0.0024   | 0.003       |
| 16   | 1    | 17   | 15    | 0     | 16    | 1621.2037 | 1621.2010  | 0.0027   | 0.003       |
| 16   | 1    | 18   | 15    | 0     | 17    | 1621.2138 | 1621.2114  | 0.0024   | 0.003       |
| 16   | 1    | 19   | 15    | 0     | 18    | 1621.2226 | 1621.2217  | 0.0009   | 0.001       |
| 15   | 1    | 18   | 16    | 0     | 19    | 1277.3491 | 1277.3491  | 0.0000   | 0.001       |
| 15   | 1    | 17   | 16    | 0     | 18    | 1277.3902 | 1277.3904  | -0.0002  | 0.001       |
| 15   | 1    | 16   | 16    | 0     | 17    | 1277.4322 | 1277.4315  | 0.0007   | 0.001       |
| 15   | 1    | 15   | 16    | 0     | 16    | 1277.4725 | 1277.4723  | 0.0002   | 0.001       |
| 15   | 1    | 14   | 16    | 0     | 15    | 1277.5123 | 1277.5125  | -0.0002  | 0.001       |
| 15   | 1    | 13   | 16    | 0     | 14    | 1277.5517 | 1277.5521  | -0.0004  | 0.001       |
| 15   | 1    | 12   | 16    | 0     | 13    | 1277.5906 | 1277.5908  | -0.0002  | 0.001       |
| 17   | 1    | 14   | 16    | 0     | 13    | 1625.9097 | 1625.9082  | 0.0015   | 0.002       |
| 17   | 1    | 15   | 16    | 0     | 14    | 1625.9196 | 1625.9181  | 0.0016   | 0.002       |
| 17   | 1    | 16   | 16    | 0     | 15    | 1625.9304 | 1625.9275  | 0.0029   | 0.003       |
| 17   | 1    | 17   | 16    | 0     | 16    | 1625.9304 | 1625.9367  | -0.0063  | 0.1         |
| 17   | 1    | 18   | 16    | 0     | 17    | 1625.9493 | 1625.9456  | 0.0037   | 0.003       |
| 17   | 1    | 19   | 16    | 0     | 18    | 1625.9493 | 1625.9543  | -0.0050  | 0.003       |
| 17   | 1    | 20   | 16    | 0     | 19    | 1625.9630 | 1625.9627  | 0.0003   | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 16   | 1    | 19   | 17    | 0     | 20    | 1261.9449 | 1261.9451  | -0.0002  | 0.001       |
| 16   | 1    | 18   | 17    | 0     | 19    | 1261.9866 | 1261.9869  | -0.0003  | 0.001       |
| 16   | 1    | 17   | 17    | 0     | 18    | 1262.0282 | 1262.0284  | -0.0002  | 0.001       |
| 16   | 1    | 16   | 17    | 0     | 17    | 1262.0694 | 1262.0695  | -0.0001  | 0.001       |
| 16   | 1    | 15   | 17    | 0     | 16    | 1262.1092 | 1262.1100  | -0.0008  | 0.001       |
| 16   | 1    | 14   | 17    | 0     | 15    | 1262.1491 | 1262.1499  | -0.0008  | 0.001       |
| 16   | 1    | 13   | 17    | 0     | 14    | 1262.1884 | 1262.1890  | -0.0006  | 0.001       |
| 18   | 1    | 15   | 17    | 0     | 14    | 1630.2261 | 1630.2176  | 0.0086   | 10          |
| 18   | 1    | 16   | 17    | 0     | 15    | 1630.2261 | 1630.2256  | 0.0005   | 0.002       |
| 18   | 1    | 17   | 17    | 0     | 16    | 1630.2261 | 1630.2332  | -0.0071  | 10          |
| 18   | 1    | 18   | 17    | 0     | 17    | 1630.2385 | 1630.2406  | -0.0021  | 0.002       |
| 18   | 1    | 19   | 17    | 0     | 18    | 1630.2385 | 1630.2476  | -0.0091  | 0.1         |
| 18   | 1    | 20   | 17    | 0     | 19    | 1630.2607 | 1630.2545  | 0.0062   | 0.1         |
| 18   | 1    | 21   | 17    | 0     | 20    | 1630.2607 | 1630.2611  | -0.0004  | 0.002       |
| 17   | 1    | 20   | 18    | 0     | 21    | 1246.3353 | 1246.3357  | -0.0004  | 0.001       |
| 17   | 1    | 19   | 18    | 0     | 20    | 1246.3774 | 1246.3778  | -0.0004  | 0.001       |
| 17   | 1    | 18   | 18    | 0     | 19    | 1246.4193 | 1246.4197  | -0.0004  | 0.001       |
| 17   | 1    | 17   | 18    | 0     | 18    | 1246.4608 | 1246.4612  | -0.0004  | 0.001       |
| 17   | 1    | 16   | 18    | 0     | 17    | 1246.5015 | 1246.5020  | -0.0005  | 0.001       |
| 17   | 1    | 15   | 18    | 0     | 16    | 1246.5410 | 1246.5422  | -0.0012  | 0.001       |
| 17   | 1    | 14   | 18    | 0     | 15    | 1246.5808 | 1246.5816  | -0.0008  | 0.001       |
| 19   | 1    | 16   | 18    | 0     | 15    | 1634.0789 | 1634.0782  | 0.0007   | 0.002       |
| 19   | 1    | 17   | 18    | 0     | 16    | 1634.0789 | 1634.0844  | -0.0055  | 0.005       |
| 19   | 1    | 18   | 18    | 0     | 17    | 1634.0906 | 1634.0901  | 0.0005   | 0.002       |
| 19   | 1    | 19   | 18    | 0     | 18    | 1634.0906 | 1634.0956  | -0.0050  | 0.005       |
| 19   | 1    | 20   | 18    | 0     | 19    | 1634.1024 | 1634.1007  | 0.0017   | 0.002       |
| 19   | 1    | 21   | 18    | 0     | 20    | 1634.1024 | 1634.1057  | -0.0033  | 0.003       |
| 19   | 1    | 22   | 18    | 0     | 21    | 1634.1123 | 1634.1104  | 0.0019   | 0.002       |
| 18   | 1    | 21   | 19    | 0     | 22    | 1230.5255 | 1230.5266  | -0.0011  | 0.001       |
| 18   | 1    | 20   | 19    | 0     | 21    | 1230.5684 | 1230.5691  | -0.0007  | 0.001       |
| 18   | 1    | 19   | 19    | 0     | 20    | 1230.6106 | 1230.6113  | -0.0007  | 0.001       |
| 18   | 1    | 18   | 19    | 0     | 19    | 1230.6528 | 1230.6531  | -0.0003  | 0.001       |
| 18   | 1    | 17   | 19    | 0     | 18    | 1230.6931 | 1230.6943  | -0.0012  | 0.001       |
| 18   | 1    | 16   | 19    | 0     | 17    | 1230.7334 | 1230.7348  | -0.0014  | 0.001       |
| 18   | 1    | 15   | 19    | 0     | 16    | 1230.7736 | 1230.7744  | -0.0008  | 0.001       |
| 20   | 1    | 17   | 19    | 0     | 16    | 1637.4862 | 1637.4841  | 0.0021   | 0.005       |
| 20   | 1    | 18   | 19    | 0     | 17    | 1637.4862 | 1637.4882  | -0.0020  | 0.002       |
| 20   | 1    | 19   | 19    | 0     | 18    | 1637.4862 | 1637.4920  | -0.0058  | 0.1         |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 20   | 1    | 20   | 19    | 0     | 19    | 1637.4994 | 1637.4955  | 0.0039   | 0.005       |
| 20   | 1    | 21   | 19    | 0     | 20    | 1637.4994 | 1637.4987  | 0.0007   | 0.002       |
| 20   | 1    | 22   | 19    | 0     | 21    | 1637.4994 | 1637.5017  | -0.0023  | 0.003       |
| 20   | 1    | 23   | 19    | 0     | 22    | 1637.4994 | 1637.5045  | -0.0051  | 0.005       |
| 19   | 1    | 22   | 20    | 0     | 23    | 1214.5223 | 1214.5233  | -0.0010  | 0.001       |
| 19   | 1    | 21   | 20    | 0     | 22    | 1214.5648 | 1214.5662  | -0.0014  | 0.001       |
| 19   | 1    | 20   | 20    | 0     | 21    | 1214.6077 | 1214.6088  | -0.0011  | 0.001       |
| 19   | 1    | 19   | 20    | 0     | 20    | 1214.6500 | 1214.6508  | -0.0008  | 0.001       |
| 19   | 1    | 18   | 20    | 0     | 19    | 1214.6912 | 1214.6923  | -0.0011  | 0.002       |
| 19   | 1    | 17   | 20    | 0     | 18    | 1214.7313 | 1214.7331  | -0.0018  | 0.001       |
| 19   | 1    | 16   | 20    | 0     | 17    | 1214.7717 | 1214.7731  | -0.0014  | 0.001       |
| 21   | 1    | 18   | 20    | 0     | 17    | 1640.4404 | 1640.4291  | 0.0113   | 1           |
| 21   | 1    | 19   | 20    | 0     | 18    | 1640.4404 | 1640.4312  | 0.0092   | 1           |
| 21   | 1    | 20   | 20    | 0     | 19    | 1640.4404 | 1640.4330  | 0.0074   | 1           |
| 21   | 1    | 21   | 20    | 0     | 20    | 1640.4404 | 1640.4344  | 0.0060   | 1           |
| 21   | 1    | 22   | 20    | 0     | 21    | 1640.4404 | 1640.4356  | 0.0048   | 1           |
| 21   | 1    | 23   | 20    | 0     | 22    | 1640.4404 | 1640.4365  | 0.0039   | 0.003       |
| 21   | 1    | 24   | 20    | 0     | 23    | 1640.4404 | 1640.4372  | 0.0032   | 0.003       |
| 20   | 1    | 23   | 21    | 0     | 24    | 1198.3304 | 1198.3312  | -0.0008  | 0.001       |
| 20   | 1    | 22   | 21    | 0     | 23    | 1198.3738 | 1198.3745  | -0.0007  | 0.001       |
| 20   | 1    | 21   | 21    | 0     | 22    | 1198.4173 | 1198.4174  | -0.0001  | 0.001       |
| 20   | 1    | 20   | 21    | 0     | 21    | 1198.4588 | 1198.4598  | -0.0010  | 0.001       |
| 20   | 1    | 19   | 21    | 0     | 20    | 1198.5008 | 1198.5015  | -0.0007  | 0.001       |
| 20   | 1    | 18   | 21    | 0     | 19    | 1198.5413 | 1198.5426  | -0.0013  | 0.001       |
| 20   | 1    | 17   | 21    | 0     | 18    | 1198.5814 | 1198.5829  | -0.0015  | 0.001       |
| 22   | 1    | 19   | 21    | 0     | 18    | 1642.9063 | 1642.9075  | -0.0012  | 0.001       |
| 22   | 1    | 20   | 21    | 0     | 19    | 1642.9063 | 1642.9076  | -0.0013  | 0.001       |
| 22   | 1    | 21   | 21    | 0     | 20    | 1642.9063 | 1642.9073  | -0.0010  | 0.001       |
| 22   | 1    | 22   | 21    | 0     | 21    | 1642.9063 | 1642.9066  | -0.0003  | 0.001       |
| 22   | 1    | 23   | 21    | 0     | 22    | 1642.9063 | 1642.9056  | 0.0007   | 0.001       |
| 22   | 1    | 24   | 21    | 0     | 23    | 1642.9063 | 1642.9044  | 0.0019   | 0.001       |
| 22   | 1    | 25   | 21    | 0     | 24    | 1642.9063 | 1642.9031  | 0.0033   | 0.001       |
| 21   | 1    | 24   | 22    | 0     | 25    | 1181.9552 | 1181.9556  | -0.0004  | 0.001       |
| 21   | 1    | 23   | 22    | 0     | 24    | 1181.9986 | 1181.9992  | -0.0006  | 0.001       |
| 21   | 1    | 22   | 22    | 0     | 23    | 1182.0419 | 1182.0424  | -0.0005  | 0.001       |
| 21   | 1    | 21   | 22    | 0     | 22    | 1182.0851 | 1182.0851  | 0.0000   | 0.001       |
| 21   | 1    | 20   | 22    | 0     | 21    | 1182.1269 | 1182.1271  | -0.0002  | 0.001       |
| 21   | 1    | 19   | 22    | 0     | 20    | 1182.1684 | 1182.1684  | 0.0000   | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 21   | 1    | 18   | 22    | 0     | 19    | 1182.2088 | 1182.2090  | -0.0002  | 0.001       |
| 23   | 1    | 20   | 22    | 0     | 19    | 1644.8992 | 1644.9141  | -0.0149  | 1           |
| 23   | 1    | 21   | 22    | 0     | 20    | 1644.8992 | 1644.9120  | -0.0128  | 1           |
| 23   | 1    | 22   | 22    | 0     | 21    | 1644.8992 | 1644.9095  | -0.0103  | 0.1         |
| 23   | 1    | 23   | 22    | 0     | 22    | 1644.8992 | 1644.9066  | -0.0074  | 0.1         |
| 23   | 1    | 24   | 22    | 0     | 23    | 1644.8992 | 1644.9035  | -0.0043  | 0.003       |
| 23   | 1    | 25   | 22    | 0     | 24    | 1644.8992 | 1644.9001  | -0.0009  | 0.002       |
| 23   | 1    | 26   | 22    | 0     | 25    | 1644.8992 | 1644.8965  | 0.0027   | 0.002       |
| 22   | 1    | 25   | 23    | 0     | 26    | 1165.4024 | 1165.4012  | 0.0012   | 0.001       |
| 22   | 1    | 24   | 23    | 0     | 25    | 1165.4451 | 1165.4452  | -0.0001  | 0.001       |
| 22   | 1    | 23   | 23    | 0     | 24    | 1165.4891 | 1165.4887  | 0.0004   | 0.001       |
| 22   | 1    | 22   | 23    | 0     | 23    | 1165.5320 | 1165.5317  | 0.0003   | 0.001       |
| 22   | 1    | 21   | 23    | 0     | 22    | 1165.5740 | 1165.5740  | 0.0000   | 0.001       |
| 22   | 1    | 20   | 23    | 0     | 21    | 1165.6157 | 1165.6156  | 0.0001   | 0.001       |
| 22   | 1    | 19   | 23    | 0     | 20    | 1165.6566 | 1165.6564  | 0.0002   | 0.001       |
| 24   | 1    | 21   | 23    | 0     | 20    | 1646.4115 | 1646.4439  | -0.0324  | 1           |
| 24   | 1    | 22   | 23    | 0     | 21    | 1646.4115 | 1646.4395  | -0.0280  | 1           |
| 24   | 1    | 23   | 23    | 0     | 22    | 1646.4115 | 1646.4347  | -0.0232  | 0.1         |
| 24   | 1    | 24   | 23    | 0     | 23    | 1646.4115 | 1646.4296  | -0.0181  | 0.1         |
| 24   | 1    | 25   | 23    | 0     | 24    | 1646.4115 | 1646.4242  | -0.0127  | 0.1         |
| 24   | 1    | 26   | 23    | 0     | 25    | 1646.4115 | 1646.4185  | -0.0070  | 0.1         |
| 24   | 1    | 27   | 23    | 0     | 26    | 1646.4115 | 1646.4127  | -0.0012  | 0.001       |
| 23   | 1    | 26   | 24    | 0     | 27    | 1148.6733 | 1148.6730  | 0.0003   | 0.001       |
| 23   | 1    | 25   | 24    | 0     | 26    | 1148.7174 | 1148.7174  | 0.0000   | 0.001       |
| 23   | 1    | 24   | 24    | 0     | 25    | 1148.7620 | 1148.7612  | 0.0008   | 0.001       |
| 23   | 1    | 23   | 24    | 0     | 24    | 1148.8046 | 1148.8044  | 0.0002   | 0.001       |
| 23   | 1    | 22   | 24    | 0     | 23    | 1148.8481 | 1148.8470  | 0.0011   | 0.001       |
| 23   | 1    | 21   | 24    | 0     | 22    | 1148.8883 | 1148.8889  | -0.0006  | 0.001       |
| 23   | 1    | 20   | 24    | 0     | 21    | 1148.9317 | 1148.9299  | 0.0018   | 0.001       |
| 25   | 1    | 22   | 24    | 0     | 21    | 1647.4427 | 1647.4922  | -0.0495  | 1           |
| 25   | 1    | 23   | 24    | 0     | 22    | 1647.4427 | 1647.4855  | -0.0428  | 1           |
| 25   | 1    | 24   | 24    | 0     | 23    | 1647.4427 | 1647.4784  | -0.0357  | 0.1         |
| 25   | 1    | 25   | 24    | 0     | 24    | 1647.4427 | 1647.4709  | -0.0282  | 0.1         |
| 25   | 1    | 26   | 24    | 0     | 25    | 1647.4427 | 1647.4632  | -0.0205  | 0.1         |
| 25   | 1    | 27   | 24    | 0     | 26    | 1647.4427 | 1647.4551  | -0.0124  | 0.1         |
| 25   | 1    | 28   | 24    | 0     | 27    | 1647.4427 | 1647.4470  | -0.0043  | 0.1         |
| 24   | 1    | 27   | 25    | 0     | 28    | 1131.7746 | 1131.7756  | -0.0010  | 0.001       |
| 24   | 1    | 26   | 25    | 0     | 27    | 1131.8216 | 1131.8202  | 0.0014   | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 24   | 1    | 25   | 25    | 0     | 26    | 1131.8643 | 1131.8644  | -0.0001  | 0.001       |
| 24   | 1    | 24   | 25    | 0     | 25    | 1131.9088 | 1131.9079  | 0.0009   | 0.001       |
| 24   | 1    | 23   | 25    | 0     | 24    | 1131.9523 | 1131.9507  | 0.0016   | 0.001       |
| 24   | 1    | 22   | 25    | 0     | 23    | 1131.9939 | 1131.9928  | 0.0011   | 0.001       |
| 24   | 1    | 21   | 25    | 0     | 22    | 1132.0347 | 1132.0341  | 0.0006   | 0.001       |
| 26   | 1    | 24   | 25    | 0     | 23    | 1648.0014 | 1648.0461  | -0.0447  | 1           |
| 26   | 1    | 25   | 25    | 0     | 24    | 1648.0014 | 1648.0366  | -0.0352  | 1           |
| 26   | 1    | 27   | 25    | 0     | 26    | 1648.0014 | 1648.0165  | -0.0151  | 1           |
| 26   | 1    | 28   | 25    | 0     | 27    | 1648.0014 | 1648.0061  | -0.0047  | 1           |
| 26   | 1    | 29   | 25    | 0     | 28    | 1648.0014 | 1647.9954  | 0.0060   | 0.002       |
| 25   | 1    | 28   | 26    | 0     | 29    | 1114.7138 | 1114.7133  | 0.0005   | 0.001       |
| 25   | 1    | 27   | 26    | 0     | 28    | 1114.7600 | 1114.7583  | 0.0017   | 0.001       |
| 25   | 1    | 26   | 26    | 0     | 27    | 1114.8033 | 1114.8027  | 0.0006   | 0.001       |
| 25   | 1    | 25   | 26    | 0     | 26    | 1114.8469 | 1114.8465  | 0.0004   | 0.001       |
| 25   | 1    | 24   | 26    | 0     | 25    | 1114.8908 | 1114.8896  | 0.0012   | 0.001       |
| 25   | 1    | 23   | 26    | 0     | 24    | 1114.9340 | 1114.9320  | 0.0020   | 0.001       |
| 25   | 1    | 22   | 26    | 0     | 23    | 1114.9734 | 1114.9735  | -0.0001  | 0.001       |
| 26   | 1    | 29   | 27    | 0     | 30    | 1097.4892 | 1097.4906  | -0.0014  | 0.001       |
| 26   | 1    | 28   | 27    | 0     | 29    | 1097.5344 | 1097.5359  | -0.0015  | 0.001       |
| 26   | 1    | 27   | 27    | 0     | 28    | 1097.5804 | 1097.5806  | -0.0002  | 0.001       |
| 26   | 1    | 26   | 27    | 0     | 27    | 1097.6246 | 1097.6247  | -0.0001  | 0.001       |
| 26   | 1    | 25   | 27    | 0     | 26    | 1097.6676 | 1097.6681  | -0.0005  | 0.001       |
| 26   | 1    | 24   | 27    | 0     | 25    | 1097.7084 | 1097.7106  | -0.0022  | 0.001       |
| 0    | 1    | 3    | 1     | 0     | 3     | 1479.4851 | 1479.4909  | -0.0058  | 0.004       |
| 1    | 1    | 4    | 2     | 0     | 4     | 1467.9990 | 1467.9961  | 0.0029   | 0.003       |
| 2    | 1    | 5    | 3     | 0     | 5     | 1456.1830 | 1456.1913  | -0.0083  | 1           |
| 0    | 1    | 3    | 1     | 0     | 2     | 1479.5298 | 1479.5427  | -0.0129  | 1           |
| 1    | 1    | 3    | 2     | 0     | 2     | 1468.0428 | 1468.0365  | 0.0063   | 1           |
| 1    | 1    | 2    | 2     | 0     | 1     | 1468.0250 | 1468.0324  | -0.0074  | 1           |
| 1    | 1    | 2    | 2     | 0     | 2     | 1467.9795 | 1467.9900  | -0.0105  | 1           |
| 2    | 1    | 3    | 3     | 0     | 3     | 1456.1585 | 1456.1656  | -0.0071  | 1           |
| 2    | 1    | 2    | 3     | 0     | 2     | 1456.1720 | 1456.1731  | -0.0011  | 0.001       |
| 1    | 1    | 3    | 0     | 0     | 3     | 1501.4732 | 1501.4774  | -0.0042  | 0.004       |
| 2    | 1    | 4    | 1     | 0     | 4     | 1512.0054 | 1512.0004  | 0.0050   | 0.004       |
| 2    | 2    | 5    | 1     | 1     | 4     | 1453.5452 | 1453.5400  | 0.0052   | 0.005       |
| 1    | 2    | 4    | 2     | 1     | 5     | 1410.4748 | 1410.4771  | -0.0023  | 0.005       |
| 1    | 2    | 3    | 2     | 1     | 4     | 1410.5096 | 1410.5057  | 0.0039   | 0.005       |
| 1    | 2    | 2    | 2     | 1     | 3     | 1410.5773 | 1410.5819  | -0.0046  | 0.005       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 3    | 2    | 2    | 2     | 1     | 1     | 1463.3151 | 1463.2895  | 0.0256   | 10          |
| 3    | 2    | 3    | 2     | 1     | 2     | 1463.3275 | 1463.3212  | 0.0063   | 10          |
| 3    | 2    | 4    | 2     | 1     | 3     | 1463.3543 | 1463.3561  | -0.0018  | 0.005       |
| 3    | 2    | 5    | 2     | 1     | 4     | 1463.3890 | 1463.3895  | -0.0005  | 0.002       |
| 3    | 2    | 6    | 2     | 1     | 5     | 1463.4170 | 1463.4140  | 0.0030   | 0.003       |
| 2    | 2    | 5    | 3     | 1     | 6     | 1398.9522 | 1398.9537  | -0.0015  | 0.002       |
| 2    | 2    | 4    | 3     | 1     | 5     | 1398.9869 | 1398.9850  | 0.0019   | 0.002       |
| 2    | 2    | 2    | 3     | 1     | 3     | 1399.0239 | 1399.0703  | -0.0464  | 100         |
| 2    | 2    | 3    | 3     | 1     | 4     | 1399.0239 | 1399.0269  | -0.0030  | 0.005       |
| 2    | 2    | 1    | 3     | 1     | 2     | 1399.1310 | 1399.1091  | 0.0220   | 100         |
| 4    | 2    | 1    | 3     | 1     | 0     | 1472.7755 | 1472.7785  | -0.0029  | 0.005       |
| 4    | 2    | 2    | 3     | 1     | 1     | 1472.7985 | 1472.8024  | -0.0039  | 0.005       |
| 4    | 2    | 3    | 3     | 1     | 2     | 1472.8257 | 1472.8286  | -0.0029  | 0.005       |
| 4    | 2    | 4    | 3     | 1     | 3     | 1472.8557 | 1472.8568  | -0.0011  | 0.002       |
| 4    | 2    | 5    | 3     | 1     | 4     | 1472.8854 | 1472.8858  | -0.0004  | 0.001       |
| 4    | 2    | 6    | 3     | 1     | 5     | 1472.9164 | 1472.9138  | 0.0026   | 0.001       |
| 4    | 2    | 7    | 3     | 1     | 6     | 1472.9392 | 1472.9379  | 0.0013   | 0.001       |
| 3    | 2    | 6    | 4     | 1     | 7     | 1387.1222 | 1387.1225  | -0.0003  | 0.001       |
| 3    | 2    | 5    | 4     | 1     | 6     | 1387.1544 | 1387.1554  | -0.0010  | 0.001       |
| 3    | 2    | 4    | 4     | 1     | 5     | 1387.1938 | 1387.1931  | 0.0007   | 0.001       |
| 3    | 2    | 3    | 4     | 1     | 4     | 1387.2327 | 1387.2318  | 0.0009   | 0.001       |
| 3    | 2    | 2    | 4     | 1     | 3     | 1387.2721 | 1387.2684  | 0.0037   | 0.001       |
| 3    | 2    | 1    | 4     | 1     | 2     | 1387.3020 | 1387.3011  | 0.0009   | 0.001       |
| 3    | 2    | 0    | 4     | 1     | 1     | 1387.3238 | 1387.3291  | -0.0053  | 0.002       |
| 5    | 2    | 2    | 4     | 1     | 1     | 1481.9498 | 1481.9529  | -0.0031  | 0.002       |
| 5    | 2    | 3    | 4     | 1     | 2     | 1481.9778 | 1481.9771  | 0.0006   | 0.002       |
| 5    | 2    | 4    | 4     | 1     | 3     | 1481.9993 | 1482.0024  | -0.0031  | 0.002       |
| 5    | 2    | 5    | 4     | 1     | 4     | 1482.0290 | 1482.0285  | 0.0005   | 0.002       |
| 5    | 2    | 6    | 4     | 1     | 5     | 1482.0561 | 1482.0548  | 0.0013   | 0.001       |
| 5    | 2    | 7    | 4     | 1     | 6     | 1482.0821 | 1482.0803  | 0.0018   | 0.001       |
| 5    | 2    | 8    | 4     | 1     | 7     | 1482.1050 | 1482.1036  | 0.0014   | 0.001       |
| 4    | 2    | 7    | 5     | 1     | 8     | 1374.9911 | 1374.9912  | -0.0001  | 0.001       |
| 4    | 2    | 6    | 5     | 1     | 7     | 1375.0252 | 1375.0253  | -0.0001  | 0.001       |
| 4    | 2    | 5    | 5     | 1     | 6     | 1375.0623 | 1375.0622  | 0.0001   | 0.001       |
| 4    | 2    | 4    | 5     | 1     | 5     | 1375.1001 | 1375.0996  | 0.0005   | 0.001       |
| 4    | 2    | 3    | 5     | 1     | 4     | 1375.1368 | 1375.1358  | 0.0010   | 0.001       |
| 4    | 2    | 2    | 5     | 1     | 3     | 1375.1703 | 1375.1695  | 0.0008   | 0.002       |
| 4    | 2    | 1    | 5     | 1     | 2     | 1375.1703 | 1375.2000  | -0.0297  | 100         |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 6    | 2    | 3    | 5     | 1     | 2     | 1490.7596 | 1490.7610  | -0.0014  | 0.001       |
| 6    | 2    | 4    | 5     | 1     | 3     | 1490.7850 | 1490.7847  | 0.0004   | 0.001       |
| 6    | 2    | 5    | 5     | 1     | 4     | 1490.8086 | 1490.8088  | -0.0002  | 0.001       |
| 6    | 2    | 6    | 5     | 1     | 5     | 1490.8360 | 1490.8333  | 0.0028   | 0.001       |
| 6    | 2    | 7    | 5     | 1     | 6     | 1490.8580 | 1490.8577  | 0.0004   | 0.001       |
| 6    | 2    | 8    | 5     | 1     | 7     | 1490.8822 | 1490.8814  | 0.0008   | 0.001       |
| 6    | 2    | 9    | 5     | 1     | 8     | 1490.9037 | 1490.9037  | 0.0000   | 0.001       |
| 5    | 2    | 8    | 6     | 1     | 9     | 1362.5670 | 1362.5671  | -0.0001  | 0.001       |
| 5    | 2    | 7    | 6     | 1     | 8     | 1362.6026 | 1362.6023  | 0.0003   | 0.001       |
| 5    | 2    | 6    | 6     | 1     | 7     | 1362.6391 | 1362.6392  | -0.0001  | 0.001       |
| 5    | 2    | 5    | 6     | 1     | 6     | 1362.6774 | 1362.6763  | 0.0011   | 0.001       |
| 5    | 2    | 4    | 6     | 1     | 5     | 1362.7121 | 1362.7126  | -0.0005  | 0.001       |
| 5    | 2    | 3    | 6     | 1     | 4     | 1362.7461 | 1362.7470  | -0.0009  | 0.001       |
| 5    | 2    | 2    | 6     | 1     | 3     | 1362.7793 | 1362.7791  | 0.0002   | 0.001       |
| 7    | 2    | 4    | 6     | 1     | 3     | 1499.1958 | 1499.1958  | 0.0000   | 0.001       |
| 7    | 2    | 5    | 6     | 1     | 4     | 1499.2187 | 1499.2185  | 0.0002   | 0.001       |
| 7    | 2    | 6    | 6     | 1     | 5     | 1499.2417 | 1499.2414  | 0.0003   | 0.001       |
| 7    | 2    | 7    | 6     | 1     | 6     | 1499.2653 | 1499.2644  | 0.0009   | 0.001       |
| 7    | 2    | 8    | 6     | 1     | 7     | 1499.2873 | 1499.2872  | 0.0001   | 0.001       |
| 7    | 2    | 9    | 6     | 1     | 8     | 1499.3094 | 1499.3094  | 0.0000   | 0.001       |
| 7    | 2    | 10   | 6     | 1     | 9     | 1499.3304 | 1499.3306  | -0.0002  | 0.001       |
| 6    | 2    | 9    | 7     | 1     | 10    | 1349.8571 | 1349.8574  | -0.0003  | 0.001       |
| 6    | 2    | 8    | 7     | 1     | 9     | 1349.8930 | 1349.8935  | -0.0005  | 0.001       |
| 6    | 2    | 7    | 7     | 1     | 8     | 1349.9303 | 1349.9307  | -0.0004  | 0.001       |
| 6    | 2    | 6    | 7     | 1     | 7     | 1349.9676 | 1349.9680  | -0.0004  | 0.001       |
| 6    | 2    | 5    | 7     | 1     | 6     | 1350.0044 | 1350.0045  | -0.0001  | 0.001       |
| 6    | 2    | 4    | 7     | 1     | 5     | 1350.0411 | 1350.0396  | 0.0015   | 0.001       |
| 6    | 2    | 3    | 7     | 1     | 4     | 1350.0718 | 1350.0729  | -0.0011  | 0.001       |
| 8    | 2    | 5    | 7     | 1     | 4     | 1507.2500 | 1507.2501  | -0.0001  | 0.001       |
| 8    | 2    | 6    | 7     | 1     | 5     | 1507.2733 | 1507.2717  | 0.0016   | 0.001       |
| 8    | 2    | 7    | 7     | 1     | 6     | 1507.2941 | 1507.2933  | 0.0008   | 0.001       |
| 8    | 2    | 8    | 7     | 1     | 7     | 1507.3150 | 1507.3148  | 0.0002   | 0.001       |
| 8    | 2    | 9    | 7     | 1     | 8     | 1507.3359 | 1507.3360  | -0.0001  | 0.001       |
| 8    | 2    | 10   | 7     | 1     | 9     | 1507.3566 | 1507.3568  | -0.0002  | 0.001       |
| 8    | 2    | 11   | 7     | 1     | 10    | 1507.3765 | 1507.3768  | -0.0003  | 0.001       |
| 7    | 2    | 10   | 8     | 1     | 11    | 1336.8686 | 1336.8691  | -0.0005  | 0.001       |
| 9    | 2    | 6    | 8     | 1     | 5     | 1514.9168 | 1514.9164  | 0.0004   | 0.001       |
| 9    | 2    | 7    | 8     | 1     | 6     | 1514.9375 | 1514.9368  | 0.0007   | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 9    | 2    | 8    | 8     | 1     | 7     | 1514.9576 | 1514.9570  | 0.0006   | 0.001       |
| 9    | 2    | 9    | 8     | 1     | 8     | 1514.9754 | 1514.9770  | -0.0016  | 0.001       |
| 9    | 2    | 10   | 8     | 1     | 9     | 1514.9969 | 1514.9968  | 0.0001   | 0.001       |
| 9    | 2    | 11   | 8     | 1     | 10    | 1515.0157 | 1515.0161  | -0.0004  | 0.001       |
| 9    | 2    | 12   | 8     | 1     | 11    | 1515.0338 | 1515.0348  | -0.0010  | 0.001       |
| 8    | 2    | 11   | 9     | 1     | 12    | 1323.6088 | 1323.6090  | -0.0002  | 0.001       |
| 8    | 2    | 10   | 9     | 1     | 11    | 1323.6467 | 1323.6466  | 0.0001   | 0.001       |
| 8    | 2    | 9    | 9     | 1     | 10    | 1323.6844 | 1323.6848  | -0.0004  | 0.001       |
| 8    | 2    | 8    | 9     | 1     | 9     | 1323.7225 | 1323.7228  | -0.0003  | 0.001       |
| 8    | 2    | 7    | 9     | 1     | 8     | 1323.7593 | 1323.7601  | -0.0008  | 0.001       |
| 8    | 2    | 6    | 9     | 1     | 7     | 1323.7965 | 1323.7965  | 0.0001   | 0.001       |
| 8    | 2    | 5    | 9     | 1     | 6     | 1323.8310 | 1323.8314  | -0.0004  | 0.001       |
| 10   | 2    | 7    | 9     | 1     | 6     | 1522.1877 | 1522.1874  | 0.0003   | 0.001       |
| 10   | 2    | 8    | 9     | 1     | 7     | 1522.2059 | 1522.2064  | -0.0005  | 0.001       |
| 10   | 2    | 9    | 9     | 1     | 8     | 1522.2241 | 1522.2252  | -0.0011  | 0.001       |
| 10   | 2    | 10   | 9     | 1     | 9     | 1522.2428 | 1522.2437  | -0.0009  | 0.001       |
| 10   | 2    | 11   | 9     | 1     | 10    | 1522.2613 | 1522.2620  | -0.0007  | 0.001       |
| 10   | 2    | 12   | 9     | 1     | 11    | 1522.2789 | 1522.2798  | -0.0009  | 0.001       |
| 10   | 2    | 13   | 9     | 1     | 12    | 1522.2956 | 1522.2971  | -0.0015  | 0.001       |
| 9    | 2    | 12   | 10    | 1     | 13    | 1310.0839 | 1310.0840  | -0.0001  | 0.001       |
| 9    | 2    | 11   | 10    | 1     | 12    | 1310.1224 | 1310.1223  | 0.0001   | 0.001       |
| 9    | 2    | 10   | 10    | 1     | 11    | 1310.1607 | 1310.1609  | -0.0002  | 0.001       |
| 9    | 2    | 9    | 10    | 1     | 10    | 1310.1989 | 1310.1994  | -0.0005  | 0.001       |
| 9    | 2    | 8    | 10    | 1     | 9     | 1310.2372 | 1310.2372  | 0.0000   | 0.001       |
| 9    | 2    | 7    | 10    | 1     | 8     | 1310.2745 | 1310.2741  | 0.0005   | 0.001       |
| 9    | 2    | 6    | 10    | 1     | 7     | 1310.3091 | 1310.3097  | -0.0006  | 0.001       |
| 11   | 2    | 8    | 10    | 1     | 7     | 1529.0548 | 1529.0555  | -0.0007  | 0.001       |
| 11   | 2    | 9    | 10    | 1     | 8     | 1529.0735 | 1529.0731  | 0.0004   | 0.001       |
| 11   | 2    | 10   | 10    | 1     | 9     | 1529.0899 | 1529.0904  | -0.0005  | 0.001       |
| 11   | 2    | 11   | 10    | 1     | 10    | 1529.1068 | 1529.1074  | -0.0006  | 0.001       |
| 11   | 2    | 12   | 10    | 1     | 11    | 1529.1234 | 1529.1241  | -0.0007  | 0.001       |
| 11   | 2    | 13   | 10    | 1     | 12    | 1529.1393 | 1529.1404  | -0.0011  | 0.001       |
| 11   | 2    | 14   | 10    | 1     | 13    | 1529.1546 | 1529.1563  | -0.0017  | 0.001       |
| 10   | 2    | 13   | 11    | 1     | 14    | 1296.3009 | 1296.3007  | 0.0002   | 0.001       |
| 10   | 2    | 12   | 11    | 1     | 13    | 1296.3392 | 1296.3396  | -0.0004  | 0.001       |
| 10   | 2    | 11   | 11    | 1     | 12    | 1296.3781 | 1296.3787  | -0.0006  | 0.001       |
| 10   | 2    | 10   | 11    | 1     | 11    | 1296.4177 | 1296.4176  | 0.0001   | 0.001       |
| 10   | 2    | 9    | 11    | 1     | 10    | 1296.4558 | 1296.4559  | -0.0001  | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 10   | 2    | 8    | 11    | 1     | 9     | 1296.4927 | 1296.4933  | -0.0006  | 0.001       |
| 10   | 2    | 7    | 11    | 1     | 8     | 1296.5293 | 1296.5295  | -0.0002  | 0.001       |
| 12   | 2    | 9    | 11    | 1     | 8     | 1535.5130 | 1535.5133  | -0.0003  | 0.001       |
| 12   | 2    | 10   | 11    | 1     | 9     | 1535.5296 | 1535.5294  | 0.0002   | 0.001       |
| 12   | 2    | 11   | 11    | 1     | 10    | 1535.5445 | 1535.5452  | -0.0007  | 0.001       |
| 12   | 2    | 12   | 11    | 1     | 11    | 1535.5603 | 1535.5606  | -0.0003  | 0.001       |
| 12   | 2    | 13   | 11    | 1     | 12    | 1535.5750 | 1535.5757  | -0.0007  | 0.001       |
| 12   | 2    | 14   | 11    | 1     | 13    | 1535.5900 | 1535.5905  | -0.0005  | 0.001       |
| 12   | 2    | 15   | 11    | 1     | 14    | 1535.6032 | 1535.6048  | -0.0016  | 0.001       |
| 11   | 2    | 14   | 12    | 1     | 15    | 1282.2661 | 1282.2655  | 0.0006   | 0.001       |
| 11   | 2    | 13   | 12    | 1     | 14    | 1282.3053 | 1282.3051  | 0.0002   | 0.001       |
| 11   | 2    | 12   | 12    | 1     | 13    | 1282.3439 | 1282.3447  | -0.0008  | 0.001       |
| 11   | 2    | 11   | 12    | 1     | 12    | 1282.3840 | 1282.3841  | -0.0001  | 0.001       |
| 11   | 2    | 10   | 12    | 1     | 11    | 1282.4224 | 1282.4228  | -0.0004  | 0.001       |
| 11   | 2    | 9    | 12    | 1     | 10    | 1282.4610 | 1282.4607  | 0.0003   | 0.001       |
| 11   | 2    | 8    | 12    | 1     | 9     | 1282.4974 | 1282.4975  | -0.0001  | 0.001       |
| 13   | 2    | 10   | 12    | 1     | 9     | 1541.5524 | 1541.5533  | -0.0009  | 0.001       |
| 13   | 2    | 11   | 12    | 1     | 10    | 1541.5681 | 1541.5678  | 0.0003   | 0.001       |
| 13   | 2    | 12   | 12    | 1     | 11    | 1541.5824 | 1541.5820  | 0.0004   | 0.001       |
| 13   | 2    | 13   | 12    | 1     | 12    | 1541.5954 | 1541.5958  | -0.0004  | 0.001       |
| 13   | 2    | 14   | 12    | 1     | 13    | 1541.6093 | 1541.6093  | 0.0000   | 0.001       |
| 13   | 2    | 15   | 12    | 1     | 14    | 1541.6227 | 1541.6224  | 0.0003   | 0.001       |
| 13   | 2    | 16   | 12    | 1     | 15    | 1541.6338 | 1541.6352  | -0.0014  | 0.001       |
| 12   | 2    | 15   | 13    | 1     | 16    | 1267.9854 | 1267.9850  | 0.0004   | 0.001       |
| 12   | 2    | 14   | 13    | 1     | 15    | 1268.0254 | 1268.0251  | 0.0003   | 0.001       |
| 12   | 2    | 13   | 13    | 1     | 14    | 1268.0654 | 1268.0652  | 0.0002   | 0.001       |
| 12   | 2    | 12   | 13    | 1     | 13    | 1268.1052 | 1268.1050  | 0.0002   | 0.001       |
| 12   | 2    | 11   | 13    | 1     | 12    | 1268.1446 | 1268.1442  | 0.0004   | 0.001       |
| 12   | 2    | 10   | 13    | 1     | 11    | 1268.1822 | 1268.1825  | -0.0003  | 0.001       |
| 12   | 2    | 9    | 13    | 1     | 10    | 1268.2204 | 1268.2199  | 0.0005   | 0.001       |
| 14   | 2    | 11   | 13    | 1     | 10    | 1547.1685 | 1547.1681  | 0.0005   | 0.001       |
| 14   | 2    | 12   | 13    | 1     | 11    | 1547.1815 | 1547.1809  | 0.0006   | 0.001       |
| 14   | 2    | 13   | 13    | 1     | 12    | 1547.1940 | 1547.1934  | 0.0006   | 0.001       |
| 14   | 2    | 14   | 13    | 1     | 13    | 1547.2058 | 1547.2056  | 0.0002   | 0.001       |
| 14   | 2    | 15   | 13    | 1     | 14    | 1547.2186 | 1547.2173  | 0.0013   | 0.001       |
| 14   | 2    | 16   | 13    | 1     | 15    | 1547.2295 | 1547.2288  | 0.0007   | 0.001       |
| 14   | 2    | 17   | 13    | 1     | 16    | 1547.2401 | 1547.2399  | 0.0002   | 0.001       |
| 13   | 2    | 16   | 14    | 1     | 17    | 1253.4654 | 1253.4652  | 0.0002   | 0.003       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 13   | 2    | 15   | 14    | 1     | 16    | 1253.5062 | 1253.5059  | 0.0004   | 0.003       |
| 13   | 2    | 14   | 14    | 1     | 15    | 1253.5460 | 1253.5464  | -0.0004  | 0.003       |
| 13   | 2    | 13   | 14    | 1     | 14    | 1253.5869 | 1253.5866  | 0.0003   | 0.003       |
| 13   | 2    | 12   | 14    | 1     | 13    | 1253.6266 | 1253.6262  | 0.0004   | 0.003       |
| 13   | 2    | 11   | 14    | 1     | 12    | 1253.6649 | 1253.6651  | -0.0002  | 0.003       |
| 13   | 2    | 10   | 14    | 1     | 11    | 1253.7028 | 1253.7029  | -0.0001  | 0.003       |
| 15   | 2    | 12   | 14    | 1     | 11    | 1552.3511 | 1552.3501  | 0.0010   | 0.003       |
| 15   | 2    | 13   | 14    | 1     | 12    | 1552.3629 | 1552.3613  | 0.0016   | 0.003       |
| 15   | 2    | 14   | 14    | 1     | 13    | 1552.3744 | 1552.3721  | 0.0024   | 0.003       |
| 15   | 2    | 15   | 14    | 1     | 14    | 1552.3841 | 1552.3824  | 0.0017   | 0.003       |
| 15   | 2    | 16   | 14    | 1     | 15    | 1552.3936 | 1552.3925  | 0.0011   | 0.003       |
| 15   | 2    | 17   | 14    | 1     | 16    | 1552.4047 | 1552.4022  | 0.0025   | 0.003       |
| 15   | 2    | 18   | 14    | 1     | 17    | 1552.4131 | 1552.4116  | 0.0015   | 0.003       |
| 14   | 2    | 17   | 15    | 1     | 18    | 1238.7124 | 1238.7121  | 0.0003   | 0.003       |
| 14   | 2    | 16   | 15    | 1     | 17    | 1238.7536 | 1238.7533  | 0.0003   | 0.003       |
| 14   | 2    | 15   | 15    | 1     | 16    | 1238.7946 | 1238.7943  | 0.0003   | 0.003       |
| 14   | 2    | 14   | 15    | 1     | 15    | 1238.8348 | 1238.8350  | -0.0002  | 0.003       |
| 14   | 2    | 13   | 15    | 1     | 14    | 1238.8750 | 1238.8750  | 0.0000   | 0.003       |
| 14   | 2    | 12   | 15    | 1     | 13    | 1238.9145 | 1238.9142  | 0.0003   | 0.003       |
| 14   | 2    | 11   | 15    | 1     | 12    | 1238.9521 | 1238.9525  | -0.0004  | 0.003       |
| 16   | 2    | 13   | 15    | 1     | 12    | 1557.0939 | 1557.0921  | 0.0018   | 0.002       |
| 16   | 2    | 14   | 15    | 1     | 13    | 1557.1040 | 1557.1015  | 0.0025   | 0.002       |
| 16   | 2    | 15   | 15    | 1     | 14    | 1557.1040 | 1557.1105  | -0.0065  | 0.003       |
| 16   | 2    | 16   | 15    | 1     | 15    | 1557.1130 | 1557.1191  | -0.0061  | 0.003       |
| 16   | 2    | 17   | 15    | 1     | 16    | 1557.1224 | 1557.1273  | -0.0049  | 0.002       |
| 16   | 2    | 18   | 15    | 1     | 17    | 1557.1312 | 1557.1352  | -0.0040  | 0.003       |
| 16   | 2    | 19   | 15    | 1     | 18    | 1557.1423 | 1557.1428  | -0.0005  | 0.002       |
| 15   | 2    | 18   | 16    | 1     | 19    | 1223.7317 | 1223.7316  | 0.0002   | 0.001       |
| 15   | 2    | 17   | 16    | 1     | 18    | 1223.7738 | 1223.7733  | 0.0005   | 0.001       |
| 15   | 2    | 16   | 16    | 1     | 17    | 1223.8145 | 1223.8148  | -0.0003  | 0.001       |
| 15   | 2    | 15   | 16    | 1     | 16    | 1223.8558 | 1223.8558  | 0.0000   | 0.001       |
| 15   | 2    | 14   | 16    | 1     | 15    | 1223.8956 | 1223.8962  | -0.0006  | 0.001       |
| 15   | 2    | 13   | 16    | 1     | 14    | 1223.9358 | 1223.9359  | -0.0001  | 0.001       |
| 15   | 2    | 12   | 16    | 1     | 13    | 1223.9750 | 1223.9746  | 0.0004   | 0.001       |
| 17   | 2    | 14   | 16    | 1     | 13    | 1561.3972 | 1561.3867  | 0.0105   | 1           |
| 17   | 2    | 15   | 16    | 1     | 14    | 1561.3972 | 1561.3943  | 0.0030   | 0.003       |
| 17   | 2    | 16   | 16    | 1     | 15    | 1561.3972 | 1561.4014  | -0.0042  | 0.002       |
| 17   | 2    | 17   | 16    | 1     | 16    | 1561.4081 | 1561.4081  | 0.0001   | 0.003       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 17   | 2    | 18   | 16    | 1     | 17    | 1561.4168 | 1561.4144  | 0.0024   | 0.003       |
| 17   | 2    | 19   | 16    | 1     | 18    | 1561.4168 | 1561.4205  | -0.0037  | 0.003       |
| 17   | 2    | 20   | 16    | 1     | 19    | 1561.4287 | 1561.4262  | 0.0025   | 0.001       |
| 16   | 2    | 19   | 17    | 1     | 20    | 1208.5299 | 1208.5291  | 0.0008   | 0.001       |
| 16   | 2    | 18   | 17    | 1     | 19    | 1208.5722 | 1208.5713  | 0.0009   | 0.001       |
| 16   | 2    | 17   | 17    | 1     | 18    | 1208.6130 | 1208.6132  | -0.0002  | 0.001       |
| 16   | 2    | 16   | 17    | 1     | 17    | 1208.6545 | 1208.6547  | -0.0002  | 0.001       |
| 16   | 2    | 15   | 17    | 1     | 16    | 1208.6958 | 1208.6955  | 0.0003   | 0.001       |
| 16   | 2    | 14   | 17    | 1     | 15    | 1208.7358 | 1208.7355  | 0.0003   | 0.001       |
| 16   | 2    | 13   | 17    | 1     | 14    | 1208.7747 | 1208.7747  | 0.0000   | 0.001       |
| 18   | 2    | 15   | 17    | 1     | 14    | 1565.2287 | 1565.2267  | 0.0020   | 0.001       |
| 18   | 2    | 16   | 17    | 1     | 15    | 1565.2287 | 1565.2323  | -0.0036  | 0.003       |
| 18   | 2    | 17   | 17    | 1     | 16    | 1565.2287 | 1565.2375  | -0.0088  | 10          |
| 18   | 2    | 18   | 17    | 1     | 17    | 1565.2460 | 1565.2422  | 0.0038   | 0.003       |
| 18   | 2    | 19   | 17    | 1     | 18    | 1565.2460 | 1565.2467  | -0.0007  | 0.002       |
| 18   | 2    | 20   | 17    | 1     | 19    | 1565.2460 | 1565.2507  | -0.0047  | 0.004       |
| 18   | 2    | 21   | 17    | 1     | 20    | 1565.2581 | 1565.2546  | 0.0036   | 0.002       |
| 17   | 2    | 20   | 18    | 1     | 21    | 1193.1114 | 1193.1102  | 0.0012   | 0.001       |
| 17   | 2    | 19   | 18    | 1     | 20    | 1193.1526 | 1193.1529  | -0.0003  | 0.001       |
| 17   | 2    | 18   | 18    | 1     | 19    | 1193.1955 | 1193.1952  | 0.0003   | 0.001       |
| 17   | 2    | 17   | 18    | 1     | 18    | 1193.2366 | 1193.2370  | -0.0004  | 0.001       |
| 17   | 2    | 16   | 18    | 1     | 17    | 1193.2787 | 1193.2782  | 0.0005   | 0.001       |
| 17   | 2    | 15   | 18    | 1     | 16    | 1193.3184 | 1193.3186  | -0.0002  | 0.001       |
| 17   | 2    | 14   | 18    | 1     | 15    | 1193.3589 | 1193.3581  | 0.0008   | 0.001       |
| 19   | 2    | 16   | 18    | 1     | 15    | 1568.6086 | 1568.6049  | 0.0037   | 0.003       |
| 19   | 2    | 17   | 18    | 1     | 16    | 1568.6086 | 1568.6085  | 0.0001   | 0.002       |
| 19   | 2    | 18   | 18    | 1     | 17    | 1568.6086 | 1568.6117  | -0.0031  | 0.002       |
| 19   | 2    | 19   | 18    | 1     | 18    | 1568.6086 | 1568.6144  | -0.0058  | 0.003       |
| 19   | 2    | 20   | 18    | 1     | 19    | 1568.6259 | 1568.6169  | 0.0091   | 1           |
| 19   | 2    | 21   | 18    | 1     | 20    | 1568.6259 | 1568.6189  | 0.0070   | 0.003       |
| 19   | 2    | 22   | 18    | 1     | 21    | 1568.6259 | 1568.6207  | 0.0052   | 0.002       |
| 18   | 2    | 21   | 19    | 1     | 22    | 1177.4808 | 1177.4798  | 0.0010   | 0.001       |
| 18   | 2    | 20   | 19    | 1     | 21    | 1177.5238 | 1177.5229  | 0.0009   | 0.001       |
| 18   | 2    | 19   | 19    | 1     | 20    | 1177.5644 | 1177.5656  | -0.0012  | 0.001       |
| 18   | 2    | 18   | 19    | 1     | 19    | 1177.6073 | 1177.6078  | -0.0005  | 0.001       |
| 18   | 2    | 17   | 19    | 1     | 18    | 1177.6493 | 1177.6494  | -0.0001  | 0.001       |
| 18   | 2    | 16   | 19    | 1     | 17    | 1177.6905 | 1177.6901  | 0.0004   | 0.001       |
| 18   | 2    | 15   | 19    | 1     | 16    | 1177.7305 | 1177.7300  | 0.0005   | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 20   | 2    | 17   | 19    | 1     | 16    | 1571.5233 | 1571.5144  | 0.0089   | 0.01        |
| 20   | 2    | 18   | 19    | 1     | 17    | 1571.5233 | 1571.5160  | 0.0074   | 0.01        |
| 20   | 2    | 19   | 19    | 1     | 18    | 1571.5233 | 1571.5171  | 0.0063   | 0.01        |
| 20   | 2    | 20   | 19    | 1     | 19    | 1571.5233 | 1571.5177  | 0.0056   | 0.01        |
| 20   | 2    | 21   | 19    | 1     | 20    | 1571.5233 | 1571.5181  | 0.0052   | 0.01        |
| 20   | 2    | 22   | 19    | 1     | 21    | 1571.5233 | 1571.5181  | 0.0053   | 0.005       |
| 20   | 2    | 23   | 19    | 1     | 22    | 1571.5233 | 1571.5178  | 0.0055   | 0.005       |
| 19   | 2    | 22   | 20    | 1     | 23    | 1161.6438 | 1161.6428  | 0.0010   | 0.001       |
| 19   | 2    | 21   | 20    | 1     | 22    | 1161.6867 | 1161.6863  | 0.0004   | 0.001       |
| 19   | 2    | 20   | 20    | 1     | 21    | 1161.7291 | 1161.7295  | -0.0004  | 0.001       |
| 19   | 2    | 19   | 20    | 1     | 20    | 1161.7732 | 1161.7720  | 0.0012   | 0.001       |
| 19   | 2    | 18   | 20    | 1     | 19    | 1161.8144 | 1161.8139  | 0.0005   | 0.001       |
| 19   | 2    | 17   | 20    | 1     | 18    | 1161.8557 | 1161.8550  | 0.0007   | 0.001       |
| 19   | 2    | 16   | 20    | 1     | 17    | 1161.8943 | 1161.8953  | -0.0010  | 0.001       |
| 21   | 2    | 18   | 20    | 1     | 17    | 1573.9457 | 1573.9485  | -0.0028  | 0.003       |
| 21   | 2    | 19   | 20    | 1     | 18    | 1573.9457 | 1573.9479  | -0.0022  | 0.002       |
| 21   | 2    | 20   | 20    | 1     | 19    | 1573.9457 | 1573.9468  | -0.0011  | 0.002       |
| 21   | 2    | 21   | 20    | 1     | 20    | 1573.9457 | 1573.9454  | 0.0003   | 0.002       |
| 21   | 2    | 22   | 20    | 1     | 21    | 1573.9457 | 1573.9435  | 0.0022   | 0.002       |
| 21   | 2    | 23   | 20    | 1     | 22    | 1573.9457 | 1573.9414  | 0.0043   | 0.002       |
| 21   | 2    | 24   | 20    | 1     | 23    | 1573.9457 | 1573.9389  | 0.0068   | 0.003       |
| 20   | 2    | 23   | 21    | 1     | 24    | 1145.6039 | 1145.6038  | 0.0001   | 0.001       |
| 20   | 2    | 22   | 21    | 1     | 23    | 1145.6486 | 1145.6478  | 0.0008   | 0.001       |
| 20   | 2    | 21   | 21    | 1     | 22    | 1145.6923 | 1145.6912  | 0.0011   | 0.001       |
| 20   | 2    | 20   | 21    | 1     | 21    | 1145.7346 | 1145.7342  | 0.0005   | 0.001       |
| 20   | 2    | 19   | 21    | 1     | 20    | 1145.7776 | 1145.7764  | 0.0012   | 0.001       |
| 20   | 2    | 18   | 21    | 1     | 19    | 1145.8187 | 1145.8178  | 0.0009   | 0.001       |
| 20   | 2    | 17   | 21    | 1     | 18    | 1145.8601 | 1145.8584  | 0.0017   | 0.001       |
| 22   | 2    | 19   | 21    | 1     | 18    | 1575.8844 | 1575.9006  | -0.0162  | 10          |
| 22   | 2    | 20   | 21    | 1     | 19    | 1575.8844 | 1575.8978  | -0.0134  | 10          |
| 22   | 2    | 21   | 21    | 1     | 20    | 1575.8844 | 1575.8945  | -0.0101  | 10          |
| 22   | 2    | 22   | 21    | 1     | 21    | 1575.8844 | 1575.8908  | -0.0064  | 10          |
| 22   | 2    | 23   | 21    | 1     | 22    | 1575.8844 | 1575.8868  | -0.0024  | 0.003       |
| 22   | 2    | 25   | 21    | 1     | 24    | 1575.8844 | 1575.8777  | 0.0067   | 0.003       |
| 21   | 2    | 24   | 22    | 1     | 25    | 1129.3676 | 1129.3671  | 0.0005   | 0.001       |
| 21   | 2    | 23   | 22    | 1     | 24    | 1129.4121 | 1129.4115  | 0.0006   | 0.001       |
| 21   | 2    | 22   | 22    | 1     | 23    | 1129.4563 | 1129.4553  | 0.0010   | 0.001       |
| 21   | 2    | 21   | 22    | 1     | 22    | 1129.4995 | 1129.4986  | 0.0009   | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 21   | 2    | 20   | 22    | 1     | 21    | 1129.5422 | 1129.5411  | 0.0011   | 0.001       |
| 21   | 2    | 19   | 22    | 1     | 20    | 1129.5828 | 1129.5829  | -0.0001  | 0.001       |
| 21   | 2    | 18   | 22    | 1     | 19    | 1129.6248 | 1129.6238  | 0.0010   | 0.001       |
| 23   | 2    | 20   | 22    | 1     | 19    | 1577.3280 | 1577.3646  | -0.0366  | 100         |
| 23   | 2    | 21   | 22    | 1     | 20    | 1577.3280 | 1577.3595  | -0.0315  | 100         |
| 23   | 2    | 22   | 22    | 1     | 21    | 1577.3280 | 1577.3540  | -0.0260  | 100         |
| 23   | 2    | 23   | 22    | 1     | 22    | 1577.3280 | 1577.3480  | -0.0200  | 100         |
| 23   | 2    | 24   | 22    | 1     | 23    | 1577.3280 | 1577.3416  | -0.0136  | 100         |
| 23   | 2    | 25   | 22    | 1     | 24    | 1577.3280 | 1577.3349  | -0.0069  | 100         |
| 23   | 2    | 26   | 22    | 1     | 25    | 1577.3280 | 1577.3279  | 0.0001   | 0.002       |
| 22   | 2    | 25   | 23    | 1     | 26    | 1112.9360 | 1112.9367  | -0.0007  | 0.001       |
| 22   | 2    | 24   | 23    | 1     | 25    | 1112.9819 | 1112.9815  | 0.0004   | 0.001       |
| 22   | 2    | 23   | 23    | 1     | 24    | 1113.0252 | 1113.0257  | -0.0005  | 0.001       |
| 22   | 2    | 22   | 23    | 1     | 23    | 1113.0701 | 1113.0693  | 0.0008   | 0.001       |
| 22   | 2    | 21   | 23    | 1     | 22    | 1113.1095 | 1113.1122  | -0.0027  | 0.001       |
| 22   | 2    | 20   | 23    | 1     | 21    | 1113.1540 | 1113.1542  | -0.0002  | 0.001       |
| 22   | 2    | 19   | 23    | 1     | 20    | 1113.1945 | 1113.1954  | -0.0009  | 0.001       |
| 24   | 2    | 24   | 23    | 1     | 23    | 1578.3087 | 1578.3110  | -0.0023  | 0.002       |
| 24   | 2    | 25   | 23    | 1     | 24    | 1578.2622 | 1578.3022  | -0.0400  | 10          |
| 24   | 2    | 26   | 23    | 1     | 25    | 1578.2898 | 1578.2931  | -0.0033  | 0.002       |
| 24   | 2    | 27   | 23    | 1     | 26    | 1578.2898 | 1578.2838  | 0.0061   | 0.003       |
| 24   | 2    | 22   | 23    | 1     | 21    | 1578.3186 | 1578.3273  | -0.0087  | 1           |
| 24   | 2    | 23   | 23    | 1     | 22    | 1578.3186 | 1578.3194  | -0.0008  | 0.001       |
| 23   | 2    | 26   | 24    | 1     | 27    | 1096.3149 | 1096.3165  | -0.0016  | 0.001       |
| 23   | 2    | 25   | 24    | 1     | 26    | 1096.3611 | 1096.3616  | -0.0005  | 0.001       |
| 23   | 2    | 24   | 24    | 1     | 25    | 1096.4043 | 1096.4062  | -0.0019  | 0.001       |
| 23   | 2    | 23   | 24    | 1     | 24    | 1096.4503 | 1096.4501  | 0.0002   | 0.001       |
| 23   | 2    | 22   | 24    | 1     | 23    | 1096.4920 | 1096.4933  | -0.0013  | 0.001       |
| 23   | 2    | 21   | 24    | 1     | 22    | 1096.5784 | 1096.5356  | 0.0428   | 10          |
| 4    | 3    | 7    | 3     | 2     | 6     | 1411.6947 | 1411.6917  | 0.0030   | 0.003       |
| 3    | 3    | 6    | 4     | 2     | 7     | 1328.5533 | 1328.5519  | 0.0015   | 0.003       |
| 3    | 3    | 5    | 4     | 2     | 6     | 1328.5881 | 1328.5842  | 0.0039   | 0.003       |
| 5    | 3    | 6    | 4     | 2     | 5     | 1420.4347 | 1420.4334  | 0.0013   | 0.003       |
| 5    | 3    | 7    | 4     | 2     | 6     | 1420.4599 | 1420.4575  | 0.0024   | 0.003       |
| 5    | 3    | 8    | 4     | 2     | 7     | 1420.4798 | 1420.4791  | 0.0007   | 0.003       |
| 4    | 3    | 7    | 5     | 2     | 8     | 1316.7117 | 1316.7106  | 0.0011   | 0.001       |
| 4    | 3    | 6    | 5     | 2     | 7     | 1316.7443 | 1316.7443  | 0.0000   | 0.001       |
| 4    | 3    | 5    | 5     | 2     | 6     | 1316.7818 | 1316.7808  | 0.0010   | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 4    | 3    | 4    | 5     | 2     | 5     | 1316.8353 | 1316.8178  | 0.0175   | 10          |
| 4    | 3    | 3    | 5     | 2     | 4     | 1316.8569 | 1316.8535  | 0.0035   | 0.002       |
| 6    | 3    | 3    | 5     | 2     | 2     | 1428.7801 | 1428.7564  | 0.0238   | 10          |
| 6    | 3    | 4    | 5     | 2     | 3     | 1428.7801 | 1428.7787  | 0.0014   | 0.003       |
| 6    | 3    | 5    | 5     | 2     | 4     | 1428.8039 | 1428.8014  | 0.0025   | 0.003       |
| 6    | 3    | 6    | 5     | 2     | 5     | 1428.8245 | 1428.8245  | 0.0000   | 0.003       |
| 6    | 3    | 7    | 5     | 2     | 6     | 1428.8478 | 1428.8475  | 0.0003   | 0.003       |
| 6    | 3    | 8    | 5     | 2     | 7     | 1428.8713 | 1428.8697  | 0.0016   | 0.003       |
| 6    | 3    | 9    | 5     | 2     | 8     | 1428.8910 | 1428.8902  | 0.0008   | 0.003       |
| 5    | 3    | 8    | 6     | 2     | 9     | 1304.5668 | 1304.5666  | 0.0002   | 0.001       |
| 5    | 3    | 7    | 6     | 2     | 8     | 1304.6027 | 1304.6014  | 0.0013   | 0.001       |
| 5    | 3    | 6    | 6     | 2     | 7     | 1304.6397 | 1304.6380  | 0.0017   | 0.001       |
| 5    | 3    | 5    | 6     | 2     | 6     | 1304.6735 | 1304.6748  | -0.0013  | 0.001       |
| 5    | 3    | 4    | 6     | 2     | 5     | 1304.7104 | 1304.7105  | -0.0001  | 0.001       |
| 5    | 3    | 3    | 6     | 2     | 4     | 1304.7469 | 1304.7444  | 0.0025   | 0.001       |
| 5    | 3    | 2    | 6     | 2     | 3     | 1304.7770 | 1304.7757  | 0.0013   | 0.001       |
| 7    | 3    | 6    | 6     | 2     | 5     | 1436.8347 | 1436.8346  | 0.0001   | 0.001       |
| 7    | 3    | 5    | 6     | 2     | 4     | 1436.8347 | 1436.8131  | 0.0216   | 10          |
| 7    | 3    | 7    | 6     | 2     | 6     | 1436.8563 | 1436.8560  | 0.0003   | 0.001       |
| 7    | 3    | 8    | 6     | 2     | 7     | 1436.8759 | 1436.8772  | -0.0013  | 0.001       |
| 7    | 3    | 9    | 6     | 2     | 8     | 1436.8984 | 1436.8978  | 0.0006   | 0.001       |
| 7    | 3    | 10   | 6     | 2     | 9     | 1436.9167 | 1436.9172  | -0.0005  | 0.001       |
| 6    | 3    | 9    | 7     | 2     | 10    | 1292.1283 | 1292.1268  | 0.0015   | 0.003       |
| 6    | 3    | 8    | 7     | 2     | 9     | 1292.1630 | 1292.1626  | 0.0004   | 0.003       |
| 6    | 3    | 7    | 7     | 2     | 8     | 1292.1998 | 1292.1995  | 0.0003   | 0.003       |
| 6    | 3    | 6    | 7     | 2     | 7     | 1292.2362 | 1292.2365  | -0.0003  | 0.003       |
| 6    | 3    | 5    | 7     | 2     | 6     | 1292.2721 | 1292.2726  | -0.0005  | 0.003       |
| 6    | 3    | 4    | 7     | 2     | 5     | 1292.3090 | 1292.3072  | 0.0019   | 0.003       |
| 6    | 3    | 3    | 7     | 2     | 4     | 1292.3395 | 1292.3397  | -0.0002  | 0.001       |
| 8    | 3    | 5    | 7     | 2     | 4     | 1444.4353 | 1444.4353  | 0.0001   | 0.001       |
| 8    | 3    | 6    | 7     | 2     | 5     | 1444.4561 | 1444.4554  | 0.0007   | 0.001       |
| 8    | 3    | 7    | 7     | 2     | 6     | 1444.4763 | 1444.4754  | 0.0009   | 0.001       |
| 8    | 3    | 8    | 7     | 2     | 7     | 1444.4951 | 1444.4953  | -0.0002  | 0.001       |
| 8    | 3    | 9    | 7     | 2     | 8     | 1444.5142 | 1444.5149  | -0.0007  | 0.001       |
| 8    | 3    | 10   | 7     | 2     | 9     | 1444.5330 | 1444.5339  | -0.0009  | 0.001       |
| 8    | 3    | 11   | 7     | 2     | 10    | 1444.5516 | 1444.5519  | -0.0003  | 0.001       |
| 7    | 3    | 10   | 8     | 2     | 11    | 1279.3985 | 1279.3978  | 0.0007   | 0.003       |
| 7    | 3    | 9    | 8     | 2     | 10    | 1279.4348 | 1279.4345  | 0.0003   | 0.003       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 7    | 3    | 8    | 8     | 2     | 9     | 1279.4717 | 1279.4719  | -0.0002  | 0.003       |
| 7    | 3    | 7    | 8     | 2     | 8     | 1279.5091 | 1279.5092  | -0.0001  | 0.003       |
| 7    | 3    | 6    | 8     | 2     | 7     | 1279.5450 | 1279.5458  | -0.0008  | 0.003       |
| 7    | 3    | 5    | 8     | 2     | 6     | 1279.5823 | 1279.5811  | 0.0012   | 0.003       |
| 7    | 3    | 4    | 8     | 2     | 5     | 1279.6149 | 1279.6146  | 0.0003   | 0.003       |
| 9    | 3    | 6    | 8     | 2     | 5     | 1451.6790 | 1451.6788  | 0.0002   | 0.001       |
| 9    | 3    | 7    | 8     | 2     | 6     | 1451.6974 | 1451.6976  | -0.0002  | 0.001       |
| 9    | 3    | 8    | 8     | 2     | 7     | 1451.7159 | 1451.7162  | -0.0003  | 0.001       |
| 9    | 3    | 9    | 8     | 2     | 8     | 1451.7340 | 1451.7345  | -0.0005  | 0.001       |
| 9    | 3    | 10   | 8     | 2     | 9     | 1451.7519 | 1451.7525  | -0.0006  | 0.001       |
| 9    | 3    | 11   | 8     | 2     | 10    | 1451.7695 | 1451.7699  | -0.0004  | 0.001       |
| 9    | 3    | 12   | 8     | 2     | 11    | 1451.7858 | 1451.7866  | -0.0008  | 0.001       |
| 8    | 3    | 11   | 9     | 2     | 12    | 1266.3870 | 1266.3863  | 0.0008   | 0.001       |
| 8    | 3    | 10   | 9     | 2     | 11    | 1266.4232 | 1266.4237  | -0.0005  | 0.001       |
| 8    | 3    | 9    | 9     | 2     | 10    | 1266.4610 | 1266.4617  | -0.0007  | 0.001       |
| 8    | 3    | 8    | 9     | 2     | 9     | 1266.4995 | 1266.4995  | 0.0000   | 0.001       |
| 8    | 3    | 7    | 9     | 2     | 8     | 1266.5362 | 1266.5366  | -0.0004  | 0.001       |
| 8    | 3    | 6    | 9     | 2     | 7     | 1266.5709 | 1266.5725  | -0.0016  | 0.001       |
| 8    | 3    | 5    | 9     | 2     | 6     | 1266.6078 | 1266.6069  | 0.0010   | 0.001       |
| 10   | 3    | 7    | 9     | 2     | 6     | 1458.5142 | 1458.5144  | -0.0002  | 0.001       |
| 10   | 3    | 8    | 9     | 2     | 7     | 1458.5341 | 1458.5318  | 0.0023   | 0.001       |
| 10   | 3    | 9    | 9     | 2     | 8     | 1458.5491 | 1458.5488  | 0.0003   | 0.001       |
| 10   | 3    | 10   | 9     | 2     | 9     | 1458.5645 | 1458.5656  | -0.0011  | 0.001       |
| 10   | 3    | 11   | 9     | 2     | 10    | 1458.5803 | 1458.5819  | -0.0016  | 0.001       |
| 10   | 3    | 12   | 9     | 2     | 11    | 1458.5970 | 1458.5978  | -0.0008  | 0.001       |
| 10   | 3    | 13   | 9     | 2     | 12    | 1458.6124 | 1458.6130  | -0.0006  | 0.001       |
| 9    | 3    | 12   | 10    | 2     | 13    | 1253.0999 | 1253.0985  | 0.0014   | 0.003       |
| 9    | 3    | 11   | 10    | 2     | 12    | 1253.1369 | 1253.1367  | 0.0002   | 0.003       |
| 9    | 3    | 10   | 10    | 2     | 11    | 1253.1749 | 1253.1752  | -0.0003  | 0.003       |
| 9    | 3    | 9    | 10    | 2     | 10    | 1253.2125 | 1253.2135  | -0.0010  | 0.003       |
| 9    | 3    | 8    | 10    | 2     | 9     | 1253.2515 | 1253.2511  | 0.0004   | 0.003       |
| 9    | 3    | 7    | 10    | 2     | 8     | 1253.2860 | 1253.2876  | -0.0016  | 0.003       |
| 9    | 3    | 6    | 10    | 2     | 7     | 1253.3216 | 1253.3228  | -0.0012  | 0.003       |
| 11   | 3    | 8    | 10    | 2     | 7     | 1464.9343 | 1464.9340  | 0.0003   | 0.001       |
| 11   | 3    | 9    | 10    | 2     | 8     | 1464.9501 | 1464.9499  | 0.0002   | 0.001       |
| 11   | 3    | 10   | 10    | 2     | 9     | 1464.9632 | 1464.9653  | -0.0021  | 0.001       |
| 11   | 3    | 11   | 10    | 2     | 10    | 1464.9795 | 1464.9805  | -0.0010  | 0.001       |
| 11   | 3    | 12   | 10    | 2     | 11    | 1464.9937 | 1464.9952  | -0.0015  | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 11   | 3    | 13   | 10    | 2     | 12    | 1465.0095 | 1465.0094  | 0.0001   | 0.001       |
| 11   | 3    | 14   | 10    | 2     | 13    | 1465.0224 | 1465.0230  | -0.0006  | 0.001       |
| 10   | 3    | 13   | 11    | 2     | 14    | 1239.5408 | 1239.5407  | 0.0001   | 0.003       |
| 10   | 3    | 12   | 11    | 2     | 13    | 1239.5794 | 1239.5797  | -0.0003  | 0.003       |
| 10   | 3    | 11   | 11    | 2     | 12    | 1239.6186 | 1239.6187  | -0.0001  | 0.003       |
| 10   | 3    | 10   | 11    | 2     | 11    | 1239.6557 | 1239.6575  | -0.0018  | 0.003       |
| 10   | 3    | 9    | 11    | 2     | 10    | 1239.6946 | 1239.6956  | -0.0010  | 0.003       |
| 10   | 3    | 8    | 11    | 2     | 9     | 1239.7328 | 1239.7327  | 0.0001   | 0.003       |
| 10   | 3    | 7    | 11    | 2     | 8     | 1239.7685 | 1239.7686  | -0.0001  | 0.003       |
| 12   | 3    | 9    | 11    | 2     | 8     | 1470.9285 | 1470.9294  | -0.0009  | 0.001       |
| 12   | 3    | 10   | 11    | 2     | 9     | 1470.9433 | 1470.9437  | -0.0004  | 0.001       |
| 12   | 3    | 11   | 11    | 2     | 10    | 1470.9589 | 1470.9575  | 0.0014   | 0.001       |
| 12   | 3    | 12   | 11    | 2     | 11    | 1470.9709 | 1470.9709  | 0.0000   | 0.001       |
| 12   | 3    | 13   | 11    | 2     | 12    | 1470.9837 | 1470.9839  | -0.0002  | 0.001       |
| 12   | 3    | 14   | 11    | 2     | 13    | 1470.9959 | 1470.9965  | -0.0006  | 0.001       |
| 12   | 3    | 15   | 11    | 2     | 14    | 1471.0079 | 1471.0085  | -0.0006  | 0.001       |
| 11   | 3    | 14   | 12    | 2     | 15    | 1225.7198 | 1225.7189  | 0.0009   | 0.001       |
| 11   | 3    | 13   | 12    | 2     | 14    | 1225.7581 | 1225.7585  | -0.0004  | 0.001       |
| 11   | 3    | 12   | 12    | 2     | 13    | 1225.7969 | 1225.7982  | -0.0013  | 0.001       |
| 11   | 3    | 11   | 12    | 2     | 12    | 1225.8376 | 1225.8375  | 0.0001   | 0.001       |
| 11   | 3    | 10   | 12    | 2     | 11    | 1225.8752 | 1225.8761  | -0.0009  | 0.001       |
| 11   | 3    | 9    | 12    | 2     | 10    | 1225.9137 | 1225.9138  | -0.0001  | 0.001       |
| 11   | 3    | 8    | 12    | 2     | 9     | 1225.9497 | 1225.9503  | -0.0006  | 0.001       |
| 13   | 3    | 10   | 12    | 2     | 9     | 1476.4901 | 1476.4924  | -0.0023  | 0.002       |
| 13   | 3    | 11   | 12    | 2     | 10    | 1476.5053 | 1476.5049  | 0.0004   | 0.001       |
| 13   | 3    | 12   | 12    | 2     | 11    | 1476.5171 | 1476.5170  | 0.0001   | 0.001       |
| 13   | 3    | 13   | 12    | 2     | 12    | 1476.5281 | 1476.5288  | -0.0007  | 0.001       |
| 13   | 3    | 14   | 12    | 2     | 13    | 1476.5410 | 1476.5400  | 0.0010   | 0.001       |
| 13   | 3    | 15   | 12    | 2     | 14    | 1476.5509 | 1476.5509  | 0.0000   | 0.001       |
| 13   | 3    | 16   | 12    | 2     | 15    | 1476.5617 | 1476.5612  | 0.0005   | 0.001       |
| 12   | 3    | 15   | 13    | 2     | 16    | 1211.6411 | 1211.6389  | 0.0022   | 0.001       |
| 12   | 3    | 14   | 13    | 2     | 15    | 1211.6804 | 1211.6792  | 0.0012   | 0.001       |
| 12   | 3    | 13   | 13    | 2     | 14    | 1211.7199 | 1211.7194  | 0.0005   | 0.001       |
| 12   | 3    | 12   | 13    | 2     | 13    | 1211.7591 | 1211.7592  | -0.0001  | 0.001       |
| 12   | 3    | 11   | 13    | 2     | 12    | 1211.7981 | 1211.7983  | -0.0002  | 0.001       |
| 12   | 3    | 10   | 13    | 2     | 11    | 1211.8366 | 1211.8365  | 0.0001   | 0.001       |
| 12   | 3    | 9    | 13    | 2     | 10    | 1211.8754 | 1211.8736  | 0.0018   | 0.001       |
| 14   | 3    | 11   | 13    | 2     | 10    | 1481.6178 | 1481.6145  | 0.0033   | 0.002       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 14   | 3    | 12   | 13    | 2     | 11    | 1481.6286 | 1481.6254  | 0.0032   | 0.002       |
| 14   | 3    | 13   | 13    | 2     | 12    | 1481.6359 | 1481.6357  | 0.0002   | 0.002       |
| 14   | 3    | 14   | 13    | 2     | 13    | 1481.6481 | 1481.6456  | 0.0025   | 0.002       |
| 14   | 3    | 15   | 13    | 2     | 14    | 1481.6563 | 1481.6551  | 0.0012   | 0.002       |
| 14   | 3    | 16   | 13    | 2     | 15    | 1481.6676 | 1481.6642  | 0.0034   | 0.002       |
| 14   | 3    | 17   | 13    | 2     | 16    | 1481.6762 | 1481.6728  | 0.0034   | 0.002       |
| 13   | 3    | 16   | 14    | 2     | 17    | 1197.3078 | 1197.3063  | 0.0015   | 0.001       |
| 13   | 3    | 15   | 14    | 2     | 16    | 1197.3473 | 1197.3472  | 0.0001   | 0.001       |
| 13   | 3    | 14   | 14    | 2     | 15    | 1197.3865 | 1197.3879  | -0.0014  | 0.001       |
| 13   | 3    | 13   | 14    | 2     | 14    | 1197.4279 | 1197.4282  | -0.0003  | 0.001       |
| 13   | 3    | 12   | 14    | 2     | 13    | 1197.4679 | 1197.4678  | 0.0001   | 0.001       |
| 13   | 3    | 11   | 14    | 2     | 12    | 1197.5063 | 1197.5065  | -0.0002  | 0.001       |
| 13   | 3    | 10   | 14    | 2     | 11    | 1197.5432 | 1197.5442  | -0.0010  | 0.001       |
| 15   | 3    | 12   | 14    | 2     | 11    | 1486.2899 | 1486.2877  | 0.0022   | 0.002       |
| 15   | 3    | 13   | 14    | 2     | 12    | 1486.2899 | 1486.2967  | -0.0068  | 0.1         |
| 15   | 3    | 14   | 14    | 2     | 13    | 1486.3094 | 1486.3052  | 0.0042   | 0.003       |
| 15   | 3    | 15   | 14    | 2     | 14    | 1486.3094 | 1486.3133  | -0.0039  | 0.003       |
| 15   | 3    | 16   | 14    | 2     | 15    | 1486.3200 | 1486.3209  | -0.0009  | 0.001       |
| 15   | 3    | 17   | 14    | 2     | 16    | 1486.3266 | 1486.3281  | -0.0015  | 0.001       |
| 15   | 3    | 18   | 14    | 2     | 17    | 1486.3353 | 1486.3349  | 0.0004   | 0.001       |
| 14   | 3    | 17   | 15    | 2     | 18    | 1182.7270 | 1182.7264  | 0.0006   | 0.001       |
| 14   | 3    | 16   | 15    | 2     | 17    | 1182.7681 | 1182.7678  | 0.0003   | 0.001       |
| 14   | 3    | 15   | 15    | 2     | 16    | 1182.8087 | 1182.8091  | -0.0004  | 0.001       |
| 14   | 3    | 14   | 15    | 2     | 15    | 1182.8492 | 1182.8498  | -0.0006  | 0.001       |
| 14   | 3    | 13   | 15    | 2     | 14    | 1182.8881 | 1182.8899  | -0.0018  | 0.001       |
| 14   | 3    | 12   | 15    | 2     | 13    | 1182.9279 | 1182.9291  | -0.0012  | 0.001       |
| 14   | 3    | 11   | 15    | 2     | 12    | 1182.9683 | 1182.9673  | 0.0010   | 0.001       |
| 16   | 3    | 13   | 15    | 2     | 12    | 1490.5116 | 1490.5034  | 0.0082   | 1           |
| 16   | 3    | 14   | 15    | 2     | 13    | 1490.5116 | 1490.5106  | 0.0011   | 0.002       |
| 16   | 3    | 15   | 15    | 2     | 14    | 1490.5116 | 1490.5172  | -0.0056  | 0.004       |
| 16   | 3    | 16   | 15    | 2     | 15    | 1490.5281 | 1490.5233  | 0.0048   | 0.004       |
| 16   | 3    | 17   | 15    | 2     | 16    | 1490.5281 | 1490.5290  | -0.0009  | 0.002       |
| 16   | 3    | 18   | 15    | 2     | 17    | 1490.5382 | 1490.5343  | 0.0039   | 0.002       |
| 16   | 3    | 19   | 15    | 2     | 18    | 1490.5382 | 1490.5392  | -0.0010  | 0.001       |
| 15   | 3    | 18   | 16    | 2     | 19    | 1167.9043 | 1167.9042  | 0.0001   | 0.001       |
| 15   | 3    | 17   | 16    | 2     | 18    | 1167.9459 | 1167.9462  | -0.0003  | 0.001       |
| 15   | 3    | 16   | 16    | 2     | 17    | 1167.9885 | 1167.9880  | 0.0005   | 0.001       |
| 15   | 3    | 15   | 16    | 2     | 16    | 1168.0314 | 1168.0292  | 0.0022   | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 15   | 3    | 14   | 16    | 2     | 15    | 1168.0702 | 1168.0697  | 0.0005   | 0.001       |
| 15   | 3    | 13   | 16    | 2     | 14    | 1168.1086 | 1168.1094  | -0.0008  | 0.001       |
| 15   | 3    | 12   | 16    | 2     | 13    | 1168.1482 | 1168.1481  | 0.0001   | 0.001       |
| 17   | 3    | 14   | 16    | 2     | 13    | 1494.2567 | 1494.2535  | 0.0033   | 0.002       |
| 17   | 3    | 15   | 16    | 2     | 14    | 1494.2567 | 1494.2586  | -0.0019  | 0.002       |
| 17   | 3    | 16   | 16    | 2     | 15    | 1494.2658 | 1494.2633  | 0.0025   | 0.002       |
| 17   | 3    | 17   | 16    | 2     | 16    | 1494.2658 | 1494.2675  | -0.0017  | 0.002       |
| 17   | 3    | 18   | 16    | 2     | 17    | 1494.2658 | 1494.2712  | -0.0054  | 0.003       |
| 17   | 3    | 19   | 16    | 2     | 18    | 1494.2800 | 1494.2745  | 0.0055   | 0.1         |
| 17   | 3    | 20   | 16    | 2     | 19    | 1494.2800 | 1494.2774  | 0.0026   | 0.002       |
| 16   | 3    | 19   | 17    | 2     | 20    | 1152.8442 | 1152.8446  | -0.0004  | 0.001       |
| 16   | 3    | 18   | 17    | 2     | 19    | 1152.8875 | 1152.8872  | 0.0004   | 0.001       |
| 16   | 3    | 17   | 17    | 2     | 18    | 1152.9306 | 1152.9294  | 0.0012   | 0.001       |
| 16   | 3    | 16   | 17    | 2     | 17    | 1152.9712 | 1152.9711  | 0.0002   | 0.001       |
| 16   | 3    | 15   | 17    | 2     | 16    | 1153.0111 | 1153.0120  | -0.0009  | 0.001       |
| 16   | 3    | 14   | 17    | 2     | 15    | 1153.0529 | 1153.0522  | 0.0007   | 0.001       |
| 16   | 3    | 13   | 17    | 2     | 14    | 1153.0907 | 1153.0913  | -0.0006  | 0.001       |
| 18   | 3    | 17   | 17    | 2     | 16    | 1497.5296 | 1497.5352  | -0.0056  | 0.002       |
| 18   | 3    | 15   | 17    | 2     | 14    | 1497.5296 | 1497.5295  | 0.0001   | 0.001       |
| 18   | 3    | 16   | 17    | 2     | 15    | 1497.5296 | 1497.5326  | -0.0030  | 0.002       |
| 18   | 3    | 18   | 17    | 2     | 17    | 1497.5440 | 1497.5374  | 0.0066   | 1           |
| 18   | 3    | 19   | 17    | 2     | 18    | 1497.5440 | 1497.5390  | 0.0050   | 1           |
| 18   | 3    | 20   | 17    | 2     | 19    | 1497.5440 | 1497.5403  | 0.0037   | 0.003       |
| 18   | 3    | 21   | 17    | 2     | 20    | 1497.5440 | 1497.5412  | 0.0028   | 0.002       |
| 17   | 3    | 20   | 18    | 2     | 21    | 1137.5515 | 1137.5520  | -0.0005  | 0.001       |
| 17   | 3    | 19   | 18    | 2     | 20    | 1137.5942 | 1137.5951  | -0.0009  | 0.001       |
| 17   | 3    | 18   | 18    | 2     | 19    | 1137.6367 | 1137.6378  | -0.0011  | 0.001       |
| 17   | 3    | 17   | 18    | 2     | 18    | 1137.6818 | 1137.6799  | 0.0019   | 0.001       |
| 17   | 3    | 16   | 18    | 2     | 17    | 1137.7226 | 1137.7213  | 0.0013   | 0.001       |
| 17   | 3    | 15   | 18    | 2     | 16    | 1137.7627 | 1137.7619  | 0.0008   | 0.001       |
| 17   | 3    | 14   | 18    | 2     | 15    | 1137.8036 | 1137.8015  | 0.0021   | 0.001       |
| 19   | 3    | 18   | 18    | 2     | 17    | 1500.3252 | 1500.3248  | 0.0004   | 0.001       |
| 19   | 3    | 19   | 18    | 2     | 18    | 1500.3252 | 1500.3249  | 0.0004   | 0.002       |
| 19   | 3    | 20   | 18    | 2     | 19    | 1500.3252 | 1500.3244  | 0.0008   | 0.001       |
| 19   | 3    | 21   | 18    | 2     | 20    | 1500.3252 | 1500.3236  | 0.0017   | 0.001       |
| 19   | 3    | 22   | 18    | 2     | 21    | 1500.3252 | 1500.3223  | 0.0029   | 0.001       |
| 19   | 3    | 16   | 18    | 2     | 15    | 1500.3252 | 1500.3233  | 0.0019   | 0.001       |
| 19   | 3    | 17   | 18    | 2     | 16    | 1500.3252 | 1500.3243  | 0.0009   | 0.001       |

| <i>N'</i> | <i>v'</i> | <i>J'</i> | <i>N''</i> | <i>v''</i> | <i>J''</i> | Observed  | Calculated | Obs-Calc | Uncertainty |
|-----------|-----------|-----------|------------|------------|------------|-----------|------------|----------|-------------|
| 20        | 3         | 19        | 19         | 2          | 18         | 1502.6154 | 1502.6240  | -0.0086  | 1           |
| 20        | 3         | 20        | 19         | 2          | 19         | 1502.6154 | 1502.6218  | -0.0064  | 0.003       |
| 20        | 3         | 21        | 19         | 2          | 20         | 1502.6154 | 1502.6192  | -0.0038  | 0.003       |
| 20        | 3         | 22        | 19         | 2          | 21         | 1502.6154 | 1502.6161  | -0.0007  | 0.001       |
| 20        | 3         | 23        | 19         | 2          | 22         | 1502.6154 | 1502.6127  | 0.0027   | 0.003       |
| 20        | 3         | 17        | 19         | 2          | 16         | 1502.6154 | 1502.6268  | -0.0114  | 0.1         |
| 20        | 3         | 18        | 19         | 2          | 17         | 1502.6154 | 1502.6257  | -0.0103  | 1           |
| 21        | 3         | 20        | 20         | 2          | 19         | 1504.4007 | 1504.4248  | -0.0241  | 1           |
| 21        | 3         | 21        | 20         | 2          | 20         | 1504.4007 | 1504.4204  | -0.0197  | 0.1         |
| 21        | 3         | 22        | 20         | 2          | 21         | 1504.4007 | 1504.4155  | -0.0148  | 1           |
| 21        | 3         | 23        | 20         | 2          | 22         | 1504.4007 | 1504.4101  | -0.0094  | 1           |
| 21        | 3         | 24        | 20         | 2          | 23         | 1504.4007 | 1504.4044  | -0.0037  | 0.003       |
| 21        | 3         | 18        | 20         | 2          | 17         | 1504.4007 | 1504.4321  | -0.0314  | 1           |
| 21        | 3         | 19        | 20         | 2          | 18         | 1504.4007 | 1504.4288  | -0.0281  | 1           |
| 22        | 3         | 19        | 21         | 2          | 18         | 1505.6792 | 1505.7316  | -0.0524  | 1           |
| 22        | 3         | 20        | 21         | 2          | 19         | 1505.6792 | 1505.7259  | -0.0467  | 1           |
| 22        | 3         | 21        | 21         | 2          | 20         | 1505.6965 | 1505.7196  | -0.0231  | 1           |
| 22        | 3         | 22        | 21         | 2          | 21         | 1505.6965 | 1505.7128  | -0.0163  | 1           |
| 22        | 3         | 23        | 21         | 2          | 22         | 1505.6965 | 1505.7055  | -0.0090  | 1           |
| 22        | 3         | 24        | 21         | 2          | 23         | 1505.6965 | 1505.6979  | -0.0014  | 0.001       |
| 22        | 3         | 25        | 21         | 2          | 24         | 1505.6965 | 1505.6898  | 0.0067   | 1           |

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|   |   |   |   |   |   |           |           |         |       |
|---|---|---|---|---|---|-----------|-----------|---------|-------|
| 1 | 1 | 4 | 2 | 0 | 5 | 1467.8086 | 1467.8115 | -0.0029 | 0.001 |
| 1 | 1 | 3 | 2 | 0 | 4 | 1467.8456 | 1467.8408 | 0.0048  | 0.004 |
| 1 | 1 | 2 | 2 | 0 | 3 | 1467.9094 | 1467.9151 | -0.0057 | 0.004 |
| 2 | 1 | 5 | 3 | 0 | 6 | 1455.9754 | 1455.9773 | -0.0019 | 0.001 |
| 2 | 1 | 4 | 3 | 0 | 5 | 1456.0095 | 1456.0091 | 0.0004  | 0.001 |
| 3 | 1 | 6 | 4 | 0 | 7 | 1443.8375 | 1443.8414 | -0.0039 | 0.001 |
| 3 | 1 | 5 | 4 | 0 | 6 | 1443.8720 | 1443.8748 | -0.0028 | 0.001 |
| 3 | 1 | 4 | 4 | 0 | 5 | 1443.9126 | 1443.9128 | -0.0002 | 0.001 |
| 3 | 1 | 3 | 4 | 0 | 4 | 1443.9517 | 1443.9517 | 0.0000  | 0.001 |
| 3 | 1 | 2 | 4 | 0 | 3 | 1443.9895 | 1443.9887 | 0.0008  | 0.001 |
| 3 | 1 | 1 | 4 | 0 | 2 | 1444.0233 | 1444.0222 | 0.0012  | 0.001 |
| 4 | 1 | 7 | 5 | 0 | 8 | 1431.4098 | 1431.4117 | -0.0019 | 0.001 |
| 4 | 1 | 6 | 5 | 0 | 7 | 1431.4450 | 1431.4462 | -0.0012 | 0.001 |
| 4 | 1 | 5 | 5 | 0 | 6 | 1431.4831 | 1431.4833 | -0.0002 | 0.001 |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 4    | 1    | 4    | 5     | 0     | 5     | 1431.5221 | 1431.5211  | 0.0011   | 0.001       |
| 4    | 1    | 3    | 5     | 0     | 4     | 1431.5581 | 1431.5576  | 0.0005   | 0.001       |
| 4    | 1    | 2    | 5     | 0     | 3     | 1431.5931 | 1431.5920  | 0.0011   | 0.001       |
| 4    | 1    | 1    | 5     | 0     | 2     | 1431.6244 | 1431.6234  | 0.0011   | 0.001       |
| 5    | 1    | 8    | 6     | 0     | 9     | 1418.6955 | 1418.6955  | 0.0000   | 0.001       |
| 5    | 1    | 7    | 6     | 0     | 8     | 1418.7303 | 1418.7310  | -0.0007  | 0.001       |
| 6    | 1    | 9    | 7     | 0     | 10    | 1405.6994 | 1405.7003  | -0.0009  | 0.001       |
| 6    | 1    | 8    | 7     | 0     | 9     | 1405.7353 | 1405.7366  | -0.0013  | 0.001       |
| 6    | 1    | 7    | 7     | 0     | 8     | 1405.7729 | 1405.7740  | -0.0011  | 0.001       |
| 6    | 1    | 6    | 7     | 0     | 7     | 1405.8107 | 1405.8115  | -0.0008  | 0.001       |
| 6    | 1    | 5    | 7     | 0     | 6     | 1405.8475 | 1405.8484  | -0.0009  | 0.001       |
| 6    | 1    | 4    | 7     | 0     | 5     | 1405.8841 | 1405.8840  | 0.0001   | 0.001       |
| 6    | 1    | 3    | 7     | 0     | 4     | 1405.9167 | 1405.9178  | -0.0011  | 0.001       |
| 7    | 1    | 10   | 8     | 0     | 11    | 1392.4321 | 1392.4333  | -0.0012  | 0.001       |
| 7    | 1    | 9    | 8     | 0     | 10    | 1392.4701 | 1392.4702  | -0.0001  | 0.001       |
| 7    | 1    | 8    | 8     | 0     | 9     | 1392.5072 | 1392.5080  | -0.0008  | 0.001       |
| 7    | 1    | 7    | 8     | 0     | 8     | 1392.5457 | 1392.5458  | -0.0001  | 0.001       |
| 7    | 1    | 6    | 8     | 0     | 7     | 1392.5816 | 1392.5831  | -0.0015  | 0.001       |
| 7    | 1    | 5    | 8     | 0     | 6     | 1392.6184 | 1392.6192  | -0.0008  | 0.001       |
| 7    | 1    | 4    | 8     | 0     | 5     | 1392.6532 | 1392.6538  | -0.0006  | 0.001       |
| 8    | 1    | 11   | 9     | 0     | 12    | 1378.9013 | 1378.9015  | -0.0002  | 0.001       |
| 8    | 1    | 10   | 9     | 0     | 11    | 1378.9390 | 1378.9392  | -0.0002  | 0.001       |
| 8    | 1    | 9    | 9     | 0     | 10    | 1378.9768 | 1378.9774  | -0.0006  | 0.001       |
| 8    | 1    | 8    | 9     | 0     | 9     | 1379.0148 | 1379.0155  | -0.0007  | 0.001       |
| 8    | 1    | 7    | 9     | 0     | 8     | 1379.0524 | 1379.0531  | -0.0007  | 0.001       |
| 8    | 1    | 6    | 9     | 0     | 7     | 1379.0903 | 1379.0898  | 0.0006   | 0.001       |
| 8    | 1    | 5    | 9     | 0     | 6     | 1379.1244 | 1379.1251  | -0.0007  | 0.001       |
| 9    | 1    | 12   | 10    | 0     | 13    | 1365.1130 | 1365.1122  | 0.0009   | 0.001       |
| 9    | 1    | 11   | 10    | 0     | 12    | 1365.1512 | 1365.1504  | 0.0008   | 0.001       |
| 9    | 1    | 10   | 10    | 0     | 11    | 1365.1904 | 1365.1891  | 0.0013   | 0.001       |
| 9    | 1    | 9    | 10    | 0     | 10    | 1365.2277 | 1365.2276  | 0.0001   | 0.001       |
| 9    | 1    | 8    | 10    | 0     | 9     | 1365.2681 | 1365.2656  | 0.0025   | 0.001       |
| 9    | 1    | 7    | 10    | 0     | 8     | 1365.3037 | 1365.3027  | 0.0010   | 0.001       |
| 9    | 1    | 6    | 10    | 0     | 7     | 1365.3414 | 1365.3387  | 0.0027   | 0.001       |
| 10   | 1    | 13   | 11    | 0     | 14    | 1351.0738 | 1351.0722  | 0.0016   | 0.001       |
| 10   | 1    | 12   | 11    | 0     | 13    | 1351.1130 | 1351.1110  | 0.0020   | 0.001       |
| 10   | 1    | 11   | 11    | 0     | 12    | 1351.1514 | 1351.1501  | 0.0013   | 0.001       |
| 10   | 1    | 10   | 11    | 0     | 11    | 1351.1907 | 1351.1890  | 0.0017   | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 10   | 1    | 9    | 11    | 0     | 10    | 1351.2284 | 1351.2274  | 0.0010   | 0.001       |
| 10   | 1    | 8    | 11    | 0     | 9     | 1351.2656 | 1351.2650  | 0.0006   | 0.001       |
| 10   | 1    | 7    | 11    | 0     | 8     | 1351.3027 | 1351.3015  | 0.0012   | 0.001       |
| 16   | 1    | 19   | 17    | 0     | 20    | 1261.9857 | 1261.9451  | 0.0406   | 1           |
| 16   | 1    | 18   | 17    | 0     | 19    | 1262.0271 | 1261.9869  | 0.0402   | 1           |
| 16   | 1    | 17   | 17    | 0     | 18    | 1262.0679 | 1262.0284  | 0.0395   | 1           |
| 16   | 1    | 16   | 17    | 0     | 17    | 1262.1085 | 1262.0695  | 0.0390   | 1           |
| 16   | 1    | 15   | 17    | 0     | 16    | 1262.1483 | 1262.1100  | 0.0383   | 1           |
| 16   | 1    | 14   | 17    | 0     | 15    | 1262.1874 | 1262.1499  | 0.0375   | 1           |
| 16   | 1    | 13   | 17    | 0     | 14    | 1262.2289 | 1262.1890  | 0.0399   | 1           |
| 12   | 2    | 9    | 11    | 1     | 8     | 1535.5121 | 1535.5133  | -0.0012  | 0.001       |
| 12   | 2    | 10   | 11    | 1     | 9     | 1535.5289 | 1535.5294  | -0.0005  | 0.001       |
| 12   | 2    | 11   | 11    | 1     | 10    | 1535.5447 | 1535.5452  | -0.0005  | 0.001       |
| 12   | 2    | 12   | 11    | 1     | 11    | 1535.5598 | 1535.5606  | -0.0008  | 0.001       |
| 12   | 2    | 13   | 11    | 1     | 12    | 1535.5747 | 1535.5757  | -0.0010  | 0.001       |
| 12   | 2    | 14   | 11    | 1     | 13    | 1535.5898 | 1535.5905  | -0.0007  | 0.001       |
| 12   | 2    | 15   | 11    | 1     | 14    | 1535.6031 | 1535.6048  | -0.0017  | 0.001       |
| 13   | 2    | 16   | 14    | 1     | 17    | 1253.4648 | 1253.4652  | -0.0004  | 0.001       |
| 13   | 2    | 15   | 14    | 1     | 16    | 1253.5054 | 1253.5059  | -0.0005  | 0.001       |
| 13   | 2    | 14   | 14    | 1     | 15    | 1253.5450 | 1253.5464  | -0.0014  | 0.001       |
| 13   | 2    | 13   | 14    | 1     | 14    | 1253.5861 | 1253.5866  | -0.0005  | 0.001       |
| 13   | 2    | 12   | 14    | 1     | 13    | 1253.6255 | 1253.6262  | -0.0007  | 0.001       |
| 13   | 2    | 11   | 14    | 1     | 12    | 1253.6629 | 1253.6651  | -0.0022  | 0.001       |
| 13   | 2    | 10   | 14    | 1     | 11    | 1253.7035 | 1253.7029  | 0.0006   | 0.001       |
| 15   | 2    | 12   | 14    | 1     | 11    | 1552.3491 | 1552.3501  | -0.0010  | 0.001       |
| 15   | 2    | 13   | 14    | 1     | 12    | 1552.3607 | 1552.3613  | -0.0006  | 0.001       |
| 15   | 2    | 14   | 14    | 1     | 13    | 1552.3719 | 1552.3721  | -0.0002  | 0.001       |
| 15   | 2    | 15   | 14    | 1     | 14    | 1552.3819 | 1552.3824  | -0.0005  | 0.001       |
| 15   | 2    | 16   | 14    | 1     | 15    | 1552.3922 | 1552.3925  | -0.0003  | 0.001       |
| 15   | 2    | 17   | 14    | 1     | 16    | 1552.4025 | 1552.4022  | 0.0003   | 0.001       |
| 15   | 2    | 18   | 14    | 1     | 17    | 1552.4117 | 1552.4116  | 0.0001   | 0.001       |
| 14   | 2    | 17   | 15    | 1     | 18    | 1238.7118 | 1238.7121  | -0.0003  | 0.001       |
| 14   | 2    | 16   | 15    | 1     | 17    | 1238.7534 | 1238.7533  | 0.0001   | 0.001       |
| 14   | 2    | 15   | 15    | 1     | 16    | 1238.7941 | 1238.7943  | -0.0002  | 0.001       |
| 14   | 2    | 14   | 15    | 1     | 15    | 1238.8351 | 1238.8350  | 0.0001   | 0.001       |
| 14   | 2    | 13   | 15    | 1     | 14    | 1238.8749 | 1238.8750  | -0.0001  | 0.001       |
| 14   | 2    | 12   | 15    | 1     | 13    | 1238.9138 | 1238.9142  | -0.0004  | 0.001       |
| 14   | 2    | 11   | 15    | 1     | 12    | 1238.9525 | 1238.9525  | 0.0000   | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 5    | 3    | 3    | 4     | 2     | 2     | 1420.3590 | 1420.3595  | -0.0005  | 0.001       |
| 5    | 3    | 4    | 4     | 2     | 3     | 1420.3850 | 1420.3836  | 0.0014   | 0.001       |
| 5    | 3    | 5    | 4     | 2     | 4     | 1420.4086 | 1420.4084  | 0.0002   | 0.001       |
| 5    | 3    | 6    | 4     | 2     | 5     | 1420.4334 | 1420.4334  | 0.0000   | 0.001       |
| 5    | 3    | 7    | 4     | 2     | 6     | 1420.4587 | 1420.4575  | 0.0012   | 0.001       |
| 5    | 3    | 8    | 4     | 2     | 7     | 1420.4808 | 1420.4791  | 0.0017   | 0.001       |
| 6    | 3    | 3    | 5     | 2     | 2     | 1428.7556 | 1428.7564  | -0.0008  | 0.001       |
| 6    | 3    | 4    | 5     | 2     | 3     | 1428.7782 | 1428.7787  | -0.0005  | 0.001       |
| 6    | 3    | 5    | 5     | 2     | 4     | 1428.8009 | 1428.8014  | -0.0005  | 0.001       |
| 6    | 3    | 6    | 5     | 2     | 5     | 1428.8234 | 1428.8245  | -0.0011  | 0.001       |
| 6    | 3    | 7    | 5     | 2     | 6     | 1428.8475 | 1428.8475  | 0.0000   | 0.001       |
| 6    | 3    | 8    | 5     | 2     | 7     | 1428.8693 | 1428.8697  | -0.0004  | 0.001       |
| 6    | 3    | 9    | 5     | 2     | 8     | 1428.8901 | 1428.8902  | -0.0001  | 0.001       |
| 6    | 3    | 9    | 7     | 2     | 10    | 1292.1273 | 1292.1268  | 0.0005   | 0.001       |
| 6    | 3    | 8    | 7     | 2     | 9     | 1292.1620 | 1292.1626  | -0.0006  | 0.001       |
| 6    | 3    | 7    | 7     | 2     | 8     | 1292.1986 | 1292.1995  | -0.0009  | 0.001       |
| 6    | 3    | 6    | 7     | 2     | 7     | 1292.2358 | 1292.2365  | -0.0007  | 0.001       |
| 6    | 3    | 5    | 7     | 2     | 6     | 1292.2717 | 1292.2726  | -0.0009  | 0.001       |
| 6    | 3    | 4    | 7     | 2     | 5     | 1292.3069 | 1292.3072  | -0.0003  | 0.001       |
| 7    | 3    | 10   | 8     | 2     | 11    | 1279.3979 | 1279.3978  | 0.0001   | 0.001       |
| 7    | 3    | 9    | 8     | 2     | 10    | 1279.4342 | 1279.4345  | -0.0003  | 0.001       |
| 7    | 3    | 8    | 8     | 2     | 9     | 1279.4711 | 1279.4719  | -0.0008  | 0.001       |
| 7    | 3    | 7    | 8     | 2     | 8     | 1279.5089 | 1279.5092  | -0.0003  | 0.001       |
| 7    | 3    | 6    | 8     | 2     | 7     | 1279.5461 | 1279.5458  | 0.0003   | 0.001       |
| 7    | 3    | 5    | 8     | 2     | 6     | 1279.5817 | 1279.5811  | 0.0006   | 0.001       |
| 7    | 3    | 4    | 8     | 2     | 5     | 1279.6148 | 1279.6146  | 0.0002   | 0.001       |
| 9    | 3    | 12   | 10    | 2     | 13    | 1253.0974 | 1253.0985  | -0.0011  | 0.001       |
| 9    | 3    | 11   | 10    | 2     | 12    | 1253.1356 | 1253.1367  | -0.0011  | 0.001       |
| 9    | 3    | 10   | 10    | 2     | 11    | 1253.1757 | 1253.1752  | 0.0005   | 0.001       |
| 9    | 3    | 9    | 10    | 2     | 10    | 1253.2121 | 1253.2135  | -0.0014  | 0.001       |
| 9    | 3    | 8    | 10    | 2     | 9     | 1253.2494 | 1253.2511  | -0.0017  | 0.001       |
| 9    | 3    | 7    | 10    | 2     | 8     | 1253.2863 | 1253.2876  | -0.0013  | 0.001       |
| 9    | 3    | 6    | 10    | 2     | 7     | 1253.3219 | 1253.3228  | -0.0009  | 0.001       |
| 10   | 3    | 13   | 11    | 2     | 14    | 1239.5417 | 1239.5407  | 0.0010   | 0.001       |
| 10   | 3    | 12   | 11    | 2     | 13    | 1239.5803 | 1239.5797  | 0.0007   | 0.001       |
| 10   | 3    | 11   | 11    | 2     | 12    | 1239.6193 | 1239.6187  | 0.0006   | 0.001       |
| 10   | 3    | 10   | 11    | 2     | 11    | 1239.6576 | 1239.6575  | 0.0001   | 0.001       |
| 10   | 3    | 9    | 11    | 2     | 10    | 1239.6954 | 1239.6956  | -0.0002  | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 10   | 3    | 8    | 11    | 2     | 9     | 1239.7330 | 1239.7327  | 0.0003   | 0.001       |
| 10   | 3    | 7    | 11    | 2     | 8     | 1239.7694 | 1239.7686  | 0.0008   | 0.001       |
| 19   | 3    | 19   | 18    | 2     | 18    | 1500.3247 | 1500.3249  | -0.0002  | 0.001       |

## A.2 Line list for MnD

Table A.2: Line list for MnD.

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 2    | 1    | 5    | 3     | 0     | 6     | 1058.3052 | 1058.3104  | -0.00519 | 0.005       |
| 2    | 1    | 4    | 3     | 0     | 5     | 1058.33   | 1058.3263  | 0.00375  | 0.005       |
| 2    | 1    | 3    | 3     | 0     | 4     | 1058.3519 | 1058.3471  | 0.00481  | 0.005       |
| 2    | 1    | 2    | 3     | 0     | 3     | 1058.3678 | 1058.3688  | -0.00095 | 0.001       |
| 2    | 1    | 1    | 3     | 0     | 2     | 1058.3843 | 1058.3884  | -0.00413 | 0.004       |
| 2    | 1    | 5    | 1     | 0     | 4     | 1087.1005 | 1087.0944  | 0.00607  | 0.01        |
| 3    | 1    | 6    | 4     | 0     | 7     | 1052.2299 | 1052.2317  | -0.00177 | 0.003       |
| 3    | 1    | 5    | 4     | 0     | 6     | 1052.2485 | 1052.2482  | 0.00032  | 0.003       |
| 3    | 1    | 4    | 4     | 0     | 5     | 1052.2657 | 1052.2671  | -0.00135 | 0.003       |
| 3    | 1    | 3    | 4     | 0     | 4     | 1052.2894 | 1052.2865  | 0.00294  | 0.003       |
| 3    | 1    | 2    | 4     | 0     | 3     | 1052.3067 | 1052.3051  | 0.00162  | 0.003       |
| 3    | 1    | 1    | 4     | 0     | 2     | 1052.3193 | 1052.3221  | -0.00276 | 0.003       |
| 3    | 1    | 0    | 4     | 0     | 1     | 1052.3323 | 1052.337   | -0.00473 | 0.1         |
| 3    | 1    | 2    | 2     | 0     | 1     | 1092.4103 | 1092.4078  | 0.00254  | 0.003       |
| 3    | 1    | 3    | 2     | 0     | 2     | 1092.4218 | 1092.4248  | -0.00298 | 0.003       |
| 3    | 1    | 4    | 2     | 0     | 3     | 1092.4344 | 1092.4433  | -0.00893 | 1           |
| 3    | 1    | 5    | 2     | 0     | 4     | 1092.4617 | 1092.4612  | 0.00047  | 0.001       |
| 3    | 1    | 6    | 2     | 0     | 5     | 1092.4774 | 1092.4752  | 0.0022   | 0.003       |
| 4    | 1    | 7    | 5     | 0     | 8     | 1046.0428 | 1046.0435  | -0.00074 | 0.003       |
| 4    | 1    | 6    | 5     | 0     | 7     | 1046.0587 | 1046.0605  | -0.00181 | 0.003       |
| 4    | 1    | 5    | 5     | 0     | 6     | 1046.0801 | 1046.0789  | 0.00119  | 0.003       |
| 4    | 1    | 4    | 5     | 0     | 5     | 1046.1003 | 1046.0977  | 0.00262  | 0.003       |
| 4    | 1    | 3    | 5     | 0     | 4     | 1046.1187 | 1046.116   | 0.00267  | 0.003       |
| 4    | 1    | 2    | 5     | 0     | 3     | 1046.134  | 1046.1334  | 0.0006   | 0.003       |
| 4    | 1    | 1    | 5     | 0     | 2     | 1046.1468 | 1046.1495  | -0.00266 | 0.003       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 4    | 1    | 1    | 3     | 0     | 0     | 1097.6434 | 1097.6446  | -0.0012  | 0.001       |
| 4    | 1    | 2    | 3     | 0     | 1     | 1097.6562 | 1097.658   | -0.00184 | 0.001       |
| 4    | 1    | 3    | 3     | 0     | 2     | 1097.6703 | 1097.6726  | -0.0023  | 0.003       |
| 4    | 1    | 4    | 3     | 0     | 3     | 1097.6829 | 1097.6882  | -0.00526 | 0.1         |
| 4    | 1    | 5    | 3     | 0     | 4     | 1097.7013 | 1097.7042  | -0.00288 | 0.003       |
| 4    | 1    | 6    | 3     | 0     | 5     | 1097.7195 | 1097.7198  | -0.00028 | 0.003       |
| 4    | 1    | 7    | 3     | 0     | 6     | 1097.734  | 1097.7337  | 0.00033  | 0.003       |
| 5    | 1    | 8    | 6     | 0     | 9     | 1039.7474 | 1039.748   | -0.00058 | 0.001       |
| 5    | 1    | 6    | 6     | 0     | 7     | 1039.7841 | 1039.7837  | 0.00045  | 0.001       |
| 5    | 1    | 5    | 6     | 0     | 6     | 1039.8011 | 1039.8022  | -0.00114 | 0.001       |
| 5    | 1    | 4    | 6     | 0     | 5     | 1039.8211 | 1039.8206  | 0.00054  | 0.001       |
| 5    | 1    | 3    | 6     | 0     | 4     | 1039.8384 | 1039.8382  | 0.00018  | 0.001       |
| 5    | 1    | 2    | 6     | 0     | 3     | 1039.854  | 1039.8549  | -0.00092 | 0.001       |
| 5    | 1    | 2    | 4     | 0     | 1     | 1102.7833 | 1102.7817  | 0.0016   | 0.003       |
| 5    | 1    | 3    | 4     | 0     | 2     | 1102.7927 | 1102.7954  | -0.00274 | 0.003       |
| 5    | 1    | 4    | 4     | 0     | 3     | 1102.8069 | 1102.8098  | -0.00285 | 0.003       |
| 5    | 1    | 5    | 4     | 0     | 4     | 1102.8216 | 1102.8245  | -0.00292 | 0.003       |
| 5    | 1    | 6    | 4     | 0     | 5     | 1102.837  | 1102.8395  | -0.00245 | 0.003       |
| 5    | 1    | 7    | 4     | 0     | 6     | 1102.8553 | 1102.8541  | 0.00123  | 0.003       |
| 5    | 1    | 8    | 4     | 0     | 7     | 1102.8699 | 1102.8677  | 0.00218  | 0.003       |
| 6    | 1    | 9    | 7     | 0     | 10    | 1033.3474 | 1033.347   | 0.00044  | 0.003       |
| 6    | 1    | 8    | 7     | 0     | 9     | 1033.3643 | 1033.3646  | -0.00033 | 0.003       |
| 6    | 1    | 7    | 7     | 0     | 8     | 1033.383  | 1033.383   | 0        | 0.003       |
| 6    | 1    | 6    | 7     | 0     | 7     | 1033.401  | 1033.4016  | -0.00059 | 0.003       |
| 6    | 1    | 5    | 7     | 0     | 6     | 1033.4201 | 1033.42    | 0.00011  | 0.003       |
| 6    | 1    | 4    | 7     | 0     | 5     | 1033.4368 | 1033.4379  | -0.00109 | 0.003       |
| 6    | 1    | 3    | 7     | 0     | 4     | 1033.4545 | 1033.4551  | -0.00056 | 0.003       |
| 6    | 1    | 3    | 5     | 0     | 2     | 1107.7913 | 1107.7921  | -0.00075 | 0.002       |
| 6    | 1    | 4    | 5     | 0     | 3     | 1107.8057 | 1107.8057  | -0.00001 | 0.002       |
| 6    | 1    | 5    | 5     | 0     | 4     | 1107.8181 | 1107.8197  | -0.00157 | 0.002       |
| 6    | 1    | 6    | 5     | 0     | 5     | 1107.8329 | 1107.8339  | -0.00095 | 0.002       |
| 6    | 1    | 7    | 5     | 0     | 6     | 1107.8484 | 1107.8481  | 0.00033  | 0.002       |
| 6    | 1    | 8    | 5     | 0     | 7     | 1107.8628 | 1107.8621  | 0.00075  | 0.001       |
| 6    | 1    | 9    | 5     | 0     | 8     | 1107.8768 | 1107.8754  | 0.0014   | 0.002       |
| 7    | 1    | 10   | 8     | 0     | 11    | 1026.8427 | 1026.8424  | 0.00031  | 0.002       |
| 7    | 1    | 9    | 8     | 0     | 10    | 1026.8604 | 1026.8603  | 0.00006  | 0.002       |
| 7    | 1    | 8    | 8     | 0     | 9     | 1026.8795 | 1026.8788  | 0.00067  | 0.002       |
| 7    | 1    | 7    | 8     | 0     | 8     | 1026.898  | 1026.8975  | 0.00051  | 0.002       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 7    | 1    | 6    | 8     | 0     | 7     | 1026.9168 | 1026.916   | 0.00079  | 0.002       |
| 7    | 1    | 5    | 8     | 0     | 6     | 1026.9328 | 1026.9341  | -0.00134 | 0.002       |
| 7    | 1    | 4    | 8     | 0     | 5     | 1026.9499 | 1026.9517  | -0.00178 | 0.002       |
| 7    | 1    | 4    | 6     | 0     | 3     | 1112.6743 | 1112.674   | 0.00028  | 0.001       |
| 7    | 1    | 5    | 6     | 0     | 4     | 1112.6865 | 1112.6874  | -0.00094 | 0.001       |
| 7    | 1    | 6    | 6     | 0     | 5     | 1112.7006 | 1112.701   | -0.00042 | 0.001       |
| 7    | 1    | 7    | 6     | 0     | 6     | 1112.7139 | 1112.7147  | -0.00079 | 0.001       |
| 7    | 1    | 8    | 6     | 0     | 7     | 1112.7275 | 1112.7283  | -0.00084 | 0.001       |
| 7    | 1    | 9    | 6     | 0     | 8     | 1112.7418 | 1112.7418  | 0.00002  | 0.001       |
| 7    | 1    | 10   | 6     | 0     | 9     | 1112.7553 | 1112.7548  | 0.00052  | 0.001       |
| 8    | 1    | 11   | 9     | 0     | 12    | 1020.2352 | 1020.2362  | -0.00097 | 0.002       |
| 8    | 1    | 10   | 9     | 0     | 11    | 1020.2544 | 1020.2544  | 0.00003  | 0.002       |
| 8    | 1    | 9    | 9     | 0     | 10    | 1020.2731 | 1020.273   | 0.00009  | 0.002       |
| 8    | 1    | 8    | 9     | 0     | 9     | 1020.2926 | 1020.2918  | 0.00082  | 0.002       |
| 8    | 1    | 7    | 9     | 0     | 8     | 1020.3111 | 1020.3104  | 0.00056  | 0.002       |
| 8    | 1    | 6    | 9     | 0     | 7     | 1020.329  | 1020.3288  | 0.00022  | 0.001       |
| 8    | 1    | 5    | 9     | 0     | 6     | 1020.3466 | 1020.3466  | -0.00004 | 0.001       |
| 8    | 1    | 5    | 7     | 0     | 4     | 1117.427  | 1117.4258  | 0.0012   | 0.001       |
| 8    | 1    | 6    | 7     | 0     | 5     | 1117.4384 | 1117.4389  | -0.0005  | 0.001       |
| 8    | 1    | 7    | 7     | 0     | 6     | 1117.4521 | 1117.4521  | 0.00002  | 0.001       |
| 8    | 1    | 8    | 7     | 0     | 7     | 1117.465  | 1117.4653  | -0.00028 | 0.001       |
| 8    | 1    | 9    | 7     | 0     | 8     | 1117.4779 | 1117.4784  | -0.00052 | 0.001       |
| 8    | 1    | 10   | 7     | 0     | 9     | 1117.4918 | 1117.4914  | 0.00043  | 0.001       |
| 8    | 1    | 11   | 7     | 0     | 10    | 1117.5049 | 1117.504   | 0.00091  | 0.001       |
| 9    | 1    | 12   | 10    | 0     | 13    | 1013.5313 | 1013.5302  | 0.00111  | 0.002       |
| 9    | 1    | 11   | 10    | 0     | 12    | 1013.5493 | 1013.5486  | 0.00067  | 0.002       |
| 9    | 1    | 10   | 10    | 0     | 11    | 1013.5686 | 1013.5674  | 0.00118  | 0.002       |
| 9    | 1    | 9    | 10    | 0     | 10    | 1013.5864 | 1013.5863  | 0.00008  | 0.002       |
| 9    | 1    | 8    | 10    | 0     | 9     | 1013.6045 | 1013.6051  | -0.00063 | 0.002       |
| 9    | 1    | 7    | 10    | 0     | 8     | 1013.6231 | 1013.6237  | -0.00058 | 0.002       |
| 9    | 1    | 6    | 10    | 0     | 7     | 1013.6407 | 1013.6418  | -0.00111 | 0.002       |
| 9    | 1    | 6    | 8     | 0     | 5     | 1122.0448 | 1122.0456  | -0.00076 | 0.002       |
| 9    | 1    | 7    | 8     | 0     | 6     | 1122.0575 | 1122.0583  | -0.00081 | 0.002       |
| 9    | 1    | 8    | 8     | 0     | 7     | 1122.0704 | 1122.0711  | -0.00067 | 0.002       |
| 9    | 1    | 9    | 8     | 0     | 8     | 1122.0831 | 1122.0838  | -0.00071 | 0.002       |
| 9    | 1    | 10   | 8     | 0     | 9     | 1122.0965 | 1122.0965  | 0.00004  | 0.002       |
| 9    | 1    | 11   | 8     | 0     | 10    | 1122.1108 | 1122.1089  | 0.00186  | 0.002       |
| 9    | 1    | 12   | 8     | 0     | 11    | 1122.1231 | 1122.1212  | 0.00194  | 0.002       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 10   | 1    | 13   | 11    | 0     | 14    | 1006.7269 | 1006.7263  | 0.00056  | 0.001       |
| 10   | 1    | 12   | 11    | 0     | 13    | 1006.7451 | 1006.745   | 0.00011  | 0.001       |
| 10   | 1    | 11   | 11    | 0     | 12    | 1006.7647 | 1006.7639  | 0.00076  | 0.001       |
| 10   | 1    | 10   | 11    | 0     | 11    | 1006.7835 | 1006.783   | 0.00052  | 0.001       |
| 10   | 1    | 9    | 11    | 0     | 10    | 1006.8021 | 1006.802   | 0.00015  | 0.001       |
| 10   | 1    | 8    | 11    | 0     | 9     | 1006.8207 | 1006.8207  | 0.00002  | 0.001       |
| 10   | 1    | 7    | 11    | 0     | 8     | 1006.8383 | 1006.8391  | -0.00077 | 0.001       |
| 10   | 1    | 7    | 9     | 0     | 6     | 1126.5351 | 1126.5315  | 0.00363  | 0.002       |
| 10   | 1    | 8    | 9     | 0     | 7     | 1126.5445 | 1126.5438  | 0.00066  | 0.001       |
| 10   | 1    | 9    | 9     | 0     | 8     | 1126.5575 | 1126.5562  | 0.00133  | 0.001       |
| 10   | 1    | 10   | 9     | 0     | 9     | 1126.5691 | 1126.5684  | 0.00066  | 0.001       |
| 10   | 1    | 11   | 9     | 0     | 10    | 1126.5814 | 1126.5806  | 0.00078  | 0.001       |
| 10   | 1    | 12   | 9     | 0     | 11    | 1126.5939 | 1126.5926  | 0.00126  | 0.001       |
| 10   | 1    | 13   | 9     | 0     | 12    | 1126.6064 | 1126.6044  | 0.00198  | 0.001       |
| 11   | 1    | 14   | 12    | 0     | 15    | 999.82742 | 999.82649  | 0.00093  | 0.002       |
| 11   | 1    | 13   | 12    | 0     | 14    | 999.84556 | 999.84534  | 0.00022  | 0.002       |
| 11   | 1    | 12   | 12    | 0     | 13    | 999.86446 | 999.86443  | 0.00003  | 0.002       |
| 11   | 1    | 11   | 12    | 0     | 12    | 999.88324 | 999.88362  | -0.00038 | 0.002       |
| 11   | 1    | 10   | 12    | 0     | 11    | 999.90242 | 999.90273  | -0.00031 | 0.002       |
| 11   | 1    | 9    | 12    | 0     | 10    | 999.9222  | 999.92165  | 0.00055  | 0.002       |
| 11   | 1    | 8    | 12    | 0     | 9     | 999.93968 | 999.94026  | -0.00058 | 0.002       |
| 11   | 1    | 8    | 10    | 0     | 7     | 1130.8794 | 1130.8817  | -0.00229 | 0.003       |
| 11   | 1    | 9    | 10    | 0     | 8     | 1130.8907 | 1130.8937  | -0.00295 | 0.003       |
| 11   | 1    | 10   | 10    | 0     | 9     | 1130.9033 | 1130.9055  | -0.00224 | 0.003       |
| 11   | 1    | 11   | 10    | 0     | 10    | 1130.9159 | 1130.9174  | -0.00145 | 0.003       |
| 11   | 1    | 12   | 10    | 0     | 11    | 1130.9284 | 1130.9291  | -0.00065 | 0.003       |
| 11   | 1    | 13   | 10    | 0     | 12    | 1130.9409 | 1130.9406  | 0.0003   | 0.003       |
| 11   | 1    | 14   | 10    | 0     | 13    | 1130.9534 | 1130.952   | 0.00145  | 0.003       |
| 12   | 1    | 15   | 13    | 0     | 16    | 992.83255 | 992.8325   | 0.00005  | 0.002       |
| 12   | 1    | 14   | 13    | 0     | 15    | 992.85059 | 992.85152  | -0.00093 | 0.002       |
| 12   | 1    | 13   | 13    | 0     | 14    | 992.87189 | 992.87076  | 0.00113  | 0.002       |
| 12   | 1    | 12   | 13    | 0     | 13    | 992.89081 | 992.89008  | 0.00073  | 0.002       |
| 12   | 1    | 11   | 13    | 0     | 12    | 992.90986 | 992.90935  | 0.00051  | 0.002       |
| 12   | 1    | 10   | 13    | 0     | 11    | 992.92851 | 992.92844  | 0.00007  | 0.001       |
| 12   | 1    | 9    | 13    | 0     | 10    | 992.9458  | 992.94725  | -0.00145 | 0.002       |
| 12   | 1    | 9    | 11    | 0     | 8     | 1135.0917 | 1135.0944  | -0.00269 | 0.002       |
| 12   | 1    | 10   | 11    | 0     | 9     | 1135.103  | 1135.1059  | -0.00292 | 0.002       |
| 12   | 1    | 11   | 11    | 0     | 10    | 1135.1157 | 1135.1174  | -0.00166 | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 12   | 1    | 12   | 11    | 0     | 11    | 1135.1284 | 1135.1287  | -0.0003  | 0.001       |
| 12   | 1    | 13   | 11    | 0     | 12    | 1135.1415 | 1135.1399  | 0.00158  | 0.001       |
| 12   | 1    | 14   | 11    | 0     | 13    | 1135.1543 | 1135.151   | 0.0033   | 0.002       |
| 12   | 1    | 15   | 11    | 0     | 14    | 1135.1645 | 1135.1619  | 0.00261  | 0.002       |
| 13   | 1    | 16   | 14    | 0     | 17    | 985.74577 | 985.74619  | -0.00042 | 0.001       |
| 13   | 1    | 15   | 14    | 0     | 16    | 985.76517 | 985.76538  | -0.00021 | 0.001       |
| 13   | 1    | 14   | 14    | 0     | 15    | 985.78601 | 985.78476  | 0.00125  | 0.001       |
| 13   | 1    | 13   | 14    | 0     | 14    | 985.80478 | 985.80421  | 0.00057  | 0.001       |
| 13   | 1    | 12   | 14    | 0     | 13    | 985.82351 | 985.82361  | -0.0001  | 0.001       |
| 13   | 1    | 11   | 14    | 0     | 12    | 985.84226 | 985.84287  | -0.00061 | 0.001       |
| 13   | 1    | 10   | 14    | 0     | 11    | 985.86059 | 985.86187  | -0.00128 | 0.001       |
| 13   | 1    | 10   | 12    | 0     | 9     | 1139.1669 | 1139.1678  | -0.00086 | 0.002       |
| 13   | 1    | 11   | 12    | 0     | 10    | 1139.1788 | 1139.1788  | -0.00004 | 0.002       |
| 13   | 1    | 12   | 12    | 0     | 11    | 1139.1922 | 1139.1898  | 0.00238  | 0.003       |
| 13   | 1    | 13   | 12    | 0     | 12    | 1139.2058 | 1139.2007  | 0.00512  | 0.01        |
| 13   | 1    | 14   | 12    | 0     | 13    | 1139.2192 | 1139.2114  | 0.00778  | 0.01        |
| 13   | 1    | 15   | 12    | 0     | 14    | 1139.2192 | 1139.222   | -0.00281 | 0.003       |
| 13   | 1    | 16   | 12    | 0     | 15    | 1139.2325 | 1139.2324  | 0.00006  | 0.002       |
| 14   | 1    | 17   | 15    | 0     | 18    | 978.56811 | 978.5694   | -0.00129 | 0.001       |
| 14   | 1    | 16   | 15    | 0     | 17    | 978.59026 | 978.58874  | 0.00152  | 0.001       |
| 14   | 1    | 15   | 15    | 0     | 16    | 978.60822 | 978.60825  | -0.00003 | 0.001       |
| 14   | 1    | 14   | 15    | 0     | 15    | 978.62755 | 978.62782  | -0.00027 | 0.001       |
| 14   | 1    | 13   | 15    | 0     | 14    | 978.64646 | 978.64736  | -0.0009  | 0.001       |
| 14   | 1    | 12   | 15    | 0     | 13    | 978.66682 | 978.66676  | 0.00006  | 0.001       |
| 14   | 1    | 11   | 15    | 0     | 12    | 978.68641 | 978.68594  | 0.00047  | 0.001       |
| 14   | 1    | 11   | 13    | 0     | 10    | 1143.1034 | 1143.1     | 0.00343  | 0.05        |
| 14   | 1    | 12   | 13    | 0     | 11    | 1143.1034 | 1143.1106  | -0.0072  | 0.05        |
| 14   | 1    | 13   | 13    | 0     | 12    | 1143.1186 | 1143.1211  | -0.0025  | 0.05        |
| 14   | 1    | 14   | 13    | 0     | 13    | 1143.133  | 1143.1315  | 0.00152  | 0.05        |
| 14   | 1    | 15   | 13    | 0     | 14    | 1143.1478 | 1143.1417  | 0.00608  | 0.05        |
| 14   | 1    | 16   | 13    | 0     | 15    | 1143.1478 | 1143.1518  | -0.00403 | 0.05        |
| 14   | 1    | 17   | 13    | 0     | 16    | 1143.1611 | 1143.1618  | -0.00067 | 0.05        |
| 15   | 1    | 18   | 16    | 0     | 19    | 971.30483 | 971.30393  | 0.0009   | 0.002       |
| 15   | 1    | 17   | 16    | 0     | 18    | 971.32298 | 971.3234   | -0.00042 | 0.002       |
| 15   | 1    | 16   | 16    | 0     | 17    | 971.34223 | 971.34303  | -0.0008  | 0.002       |
| 15   | 1    | 15   | 16    | 0     | 16    | 971.36504 | 971.36273  | 0.00231  | 0.002       |
| 15   | 1    | 14   | 16    | 0     | 15    | 971.38294 | 971.38239  | 0.00055  | 0.002       |
| 15   | 1    | 13   | 16    | 0     | 14    | 971.40263 | 971.40193  | 0.0007   | 0.002       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 15   | 1    | 12   | 16    | 0     | 13    | 971.42007 | 971.42127  | -0.0012  | 0.002       |
| 15   | 1    | 12   | 14    | 0     | 11    | 1146.887  | 1146.8892  | -0.00224 | 0.03        |
| 15   | 1    | 13   | 14    | 0     | 12    | 1146.898  | 1146.8994  | -0.00139 | 0.03        |
| 15   | 1    | 14   | 14    | 0     | 13    | 1146.9128 | 1146.9094  | 0.00339  | 0.03        |
| 15   | 1    | 15   | 14    | 0     | 14    | 1146.9128 | 1146.9193  | -0.00649 | 0.03        |
| 15   | 1    | 16   | 14    | 0     | 15    | 1146.928  | 1146.929   | -0.00104 | 0.03        |
| 15   | 1    | 17   | 14    | 0     | 16    | 1146.9438 | 1146.9386  | 0.00516  | 0.03        |
| 15   | 1    | 18   | 14    | 0     | 17    | 1146.9438 | 1146.9481  | -0.00428 | 0.03        |
| 16   | 1    | 19   | 17    | 0     | 20    | 963.95258 | 963.95157  | 0.00101  | 0.001       |
| 16   | 1    | 18   | 17    | 0     | 19    | 963.97018 | 963.97116  | -0.00098 | 0.001       |
| 16   | 1    | 17   | 17    | 0     | 18    | 963.98978 | 963.9909   | -0.00112 | 0.001       |
| 16   | 1    | 16   | 17    | 0     | 17    | 964.01241 | 964.0107   | 0.00171  | 0.001       |
| 16   | 1    | 15   | 17    | 0     | 16    | 964.03108 | 964.03047  | 0.00061  | 0.001       |
| 16   | 1    | 14   | 17    | 0     | 15    | 964.04951 | 964.05014  | -0.00063 | 0.001       |
| 16   | 1    | 13   | 17    | 0     | 14    | 964.06848 | 964.06963  | -0.00115 | 0.001       |
| 16   | 1    | 13   | 15    | 0     | 12    | 1150.535  | 1150.5338  | 0.00122  | 0.001       |
| 16   | 1    | 14   | 15    | 0     | 13    | 1150.5469 | 1150.5434  | 0.00346  | 0.003       |
| 16   | 1    | 15   | 15    | 0     | 14    | 1150.5469 | 1150.553   | -0.00606 | 0.006       |
| 16   | 1    | 16   | 15    | 0     | 15    | 1150.5642 | 1150.5623  | 0.00186  | 0.002       |
| 16   | 1    | 17   | 15    | 0     | 16    | 1150.5643 | 1150.5716  | -0.00727 | 0.01        |
| 16   | 1    | 19   | 15    | 0     | 18    | 1150.5923 | 1150.5896  | 0.00271  | 0.003       |
| 17   | 1    | 20   | 18    | 0     | 21    | 956.51467 | 956.51406  | 0.00061  | 0.001       |
| 17   | 1    | 19   | 18    | 0     | 20    | 956.53382 | 956.53377  | 0.00005  | 0.001       |
| 17   | 1    | 18   | 18    | 0     | 19    | 956.5524  | 956.55361  | -0.00121 | 0.001       |
| 17   | 1    | 17   | 18    | 0     | 18    | 956.57444 | 956.57351  | 0.00093  | 0.001       |
| 17   | 1    | 16   | 18    | 0     | 17    | 956.59337 | 956.59338  | -0.00001 | 0.001       |
| 17   | 1    | 15   | 18    | 0     | 16    | 956.61264 | 956.61316  | -0.00052 | 0.001       |
| 17   | 1    | 14   | 18    | 0     | 15    | 956.6311  | 956.63278  | -0.00168 | 0.001       |
| 17   | 1    | 14   | 16    | 0     | 13    | 1154.033  | 1154.0318  | 0.0012   | 0.003       |
| 17   | 1    | 15   | 16    | 0     | 14    | 1154.0479 | 1154.041   | 0.00694  | 0.007       |
| 17   | 1    | 16   | 16    | 0     | 15    | 1154.0479 | 1154.05    | -0.00207 | 0.003       |
| 17   | 1    | 17   | 16    | 0     | 16    | 1154.0588 | 1154.0588  | -0.00003 | 0.003       |
| 17   | 1    | 18   | 16    | 0     | 17    | 1154.0676 | 1154.0675  | 0.00006  | 0.003       |
| 17   | 1    | 19   | 16    | 0     | 18    | 1154.0762 | 1154.0761  | 0.00009  | 0.003       |
| 17   | 1    | 20   | 16    | 0     | 19    | 1154.0857 | 1154.0845  | 0.00118  | 0.003       |
| 18   | 1    | 21   | 19    | 0     | 22    | 948.99257 | 948.99316  | -0.00059 | 0.001       |
| 18   | 1    | 20   | 19    | 0     | 21    | 949.01316 | 949.01296  | 0.0002   | 0.001       |
| 18   | 1    | 19   | 19    | 0     | 20    | 949.03159 | 949.03289  | -0.0013  | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 18   | 1    | 18   | 19    | 0     | 19    | 949.05525 | 949.05288  | 0.00237  | 0.001       |
| 18   | 1    | 17   | 19    | 0     | 18    | 949.07405 | 949.07285  | 0.0012   | 0.001       |
| 18   | 1    | 16   | 19    | 0     | 17    | 949.09194 | 949.09273  | -0.00079 | 0.001       |
| 18   | 1    | 15   | 19    | 0     | 16    | 949.11247 | 949.11247  | 0        | 0.001       |
| 18   | 1    | 15   | 17    | 0     | 14    | 1157.3831 | 1157.3815  | 0.00157  | 0.008       |
| 18   | 1    | 16   | 17    | 0     | 15    | 1157.394  | 1157.3902  | 0.00381  | 0.008       |
| 18   | 1    | 17   | 17    | 0     | 16    | 1157.394  | 1157.3987  | -0.00468 | 0.008       |
| 18   | 1    | 18   | 17    | 0     | 17    | 1157.4055 | 1157.407   | -0.00151 | 0.008       |
| 18   | 1    | 19   | 17    | 0     | 18    | 1157.4178 | 1157.4152  | 0.00261  | 0.008       |
| 18   | 1    | 20   | 17    | 0     | 19    | 1157.4292 | 1157.4232  | 0.00598  | 0.008       |
| 18   | 1    | 21   | 17    | 0     | 20    | 1157.4292 | 1157.4311  | -0.0019  | 0.008       |
| 19   | 1    | 22   | 20    | 0     | 23    | 941.38978 | 941.39056  | -0.00078 | 0.001       |
| 19   | 1    | 21   | 20    | 0     | 22    | 941.40829 | 941.41045  | -0.00216 | 0.001       |
| 19   | 1    | 20   | 20    | 0     | 21    | 941.4316  | 941.43046  | 0.00114  | 0.001       |
| 19   | 1    | 19   | 20    | 0     | 20    | 941.45041 | 941.45052  | -0.00011 | 0.001       |
| 19   | 1    | 18   | 20    | 0     | 19    | 941.47102 | 941.47057  | 0.00045  | 0.001       |
| 19   | 1    | 17   | 20    | 0     | 18    | 941.49196 | 941.49055  | 0.00141  | 0.001       |
| 19   | 1    | 16   | 20    | 0     | 17    | 941.51079 | 941.51039  | 0.0004   | 0.001       |
| 19   | 1    | 16   | 18    | 0     | 15    | 1160.5885 | 1160.5812  | 0.00726  | 0.008       |
| 19   | 1    | 17   | 18    | 0     | 16    | 1160.5885 | 1160.5894  | -0.00086 | 0.002       |
| 19   | 1    | 18   | 18    | 0     | 17    | 1160.6028 | 1160.5973  | 0.00548  | 0.006       |
| 19   | 1    | 19   | 18    | 0     | 18    | 1160.6028 | 1160.6051  | -0.00232 | 0.002       |
| 19   | 1    | 20   | 18    | 0     | 19    | 1160.6129 | 1160.6128  | 0.00015  | 0.002       |
| 19   | 1    | 21   | 18    | 0     | 20    | 1160.6239 | 1160.6202  | 0.00366  | 0.005       |
| 19   | 1    | 22   | 18    | 0     | 21    | 1160.6239 | 1160.6276  | -0.00367 | 0.005       |
| 20   | 1    | 23   | 21    | 0     | 24    | 933.70587 | 933.70795  | -0.00208 | 0.001       |
| 20   | 1    | 22   | 21    | 0     | 23    | 933.72788 | 933.7279   | -0.00002 | 0.001       |
| 20   | 1    | 21   | 21    | 0     | 22    | 933.7476  | 933.74798  | -0.00038 | 0.001       |
| 20   | 1    | 20   | 21    | 0     | 21    | 933.76473 | 933.76811  | -0.00338 | 0.001       |
| 20   | 1    | 19   | 21    | 0     | 20    | 933.79142 | 933.78824  | 0.00318  | 0.001       |
| 20   | 1    | 18   | 21    | 0     | 19    | 933.80892 | 933.80829  | 0.00063  | 0.001       |
| 20   | 1    | 17   | 21    | 0     | 18    | 933.82519 | 933.82823  | -0.00304 | 0.001       |
| 20   | 1    | 17   | 19    | 0     | 16    | 1163.6301 | 1163.6292  | 0.00095  | 0.003       |
| 20   | 1    | 18   | 19    | 0     | 17    | 1163.6301 | 1163.6367  | -0.00664 | 0.007       |
| 20   | 1    | 19   | 19    | 0     | 18    | 1163.6437 | 1163.6442  | -0.00046 | 0.007       |
| 20   | 1    | 20   | 19    | 0     | 19    | 1163.6437 | 1163.6514  | -0.0077  | 0.008       |
| 20   | 1    | 21   | 19    | 0     | 20    | 1163.6595 | 1163.6585  | 0.00101  | 0.007       |
| 20   | 1    | 22   | 19    | 0     | 21    | 1163.6679 | 1163.6654  | 0.00249  | 0.007       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 20   | 1    | 23   | 19    | 0     | 22    | 1163.6679 | 1163.6722  | -0.00429 | 0.007       |
| 21   | 1    | 24   | 22    | 0     | 25    | 925.94513 | 925.94697  | -0.00184 | 0.001       |
| 21   | 1    | 23   | 22    | 0     | 24    | 925.96926 | 925.96698  | 0.00228  | 0.001       |
| 21   | 1    | 22   | 22    | 0     | 23    | 925.98687 | 925.98711  | -0.00024 | 0.001       |
| 21   | 1    | 21   | 22    | 0     | 22    | 926.01054 | 926.0073   | 0.00324  | 0.001       |
| 21   | 1    | 20   | 22    | 0     | 21    | 926.02894 | 926.02749  | 0.00145  | 0.001       |
| 21   | 1    | 19   | 22    | 0     | 20    | 926.04587 | 926.04761  | -0.00174 | 0.001       |
| 21   | 1    | 18   | 22    | 0     | 19    | 926.07019 | 926.06763  | 0.00256  | 0.001       |
| 21   | 1    | 18   | 20    | 0     | 17    | 1166.5234 | 1166.5236  | -0.00016 | 0.003       |
| 21   | 1    | 19   | 20    | 0     | 18    | 1166.5295 | 1166.5306  | -0.0011  | 0.004       |
| 21   | 1    | 20   | 20    | 0     | 19    | 1166.536  | 1166.5375  | -0.00145 | 0.003       |
| 21   | 1    | 21   | 20    | 0     | 20    | 1166.5436 | 1166.5441  | -0.00054 | 0.003       |
| 21   | 1    | 22   | 20    | 0     | 21    | 1166.5492 | 1166.5507  | -0.00146 | 0.003       |
| 21   | 1    | 23   | 20    | 0     | 22    | 1166.5578 | 1166.557   | 0.00078  | 0.003       |
| 21   | 1    | 24   | 20    | 0     | 23    | 1166.5578 | 1166.5632  | -0.00542 | 0.003       |
| 22   | 1    | 25   | 23    | 0     | 26    | 918.107   | 918.10922  | -0.00222 | 0.001       |
| 22   | 1    | 24   | 23    | 0     | 25    | 918.12718 | 918.12929  | -0.00211 | 0.001       |
| 22   | 1    | 23   | 23    | 0     | 24    | 918.15238 | 918.14947  | 0.00291  | 0.001       |
| 22   | 1    | 22   | 23    | 0     | 23    | 918.17079 | 918.1697   | 0.00109  | 0.001       |
| 22   | 1    | 21   | 23    | 0     | 22    | 918.1899  | 918.18993  | -0.00003 | 0.001       |
| 22   | 1    | 20   | 23    | 0     | 21    | 918.21243 | 918.21012  | 0.00231  | 0.001       |
| 22   | 1    | 19   | 21    | 0     | 18    | 1169.2664 | 1169.2627  | 0.00368  | 0.004       |
| 22   | 1    | 20   | 21    | 0     | 19    | 1169.2664 | 1169.2692  | -0.00279 | 0.004       |
| 22   | 1    | 21   | 21    | 0     | 20    | 1169.2778 | 1169.2755  | 0.00232  | 0.003       |
| 22   | 1    | 22   | 21    | 0     | 21    | 1169.2778 | 1169.2816  | -0.0038  | 0.004       |
| 22   | 1    | 23   | 21    | 0     | 22    | 1169.2891 | 1169.2875  | 0.00156  | 0.002       |
| 22   | 1    | 24   | 21    | 0     | 23    | 1169.2891 | 1169.2933  | -0.00422 | 0.004       |
| 22   | 1    | 25   | 21    | 0     | 24    | 1169.2891 | 1169.2989  | -0.00984 | 1           |
| 23   | 1    | 26   | 24    | 0     | 27    | 910.1955  | 910.1963   | -0.0008  | 0.001       |
| 23   | 1    | 20   | 22    | 0     | 19    | 1171.8567 | 1171.8449  | 0.01178  | 1           |
| 23   | 1    | 21   | 22    | 0     | 20    | 1171.8567 | 1171.8508  | 0.00587  | 0.006       |
| 23   | 1    | 22   | 22    | 0     | 21    | 1171.8567 | 1171.8565  | 0.00016  | 0.002       |
| 23   | 1    | 23   | 22    | 0     | 22    | 1171.8567 | 1171.8621  | -0.00536 | 0.006       |
| 23   | 1    | 24   | 22    | 0     | 23    | 1171.8712 | 1171.8674  | 0.00378  | 0.004       |
| 23   | 1    | 25   | 22    | 0     | 24    | 1171.8712 | 1171.8726  | -0.00141 | 0.002       |
| 23   | 1    | 26   | 22    | 0     | 25    | 1171.8712 | 1171.8776  | -0.00644 | 0.007       |
| 24   | 1    | 26   | 25    | 0     | 27    | 902.22849 | 902.22985  | -0.00136 | 0.001       |
| 24   | 1    | 27   | 25    | 0     | 28    | 902.22849 | 902.20972  | 0.01877  | 1           |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 24   | 1    | 25   | 25    | 0     | 26    | 902.25265 | 902.25008  | 0.00257  | 0.002       |
| 24   | 1    | 24   | 25    | 0     | 25    | 902.27025 | 902.27037  | -0.00012 | 0.001       |
| 24   | 1    | 23   | 25    | 0     | 24    | 902.29534 | 902.29067  | 0.00467  | 1           |
| 24   | 1    | 22   | 25    | 0     | 23    | 902.3121  | 902.31093  | 0.00117  | 0.002       |
| 24   | 1    | 21   | 23    | 0     | 20    | 1174.2683 | 1174.2685  | -0.00017 | 0.002       |
| 24   | 1    | 22   | 23    | 0     | 21    | 1174.2683 | 1174.2738  | -0.00548 | 0.007       |
| 24   | 1    | 23   | 23    | 0     | 22    | 1174.2818 | 1174.2789  | 0.0029   | 0.003       |
| 24   | 1    | 24   | 23    | 0     | 23    | 1174.2818 | 1174.2838  | -0.00203 | 0.002       |
| 24   | 1    | 25   | 23    | 0     | 24    | 1174.2918 | 1174.2886  | 0.00321  | 0.004       |
| 24   | 1    | 26   | 23    | 0     | 25    | 1174.2918 | 1174.2932  | -0.00137 | 0.002       |
| 24   | 1    | 27   | 23    | 0     | 26    | 1174.2918 | 1174.2976  | -0.0058  | 1           |
| 25   | 1    | 22   | 24    | 0     | 21    | 1176.5428 | 1176.5317  | 0.01115  | 1           |
| 25   | 1    | 23   | 24    | 0     | 22    | 1176.5428 | 1176.5364  | 0.00643  | 0.008       |
| 25   | 1    | 24   | 24    | 0     | 23    | 1176.5428 | 1176.5409  | 0.00191  | 0.002       |
| 25   | 1    | 25   | 24    | 0     | 24    | 1176.5428 | 1176.5452  | -0.00241 | 0.002       |
| 25   | 1    | 26   | 24    | 0     | 25    | 1176.5428 | 1176.5494  | -0.00656 | 0.008       |
| 25   | 1    | 27   | 24    | 0     | 26    | 1176.5536 | 1176.5533  | 0.00027  | 0.002       |
| 25   | 1    | 28   | 24    | 0     | 27    | 1176.5536 | 1176.5571  | -0.00353 | 0.004       |
| 26   | 1    | 23   | 25    | 0     | 22    | 1178.6368 | 1178.6328  | 0.004    | 0.004       |
| 26   | 1    | 24   | 25    | 0     | 23    | 1178.6368 | 1178.6369  | -0.00011 | 0.002       |
| 26   | 1    | 25   | 25    | 0     | 24    | 1178.6368 | 1178.6408  | -0.00401 | 0.004       |
| 26   | 1    | 26   | 25    | 0     | 25    | 1178.6368 | 1178.6445  | -0.00771 | 0.01        |
| 26   | 1    | 27   | 25    | 0     | 26    | 1178.6485 | 1178.648   | 0.00047  | 0.002       |
| 26   | 1    | 28   | 25    | 0     | 27    | 1178.6485 | 1178.6514  | -0.00288 | 0.003       |
| 26   | 1    | 29   | 25    | 0     | 28    | 1178.6485 | 1178.6546  | -0.00605 | 0.008       |
| 27   | 1    | 24   | 26    | 0     | 23    | 1180.5706 | 1180.5702  | 0.00038  | 0.002       |
| 27   | 1    | 25   | 26    | 0     | 24    | 1180.5706 | 1180.5737  | -0.0031  | 0.003       |
| 27   | 1    | 26   | 26    | 0     | 25    | 1180.5807 | 1180.577   | 0.00372  | 0.004       |
| 27   | 1    | 27   | 26    | 0     | 26    | 1180.5807 | 1180.5801  | 0.00064  | 0.002       |
| 27   | 1    | 28   | 26    | 0     | 27    | 1180.5807 | 1180.5829  | -0.00224 | 0.002       |
| 27   | 1    | 29   | 26    | 0     | 28    | 1180.5807 | 1180.5857  | -0.00495 | 0.006       |
| 27   | 1    | 30   | 26    | 0     | 29    | 1180.5807 | 1180.5882  | -0.00748 | 0.1         |
| 28   | 1    | 25   | 27    | 0     | 24    | 1182.349  | 1182.3422  | 0.00676  | 0.009       |
| 28   | 1    | 26   | 27    | 0     | 25    | 1182.349  | 1182.3451  | 0.0039   | 0.006       |
| 28   | 1    | 27   | 27    | 0     | 26    | 1182.349  | 1182.3477  | 0.00127  | 0.002       |
| 28   | 1    | 28   | 27    | 0     | 27    | 1182.349  | 1182.3502  | -0.00117 | 0.002       |
| 28   | 1    | 29   | 27    | 0     | 28    | 1182.349  | 1182.3524  | -0.00341 | 0.003       |
| 28   | 1    | 30   | 27    | 0     | 29    | 1182.349  | 1182.3545  | -0.00546 | 0.008       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 28   | 1    | 31   | 27    | 0     | 30    | 1182.349  | 1182.3563  | -0.00734 | 0.008       |
| 29   | 1    | 26   | 28    | 0     | 25    | 1183.9515 | 1183.9472  | 0.00429  | 0.005       |
| 29   | 1    | 27   | 28    | 0     | 26    | 1183.9515 | 1183.9494  | 0.00209  | 0.002       |
| 29   | 1    | 28   | 28    | 0     | 27    | 1183.9515 | 1183.9514  | 0.0001   | 0.002       |
| 29   | 1    | 29   | 28    | 0     | 28    | 1183.9515 | 1183.9532  | -0.00168 | 0.002       |
| 29   | 1    | 30   | 28    | 0     | 29    | 1183.9515 | 1183.9548  | -0.00326 | 0.005       |
| 29   | 1    | 31   | 28    | 0     | 30    | 1183.9515 | 1183.9562  | -0.00466 | 0.005       |
| 29   | 1    | 32   | 28    | 0     | 31    | 1183.9515 | 1183.9574  | -0.00587 | 0.008       |
| 30   | 1    | 27   | 29    | 0     | 26    | 1185.3851 | 1185.3835  | 0.00165  | 0.002       |
| 30   | 1    | 28   | 29    | 0     | 27    | 1185.3851 | 1185.385   | 0.0001   | 0.002       |
| 30   | 1    | 29   | 29    | 0     | 28    | 1185.3851 | 1185.3863  | -0.00123 | 0.002       |
| 30   | 1    | 30   | 29    | 0     | 29    | 1185.3851 | 1185.3874  | -0.00234 | 0.003       |
| 30   | 1    | 31   | 29    | 0     | 30    | 1185.3851 | 1185.3884  | -0.00325 | 0.004       |
| 30   | 1    | 32   | 29    | 0     | 31    | 1185.3851 | 1185.3891  | -0.00397 | 0.005       |
| 30   | 1    | 33   | 29    | 0     | 32    | 1185.3851 | 1185.3896  | -0.00451 | 0.009       |
| 31   | 1    | 28   | 30    | 0     | 27    | 1186.6496 | 1186.6493  | 0.00028  | 0.002       |
| 31   | 1    | 29   | 30    | 0     | 28    | 1186.6496 | 1186.6502  | -0.0006  | 0.002       |
| 31   | 1    | 30   | 30    | 0     | 29    | 1186.6496 | 1186.6509  | -0.00126 | 0.002       |
| 31   | 1    | 31   | 30    | 0     | 30    | 1186.6496 | 1186.6513  | -0.00169 | 0.002       |
| 31   | 1    | 32   | 30    | 0     | 31    | 1186.6496 | 1186.6515  | -0.00192 | 0.002       |
| 31   | 1    | 33   | 30    | 0     | 32    | 1186.6496 | 1186.6516  | -0.00196 | 0.002       |
| 31   | 1    | 34   | 30    | 0     | 33    | 1186.6496 | 1186.6514  | -0.0018  | 0.002       |
| 32   | 1    | 29   | 31    | 0     | 28    | 1187.7413 | 1187.7432  | -0.00186 | 0.002       |
| 32   | 1    | 30   | 31    | 0     | 29    | 1187.7413 | 1187.7434  | -0.00206 | 0.002       |
| 32   | 1    | 31   | 31    | 0     | 30    | 1187.7413 | 1187.7433  | -0.00203 | 0.002       |
| 32   | 1    | 32   | 31    | 0     | 31    | 1187.7413 | 1187.7431  | -0.00178 | 0.002       |
| 32   | 1    | 33   | 31    | 0     | 32    | 1187.7413 | 1187.7426  | -0.00131 | 0.002       |
| 32   | 1    | 34   | 31    | 0     | 33    | 1187.7413 | 1187.742   | -0.00065 | 0.002       |
| 32   | 1    | 35   | 31    | 0     | 34    | 1187.7413 | 1187.7411  | 0.0002   | 0.002       |
| 33   | 1    | 30   | 32    | 0     | 29    | 1188.6607 | 1188.6633  | -0.00263 | 0.003       |
| 33   | 1    | 31   | 32    | 0     | 30    | 1188.6607 | 1188.6628  | -0.00214 | 0.003       |
| 33   | 1    | 32   | 32    | 0     | 31    | 1188.6607 | 1188.6621  | -0.00141 | 0.002       |
| 33   | 1    | 33   | 32    | 0     | 32    | 1188.6607 | 1188.6612  | -0.00045 | 0.002       |
| 33   | 1    | 34   | 32    | 0     | 33    | 1188.6607 | 1188.66    | 0.00072  | 0.002       |
| 33   | 1    | 35   | 32    | 0     | 34    | 1188.6607 | 1188.6586  | 0.00209  | 0.002       |
| 33   | 1    | 36   | 32    | 0     | 35    | 1188.6607 | 1188.6571  | 0.00365  | 0.003       |
| 34   | 1    | 31   | 33    | 0     | 30    | 1189.4042 | 1189.4082  | -0.00397 | 0.005       |
| 34   | 1    | 32   | 33    | 0     | 31    | 1189.4042 | 1189.407   | -0.00277 | 0.003       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 34   | 1    | 33   | 33    | 0     | 32    | 1189.4042 | 1189.4055  | -0.00134 | 0.003       |
| 34   | 1    | 34   | 33    | 0     | 33    | 1189.4042 | 1189.4039  | 0.00033  | 0.002       |
| 34   | 1    | 35   | 33    | 0     | 34    | 1189.4042 | 1189.402   | 0.00222  | 0.002       |
| 34   | 1    | 36   | 33    | 0     | 35    | 1189.4042 | 1189.3999  | 0.00431  | 0.003       |
| 34   | 1    | 37   | 33    | 0     | 36    | 1189.4042 | 1189.3976  | 0.0066   | 0.01        |
| 35   | 1    | 32   | 34    | 0     | 31    | 1189.9714 | 1189.9761  | -0.00465 | 0.005       |
| 35   | 1    | 33   | 34    | 0     | 32    | 1189.9714 | 1189.9741  | -0.00273 | 0.003       |
| 35   | 1    | 34   | 34    | 0     | 33    | 1189.9714 | 1189.972   | -0.00057 | 0.002       |
| 35   | 1    | 36   | 34    | 0     | 35    | 1189.9714 | 1189.967   | 0.00443  | 0.005       |
| 35   | 1    | 37   | 34    | 0     | 36    | 1189.9714 | 1189.9641  | 0.00726  | 0.01        |
| 35   | 1    | 38   | 34    | 0     | 37    | 1189.9714 | 1189.9611  | 0.01028  | 0.01        |
| 36   | 1    | 33   | 35    | 0     | 32    | 1190.3588 | 1190.3653  | -0.0065  | 0.01        |
| 36   | 1    | 34   | 35    | 0     | 33    | 1190.3588 | 1190.3627  | -0.00386 | 0.01        |
| 36   | 1    | 35   | 35    | 0     | 34    | 1190.3588 | 1190.3598  | -0.00097 | 0.002       |
| 36   | 1    | 36   | 35    | 0     | 35    | 1190.3588 | 1190.3566  | 0.00216  | 0.003       |
| 36   | 1    | 37   | 35    | 0     | 36    | 1190.3588 | 1190.3533  | 0.00551  | 0.01        |
| 36   | 1    | 38   | 35    | 0     | 37    | 1190.3588 | 1190.3497  | 0.00908  | 0.01        |
| 36   | 1    | 39   | 35    | 0     | 38    | 1190.3588 | 1190.3459  | 0.01286  | 1           |
| 37   | 1    | 34   | 36    | 0     | 33    | 1190.5726 | 1190.5743  | -0.00169 | 0.002       |
| 37   | 1    | 35   | 36    | 0     | 34    | 1190.5726 | 1190.5709  | 0.00169  | 0.002       |
| 37   | 1    | 36   | 36    | 0     | 35    | 1190.5726 | 1190.5673  | 0.00533  | 0.005       |
| 37   | 1    | 37   | 36    | 0     | 36    | 1190.561  | 1190.5634  | -0.0024  | 0.003       |
| 37   | 1    | 38   | 36    | 0     | 37    | 1190.561  | 1190.5593  | 0.00171  | 0.002       |
| 37   | 1    | 39   | 36    | 0     | 38    | 1190.561  | 1190.555   | 0.00603  | 0.01        |
| 37   | 1    | 40   | 36    | 0     | 39    | 1190.561  | 1190.5504  | 0.01057  | 0.01        |
| 38   | 1    | 35   | 37    | 0     | 34    | 1190.6033 | 1190.6014  | 0.00194  | 0.002       |
| 38   | 1    | 36   | 37    | 0     | 35    | 1190.6033 | 1190.5972  | 0.00607  | 0.01        |
| 38   | 1    | 37   | 37    | 0     | 36    | 1190.6033 | 1190.5928  | 0.01046  | 1           |
| 0    | 1    | 3    | 1     | 0     | 2     | 1070.2317 | 1070.2373  | -0.00558 | 0.005       |
| 1    | 1    | 2    | 2     | 0     | 1     | 1064.382  | 1064.3903  | -0.00826 | 1           |
| 1    | 1    | 4    | 2     | 0     | 4     | 1064.3709 | 1064.3713  | -0.00041 | 0.001       |
| 1    | 1    | 3    | 0     | 0     | 3     | 1081.5099 | 1081.5153  | -0.00536 | 0.003       |
| 3    | 1    | 5    | 2     | 0     | 5     | 1092.3669 | 1092.3674  | -0.00054 | 0.001       |
| 1    | 1    | 2    | 0     | 0     | 3     | 1081.4949 | 1081.4896  | 0.00532  | 0.005       |
| 3    | 1    | 4    | 2     | 0     | 4     | 1092.3801 | 1092.3812  | -0.00111 | 0.003       |
| 2    | 1    | 1    | 3     | 0     | 0     | 1058.4212 | 1058.4263  | -0.00512 | 0.005       |
| 2    | 1    | 2    | 3     | 0     | 1     | 1058.4357 | 1058.4352  | 0.00046  | 0.001       |
| 0    | 1    | 3    | 1     | 0     | 4     | 1070.1269 | 1070.13    | -0.00312 | 0.003       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 1    | 1    | 4    | 2     | 0     | 5     | 1064.269  | 1064.2775  | -0.00852 | 1           |
| 1    | 1    | 4    | 0     | 0     | 3     | 1081.5961 | 1081.5943  | 0.00182  | 0.002       |
| 1    | 1    | 3    | 2     | 0     | 4     | 1064.2928 | 1064.2923  | 0.00051  | 0.001       |
| 1    | 1    | 3    | 2     | 0     | 3     | 1064.3574 | 1064.3544  | 0.003    | 0.003       |
| 3    | 1    | 1    | 2     | 0     | 1     | 1092.3801 | 1092.3832  | -0.00311 | 0.003       |
| 2    | 1    | 2    | 1     | 0     | 3     | 1086.978  | 1086.9825  | -0.00451 | 0.005       |
| 0    | 2    | 3    | 1     | 1     | 4     | 1041.0227 | 1041.0219  | 0.00082  | 0.001       |
| 2    | 2    | 4    | 1     | 1     | 3     | 1057.6118 | 1057.617   | -0.00517 | 0.005       |
| 2    | 2    | 5    | 1     | 1     | 4     | 1057.6351 | 1057.6301  | 0.00497  | 0.005       |
| 1    | 2    | 4    | 2     | 1     | 5     | 1035.2794 | 1035.2852  | -0.00576 | 0.005       |
| 3    | 2    | 4    | 2     | 1     | 3     | 1062.8567 | 1062.859   | -0.00226 | 0.003       |
| 3    | 2    | 5    | 2     | 1     | 4     | 1062.8758 | 1062.8767  | -0.00087 | 0.001       |
| 3    | 2    | 6    | 2     | 1     | 5     | 1062.8943 | 1062.8902  | 0.00414  | 0.003       |
| 2    | 2    | 5    | 3     | 1     | 6     | 1029.4302 | 1029.4325  | -0.00226 | 0.003       |
| 2    | 2    | 4    | 3     | 1     | 5     | 1029.4496 | 1029.448   | 0.00157  | 0.002       |
| 2    | 2    | 3    | 3     | 1     | 4     | 1029.4668 | 1029.4688  | -0.00202 | 0.002       |
| 4    | 2    | 1    | 3     | 1     | 0     | 1067.9206 | 1067.9398  | -0.01923 | 1           |
| 4    | 2    | 2    | 3     | 1     | 1     | 1067.9474 | 1067.9528  | -0.00541 | 0.006       |
| 4    | 2    | 3    | 3     | 1     | 2     | 1067.9664 | 1067.967   | -0.00061 | 0.001       |
| 4    | 2    | 4    | 3     | 1     | 3     | 1067.9767 | 1067.9823  | -0.00555 | 0.006       |
| 4    | 2    | 5    | 3     | 1     | 4     | 1067.9962 | 1067.998   | -0.00179 | 0.002       |
| 4    | 2    | 6    | 3     | 1     | 5     | 1068.016  | 1068.0133  | 0.00275  | 0.003       |
| 4    | 2    | 7    | 3     | 1     | 6     | 1068.03   | 1068.0267  | 0.00333  | 0.003       |
| 3    | 2    | 6    | 4     | 1     | 7     | 1023.4656 | 1023.4669  | -0.00129 | 0.001       |
| 5    | 2    | 2    | 4     | 1     | 1     | 1072.9533 | 1072.9539  | -0.00055 | 0.001       |
| 5    | 2    | 3    | 4     | 1     | 2     | 1072.9663 | 1072.9672  | -0.00087 | 0.001       |
| 5    | 2    | 4    | 4     | 1     | 3     | 1072.9809 | 1072.9811  | -0.0002  | 0.001       |
| 5    | 2    | 5    | 4     | 1     | 4     | 1072.9931 | 1072.9955  | -0.00241 | 0.001       |
| 5    | 2    | 6    | 4     | 1     | 5     | 1073.007  | 1073.0101  | -0.00308 | 0.001       |
| 5    | 2    | 7    | 4     | 1     | 6     | 1073.0248 | 1073.0243  | 0.00049  | 0.001       |
| 5    | 2    | 8    | 4     | 1     | 7     | 1073.0389 | 1073.0375  | 0.00141  | 0.001       |
| 4    | 2    | 7    | 5     | 1     | 8     | 1017.3898 | 1017.3906  | -0.00082 | 0.001       |
| 4    | 2    | 6    | 5     | 1     | 7     | 1017.4073 | 1017.4074  | -0.00007 | 0.001       |
| 4    | 2    | 5    | 5     | 1     | 6     | 1017.4259 | 1017.4256  | 0.00031  | 0.001       |
| 4    | 2    | 4    | 5     | 1     | 5     | 1017.4441 | 1017.4442  | -0.00009 | 0.001       |
| 6    | 2    | 3    | 5     | 1     | 2     | 1077.841  | 1077.8398  | 0.00118  | 0.003       |
| 6    | 2    | 4    | 5     | 1     | 3     | 1077.8545 | 1077.8531  | 0.00145  | 0.003       |
| 6    | 2    | 5    | 5     | 1     | 4     | 1077.8662 | 1077.8666  | -0.00042 | 0.003       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 6    | 2    | 6    | 5     | 1     | 5     | 1077.8793 | 1077.8804  | -0.00112 | 0.003       |
| 6    | 2    | 7    | 5     | 1     | 6     | 1077.8936 | 1077.8942  | -0.00064 | 0.003       |
| 6    | 2    | 8    | 5     | 1     | 7     | 1077.9079 | 1077.9078  | 0.00011  | 0.003       |
| 6    | 2    | 9    | 5     | 1     | 8     | 1077.9206 | 1077.9207  | -0.00005 | 0.003       |
| 5    | 2    | 8    | 6     | 1     | 9     | 1011.2059 | 1011.2056  | 0.00027  | 0.003       |
| 5    | 2    | 7    | 6     | 1     | 8     | 1011.2227 | 1011.2228  | -0.00008 | 0.003       |
| 5    | 2    | 6    | 6     | 1     | 7     | 1011.2421 | 1011.2409  | 0.00118  | 0.003       |
| 5    | 2    | 5    | 6     | 1     | 6     | 1011.2596 | 1011.2593  | 0.00027  | 0.003       |
| 5    | 2    | 4    | 6     | 1     | 5     | 1011.2806 | 1011.2775  | 0.00315  | 0.003       |
| 5    | 2    | 3    | 6     | 1     | 4     | 1011.2947 | 1011.2949  | -0.00016 | 0.003       |
| 5    | 2    | 2    | 6     | 1     | 3     | 1011.3097 | 1011.3113  | -0.00156 | 0.003       |
| 7    | 2    | 4    | 6     | 1     | 3     | 1082.5953 | 1082.5961  | -0.00078 | 0.001       |
| 7    | 2    | 5    | 6     | 1     | 4     | 1082.6088 | 1082.6091  | -0.00027 | 0.001       |
| 7    | 2    | 6    | 6     | 1     | 5     | 1082.6218 | 1082.6222  | -0.00043 | 0.001       |
| 7    | 2    | 7    | 6     | 1     | 6     | 1082.6349 | 1082.6355  | -0.00059 | 0.001       |
| 7    | 2    | 8    | 6     | 1     | 7     | 1082.6479 | 1082.6487  | -0.00082 | 0.001       |
| 7    | 2    | 9    | 6     | 1     | 8     | 1082.6617 | 1082.6617  | -0.00001 | 0.001       |
| 7    | 2    | 10   | 6     | 1     | 9     | 1082.6749 | 1082.6742  | 0.00069  | 0.001       |
| 6    | 2    | 9    | 7     | 1     | 10    | 1004.9151 | 1004.9139  | 0.00124  | 0.003       |
| 6    | 2    | 8    | 7     | 1     | 9     | 1004.9307 | 1004.9314  | -0.00065 | 0.003       |
| 6    | 2    | 7    | 7     | 1     | 8     | 1004.9513 | 1004.9496  | 0.00175  | 0.003       |
| 6    | 2    | 6    | 7     | 1     | 7     | 1004.9687 | 1004.968   | 0.00074  | 0.003       |
| 6    | 2    | 5    | 7     | 1     | 6     | 1004.9865 | 1004.9862  | 0.00033  | 0.003       |
| 6    | 2    | 4    | 7     | 1     | 5     | 1005.0034 | 1005.0038  | -0.00043 | 0.003       |
| 6    | 2    | 3    | 7     | 1     | 4     | 1005.0187 | 1005.0207  | -0.00202 | 0.003       |
| 8    | 2    | 5    | 7     | 1     | 4     | 1087.222  | 1087.2208  | 0.0012   | 0.001       |
| 8    | 2    | 6    | 7     | 1     | 5     | 1087.2332 | 1087.2335  | -0.00027 | 0.001       |
| 8    | 2    | 7    | 7     | 1     | 6     | 1087.2461 | 1087.2462  | -0.00011 | 0.001       |
| 8    | 2    | 8    | 7     | 1     | 7     | 1087.2584 | 1087.259   | -0.00058 | 0.001       |
| 8    | 2    | 9    | 7     | 1     | 8     | 1087.2717 | 1087.2717  | 0.00003  | 0.001       |
| 8    | 2    | 10   | 7     | 1     | 9     | 1087.2846 | 1087.2842  | 0.00045  | 0.001       |
| 8    | 2    | 11   | 7     | 1     | 10    | 1087.2976 | 1087.2963  | 0.00134  | 0.001       |
| 7    | 2    | 10   | 8     | 1     | 11    | 998.51709 | 998.51719  | -0.0001  | 0.001       |
| 7    | 2    | 9    | 8     | 1     | 10    | 998.53445 | 998.53497  | -0.00052 | 0.001       |
| 7    | 2    | 8    | 8     | 1     | 9     | 998.55282 | 998.55331  | -0.00049 | 0.001       |
| 7    | 2    | 7    | 8     | 1     | 8     | 998.57185 | 998.5718   | 0.00005  | 0.001       |
| 7    | 2    | 6    | 8     | 1     | 7     | 998.58906 | 998.59014  | -0.00108 | 0.001       |
| 7    | 2    | 5    | 8     | 1     | 6     | 998.60801 | 998.60805  | -0.00004 | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 7    | 2    | 4    | 8     | 1     | 5     | 998.62345 | 998.62534  | -0.00189 | 0.001       |
| 9    | 2    | 6    | 8     | 1     | 5     | 1091.713  | 1091.7121  | 0.00088  | 0.003       |
| 9    | 2    | 7    | 8     | 1     | 6     | 1091.7255 | 1091.7244  | 0.00107  | 0.003       |
| 9    | 2    | 8    | 8     | 1     | 7     | 1091.7384 | 1091.7367  | 0.00166  | 0.003       |
| 9    | 2    | 9    | 8     | 1     | 8     | 1091.7494 | 1091.749   | 0.00038  | 0.003       |
| 9    | 2    | 10   | 8     | 1     | 9     | 1091.762  | 1091.7612  | 0.0008   | 0.003       |
| 9    | 2    | 11   | 8     | 1     | 10    | 1091.7746 | 1091.7732  | 0.00141  | 0.003       |
| 9    | 2    | 12   | 8     | 1     | 11    | 1091.787  | 1091.7849  | 0.00212  | 0.003       |
| 8    | 2    | 11   | 9     | 1     | 12    | 992.01876 | 992.01749  | 0.00127  | 0.003       |
| 8    | 2    | 10   | 9     | 1     | 11    | 992.03575 | 992.03555  | 0.0002   | 0.003       |
| 8    | 2    | 9    | 9     | 1     | 10    | 992.05398 | 992.05404  | -0.00006 | 0.003       |
| 8    | 2    | 8    | 9     | 1     | 9     | 992.07173 | 992.07266  | -0.00093 | 0.003       |
| 8    | 2    | 7    | 9     | 1     | 8     | 992.09103 | 992.09115  | -0.00012 | 0.003       |
| 8    | 2    | 6    | 9     | 1     | 7     | 992.10828 | 992.10929  | -0.00101 | 0.003       |
| 8    | 2    | 5    | 9     | 1     | 6     | 992.12689 | 992.12691  | -0.00002 | 0.003       |
| 10   | 2    | 7    | 9     | 1     | 6     | 1096.0679 | 1096.0682  | -0.00028 | 0.003       |
| 10   | 2    | 8    | 9     | 1     | 7     | 1096.0753 | 1096.0801  | -0.00478 | 0.01        |
| 10   | 2    | 9    | 9     | 1     | 8     | 1096.088  | 1096.092   | -0.00395 | 0.01        |
| 10   | 2    | 10   | 9     | 1     | 9     | 1096.102  | 1096.1038  | -0.00175 | 0.003       |
| 10   | 2    | 11   | 9     | 1     | 10    | 1096.1132 | 1096.1154  | -0.00223 | 0.003       |
| 10   | 2    | 12   | 9     | 1     | 11    | 1096.1257 | 1096.1269  | -0.00124 | 0.003       |
| 10   | 2    | 13   | 9     | 1     | 12    | 1096.1382 | 1096.1382  | 0.00001  | 0.003       |
| 9    | 2    | 12   | 10    | 1     | 13    | 985.41709 | 985.41662  | 0.00047  | 0.003       |
| 9    | 2    | 11   | 10    | 1     | 12    | 985.43548 | 985.43493  | 0.00055  | 0.003       |
| 9    | 2    | 10   | 10    | 1     | 11    | 985.45419 | 985.45359  | 0.0006   | 0.003       |
| 9    | 2    | 9    | 10    | 1     | 10    | 985.47243 | 985.47236  | 0.00007  | 0.003       |
| 9    | 2    | 8    | 10    | 1     | 9     | 985.49066 | 985.49101  | -0.00035 | 0.003       |
| 9    | 2    | 7    | 10    | 1     | 8     | 985.50926 | 985.50937  | -0.00011 | 0.003       |
| 9    | 2    | 6    | 10    | 1     | 7     | 985.52676 | 985.52729  | -0.00053 | 0.003       |
| 11   | 2    | 8    | 10    | 1     | 7     | 1100.2815 | 1100.2871  | -0.00558 | 0.004       |
| 11   | 2    | 9    | 10    | 1     | 8     | 1100.292  | 1100.2986  | -0.00656 | 0.004       |
| 11   | 2    | 10   | 10    | 1     | 9     | 1100.3058 | 1100.31    | -0.00417 | 0.003       |
| 11   | 2    | 11   | 10    | 1     | 10    | 1100.3189 | 1100.3213  | -0.00239 | 0.001       |
| 11   | 2    | 12   | 10    | 1     | 11    | 1100.3314 | 1100.3325  | -0.00108 | 0.001       |
| 11   | 2    | 13   | 10    | 1     | 12    | 1100.3444 | 1100.3435  | 0.0009   | 0.001       |
| 11   | 2    | 14   | 10    | 1     | 13    | 1100.3562 | 1100.3543  | 0.00191  | 0.001       |
| 10   | 2    | 13   | 11    | 1     | 14    | 978.7167  | 978.71643  | 0.00027  | 0.001       |
| 10   | 2    | 12   | 11    | 1     | 13    | 978.73426 | 978.73497  | -0.00071 | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 10   | 2    | 11   | 11    | 1     | 12    | 978.75347 | 978.7538   | -0.00033 | 0.001       |
| 10   | 2    | 10   | 11    | 1     | 11    | 978.77175 | 978.77272  | -0.00097 | 0.001       |
| 10   | 2    | 9    | 11    | 1     | 10    | 978.79112 | 978.79154  | -0.00042 | 0.001       |
| 10   | 2    | 8    | 11    | 1     | 9     | 978.80917 | 978.81011  | -0.00094 | 0.001       |
| 10   | 2    | 7    | 11    | 1     | 8     | 978.8269  | 978.8283   | -0.0014  | 0.001       |
| 12   | 2    | 9    | 11    | 1     | 8     | 1104.3625 | 1104.367   | -0.00446 | 0.003       |
| 12   | 2    | 10   | 11    | 1     | 9     | 1104.3722 | 1104.378   | -0.00579 | 0.003       |
| 12   | 2    | 11   | 11    | 1     | 10    | 1104.3859 | 1104.3889  | -0.00303 | 0.003       |
| 12   | 2    | 12   | 11    | 1     | 11    | 1104.3996 | 1104.3998  | -0.00017 | 0.003       |
| 12   | 2    | 13   | 11    | 1     | 12    | 1104.4139 | 1104.4105  | 0.00344  | 0.003       |
| 12   | 2    | 14   | 11    | 1     | 13    | 1104.4139 | 1104.421   | -0.00709 | 0.003       |
| 12   | 2    | 15   | 11    | 1     | 14    | 1104.4277 | 1104.4313  | -0.00361 | 0.003       |
| 11   | 2    | 14   | 12    | 1     | 15    | 971.91991 | 971.91875  | 0.00116  | 0.001       |
| 11   | 2    | 13   | 12    | 1     | 14    | 971.9372  | 971.93749  | -0.00029 | 0.001       |
| 11   | 2    | 12   | 12    | 1     | 13    | 971.95547 | 971.95649  | -0.00102 | 0.001       |
| 11   | 2    | 11   | 12    | 1     | 12    | 971.97441 | 971.97557  | -0.00116 | 0.001       |
| 11   | 2    | 10   | 12    | 1     | 11    | 971.99364 | 971.99456  | -0.00092 | 0.001       |
| 11   | 2    | 9    | 12    | 1     | 10    | 972.0132  | 972.01333  | -0.00013 | 0.001       |
| 11   | 2    | 8    | 12    | 1     | 9     | 972.03052 | 972.03176  | -0.00124 | 0.001       |
| 13   | 2    | 10   | 12    | 1     | 9     | 1108.3063 | 1108.3059  | 0.00037  | 0.001       |
| 13   | 2    | 11   | 12    | 1     | 10    | 1108.3189 | 1108.3165  | 0.00239  | 0.002       |
| 13   | 2    | 12   | 12    | 1     | 11    | 1108.3328 | 1108.327   | 0.00583  | 0.006       |
| 13   | 2    | 13   | 12    | 1     | 12    | 1108.3328 | 1108.3373  | -0.00451 | 0.004       |
| 13   | 2    | 14   | 12    | 1     | 13    | 1108.3461 | 1108.3475  | -0.0014  | 0.002       |
| 13   | 2    | 15   | 12    | 1     | 14    | 1108.3606 | 1108.3575  | 0.00307  | 0.003       |
| 13   | 2    | 16   | 12    | 1     | 15    | 1108.3606 | 1108.3674  | -0.00676 | 0.009       |
| 12   | 2    | 15   | 13    | 1     | 16    | 965.02592 | 965.02537  | 0.00055  | 0.001       |
| 12   | 2    | 14   | 13    | 1     | 15    | 965.04331 | 965.04431  | -0.001   | 0.001       |
| 12   | 2    | 13   | 13    | 1     | 14    | 965.0618  | 965.06348  | -0.00168 | 0.001       |
| 12   | 2    | 12   | 13    | 1     | 13    | 965.08082 | 965.0827   | -0.00188 | 0.001       |
| 12   | 2    | 11   | 13    | 1     | 12    | 965.1026  | 965.10185  | 0.00075  | 0.001       |
| 12   | 2    | 10   | 13    | 1     | 11    | 965.1225  | 965.12081  | 0.00169  | 0.001       |
| 12   | 2    | 9    | 13    | 1     | 10    | 965.13938 | 965.13947  | -0.00009 | 0.001       |
| 14   | 2    | 11   | 13    | 1     | 10    | 1112.1028 | 1112.1021  | 0.00066  | 0.003       |
| 14   | 2    | 12   | 13    | 1     | 11    | 1112.1171 | 1112.1122  | 0.00486  | 0.01        |
| 14   | 2    | 13   | 13    | 1     | 12    | 1112.1171 | 1112.1222  | -0.00511 | 0.003       |
| 14   | 2    | 14   | 13    | 1     | 13    | 1112.1324 | 1112.132   | 0.00036  | 0.003       |
| 14   | 2    | 15   | 13    | 1     | 14    | 1112.1481 | 1112.1417  | 0.00638  | 0.01        |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 14   | 2    | 16   | 13    | 1     | 15    | 1112.1481 | 1112.1512  | -0.00314 | 0.003       |
| 14   | 2    | 17   | 13    | 1     | 16    | 1112.1599 | 1112.1606  | -0.00068 | 0.003       |
| 13   | 2    | 16   | 14    | 1     | 17    | 958.03896 | 958.03809  | 0.00087  | 0.001       |
| 13   | 2    | 15   | 14    | 1     | 16    | 958.05777 | 958.05722  | 0.00055  | 0.001       |
| 13   | 2    | 14   | 14    | 1     | 15    | 958.07674 | 958.07654  | 0.0002   | 0.001       |
| 13   | 2    | 13   | 14    | 1     | 14    | 958.09484 | 958.09591  | -0.00107 | 0.001       |
| 13   | 2    | 12   | 14    | 1     | 13    | 958.11374 | 958.11521  | -0.00147 | 0.001       |
| 13   | 2    | 11   | 14    | 1     | 12    | 958.13363 | 958.13435  | -0.00072 | 0.001       |
| 13   | 2    | 10   | 14    | 1     | 11    | 958.15254 | 958.15321  | -0.00067 | 0.001       |
| 15   | 2    | 12   | 14    | 1     | 11    | 1115.7546 | 1115.7537  | 0.0009   | 0.003       |
| 15   | 2    | 13   | 14    | 1     | 12    | 1115.7688 | 1115.7633  | 0.00548  | 0.003       |
| 15   | 2    | 14   | 14    | 1     | 13    | 1115.7688 | 1115.7728  | -0.00398 | 0.003       |
| 15   | 2    | 15   | 14    | 1     | 14    | 1115.7787 | 1115.7821  | -0.0034  | 0.003       |
| 15   | 2    | 16   | 14    | 1     | 15    | 1115.7884 | 1115.7913  | -0.00287 | 0.003       |
| 15   | 2    | 17   | 14    | 1     | 16    | 1115.8055 | 1115.8003  | 0.00523  | 0.003       |
| 15   | 2    | 18   | 14    | 1     | 17    | 1115.8055 | 1115.8091  | -0.00359 | 0.003       |
| 14   | 2    | 17   | 15    | 1     | 18    | 950.95949 | 950.95869  | 0.0008   | 0.001       |
| 14   | 2    | 16   | 15    | 1     | 17    | 950.97789 | 950.97798  | -0.00009 | 0.001       |
| 14   | 2    | 15   | 15    | 1     | 16    | 950.99639 | 950.99744  | -0.00105 | 0.001       |
| 14   | 2    | 14   | 15    | 1     | 15    | 951.01635 | 951.01696  | -0.00061 | 0.001       |
| 14   | 2    | 13   | 15    | 1     | 14    | 951.03798 | 951.03641  | 0.00157  | 0.001       |
| 14   | 2    | 12   | 15    | 1     | 13    | 951.05629 | 951.05571  | 0.00058  | 0.001       |
| 14   | 2    | 11   | 15    | 1     | 12    | 951.07432 | 951.07477  | -0.00045 | 0.001       |
| 16   | 2    | 13   | 15    | 1     | 12    | 1119.2591 | 1119.2588  | 0.00032  | 0.003       |
| 16   | 2    | 14   | 15    | 1     | 13    | 1119.2698 | 1119.2679  | 0.00191  | 0.003       |
| 16   | 2    | 15   | 15    | 1     | 14    | 1119.2698 | 1119.2768  | -0.00704 | 0.01        |
| 16   | 2    | 16   | 15    | 1     | 15    | 1119.2874 | 1119.2856  | 0.00176  | 0.003       |
| 16   | 2    | 17   | 15    | 1     | 16    | 1119.2874 | 1119.2943  | -0.00687 | 0.01        |
| 16   | 2    | 18   | 15    | 1     | 17    | 1119.3021 | 1119.3028  | -0.00065 | 0.003       |
| 16   | 2    | 19   | 15    | 1     | 18    | 1119.314  | 1119.311   | 0.00296  | 0.003       |
| 15   | 2    | 18   | 16    | 1     | 19    | 943.78887 | 943.7889   | -0.00003 | 0.001       |
| 15   | 2    | 17   | 16    | 1     | 18    | 943.80846 | 943.80835  | 0.00011  | 0.001       |
| 15   | 2    | 16   | 16    | 1     | 17    | 943.82741 | 943.82795  | -0.00054 | 0.001       |
| 15   | 2    | 15   | 16    | 1     | 16    | 943.84852 | 943.84759  | 0.00093  | 0.001       |
| 15   | 2    | 14   | 16    | 1     | 15    | 943.86584 | 943.86718  | -0.00134 | 0.001       |
| 15   | 2    | 13   | 16    | 1     | 14    | 943.88825 | 943.88664  | 0.00161  | 0.001       |
| 15   | 2    | 12   | 16    | 1     | 13    | 943.90497 | 943.90587  | -0.0009  | 0.001       |
| 17   | 2    | 14   | 16    | 1     | 13    | 1122.6143 | 1122.6155  | -0.00121 | 0.003       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 17   | 2    | 15   | 16    | 1     | 14    | 1122.6265 | 1122.6241  | 0.0024   | 0.003       |
| 17   | 2    | 16   | 16    | 1     | 15    | 1122.6265 | 1122.6325  | -0.00603 | 0.003       |
| 17   | 2    | 17   | 16    | 1     | 16    | 1122.6415 | 1122.6408  | 0.00071  | 0.003       |
| 17   | 2    | 18   | 16    | 1     | 17    | 1122.6497 | 1122.6489  | 0.00081  | 0.003       |
| 17   | 2    | 19   | 16    | 1     | 18    | 1122.6497 | 1122.6568  | -0.00712 | 0.003       |
| 17   | 2    | 20   | 16    | 1     | 19    | 1122.6639 | 1122.6646  | -0.00068 | 0.003       |
| 16   | 2    | 19   | 17    | 1     | 20    | 936.53135 | 936.53045  | 0.0009   | 0.001       |
| 16   | 2    | 18   | 17    | 1     | 19    | 936.54954 | 936.55004  | -0.0005  | 0.001       |
| 16   | 2    | 17   | 17    | 1     | 18    | 936.56732 | 936.56977  | -0.00245 | 0.001       |
| 16   | 2    | 16   | 17    | 1     | 17    | 936.58806 | 936.58953  | -0.00147 | 0.001       |
| 16   | 2    | 15   | 17    | 1     | 16    | 936.60967 | 936.60926  | 0.00041  | 0.001       |
| 16   | 2    | 14   | 17    | 1     | 15    | 936.62887 | 936.62885  | 0.00002  | 0.001       |
| 16   | 2    | 13   | 17    | 1     | 14    | 936.64779 | 936.64825  | -0.00046 | 0.001       |
| 18   | 2    | 15   | 17    | 1     | 14    | 1125.8254 | 1125.822   | 0.00336  | 0.01        |
| 18   | 2    | 16   | 17    | 1     | 15    | 1125.8254 | 1125.8301  | -0.0047  | 0.01        |
| 18   | 2    | 17   | 17    | 1     | 16    | 1125.8353 | 1125.838   | -0.00269 | 0.01        |
| 18   | 2    | 18   | 17    | 1     | 17    | 1125.8509 | 1125.8457  | 0.00519  | 0.01        |
| 18   | 2    | 19   | 17    | 1     | 18    | 1125.8509 | 1125.8533  | -0.00236 | 0.01        |
| 18   | 2    | 20   | 17    | 1     | 19    | 1125.8509 | 1125.8606  | -0.00974 | 0.01        |
| 18   | 2    | 21   | 17    | 1     | 20    | 1125.8635 | 1125.8679  | -0.00435 | 0.01        |
| 17   | 2    | 20   | 18    | 1     | 21    | 929.18647 | 929.18504  | 0.00143  | 0.001       |
| 17   | 2    | 19   | 18    | 1     | 20    | 929.2087  | 929.20476  | 0.00394  | 0.001       |
| 17   | 2    | 18   | 18    | 1     | 19    | 929.22664 | 929.2246   | 0.00204  | 0.001       |
| 17   | 2    | 17   | 18    | 1     | 18    | 929.24548 | 929.24448  | 0.001    | 0.001       |
| 17   | 2    | 16   | 18    | 1     | 17    | 929.2643  | 929.26432  | -0.00002 | 0.001       |
| 17   | 2    | 15   | 18    | 1     | 16    | 929.28297 | 929.28405  | -0.00108 | 0.001       |
| 17   | 2    | 14   | 18    | 1     | 15    | 929.30335 | 929.3036   | -0.00025 | 0.001       |
| 19   | 2    | 16   | 18    | 1     | 15    | 1128.8826 | 1128.8765  | 0.00607  | 0.006       |
| 19   | 2    | 17   | 18    | 1     | 16    | 1128.8826 | 1128.8841  | -0.00145 | 0.002       |
| 19   | 2    | 18   | 18    | 1     | 17    | 1128.8826 | 1128.8914  | -0.00879 | 0.01        |
| 19   | 2    | 19   | 18    | 1     | 18    | 1128.898  | 1128.8986  | -0.00056 | 0.002       |
| 19   | 2    | 20   | 18    | 1     | 19    | 1128.898  | 1128.9056  | -0.00755 | 0.01        |
| 19   | 2    | 21   | 18    | 1     | 20    | 1128.9135 | 1128.9124  | 0.00113  | 0.002       |
| 19   | 2    | 22   | 18    | 1     | 21    | 1128.9135 | 1128.919   | -0.00551 | 0.008       |
| 18   | 2    | 21   | 19    | 1     | 22    | 921.74752 | 921.75434  | -0.00682 | 0.01        |
| 18   | 2    | 20   | 19    | 1     | 21    | 921.77298 | 921.77417  | -0.00119 | 0.001       |
| 18   | 2    | 19   | 19    | 1     | 20    | 921.79499 | 921.79412  | 0.00087  | 0.001       |
| 18   | 2    | 18   | 19    | 1     | 19    | 921.81629 | 921.8141   | 0.00219  | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 18   | 2    | 17   | 19    | 1     | 18    | 921.83324 | 921.83405  | -0.00081 | 0.001       |
| 18   | 2    | 16   | 19    | 1     | 17    | 921.85431 | 921.8539   | 0.00041  | 0.001       |
| 20   | 2    | 17   | 19    | 1     | 16    | 1131.781  | 1131.7772  | 0.00385  | 0.004       |
| 20   | 2    | 18   | 19    | 1     | 17    | 1131.781  | 1131.7841  | -0.00312 | 0.003       |
| 20   | 2    | 19   | 19    | 1     | 18    | 1131.7928 | 1131.7909  | 0.0019   | 0.002       |
| 20   | 2    | 20   | 19    | 1     | 19    | 1131.7928 | 1131.7975  | -0.00469 | 0.006       |
| 20   | 2    | 21   | 19    | 1     | 20    | 1131.8119 | 1131.8039  | 0.00799  | 0.008       |
| 20   | 2    | 22   | 19    | 1     | 21    | 1131.8119 | 1131.8102  | 0.00174  | 0.002       |
| 20   | 2    | 23   | 19    | 1     | 22    | 1131.8119 | 1131.8162  | -0.00433 | 0.006       |
| 19   | 2    | 22   | 20    | 1     | 23    | 914.24141 | 914.23998  | 0.00143  | 0.001       |
| 19   | 2    | 21   | 20    | 1     | 22    | 914.25873 | 914.25991  | -0.00118 | 0.001       |
| 19   | 2    | 19   | 20    | 1     | 20    | 914.29788 | 914.30003  | -0.00215 | 0.001       |
| 19   | 2    | 18   | 20    | 1     | 19    | 914.31517 | 914.32008  | -0.00491 | 0.005       |
| 19   | 2    | 17   | 20    | 1     | 18    | 914.34063 | 914.34004  | 0.00059  | 0.001       |
| 19   | 2    | 16   | 20    | 1     | 17    | 914.35739 | 914.35985  | -0.00246 | 0.001       |
| 21   | 2    | 18   | 20    | 1     | 17    | 1134.5283 | 1134.5221  | 0.00624  | 0.01        |
| 21   | 2    | 19   | 20    | 1     | 18    | 1134.5283 | 1134.5285  | -0.00016 | 0.01        |
| 21   | 2    | 20   | 20    | 1     | 19    | 1134.5283 | 1134.5347  | -0.00637 | 0.01        |
| 21   | 2    | 21   | 20    | 1     | 20    | 1134.5438 | 1134.5407  | 0.00311  | 0.01        |
| 21   | 2    | 22   | 20    | 1     | 21    | 1134.5541 | 1134.5465  | 0.00758  | 0.01        |
| 21   | 2    | 23   | 20    | 1     | 22    | 1134.5541 | 1134.5522  | 0.00192  | 0.01        |
| 21   | 2    | 24   | 20    | 1     | 23    | 1134.5541 | 1134.5577  | -0.00357 | 0.01        |
| 22   | 2    | 19   | 21    | 1     | 18    | 1137.116  | 1137.1094  | 0.00657  | 0.01        |
| 22   | 2    | 20   | 21    | 1     | 19    | 1137.116  | 1137.1153  | 0.00074  | 0.002       |
| 22   | 2    | 21   | 21    | 1     | 20    | 1137.1259 | 1137.1209  | 0.00502  | 0.005       |
| 22   | 2    | 22   | 21    | 1     | 21    | 1137.1259 | 1137.1263  | -0.00041 | 0.002       |
| 22   | 2    | 23   | 21    | 1     | 22    | 1137.1371 | 1137.1316  | 0.00555  | 0.006       |
| 22   | 2    | 24   | 21    | 1     | 23    | 1137.1371 | 1137.1366  | 0.00048  | 0.002       |
| 22   | 2    | 25   | 21    | 1     | 24    | 1137.1371 | 1137.1415  | -0.0044  | 0.005       |
| 21   | 2    | 24   | 22    | 1     | 25    | 898.96635 | 898.96668  | -0.00033 | 0.001       |
| 21   | 2    | 23   | 22    | 1     | 24    | 898.98662 | 898.98677  | -0.00015 | 0.001       |
| 21   | 2    | 22   | 22    | 1     | 23    | 899.00556 | 899.00697  | -0.00141 | 0.001       |
| 21   | 2    | 21   | 22    | 1     | 22    | 899.02822 | 899.0272   | 0.00102  | 0.001       |
| 21   | 2    | 20   | 22    | 1     | 21    | 899.04671 | 899.04742  | -0.00071 | 0.001       |
| 21   | 2    | 19   | 22    | 1     | 20    | 899.07019 | 899.06756  | 0.00263  | 0.002       |
| 21   | 2    | 18   | 22    | 1     | 19    | 899.08969 | 899.08757  | 0.00212  | 0.002       |
| 23   | 2    | 20   | 22    | 1     | 19    | 1139.5446 | 1139.5375  | 0.00715  | 0.008       |
| 23   | 2    | 21   | 22    | 1     | 20    | 1139.5446 | 1139.5427  | 0.00192  | 0.002       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 23   | 2    | 22   | 22    | 1     | 21    | 1139.5446 | 1139.5477  | -0.00311 | 0.003       |
| 23   | 2    | 23   | 22    | 1     | 22    | 1139.5527 | 1139.5525  | 0.00016  | 0.002       |
| 23   | 2    | 24   | 22    | 1     | 23    | 1139.5609 | 1139.5572  | 0.00373  | 0.005       |
| 23   | 2    | 25   | 22    | 1     | 24    | 1139.5609 | 1139.5616  | -0.00073 | 0.005       |
| 23   | 2    | 26   | 22    | 1     | 25    | 1139.5609 | 1139.5659  | -0.00501 | 0.006       |
| 24   | 2    | 21   | 23    | 1     | 20    | 1141.8068 | 1141.8043  | 0.00252  | 0.003       |
| 24   | 2    | 22   | 23    | 1     | 21    | 1141.8068 | 1141.8089  | -0.00211 | 0.003       |
| 24   | 2    | 23   | 23    | 1     | 22    | 1141.8068 | 1141.8133  | -0.00653 | 0.008       |
| 24   | 2    | 24   | 23    | 1     | 23    | 1141.8205 | 1141.8176  | 0.00295  | 0.003       |
| 24   | 2    | 25   | 23    | 1     | 24    | 1141.8205 | 1141.8216  | -0.00107 | 0.002       |
| 24   | 2    | 26   | 23    | 1     | 25    | 1141.8205 | 1141.8254  | -0.0049  | 0.005       |
| 24   | 2    | 27   | 23    | 1     | 26    | 1141.8205 | 1141.8291  | -0.00856 | 0.01        |
| 25   | 2    | 22   | 24    | 1     | 21    | 1143.914  | 1143.9081  | 0.00588  | 0.01        |
| 25   | 2    | 23   | 24    | 1     | 22    | 1143.914  | 1143.9121  | 0.00187  | 0.002       |
| 25   | 2    | 24   | 24    | 1     | 23    | 1143.914  | 1143.9159  | -0.00193 | 0.002       |
| 25   | 2    | 25   | 24    | 1     | 24    | 1143.9244 | 1143.9195  | 0.00487  | 0.006       |
| 25   | 2    | 26   | 24    | 1     | 25    | 1143.9244 | 1143.9229  | 0.00148  | 0.002       |
| 25   | 2    | 27   | 24    | 1     | 26    | 1143.9244 | 1143.9261  | -0.00172 | 0.002       |
| 25   | 2    | 28   | 24    | 1     | 27    | 1143.9244 | 1143.9291  | -0.00474 | 0.005       |
| 26   | 2    | 23   | 25    | 1     | 22    | 1145.8503 | 1145.8471  | 0.00316  | 0.003       |
| 26   | 2    | 24   | 25    | 1     | 23    | 1145.8503 | 1145.8505  | -0.00023 | 0.002       |
| 26   | 2    | 25   | 25    | 1     | 24    | 1145.8503 | 1145.8537  | -0.0034  | 0.005       |
| 26   | 2    | 26   | 25    | 1     | 25    | 1145.8603 | 1145.8567  | 0.00364  | 0.005       |
| 26   | 2    | 27   | 25    | 1     | 26    | 1145.8603 | 1145.8594  | 0.00089  | 0.002       |
| 26   | 2    | 28   | 25    | 1     | 27    | 1145.8603 | 1145.862   | -0.00167 | 0.002       |
| 26   | 2    | 29   | 25    | 1     | 28    | 1145.8603 | 1145.8644  | -0.00405 | 0.004       |
| 27   | 2    | 24   | 26    | 1     | 23    | 1147.6211 | 1147.6195  | 0.00156  | 0.002       |
| 27   | 2    | 25   | 26    | 1     | 24    | 1147.6211 | 1147.6223  | -0.0012  | 0.002       |
| 27   | 2    | 26   | 26    | 1     | 25    | 1147.6211 | 1147.6248  | -0.00372 | 0.004       |
| 27   | 2    | 27   | 26    | 1     | 26    | 1147.6316 | 1147.6271  | 0.00447  | 0.004       |
| 27   | 2    | 28   | 26    | 1     | 27    | 1147.6317 | 1147.6292  | 0.00247  | 0.002       |
| 27   | 2    | 29   | 26    | 1     | 28    | 1147.6317 | 1147.6311  | 0.00056  | 0.002       |
| 27   | 2    | 30   | 26    | 1     | 29    | 1147.6317 | 1147.6329  | -0.00115 | 0.002       |
| 28   | 2    | 25   | 27    | 1     | 24    | 1149.233  | 1149.2235  | 0.00949  | 0.01        |
| 28   | 2    | 26   | 27    | 1     | 25    | 1149.233  | 1149.2256  | 0.00739  | 0.01        |
| 28   | 2    | 27   | 27    | 1     | 26    | 1149.233  | 1149.2275  | 0.00552  | 0.01        |
| 28   | 2    | 28   | 27    | 1     | 27    | 1149.233  | 1149.2291  | 0.00387  | 0.003       |
| 28   | 2    | 29   | 27    | 1     | 28    | 1149.233  | 1149.2306  | 0.00243  | 0.002       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 28   | 2    | 30   | 27    | 1     | 29    | 1149.233  | 1149.2318  | 0.00119  | 0.002       |
| 28   | 2    | 31   | 27    | 1     | 30    | 1149.233  | 1149.2329  | 0.00015  | 0.002       |
| 29   | 2    | 26   | 28    | 1     | 25    | 1150.6601 | 1150.6572  | 0.00287  | 0.003       |
| 29   | 2    | 27   | 28    | 1     | 26    | 1150.6601 | 1150.6587  | 0.00144  | 0.002       |
| 29   | 2    | 28   | 28    | 1     | 27    | 1150.6601 | 1150.6599  | 0.00023  | 0.002       |
| 29   | 2    | 29   | 28    | 1     | 28    | 1150.6601 | 1150.6609  | -0.00075 | 0.002       |
| 29   | 2    | 30   | 28    | 1     | 29    | 1150.6601 | 1150.6616  | -0.00151 | 0.002       |
| 29   | 2    | 31   | 28    | 1     | 30    | 1150.6601 | 1150.6622  | -0.00207 | 0.003       |
| 29   | 2    | 32   | 28    | 1     | 31    | 1150.6601 | 1150.6625  | -0.00244 | 0.003       |
| 30   | 2    | 27   | 29    | 1     | 26    | 1151.9218 | 1151.9189  | 0.00292  | 0.003       |
| 30   | 2    | 28   | 29    | 1     | 27    | 1151.9218 | 1151.9197  | 0.00215  | 0.002       |
| 30   | 2    | 29   | 29    | 1     | 28    | 1151.9218 | 1151.9202  | 0.00163  | 0.002       |
| 30   | 2    | 30   | 29    | 1     | 29    | 1151.9218 | 1151.9205  | 0.00133  | 0.002       |
| 30   | 2    | 31   | 29    | 1     | 30    | 1151.9218 | 1151.9206  | 0.00125  | 0.002       |
| 30   | 2    | 32   | 29    | 1     | 31    | 1151.9218 | 1151.9204  | 0.00138  | 0.002       |
| 30   | 2    | 33   | 29    | 1     | 32    | 1151.9218 | 1151.9201  | 0.00171  | 0.002       |
| 31   | 2    | 28   | 30    | 1     | 27    | 1153.008  | 1153.0067  | 0.00133  | 0.002       |
| 31   | 2    | 29   | 30    | 1     | 28    | 1153.008  | 1153.0068  | 0.00125  | 0.002       |
| 31   | 2    | 30   | 30    | 1     | 29    | 1153.008  | 1153.0066  | 0.00142  | 0.002       |
| 31   | 2    | 31   | 30    | 1     | 30    | 1153.008  | 1153.0062  | 0.00181  | 0.002       |
| 31   | 2    | 32   | 30    | 1     | 31    | 1153.008  | 1153.0056  | 0.00243  | 0.002       |
| 31   | 2    | 33   | 30    | 1     | 32    | 1153.008  | 1153.0047  | 0.00327  | 0.003       |
| 31   | 2    | 34   | 30    | 1     | 33    | 1153.008  | 1153.0037  | 0.0043   | 0.004       |
| 32   | 2    | 29   | 31    | 1     | 28    | 1153.918  | 1153.9188  | -0.00076 | 0.001       |
| 32   | 2    | 30   | 31    | 1     | 29    | 1153.918  | 1153.9181  | -0.00014 | 0.001       |
| 32   | 2    | 31   | 31    | 1     | 30    | 1153.918  | 1153.9173  | 0.00072  | 0.001       |
| 32   | 2    | 32   | 31    | 1     | 31    | 1153.918  | 1153.9162  | 0.00183  | 0.002       |
| 32   | 2    | 33   | 31    | 1     | 32    | 1153.918  | 1153.9148  | 0.00316  | 0.003       |
| 32   | 2    | 34   | 31    | 1     | 33    | 1153.918  | 1153.9133  | 0.0047   | 0.005       |
| 32   | 2    | 35   | 31    | 1     | 34    | 1153.918  | 1153.9115  | 0.00646  | 0.007       |
| 33   | 2    | 30   | 32    | 1     | 29    | 1154.6496 | 1154.6534  | -0.00375 | 0.003       |
| 33   | 2    | 31   | 32    | 1     | 30    | 1154.6496 | 1154.652   | -0.00242 | 0.002       |
| 33   | 2    | 32   | 32    | 1     | 31    | 1154.6496 | 1154.6504  | -0.00084 | 0.002       |
| 33   | 2    | 33   | 32    | 1     | 32    | 1154.6496 | 1154.6486  | 0.00098  | 0.002       |
| 33   | 2    | 34   | 32    | 1     | 33    | 1154.6496 | 1154.6466  | 0.00303  | 0.003       |
| 33   | 2    | 35   | 32    | 1     | 34    | 1154.6496 | 1154.6443  | 0.00531  | 0.01        |
| 33   | 2    | 36   | 32    | 1     | 35    | 1154.6496 | 1154.6418  | 0.00779  | 0.01        |
| 34   | 2    | 33   | 33    | 1     | 32    | 1155.2007 | 1155.2042  | -0.00354 | 0.01        |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 34   | 2    | 31   | 33    | 1     | 30    | 1155.2007 | 1155.2086  | -0.0079  | 0.01        |
| 34   | 2    | 32   | 33    | 1     | 31    | 1155.2007 | 1155.2066  | -0.00585 | 0.01        |
| 34   | 2    | 34   | 33    | 1     | 33    | 1155.2007 | 1155.2017  | -0.00099 | 0.002       |
| 34   | 2    | 35   | 33    | 1     | 34    | 1155.2007 | 1155.1989  | 0.00179  | 0.002       |
| 34   | 2    | 36   | 33    | 1     | 35    | 1155.2007 | 1155.1959  | 0.0048   | 0.01        |
| 34   | 2    | 37   | 33    | 1     | 36    | 1155.2007 | 1155.1927  | 0.00803  | 0.01        |
| 35   | 2    | 32   | 34    | 1     | 31    | 1155.5817 | 1155.5827  | -0.00098 | 0.002       |
| 35   | 2    | 33   | 34    | 1     | 32    | 1155.5687 | 1155.5799  | -0.0112  | 1           |
| 35   | 2    | 34   | 34    | 1     | 33    | 1155.5687 | 1155.5769  | -0.00815 | 1           |
| 35   | 2    | 35   | 34    | 1     | 34    | 1155.5687 | 1155.5736  | -0.00486 | 1           |
| 35   | 2    | 36   | 34    | 1     | 35    | 1155.5687 | 1155.57    | -0.00133 | 0.002       |
| 35   | 2    | 37   | 34    | 1     | 36    | 1155.5687 | 1155.5663  | 0.00243  | 0.003       |
| 35   | 2    | 38   | 34    | 1     | 37    | 1155.5687 | 1155.5623  | 0.00641  | 1           |
| 36   | 2    | 34   | 35    | 1     | 33    | 1155.7699 | 1155.7702  | -0.00033 | 0.002       |
| 36   | 2    | 35   | 35    | 1     | 34    | 1155.7699 | 1155.7664  | 0.00346  | 1           |
| 36   | 2    | 36   | 35    | 1     | 35    | 1155.7556 | 1155.7624  | -0.00679 | 1           |
| 36   | 2    | 37   | 35    | 1     | 36    | 1155.7556 | 1155.7581  | -0.0025  | 0.002       |
| 36   | 2    | 33   | 35    | 1     | 32    | 1155.7699 | 1155.7738  | -0.00386 | 0.003       |
| 36   | 2    | 38   | 35    | 1     | 37    | 1155.7556 | 1155.7536  | 0.00202  | 0.003       |
| 36   | 2    | 39   | 35    | 1     | 38    | 1155.7556 | 1155.7488  | 0.00676  | 1           |
| 37   | 2    | 34   | 36    | 1     | 33    | 1155.7699 | 1155.78    | -0.01008 | 1           |
| 37   | 2    | 35   | 36    | 1     | 34    | 1155.7699 | 1155.7757  | -0.00579 | 0.005       |
| 37   | 2    | 36   | 36    | 1     | 35    | 1155.7699 | 1155.7711  | -0.00124 | 0.002       |
| 3    | 3    | 6    | 4     | 2     | 7     | 994.18893 | 994.18881  | 0.00012  | 0.001       |
| 3    | 3    | 5    | 4     | 2     | 6     | 994.2047  | 994.20479  | -0.00009 | 0.001       |
| 3    | 3    | 4    | 4     | 2     | 5     | 994.22946 | 994.22334  | 0.00612  | 0.005       |
| 3    | 3    | 3    | 4     | 2     | 4     | 994.24777 | 994.24246  | 0.00531  | 0.005       |
| 3    | 3    | 2    | 4     | 2     | 3     | 994.2597  | 994.26067  | -0.00097 | 0.001       |
| 3    | 3    | 1    | 4     | 2     | 2     | 994.2793  | 994.27706  | 0.00224  | 0.003       |
| 3    | 3    | 0    | 4     | 2     | 1     | 994.29682 | 994.2912   | 0.00562  | 0.005       |
| 5    | 3    | 2    | 4     | 2     | 1     | 1042.5966 | 1042.5966  | 0.00005  | 0.001       |
| 5    | 3    | 3    | 4     | 2     | 2     | 1042.6104 | 1042.6094  | 0.00098  | 0.001       |
| 5    | 3    | 4    | 4     | 2     | 3     | 1042.6239 | 1042.623   | 0.00095  | 0.001       |
| 5    | 3    | 5    | 4     | 2     | 4     | 1042.637  | 1042.637   | 0.00001  | 0.001       |
| 5    | 3    | 6    | 4     | 2     | 5     | 1042.649  | 1042.6512  | -0.00219 | 0.001       |
| 5    | 3    | 7    | 4     | 2     | 6     | 1042.6631 | 1042.665   | -0.00192 | 0.001       |
| 5    | 3    | 8    | 4     | 2     | 7     | 1042.678  | 1042.6777  | 0.0003   | 0.001       |
| 4    | 3    | 7    | 5     | 2     | 8     | 988.22415 | 988.22351  | 0.00064  | 0.003       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 4    | 3    | 6    | 5     | 2     | 7     | 988.23952 | 988.24001  | -0.00049 | 0.003       |
| 4    | 3    | 5    | 5     | 2     | 6     | 988.25748 | 988.25805  | -0.00057 | 0.003       |
| 4    | 3    | 4    | 5     | 2     | 5     | 988.28042 | 988.27646  | 0.00396  | 0.001       |
| 4    | 3    | 3    | 5     | 2     | 4     | 988.2958  | 988.29438  | 0.00142  | 0.001       |
| 4    | 3    | 2    | 5     | 2     | 3     | 988.30849 | 988.3112   | -0.00271 | 0.001       |
| 4    | 3    | 1    | 5     | 2     | 2     | 988.32377 | 988.32656  | -0.00279 | 0.001       |
| 6    | 3    | 5    | 5     | 2     | 4     | 1047.3794 | 1047.3795  | -0.00008 | 0.001       |
| 6    | 3    | 6    | 5     | 2     | 5     | 1047.3927 | 1047.3929  | -0.00018 | 0.001       |
| 6    | 3    | 7    | 5     | 2     | 6     | 1047.4066 | 1047.4063  | 0.00031  | 0.001       |
| 6    | 3    | 8    | 5     | 2     | 7     | 1047.4197 | 1047.4194  | 0.0003   | 0.001       |
| 6    | 3    | 9    | 5     | 2     | 8     | 1047.4333 | 1047.4318  | 0.00154  | 0.001       |
| 5    | 3    | 8    | 6     | 2     | 9     | 982.1472  | 982.14767  | -0.00047 | 0.003       |
| 5    | 3    | 7    | 6     | 2     | 8     | 982.16537 | 982.16459  | 0.00078  | 0.003       |
| 7    | 3    | 4    | 6     | 2     | 3     | 1051.9812 | 1051.9789  | 0.0023   | 0.003       |
| 7    | 3    | 5    | 6     | 2     | 4     | 1051.9934 | 1051.9915  | 0.00195  | 0.003       |
| 7    | 3    | 6    | 6     | 2     | 5     | 1052.0054 | 1052.0042  | 0.00122  | 0.003       |
| 7    | 3    | 7    | 6     | 2     | 6     | 1052.0159 | 1052.017   | -0.00112 | 0.003       |
| 7    | 3    | 8    | 6     | 2     | 7     | 1052.0308 | 1052.0298  | 0.00099  | 0.003       |
| 7    | 3    | 9    | 6     | 2     | 8     | 1052.0441 | 1052.0423  | 0.00177  | 0.003       |
| 7    | 3    | 10   | 6     | 2     | 9     | 1052.0549 | 1052.0543  | 0.00058  | 0.003       |
| 6    | 3    | 9    | 7     | 2     | 10    | 975.96444 | 975.96318  | 0.00126  | 0.003       |
| 6    | 3    | 8    | 7     | 2     | 9     | 975.98038 | 975.98047  | -0.00009 | 0.003       |
| 6    | 3    | 7    | 7     | 2     | 8     | 976.00176 | 975.99849  | 0.00327  | 0.003       |
| 6    | 3    | 6    | 7     | 2     | 7     | 976.01901 | 976.01672  | 0.00229  | 0.003       |
| 6    | 3    | 5    | 7     | 2     | 6     | 976.03629 | 976.03471  | 0.00158  | 0.003       |
| 6    | 3    | 4    | 7     | 2     | 5     | 976.05318 | 976.05212  | 0.00106  | 0.003       |
| 6    | 3    | 3    | 7     | 2     | 4     | 976.06624 | 976.06872  | -0.00248 | 0.003       |
| 8    | 3    | 5    | 7     | 2     | 4     | 1056.4702 | 1056.4708  | -0.00058 | 0.003       |
| 8    | 3    | 6    | 7     | 2     | 5     | 1056.4826 | 1056.483   | -0.0004  | 0.003       |
| 8    | 3    | 7    | 7     | 2     | 6     | 1056.4954 | 1056.4953  | 0.00011  | 0.003       |
| 8    | 3    | 8    | 7     | 2     | 7     | 1056.5073 | 1056.5076  | -0.00031 | 0.003       |
| 8    | 3    | 9    | 7     | 2     | 8     | 1056.5195 | 1056.5198  | -0.00033 | 0.003       |
| 8    | 3    | 10   | 7     | 2     | 9     | 1056.5328 | 1056.5318  | 0.00097  | 0.003       |
| 8    | 3    | 11   | 7     | 2     | 10    | 1056.5447 | 1056.5434  | 0.0013   | 0.003       |
| 7    | 3    | 10   | 8     | 2     | 11    | 969.67406 | 969.67192  | 0.00214  | 0.001       |
| 7    | 3    | 9    | 8     | 2     | 10    | 969.68993 | 969.68953  | 0.0004   | 0.001       |
| 7    | 3    | 8    | 8     | 2     | 9     | 969.70668 | 969.70769  | -0.00101 | 0.001       |
| 7    | 3    | 7    | 8     | 2     | 8     | 969.72567 | 969.726    | -0.00033 | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed   | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|------------|------------|----------|-------------|
| 7    | 3    | 6    | 8     | 2     | 7     | 969.74527  | 969.74414  | 0.00113  | 0.001       |
| 7    | 3    | 5    | 8     | 2     | 6     | 969.76395  | 969.76182  | 0.00213  | 0.001       |
| 7    | 3    | 4    | 8     | 2     | 5     | 969.77845  | 969.77883  | -0.00038 | 0.001       |
| 9    | 3    | 6    | 8     | 2     | 5     | 1060.8277  | 1060.8273  | 0.00044  | 0.003       |
| 9    | 3    | 7    | 8     | 2     | 6     | 1060.8405  | 1060.8391  | 0.0014   | 0.003       |
| 9    | 3    | 8    | 8     | 2     | 7     | 1060.8557  | 1060.8509  | 0.00476  | 0.003       |
| 9    | 3    | 9    | 8     | 2     | 8     | 1060.8663  | 1060.8628  | 0.00355  | 0.003       |
| 9    | 3    | 10   | 8     | 2     | 9     | 1060.8774  | 1060.8745  | 0.00295  | 0.003       |
| 9    | 3    | 11   | 8     | 2     | 10    | 1060.8891  | 1060.8859  | 0.00316  | 0.003       |
| 9    | 3    | 12   | 8     | 2     | 11    | 1060.9007  | 1060.8971  | 0.00362  | 0.003       |
| 10   | 3    | 7    | 9     | 2     | 6     | 1065.0481  | 1065.0464  | 0.00168  | 0.003       |
| 10   | 3    | 8    | 9     | 2     | 7     | 1065.0596  | 1065.0578  | 0.00176  | 0.003       |
| 10   | 3    | 9    | 9     | 2     | 8     | 1065.0742  | 1065.0692  | 0.00497  | 0.003       |
| 10   | 3    | 10   | 9     | 2     | 9     | 1065.0837  | 1065.0805  | 0.00317  | 0.003       |
| 10   | 3    | 12   | 9     | 2     | 11    | 1065.101   | 1065.1027  | -0.0017  | 0.003       |
| 10   | 3    | 13   | 9     | 2     | 12    | 1065.114   | 1065.1134  | 0.00062  | 0.003       |
| 9    | 3    | 12   | 10    | 2     | 13    | 956.77601  | 956.77638  | -0.00037 | 0.001       |
| 11   | 3    | 8    | 10    | 2     | 7     | 1069.1291  | 1069.1263  | 0.00279  | 0.003       |
| 11   | 3    | 9    | 10    | 2     | 8     | 1069.1425  | 1069.1373  | 0.0052   | 0.006       |
| 11   | 3    | 10   | 10    | 2     | 9     | 1069.1425  | 1069.1482  | -0.0057  | 0.006       |
| 11   | 3    | 11   | 10    | 2     | 10    | 1069.1545  | 1069.159   | -0.00451 | 0.006       |
| 11   | 3    | 12   | 10    | 2     | 11    | 1069.1677  | 1069.1697  | -0.00198 | 0.003       |
| 11   | 3    | 13   | 10    | 2     | 12    | 1069.1816  | 1069.1802  | 0.00144  | 0.003       |
| 11   | 3    | 14   | 10    | 2     | 13    | 1069.1933  | 1069.1904  | 0.00293  | 0.003       |
| 10   | 3    | 13   | 11    | 2     | 14    | 950.17507  | 950.17571  | -0.00064 | 0.001       |
| 10   | 3    | 12   | 11    | 2     | 13    | 950.19409  | 950.19413  | -0.00004 | 0.001       |
| 10   | 3    | 11   | 11    | 2     | 12    | 950.21159  | 950.21283  | -0.00124 | 0.001       |
| 10   | 3    | 10   | 11    | 2     | 11    | 950.22793  | 950.2316   | -0.00367 | 0.001       |
| 10   | 3    | 9    | 11    | 2     | 10    | 950.24845  | 950.25027  | -0.00182 | 0.001       |
| 10   | 3    | 8    | 11    | 2     | 9     | 950.26724  | 950.26865  | -0.00141 | 0.001       |
| 10   | 3    | 7    | 11    | 2     | 8     | 950.28493  | 950.28663  | -0.0017  | 0.001       |
| 12   | 3    | 9    | 11    | 2     | 8     | 1073.0707  | 1073.065   | 0.00571  | 0.006       |
| 12   | 3    | 10   | 11    | 2     | 9     | 1073.0707  | 1073.0755  | -0.00482 | 0.005       |
| 12   | 3    | 11   | 11    | 2     | 10    | 1073.0866  | 1073.0859  | 0.00066  | 0.002       |
| 12   | 3    | 13   | 11    | 2     | 12    | 1073.1003  | 1073.1064  | -0.0061  | 0.008       |
| 12   | 3    | 12   | 11    | 2     | 11    | 1073.10034 | 1073.0963  | 0.00409  | 0.005       |
| 12   | 3    | 14   | 11    | 2     | 13    | 1073.1141  | 1073.1164  | -0.00227 | 0.003       |
| 12   | 3    | 15   | 11    | 2     | 14    | 1073.1271  | 1073.1261  | 0.00101  | 0.002       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 11   | 3    | 14   | 12    | 2     | 15    | 943.47791 | 943.4755   | 0.00241  | 0.001       |
| 11   | 3    | 13   | 12    | 2     | 14    | 943.49576 | 943.49414  | 0.00162  | 0.001       |
| 11   | 3    | 12   | 12    | 2     | 13    | 943.51381 | 943.51302  | 0.00079  | 0.001       |
| 11   | 3    | 11   | 12    | 2     | 12    | 943.53336 | 943.53197  | 0.00139  | 0.001       |
| 11   | 3    | 10   | 12    | 2     | 11    | 943.55122 | 943.55081  | 0.00041  | 0.001       |
| 11   | 3    | 9    | 12    | 2     | 10    | 943.57112 | 943.56941  | 0.00171  | 0.001       |
| 13   | 3    | 10   | 12    | 2     | 9     | 1076.862  | 1076.8605  | 0.00148  | 0.001       |
| 13   | 3    | 11   | 12    | 2     | 10    | 1076.8715 | 1076.8706  | 0.00093  | 0.001       |
| 13   | 3    | 12   | 12    | 2     | 11    | 1076.8862 | 1076.8805  | 0.0057   | 0.005       |
| 13   | 3    | 13   | 12    | 2     | 12    | 1076.8862 | 1076.8903  | -0.00409 | 0.003       |
| 13   | 3    | 14   | 12    | 2     | 13    | 1076.8993 | 1076.8999  | -0.00062 | 0.002       |
| 13   | 3    | 15   | 12    | 2     | 14    | 1076.9138 | 1076.9094  | 0.00443  | 0.005       |
| 13   | 3    | 16   | 12    | 2     | 15    | 1076.9138 | 1076.9186  | -0.0048  | 0.005       |
| 14   | 3    | 11   | 13    | 2     | 10    | 1080.5212 | 1080.5109  | 0.01026  | 1           |
| 14   | 3    | 12   | 13    | 2     | 11    | 1080.5212 | 1080.5205  | 0.0007   | 0.002       |
| 14   | 3    | 13   | 13    | 2     | 12    | 1080.5212 | 1080.5299  | -0.00872 | 1           |
| 14   | 3    | 17   | 13    | 2     | 16    | 1080.5667 | 1080.5659  | 0.00077  | 0.002       |
| 15   | 3    | 12   | 14    | 2     | 11    | 1084.0232 | 1084.0143  | 0.00889  | 1           |
| 15   | 3    | 13   | 14    | 2     | 12    | 1084.0232 | 1084.0234  | -0.00016 | 0.003       |
| 15   | 3    | 14   | 14    | 2     | 13    | 1084.0365 | 1084.0323  | 0.00424  | 0.005       |
| 15   | 3    | 15   | 14    | 2     | 14    | 1084.0365 | 1084.041   | -0.0045  | 0.005       |
| 15   | 3    | 16   | 14    | 2     | 15    | 1084.0503 | 1084.0496  | 0.00073  | 0.003       |
| 15   | 3    | 17   | 14    | 2     | 16    | 1084.0503 | 1084.058   | -0.00766 | 1           |
| 15   | 3    | 18   | 14    | 2     | 17    | 1084.0636 | 1084.0661  | -0.00254 | 0.003       |
| 14   | 3    | 11   | 15    | 2     | 12    | 922.90984 | 922.91045  | -0.00061 | 0.001       |
| 16   | 3    | 13   | 15    | 2     | 12    | 1087.3732 | 1087.3687  | 0.00454  | 0.005       |
| 16   | 3    | 14   | 15    | 2     | 13    | 1087.3732 | 1087.3772  | -0.004   | 0.005       |
| 16   | 3    | 15   | 15    | 2     | 14    | 1087.3829 | 1087.3856  | -0.00267 | 0.005       |
| 16   | 3    | 16   | 15    | 2     | 15    | 1087.3964 | 1087.3938  | 0.00263  | 0.005       |
| 16   | 3    | 17   | 15    | 2     | 16    | 1087.3964 | 1087.4018  | -0.00539 | 0.005       |
| 16   | 3    | 18   | 15    | 2     | 17    | 1087.4089 | 1087.4096  | -0.00073 | 0.005       |
| 16   | 3    | 19   | 15    | 2     | 18    | 1087.4185 | 1087.4173  | 0.00123  | 0.005       |
| 15   | 3    | 18   | 16    | 2     | 19    | 915.70969 | 915.71378  | -0.00409 | 0.005       |
| 15   | 3    | 17   | 16    | 2     | 18    | 915.72888 | 915.73319  | -0.00431 | 0.005       |
| 15   | 3    | 16   | 16    | 2     | 17    | 915.74558 | 915.75274  | -0.00716 | 1           |
| 15   | 3    | 15   | 16    | 2     | 16    | 915.77199 | 915.77232  | -0.00033 | 0.002       |
| 15   | 3    | 14   | 16    | 2     | 15    | 915.79541 | 915.79183  | 0.00358  | 0.003       |
| 15   | 3    | 13   | 16    | 2     | 14    | 915.81326 | 915.81118  | 0.00208  | 0.002       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 17   | 3    | 14   | 16    | 2     | 13    | 1090.5784 | 1090.5721  | 0.00634  | 0.01        |
| 17   | 3    | 15   | 16    | 2     | 14    | 1090.5784 | 1090.5801  | -0.00166 | 0.002       |
| 17   | 3    | 16   | 16    | 2     | 15    | 1090.5924 | 1090.5879  | 0.00451  | 0.005       |
| 17   | 3    | 17   | 16    | 2     | 16    | 1090.5924 | 1090.5955  | -0.00314 | 0.003       |
| 17   | 3    | 18   | 16    | 2     | 17    | 1090.6025 | 1090.603   | -0.0005  | 0.002       |
| 17   | 3    | 19   | 16    | 2     | 18    | 1090.6025 | 1090.6103  | -0.00779 | 0.01        |
| 17   | 3    | 20   | 16    | 2     | 19    | 1090.6134 | 1090.6174  | -0.00397 | 0.004       |
| 16   | 3    | 19   | 17    | 2     | 20    | 908.5393  | 908.54159  | -0.00229 | 0.003       |
| 16   | 3    | 18   | 17    | 2     | 19    | 908.5565  | 908.56116  | -0.00466 | 0.005       |
| 16   | 3    | 17   | 17    | 2     | 18    | 908.57535 | 908.58085  | -0.0055  | 0.005       |
| 16   | 3    | 16   | 17    | 2     | 17    | 908.59605 | 908.60057  | -0.00452 | 0.005       |
| 16   | 3    | 15   | 17    | 2     | 16    | 908.61314 | 908.62022  | -0.00708 | 0.01        |
| 16   | 3    | 14   | 17    | 2     | 15    | 908.64275 | 908.63974  | 0.00301  | 0.003       |
| 18   | 3    | 15   | 17    | 2     | 14    | 1093.6273 | 1093.6225  | 0.00477  | 0.005       |
| 18   | 3    | 16   | 17    | 2     | 15    | 1093.6273 | 1093.63    | -0.00269 | 0.003       |
| 18   | 3    | 17   | 17    | 2     | 16    | 1093.6445 | 1093.6373  | 0.00723  | 0.01        |
| 18   | 3    | 18   | 17    | 2     | 17    | 1093.6445 | 1093.6444  | 0.00015  | 0.002       |
| 18   | 3    | 19   | 17    | 2     | 18    | 1093.6445 | 1093.6513  | -0.00676 | 0.01        |
| 18   | 3    | 20   | 17    | 2     | 19    | 1093.6568 | 1093.658   | -0.00117 | 0.002       |
| 18   | 3    | 21   | 17    | 2     | 20    | 1093.6568 | 1093.6645  | -0.00769 | 1           |
| 19   | 3    | 16   | 18    | 2     | 15    | 1096.5223 | 1096.5181  | 0.00416  | 0.004       |
| 19   | 3    | 17   | 18    | 2     | 16    | 1096.5223 | 1096.525   | -0.00274 | 0.003       |
| 19   | 3    | 18   | 18    | 2     | 17    | 1096.5364 | 1096.5318  | 0.00465  | 0.005       |
| 19   | 3    | 19   | 18    | 2     | 18    | 1096.5364 | 1096.5383  | -0.00186 | 0.002       |
| 19   | 3    | 20   | 18    | 2     | 19    | 1096.5364 | 1096.5446  | -0.00819 | 1           |
| 19   | 3    | 21   | 18    | 2     | 20    | 1096.5579 | 1096.5507  | 0.00718  | 1           |
| 19   | 3    | 22   | 18    | 2     | 21    | 1096.5579 | 1096.5567  | 0.00123  | 0.002       |
| 20   | 3    | 17   | 19    | 2     | 16    | 1099.2634 | 1099.2569  | 0.00648  | 1           |
| 20   | 3    | 18   | 19    | 2     | 17    | 1099.2634 | 1099.2633  | 0.00015  | 0.002       |
| 20   | 3    | 19   | 19    | 2     | 18    | 1099.2634 | 1099.2694  | -0.00598 | 1           |
| 20   | 3    | 20   | 19    | 2     | 19    | 1099.2755 | 1099.2753  | 0.00019  | 0.002       |
| 20   | 3    | 21   | 19    | 2     | 20    | 1099.2755 | 1099.281   | -0.00554 | 1           |
| 20   | 3    | 22   | 19    | 2     | 21    | 1099.2875 | 1099.2866  | 0.00091  | 0.002       |
| 20   | 3    | 23   | 19    | 2     | 22    | 1099.2875 | 1099.2919  | -0.00444 | 0.003       |
| 21   | 3    | 18   | 20    | 2     | 17    | 1101.8474 | 1101.8369  | 0.0105   | 1           |
| 21   | 3    | 19   | 20    | 2     | 18    | 1101.8474 | 1101.8427  | 0.00475  | 0.005       |
| 21   | 3    | 20   | 20    | 2     | 19    | 1101.8474 | 1101.8482  | -0.00079 | 0.003       |
| 21   | 3    | 21   | 20    | 2     | 20    | 1101.8474 | 1101.8535  | -0.00613 | 1           |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 21   | 3    | 22   | 20    | 2     | 21    | 1101.8667 | 1101.8587  | 0.00804  | 1           |
| 21   | 3    | 23   | 20    | 2     | 22    | 1101.8667 | 1101.8636  | 0.00309  | 0.003       |
| 21   | 3    | 24   | 20    | 2     | 23    | 1101.8667 | 1101.8684  | -0.00166 | 0.003       |
| 22   | 3    | 19   | 21    | 2     | 18    | 1104.2637 | 1104.2561  | 0.00757  | 1           |
| 22   | 3    | 20   | 21    | 2     | 19    | 1104.2637 | 1104.2613  | 0.00241  | 0.003       |
| 22   | 3    | 21   | 21    | 2     | 20    | 1104.2637 | 1104.2662  | -0.00253 | 0.003       |
| 22   | 3    | 22   | 21    | 2     | 21    | 1104.2637 | 1104.271   | -0.00726 | 1           |
| 22   | 3    | 23   | 21    | 2     | 22    | 1104.2833 | 1104.2755  | 0.00782  | 1           |
| 22   | 3    | 24   | 21    | 2     | 23    | 1104.2833 | 1104.2798  | 0.00349  | 0.003       |
| 22   | 3    | 25   | 21    | 2     | 24    | 1104.2833 | 1104.284   | -0.00065 | 0.003       |
| 23   | 3    | 20   | 22    | 2     | 19    | 1106.5148 | 1106.5127  | 0.00215  | 0.003       |
| 23   | 3    | 21   | 22    | 2     | 20    | 1106.5148 | 1106.5172  | -0.00239 | 0.003       |
| 23   | 3    | 22   | 22    | 2     | 21    | 1106.5248 | 1106.5215  | 0.00328  | 0.003       |
| 23   | 3    | 23   | 22    | 2     | 22    | 1106.5248 | 1106.5256  | -0.00083 | 0.003       |
| 23   | 3    | 24   | 22    | 2     | 23    | 1106.538  | 1106.5295  | 0.00846  | 1           |
| 23   | 3    | 25   | 22    | 2     | 24    | 1106.538  | 1106.5332  | 0.00476  | 0.003       |
| 23   | 3    | 26   | 22    | 2     | 25    | 1106.538  | 1106.5368  | 0.00125  | 0.003       |
| 24   | 3    | 21   | 23    | 2     | 20    | 1108.613  | 1108.6045  | 0.00852  | 1           |
| 24   | 3    | 22   | 23    | 2     | 21    | 1108.613  | 1108.6084  | 0.0046   | 0.005       |
| 24   | 3    | 23   | 23    | 2     | 22    | 1108.613  | 1108.6121  | 0.00089  | 0.003       |
| 24   | 3    | 24   | 23    | 2     | 23    | 1108.613  | 1108.6156  | -0.00259 | 0.003       |
| 24   | 3    | 25   | 23    | 2     | 24    | 1108.6286 | 1108.6189  | 0.00974  | 1           |
| 24   | 3    | 26   | 23    | 2     | 25    | 1108.6286 | 1108.6219  | 0.00667  | 1           |
| 24   | 3    | 27   | 23    | 2     | 26    | 1108.6286 | 1108.6248  | 0.0038   | 0.004       |
| 25   | 3    | 22   | 24    | 2     | 21    | 1110.5352 | 1110.5297  | 0.00555  | 1           |
| 25   | 3    | 23   | 24    | 2     | 22    | 1110.5352 | 1110.5329  | 0.00226  | 0.002       |
| 25   | 3    | 24   | 24    | 2     | 23    | 1110.5352 | 1110.536   | -0.00081 | 0.002       |
| 25   | 3    | 25   | 24    | 2     | 24    | 1110.5352 | 1110.5389  | -0.00365 | 0.003       |
| 25   | 3    | 26   | 24    | 2     | 25    | 1110.5352 | 1110.5415  | -0.00628 | 1           |
| 25   | 3    | 27   | 24    | 2     | 26    | 1110.5352 | 1110.5439  | -0.0087  | 1           |
| 25   | 3    | 28   | 24    | 2     | 27    | 1110.5352 | 1110.5461  | -0.01091 | 1           |
| 26   | 3    | 23   | 25    | 2     | 22    | 1112.2944 | 1112.2862  | 0.00822  | 1           |
| 26   | 3    | 24   | 25    | 2     | 23    | 1112.2944 | 1112.2888  | 0.00557  | 1           |
| 26   | 3    | 25   | 25    | 2     | 24    | 1112.2944 | 1112.2913  | 0.00315  | 1           |
| 26   | 3    | 26   | 25    | 2     | 25    | 1112.2944 | 1112.2934  | 0.00096  | 0.002       |
| 26   | 3    | 27   | 25    | 2     | 26    | 1112.2944 | 1112.2954  | -0.00101 | 0.002       |
| 26   | 3    | 28   | 25    | 2     | 27    | 1112.2944 | 1112.2972  | -0.00277 | 0.002       |
| 26   | 3    | 29   | 25    | 2     | 28    | 1112.2944 | 1112.2987  | -0.00432 | 1           |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 27   | 3    | 24   | 26    | 2     | 23    | 1113.8793 | 1113.8721  | 0.00721  | 1           |
| 27   | 3    | 25   | 26    | 2     | 24    | 1113.8793 | 1113.8741  | 0.00521  | 1           |
| 27   | 3    | 26   | 26    | 2     | 25    | 1113.8793 | 1113.8759  | 0.00345  | 0.004       |
| 27   | 3    | 27   | 26    | 2     | 26    | 1113.8793 | 1113.8774  | 0.00193  | 0.003       |
| 27   | 3    | 28   | 26    | 2     | 27    | 1113.8793 | 1113.8787  | 0.00062  | 0.001       |
| 27   | 3    | 29   | 26    | 2     | 28    | 1113.8793 | 1113.8798  | -0.00046 | 0.001       |
| 27   | 3    | 30   | 26    | 2     | 29    | 1113.8793 | 1113.8806  | -0.00134 | 0.001       |
| 28   | 3    | 25   | 27    | 2     | 24    | 1115.29   | 1115.2854  | 0.00461  | 0.01        |
| 28   | 3    | 26   | 27    | 2     | 25    | 1115.29   | 1115.2867  | 0.00328  | 0.004       |
| 28   | 3    | 27   | 27    | 2     | 26    | 1115.29   | 1115.2878  | 0.00219  | 0.003       |
| 28   | 3    | 28   | 27    | 2     | 27    | 1115.29   | 1115.2887  | 0.00134  | 0.001       |
| 28   | 3    | 29   | 27    | 2     | 28    | 1115.29   | 1115.2893  | 0.00072  | 0.001       |
| 28   | 3    | 30   | 27    | 2     | 29    | 1115.29   | 1115.2897  | 0.00031  | 0.001       |
| 28   | 3    | 31   | 27    | 2     | 30    | 1115.29   | 1115.2899  | 0.00012  | 0.001       |
| 29   | 3    | 26   | 28    | 2     | 25    | 1116.5253 | 1116.5241  | 0.00121  | 0.001       |
| 29   | 3    | 27   | 28    | 2     | 26    | 1116.5253 | 1116.5247  | 0.00056  | 0.001       |
| 29   | 3    | 28   | 28    | 2     | 27    | 1116.5253 | 1116.5251  | 0.00016  | 0.001       |
| 29   | 3    | 29   | 28    | 2     | 28    | 1116.5253 | 1116.5253  | -0.00001 | 0.001       |
| 29   | 3    | 30   | 28    | 2     | 29    | 1116.5253 | 1116.5252  | 0.00006  | 0.001       |
| 29   | 3    | 31   | 28    | 2     | 30    | 1116.5253 | 1116.525   | 0.00035  | 0.001       |
| 29   | 3    | 32   | 28    | 2     | 31    | 1116.5253 | 1116.5244  | 0.00086  | 0.001       |
| 30   | 3    | 27   | 29    | 2     | 26    | 1117.5873 | 1117.5862  | 0.00113  | 0.001       |
| 30   | 3    | 28   | 29    | 2     | 27    | 1117.5873 | 1117.5861  | 0.00117  | 0.001       |
| 30   | 3    | 29   | 29    | 2     | 28    | 1117.5873 | 1117.5858  | 0.00146  | 0.003       |
| 30   | 3    | 30   | 29    | 2     | 29    | 1117.5873 | 1117.5853  | 0.00199  | 0.003       |
| 30   | 3    | 31   | 29    | 2     | 30    | 1117.5873 | 1117.5845  | 0.00276  | 0.004       |
| 30   | 3    | 32   | 29    | 2     | 31    | 1117.5873 | 1117.5835  | 0.00376  | 1           |
| 30   | 3    | 33   | 29    | 2     | 32    | 1117.5873 | 1117.5823  | 0.00498  | 1           |
| 31   | 3    | 28   | 30    | 2     | 27    | 1118.466  | 1118.4696  | -0.00363 | 0.002       |
| 31   | 3    | 29   | 30    | 2     | 28    | 1118.466  | 1118.4689  | -0.00289 | 0.002       |
| 31   | 3    | 30   | 30    | 2     | 29    | 1118.466  | 1118.4679  | -0.00189 | 0.002       |
| 31   | 3    | 31   | 30    | 2     | 30    | 1118.466  | 1118.4667  | -0.00065 | 0.002       |
| 31   | 3    | 32   | 30    | 2     | 31    | 1118.466  | 1118.4652  | 0.00084  | 0.002       |
| 31   | 3    | 33   | 30    | 2     | 32    | 1118.466  | 1118.4634  | 0.00256  | 0.004       |
| 31   | 3    | 34   | 30    | 2     | 33    | 1118.466  | 1118.4615  | 0.0045   | 1           |
| 32   | 3    | 29   | 31    | 2     | 28    | 1119.1619 | 1119.1724  | -0.01054 | 1           |
| 32   | 3    | 30   | 31    | 2     | 29    | 1119.1619 | 1119.171   | -0.00909 | 1           |
| 32   | 3    | 31   | 31    | 2     | 30    | 1119.1619 | 1119.1693  | -0.00737 | 1           |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 32   | 3    | 32   | 31    | 2     | 31    | 1119.1619 | 1119.1673  | -0.0054  | 0.003       |
| 32   | 3    | 33   | 31    | 2     | 32    | 1119.1619 | 1119.1651  | -0.00319 | 0.002       |
| 32   | 3    | 34   | 31    | 2     | 33    | 1119.1619 | 1119.1626  | -0.00074 | 0.002       |
| 32   | 3    | 35   | 31    | 2     | 34    | 1119.1619 | 1119.16    | 0.00193  | 0.003       |
| 33   | 3    | 30   | 32    | 2     | 29    | 1119.6762 | 1119.6926  | -0.01636 | 1           |
| 33   | 3    | 31   | 32    | 2     | 30    | 1119.6762 | 1119.6904  | -0.01418 | 1           |
| 33   | 3    | 32   | 32    | 2     | 31    | 1119.6762 | 1119.6879  | -0.01173 | 1           |
| 33   | 3    | 33   | 32    | 2     | 32    | 1119.6762 | 1119.6852  | -0.00903 | 1           |
| 33   | 3    | 34   | 32    | 2     | 33    | 1119.6762 | 1119.6823  | -0.00608 | 1           |
| 33   | 3    | 35   | 32    | 2     | 34    | 1119.6762 | 1119.6791  | -0.00289 | 0.002       |
| 33   | 3    | 36   | 32    | 2     | 35    | 1119.6762 | 1119.6757  | 0.00053  | 0.002       |
| 34   | 3    | 31   | 33    | 2     | 30    | 1120.0112 | 1120.028   | -0.01675 | 1           |
| 34   | 3    | 32   | 33    | 2     | 31    | 1120.0112 | 1120.025   | -0.01383 | 1           |
| 34   | 3    | 33   | 33    | 2     | 32    | 1120.0112 | 1120.0218  | -0.01064 | 1           |
| 34   | 3    | 34   | 33    | 2     | 33    | 1120.0112 | 1120.0184  | -0.00719 | 1           |
| 34   | 3    | 35   | 33    | 2     | 34    | 1120.0112 | 1120.0147  | -0.00349 | 0.002       |
| 34   | 3    | 36   | 33    | 2     | 35    | 1120.0112 | 1120.0108  | 0.00045  | 0.002       |
| 34   | 3    | 37   | 33    | 2     | 36    | 1120.0112 | 1120.0066  | 0.00463  | 1           |

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|   |   |   |   |   |   |           |           |          |       |
|---|---|---|---|---|---|-----------|-----------|----------|-------|
| 3 | 1 | 6 | 4 | 0 | 7 | 1052.2295 | 1052.2317 | -0.00217 | 0.001 |
| 3 | 1 | 5 | 4 | 0 | 6 | 1052.2472 | 1052.2482 | -0.00098 | 0.001 |
| 3 | 1 | 4 | 4 | 0 | 5 | 1052.2681 | 1052.2671 | 0.00105  | 0.001 |
| 3 | 1 | 3 | 4 | 0 | 4 | 1052.2881 | 1052.2865 | 0.00164  | 0.001 |
| 3 | 1 | 2 | 4 | 0 | 3 | 1052.3038 | 1052.3051 | -0.00128 | 0.001 |
| 3 | 1 | 1 | 4 | 0 | 2 | 1052.3193 | 1052.3221 | -0.00276 | 0.001 |
| 3 | 1 | 0 | 4 | 0 | 1 | 1052.3361 | 1052.337  | -0.00093 | 0.001 |
| 3 | 1 | 6 | 2 | 0 | 5 | 1092.4761 | 1092.4752 | 0.0009   | 0.001 |
| 4 | 1 | 7 | 5 | 0 | 8 | 1046.0431 | 1046.0435 | -0.00044 | 0.001 |
| 4 | 1 | 6 | 5 | 0 | 7 | 1046.0602 | 1046.0605 | -0.00031 | 0.001 |
| 4 | 1 | 5 | 5 | 0 | 6 | 1046.0797 | 1046.0789 | 0.00079  | 0.001 |
| 4 | 1 | 4 | 5 | 0 | 5 | 1046.0995 | 1046.0977 | 0.00182  | 0.001 |
| 4 | 1 | 3 | 5 | 0 | 4 | 1046.1189 | 1046.116  | 0.00287  | 0.001 |
| 4 | 1 | 2 | 5 | 0 | 3 | 1046.1313 | 1046.1334 | -0.0021  | 0.001 |
| 4 | 1 | 1 | 5 | 0 | 2 | 1046.1468 | 1046.1495 | -0.00266 | 0.001 |
| 4 | 1 | 3 | 3 | 0 | 2 | 1097.6693 | 1097.6726 | -0.0033  | 0.001 |
| 4 | 1 | 4 | 3 | 0 | 3 | 1097.6842 | 1097.6882 | -0.00396 | 0.001 |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 4    | 1    | 5    | 3     | 0     | 4     | 1097.7008 | 1097.7042  | -0.00338 | 0.001       |
| 4    | 1    | 6    | 3     | 0     | 5     | 1097.7214 | 1097.7198  | 0.00162  | 0.001       |
| 4    | 1    | 7    | 3     | 0     | 6     | 1097.7351 | 1097.7337  | 0.00143  | 0.001       |
| 5    | 1    | 2    | 4     | 0     | 1     | 1102.7808 | 1102.7817  | -0.0009  | 0.001       |
| 5    | 1    | 3    | 4     | 0     | 2     | 1102.7931 | 1102.7954  | -0.00234 | 0.001       |
| 5    | 1    | 4    | 4     | 0     | 3     | 1102.8065 | 1102.8098  | -0.00325 | 0.001       |
| 5    | 1    | 5    | 4     | 0     | 4     | 1102.8226 | 1102.8245  | -0.00192 | 0.001       |
| 5    | 1    | 6    | 4     | 0     | 5     | 1102.8376 | 1102.8395  | -0.00185 | 0.001       |
| 5    | 1    | 7    | 4     | 0     | 6     | 1102.855  | 1102.8541  | 0.00093  | 0.001       |
| 5    | 1    | 8    | 4     | 0     | 7     | 1102.8683 | 1102.8677  | 0.00058  | 0.001       |
| 6    | 1    | 9    | 7     | 0     | 10    | 1033.3477 | 1033.347   | 0.00074  | 0.001       |
| 6    | 1    | 8    | 7     | 0     | 9     | 1033.3654 | 1033.3646  | 0.00077  | 0.001       |
| 6    | 1    | 7    | 7     | 0     | 8     | 1033.3838 | 1033.383   | 0.0008   | 0.001       |
| 6    | 1    | 6    | 7     | 0     | 7     | 1033.4032 | 1033.4016  | 0.00161  | 0.001       |
| 6    | 1    | 5    | 7     | 0     | 6     | 1033.4214 | 1033.42    | 0.00141  | 0.001       |
| 6    | 1    | 4    | 7     | 0     | 5     | 1033.4384 | 1033.4379  | 0.00051  | 0.001       |
| 6    | 1    | 3    | 7     | 0     | 4     | 1033.4539 | 1033.4551  | -0.00116 | 0.001       |
| 6    | 1    | 3    | 5     | 0     | 2     | 1107.7936 | 1107.7921  | 0.00155  | 0.001       |
| 6    | 1    | 4    | 5     | 0     | 3     | 1107.8063 | 1107.8057  | 0.00059  | 0.001       |
| 6    | 1    | 5    | 5     | 0     | 4     | 1107.8199 | 1107.8197  | 0.00023  | 0.001       |
| 6    | 1    | 6    | 5     | 0     | 5     | 1107.8345 | 1107.8339  | 0.00065  | 0.001       |
| 6    | 1    | 7    | 5     | 0     | 6     | 1107.85   | 1107.8481  | 0.00193  | 0.001       |
| 6    | 1    | 9    | 5     | 0     | 8     | 1107.8784 | 1107.8754  | 0.00300  | 0.001       |
| 7    | 1    | 10   | 8     | 0     | 11    | 1026.8409 | 1026.8424  | -0.00149 | 0.001       |
| 7    | 1    | 9    | 8     | 0     | 10    | 1026.8597 | 1026.8603  | -0.00064 | 0.001       |
| 7    | 1    | 8    | 8     | 0     | 9     | 1026.8783 | 1026.8788  | -0.00053 | 0.001       |
| 7    | 1    | 7    | 8     | 0     | 8     | 1026.8969 | 1026.8975  | -0.00059 | 0.001       |
| 7    | 1    | 6    | 8     | 0     | 7     | 1026.9161 | 1026.916   | 0.00009  | 0.001       |
| 7    | 1    | 5    | 8     | 0     | 6     | 1026.934  | 1026.9341  | -0.00014 | 0.001       |
| 7    | 1    | 4    | 8     | 0     | 5     | 1026.9504 | 1026.9517  | -0.00128 | 0.001       |
| 8    | 1    | 11   | 9     | 0     | 12    | 1020.2361 | 1020.2362  | -0.00007 | 0.001       |
| 8    | 1    | 10   | 9     | 0     | 11    | 1020.2545 | 1020.2544  | 0.00013  | 0.001       |
| 8    | 1    | 9    | 9     | 0     | 10    | 1020.2735 | 1020.273   | 0.00049  | 0.001       |
| 8    | 1    | 8    | 9     | 0     | 9     | 1020.2916 | 1020.2918  | -0.00018 | 0.001       |
| 8    | 1    | 7    | 9     | 0     | 8     | 1020.3117 | 1020.3104  | 0.00126  | 0.001       |
| 9    | 1    | 12   | 10    | 0     | 13    | 1013.53   | 1013.5302  | -0.00019 | 0.001       |
| 9    | 1    | 11   | 10    | 0     | 12    | 1013.5485 | 1013.5486  | -0.00013 | 0.001       |
| 9    | 1    | 10   | 10    | 0     | 11    | 1013.5677 | 1013.5674  | 0.00028  | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 9    | 1    | 9    | 10    | 0     | 10    | 1013.5864 | 1013.5863  | 0.00008  | 0.001       |
| 9    | 1    | 8    | 10    | 0     | 9     | 1013.6055 | 1013.6051  | 0.00037  | 0.001       |
| 9    | 1    | 7    | 10    | 0     | 8     | 1013.624  | 1013.6237  | 0.00032  | 0.001       |
| 9    | 1    | 6    | 10    | 0     | 7     | 1013.6433 | 1013.6418  | 0.00149  | 0.001       |
| 9    | 1    | 6    | 8     | 0     | 5     | 1122.0472 | 1122.0456  | 0.00164  | 0.001       |
| 9    | 1    | 7    | 8     | 0     | 6     | 1122.0587 | 1122.0583  | 0.00039  | 0.001       |
| 9    | 1    | 8    | 8     | 0     | 7     | 1122.0713 | 1122.0711  | 0.00023  | 0.001       |
| 9    | 1    | 9    | 8     | 0     | 8     | 1122.0838 | 1122.0838  | -0.00001 | 0.001       |
| 9    | 1    | 10   | 8     | 0     | 9     | 1122.0972 | 1122.0965  | 0.00074  | 0.001       |
| 9    | 1    | 11   | 8     | 0     | 10    | 1122.1097 | 1122.1089  | 0.00076  | 0.001       |
| 9    | 1    | 12   | 8     | 0     | 11    | 1122.1219 | 1122.1212  | 0.00074  | 0.001       |
| 11   | 1    | 14   | 12    | 0     | 15    | 999.8268  | 999.82649  | 0.00031  | 0.001       |
| 11   | 1    | 13   | 12    | 0     | 14    | 999.8451  | 999.84534  | -0.00024 | 0.001       |
| 11   | 1    | 12   | 12    | 0     | 13    | 999.8645  | 999.86443  | 0.00007  | 0.001       |
| 11   | 1    | 11   | 12    | 0     | 12    | 999.8838  | 999.88362  | 0.00018  | 0.001       |
| 11   | 1    | 10   | 12    | 0     | 11    | 999.9028  | 999.90273  | 0.00007  | 0.001       |
| 11   | 1    | 9    | 12    | 0     | 10    | 999.9218  | 999.92165  | 0.00015  | 0.001       |
| 11   | 1    | 8    | 12    | 0     | 9     | 999.9393  | 999.94026  | -0.00096 | 0.001       |
| 11   | 1    | 8    | 10    | 0     | 7     | 1130.8839 | 1130.8817  | 0.00221  | 0.001       |
| 11   | 1    | 9    | 10    | 0     | 8     | 1130.894  | 1130.8937  | 0.00035  | 0.001       |
| 11   | 1    | 10   | 10    | 0     | 9     | 1130.9061 | 1130.9055  | 0.00056  | 0.001       |
| 11   | 1    | 11   | 10    | 0     | 10    | 1130.918  | 1130.9174  | 0.00065  | 0.001       |
| 11   | 1    | 12   | 10    | 0     | 11    | 1130.9301 | 1130.9291  | 0.00105  | 0.001       |
| 11   | 1    | 13   | 10    | 0     | 12    | 1130.9412 | 1130.9406  | 0.0006   | 0.001       |
| 11   | 1    | 14   | 10    | 0     | 13    | 1130.9529 | 1130.952   | 0.00095  | 0.001       |
| 12   | 1    | 15   | 13    | 0     | 16    | 992.8329  | 992.8325   | 0.0004   | 0.001       |
| 12   | 1    | 14   | 13    | 0     | 15    | 992.8512  | 992.85152  | -0.00032 | 0.001       |
| 12   | 1    | 13   | 13    | 0     | 14    | 992.8708  | 992.87076  | 0.00004  | 0.001       |
| 12   | 1    | 12   | 13    | 0     | 13    | 992.8909  | 992.89008  | 0.00082  | 0.001       |
| 12   | 1    | 11   | 13    | 0     | 12    | 992.9101  | 992.90935  | 0.00075  | 0.001       |
| 12   | 1    | 9    | 13    | 0     | 10    | 992.9473  | 992.94725  | 0.00005  | 0.001       |
| 13   | 1    | 10   | 12    | 0     | 9     | 1139.1682 | 1139.1678  | 0.00044  | 0.001       |
| 13   | 1    | 11   | 12    | 0     | 10    | 1139.1801 | 1139.1788  | 0.00126  | 0.001       |
| 13   | 1    | 12   | 12    | 0     | 11    | 1139.1902 | 1139.1898  | 0.00038  | 0.001       |
| 13   | 1    | 13   | 12    | 0     | 12    | 1139.2008 | 1139.2007  | 0.00012  | 0.001       |
| 13   | 1    | 14   | 12    | 0     | 13    | 1139.2113 | 1139.2114  | -0.00012 | 0.001       |
| 13   | 1    | 15   | 12    | 0     | 14    | 1139.2222 | 1139.222   | 0.00019  | 0.001       |
| 13   | 1    | 16   | 12    | 0     | 15    | 1139.2327 | 1139.2324  | 0.00026  | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 14   | 1    | 11   | 13    | 0     | 10    | 1143.1007 | 1143.1     | 0.00073  | 0.001       |
| 14   | 1    | 12   | 13    | 0     | 11    | 1143.1105 | 1143.1106  | -0.0001  | 0.001       |
| 14   | 1    | 13   | 13    | 0     | 12    | 1143.1208 | 1143.1211  | -0.0003  | 0.001       |
| 14   | 1    | 14   | 13    | 0     | 13    | 1143.1311 | 1143.1315  | -0.00038 | 0.001       |
| 14   | 1    | 15   | 13    | 0     | 14    | 1143.1414 | 1143.1417  | -0.00032 | 0.001       |
| 14   | 1    | 16   | 13    | 0     | 15    | 1143.1519 | 1143.1518  | 0.00007  | 0.001       |
| 14   | 1    | 17   | 13    | 0     | 16    | 1143.1619 | 1143.1618  | 0.00013  | 0.001       |
| 15   | 1    | 18   | 16    | 0     | 19    | 971.3024  | 971.30393  | -0.00153 | 0.001       |
| 15   | 1    | 17   | 16    | 0     | 18    | 971.3212  | 971.3234   | -0.0022  | 0.001       |
| 15   | 1    | 16   | 16    | 0     | 17    | 971.3425  | 971.34303  | -0.00053 | 0.001       |
| 15   | 1    | 15   | 16    | 0     | 16    | 971.3633  | 971.36273  | 0.00057  | 0.001       |
| 15   | 1    | 14   | 16    | 0     | 15    | 971.3831  | 971.38239  | 0.00071  | 0.001       |
| 15   | 1    | 13   | 16    | 0     | 14    | 971.4019  | 971.40193  | -0.00003 | 0.001       |
| 15   | 1    | 12   | 16    | 0     | 13    | 971.4203  | 971.42127  | -0.00097 | 0.001       |
| 15   | 1    | 12   | 14    | 0     | 11    | 1146.8901 | 1146.8892  | 0.00086  | 0.001       |
| 15   | 1    | 13   | 14    | 0     | 12    | 1146.899  | 1146.8994  | -0.00039 | 0.001       |
| 15   | 1    | 14   | 14    | 0     | 13    | 1146.9097 | 1146.9094  | 0.00029  | 0.001       |
| 15   | 1    | 15   | 14    | 0     | 14    | 1146.9196 | 1146.9193  | 0.00031  | 0.001       |
| 15   | 1    | 16   | 14    | 0     | 15    | 1146.9293 | 1146.929   | 0.00026  | 0.001       |
| 15   | 1    | 17   | 14    | 0     | 16    | 1146.9388 | 1146.9386  | 0.00016  | 0.001       |
| 15   | 1    | 18   | 14    | 0     | 17    | 1146.9481 | 1146.9481  | 0.00002  | 0.001       |
| 17   | 1    | 14   | 16    | 0     | 13    | 1154.033  | 1154.0318  | 0.0012   | 0.001       |
| 17   | 1    | 15   | 16    | 0     | 14    | 1154.0416 | 1154.041   | 0.00064  | 0.001       |
| 17   | 1    | 16   | 16    | 0     | 15    | 1154.0508 | 1154.05    | 0.00083  | 0.001       |
| 17   | 1    | 17   | 16    | 0     | 16    | 1154.0588 | 1154.0588  | -0.00003 | 0.001       |
| 17   | 1    | 18   | 16    | 0     | 17    | 1154.0676 | 1154.0675  | 0.00006  | 0.001       |
| 17   | 1    | 19   | 16    | 0     | 18    | 1154.0762 | 1154.0761  | 0.00009  | 0.001       |
| 17   | 1    | 20   | 16    | 0     | 19    | 1154.0857 | 1154.0845  | 0.00118  | 0.001       |
| 18   | 1    | 15   | 17    | 0     | 14    | 1157.3818 | 1157.3815  | 0.00027  | 0.001       |
| 18   | 1    | 16   | 17    | 0     | 15    | 1157.3904 | 1157.3902  | 0.00021  | 0.001       |
| 18   | 1    | 17   | 17    | 0     | 16    | 1157.3986 | 1157.3987  | -0.00008 | 0.001       |
| 18   | 1    | 18   | 17    | 0     | 17    | 1157.4067 | 1157.407   | -0.00031 | 0.001       |
| 18   | 1    | 19   | 17    | 0     | 18    | 1157.4144 | 1157.4152  | -0.00079 | 0.001       |
| 18   | 1    | 20   | 17    | 0     | 19    | 1157.423  | 1157.4232  | -0.00022 | 0.001       |
| 18   | 1    | 21   | 17    | 0     | 20    | 1157.4312 | 1157.4311  | 0.0001   | 0.001       |
| 20   | 1    | 17   | 19    | 0     | 16    | 1163.6296 | 1163.6292  | 0.00045  | 0.001       |
| 20   | 1    | 18   | 19    | 0     | 17    | 1163.6364 | 1163.6367  | -0.00034 | 0.001       |
| 20   | 1    | 19   | 19    | 0     | 18    | 1163.6436 | 1163.6442  | -0.00056 | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 20   | 1    | 20   | 19    | 0     | 19    | 1163.6515 | 1163.6514  | 0.0001   | 0.001       |
| 20   | 1    | 21   | 19    | 0     | 20    | 1163.6577 | 1163.6585  | -0.00079 | 0.001       |
| 20   | 1    | 22   | 19    | 0     | 21    | 1163.6653 | 1163.6654  | -0.00011 | 0.001       |
| 20   | 1    | 23   | 19    | 0     | 22    | 1163.6727 | 1163.6722  | 0.00051  | 0.001       |
| 21   | 1    | 18   | 20    | 0     | 17    | 1166.5231 | 1166.5236  | -0.00046 | 0.001       |
| 21   | 1    | 19   | 20    | 0     | 18    | 1166.5295 | 1166.5306  | -0.0011  | 0.001       |
| 21   | 1    | 20   | 20    | 0     | 19    | 1166.5367 | 1166.5375  | -0.00075 | 0.001       |
| 21   | 1    | 21   | 20    | 0     | 20    | 1166.5436 | 1166.5441  | -0.00054 | 0.001       |
| 21   | 1    | 22   | 20    | 0     | 21    | 1166.5492 | 1166.5507  | -0.00146 | 0.001       |
| 21   | 1    | 23   | 20    | 0     | 22    | 1166.5565 | 1166.557   | -0.00052 | 0.001       |
| 21   | 1    | 24   | 20    | 0     | 23    | 1166.5631 | 1166.5632  | -0.00012 | 0.001       |
| 6    | 2    | 3    | 5     | 1     | 2     | 1077.8402 | 1077.8398  | 0.00038  | 0.001       |
| 6    | 2    | 4    | 5     | 1     | 3     | 1077.8521 | 1077.8531  | -0.00095 | 0.001       |
| 6    | 2    | 5    | 5     | 1     | 4     | 1077.8647 | 1077.8666  | -0.00192 | 0.001       |
| 6    | 2    | 6    | 5     | 1     | 5     | 1077.8793 | 1077.8804  | -0.00112 | 0.001       |
| 6    | 2    | 7    | 5     | 1     | 6     | 1077.8933 | 1077.8942  | -0.00094 | 0.001       |
| 6    | 2    | 8    | 5     | 1     | 7     | 1077.9089 | 1077.9078  | 0.00111  | 0.001       |
| 6    | 2    | 9    | 5     | 1     | 8     | 1077.9216 | 1077.9207  | 0.00095  | 0.001       |
| 5    | 2    | 8    | 6     | 1     | 9     | 1011.2045 | 1011.2056  | -0.00113 | 0.001       |
| 5    | 2    | 7    | 6     | 1     | 8     | 1011.222  | 1011.2228  | -0.00078 | 0.001       |
| 5    | 2    | 6    | 6     | 1     | 7     | 1011.2407 | 1011.2409  | -0.00022 | 0.001       |
| 5    | 2    | 5    | 6     | 1     | 6     | 1011.2605 | 1011.2593  | 0.00117  | 0.001       |
| 5    | 2    | 4    | 6     | 1     | 5     | 1011.2785 | 1011.2775  | 0.00105  | 0.001       |
| 5    | 2    | 3    | 6     | 1     | 4     | 1011.294  | 1011.2949  | -0.00086 | 0.001       |
| 5    | 2    | 2    | 6     | 1     | 3     | 1011.3098 | 1011.3113  | -0.00146 | 0.001       |
| 6    | 2    | 9    | 7     | 1     | 10    | 1004.9167 | 1004.9139  | 0.00284  | 0.001       |
| 6    | 2    | 8    | 7     | 1     | 9     | 1004.9337 | 1004.9314  | 0.00235  | 0.001       |
| 6    | 2    | 7    | 7     | 1     | 8     | 1004.9525 | 1004.9496  | 0.00295  | 0.001       |
| 6    | 2    | 6    | 7     | 1     | 7     | 1004.9712 | 1004.968   | 0.00324  | 0.001       |
| 6    | 2    | 5    | 7     | 1     | 6     | 1004.9895 | 1004.9862  | 0.00333  | 0.001       |
| 6    | 2    | 4    | 7     | 1     | 5     | 1005.0056 | 1005.0038  | 0.00177  | 0.001       |
| 6    | 2    | 3    | 7     | 1     | 4     | 1005.0212 | 1005.0207  | 0.00048  | 0.001       |
| 9    | 2    | 6    | 8     | 1     | 5     | 1091.7133 | 1091.7121  | 0.00118  | 0.001       |
| 9    | 2    | 7    | 8     | 1     | 6     | 1091.7247 | 1091.7244  | 0.00027  | 0.001       |
| 9    | 2    | 8    | 8     | 1     | 7     | 1091.7368 | 1091.7367  | 0.00006  | 0.001       |
| 9    | 2    | 9    | 8     | 1     | 8     | 1091.7493 | 1091.749   | 0.00028  | 0.001       |
| 9    | 2    | 10   | 8     | 1     | 9     | 1091.7615 | 1091.7612  | 0.0003   | 0.001       |
| 9    | 2    | 11   | 8     | 1     | 10    | 1091.7742 | 1091.7732  | 0.00101  | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 9    | 2    | 12   | 8     | 1     | 11    | 1091.7861 | 1091.7849  | 0.00122  | 0.001       |
| 8    | 2    | 11   | 9     | 1     | 12    | 992.0181  | 992.01749  | 0.00061  | 0.001       |
| 8    | 2    | 10   | 9     | 1     | 11    | 992.0354  | 992.03555  | -0.00015 | 0.001       |
| 8    | 2    | 9    | 9     | 1     | 10    | 992.0547  | 992.05404  | 0.00066  | 0.001       |
| 8    | 2    | 8    | 9     | 1     | 9     | 992.0737  | 992.07266  | 0.00104  | 0.001       |
| 8    | 2    | 7    | 9     | 1     | 8     | 992.0917  | 992.09115  | 0.00055  | 0.001       |
| 8    | 2    | 6    | 9     | 1     | 7     | 992.1103  | 992.10929  | 0.00101  | 0.001       |
| 8    | 2    | 5    | 9     | 1     | 6     | 992.1272  | 992.12691  | 0.00029  | 0.001       |
| 10   | 2    | 7    | 9     | 1     | 6     | 1096.0693 | 1096.0682  | 0.00112  | 0.001       |
| 10   | 2    | 8    | 9     | 1     | 7     | 1096.0804 | 1096.0801  | 0.00032  | 0.001       |
| 10   | 2    | 9    | 9     | 1     | 8     | 1096.0916 | 1096.092   | -0.00035 | 0.001       |
| 10   | 2    | 10   | 9     | 1     | 9     | 1096.1033 | 1096.1038  | -0.00045 | 0.001       |
| 10   | 2    | 11   | 9     | 1     | 10    | 1096.1154 | 1096.1154  | -0.00003 | 0.001       |
| 10   | 2    | 12   | 9     | 1     | 11    | 1096.1281 | 1096.1269  | 0.00116  | 0.001       |
| 10   | 2    | 13   | 9     | 1     | 12    | 1096.1389 | 1096.1382  | 0.00071  | 0.001       |
| 9    | 2    | 12   | 10    | 1     | 13    | 985.4176  | 985.41662  | 0.00098  | 0.001       |
| 9    | 2    | 11   | 10    | 1     | 12    | 985.436   | 985.43493  | 0.00107  | 0.001       |
| 9    | 2    | 10   | 10    | 1     | 11    | 985.4546  | 985.45359  | 0.00101  | 0.001       |
| 9    | 2    | 9    | 10    | 1     | 10    | 985.4743  | 985.47236  | 0.00194  | 0.001       |
| 9    | 2    | 8    | 10    | 1     | 9     | 985.4931  | 985.49101  | 0.00209  | 0.001       |
| 9    | 2    | 7    | 10    | 1     | 8     | 985.5092  | 985.50937  | -0.00017 | 0.001       |
| 9    | 2    | 6    | 10    | 1     | 7     | 985.5288  | 985.52729  | 0.00151  | 0.001       |
| 12   | 2    | 9    | 11    | 1     | 8     | 1104.3666 | 1104.367   | -0.00036 | 0.001       |
| 12   | 2    | 10   | 11    | 1     | 9     | 1104.3777 | 1104.378   | -0.00029 | 0.001       |
| 12   | 2    | 11   | 11    | 1     | 10    | 1104.3877 | 1104.3889  | -0.00123 | 0.001       |
| 12   | 2    | 12   | 11    | 1     | 11    | 1104.3981 | 1104.3998  | -0.00167 | 0.001       |
| 12   | 2    | 13   | 11    | 1     | 12    | 1104.4091 | 1104.4105  | -0.00136 | 0.001       |
| 12   | 2    | 14   | 11    | 1     | 13    | 1104.4204 | 1104.421   | -0.00059 | 0.001       |
| 12   | 2    | 15   | 11    | 1     | 14    | 1104.4313 | 1104.4313  | -0.00001 | 0.001       |
| 14   | 2    | 11   | 13    | 1     | 10    | 1112.1023 | 1112.1021  | 0.00016  | 0.001       |
| 14   | 2    | 12   | 13    | 1     | 11    | 1112.1121 | 1112.1122  | -0.00014 | 0.001       |
| 14   | 2    | 13   | 13    | 1     | 12    | 1112.1215 | 1112.1222  | -0.00071 | 0.001       |
| 14   | 2    | 14   | 13    | 1     | 13    | 1112.1312 | 1112.132   | -0.00084 | 0.001       |
| 14   | 2    | 15   | 13    | 1     | 14    | 1112.1412 | 1112.1417  | -0.00052 | 0.001       |
| 14   | 2    | 16   | 13    | 1     | 15    | 1112.1515 | 1112.1512  | 0.00026  | 0.001       |
| 14   | 2    | 17   | 13    | 1     | 16    | 1112.1611 | 1112.1606  | 0.00052  | 0.001       |
| 15   | 2    | 12   | 14    | 1     | 11    | 1115.7545 | 1115.7537  | 0.0008   | 0.001       |
| 15   | 2    | 13   | 14    | 1     | 12    | 1115.7635 | 1115.7633  | 0.00018  | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 15   | 2    | 14   | 14    | 1     | 13    | 1115.7723 | 1115.7728  | -0.00048 | 0.001       |
| 15   | 2    | 15   | 14    | 1     | 14    | 1115.7813 | 1115.7821  | -0.0008  | 0.001       |
| 15   | 2    | 16   | 14    | 1     | 15    | 1115.7908 | 1115.7913  | -0.00047 | 0.001       |
| 15   | 2    | 17   | 14    | 1     | 16    | 1115.8004 | 1115.8003  | 0.00013  | 0.001       |
| 15   | 2    | 18   | 14    | 1     | 17    | 1115.8097 | 1115.8091  | 0.00061  | 0.001       |
| 16   | 2    | 13   | 15    | 1     | 12    | 1119.2587 | 1119.2588  | -0.00008 | 0.001       |
| 16   | 2    | 14   | 15    | 1     | 13    | 1119.2677 | 1119.2679  | -0.00019 | 0.001       |
| 16   | 2    | 15   | 15    | 1     | 14    | 1119.2762 | 1119.2768  | -0.00064 | 0.001       |
| 16   | 2    | 16   | 15    | 1     | 15    | 1119.2847 | 1119.2856  | -0.00094 | 0.001       |
| 16   | 2    | 17   | 15    | 1     | 16    | 1119.2942 | 1119.2943  | -0.00007 | 0.001       |
| 16   | 2    | 18   | 15    | 1     | 17    | 1119.3033 | 1119.3028  | 0.00055  | 0.001       |
| 16   | 2    | 19   | 15    | 1     | 18    | 1119.3124 | 1119.311   | 0.00136  | 0.001       |
| 17   | 2    | 14   | 16    | 1     | 13    | 1122.6156 | 1122.6155  | 0.00009  | 0.001       |
| 17   | 2    | 15   | 16    | 1     | 14    | 1122.624  | 1122.6241  | -0.0001  | 0.001       |
| 17   | 2    | 16   | 16    | 1     | 15    | 1122.6324 | 1122.6325  | -0.00013 | 0.001       |
| 17   | 2    | 17   | 16    | 1     | 16    | 1122.641  | 1122.6408  | 0.00021  | 0.001       |
| 17   | 2    | 18   | 16    | 1     | 17    | 1122.6505 | 1122.6489  | 0.00161  | 0.001       |
| 17   | 2    | 19   | 16    | 1     | 18    | 1122.6602 | 1122.6568  | 0.00338  | 0.001       |
| 17   | 2    | 20   | 16    | 1     | 19    | 1122.6678 | 1122.6646  | 0.00322  | 0.001       |
| 18   | 2    | 15   | 17    | 1     | 14    | 1125.8224 | 1125.822   | 0.00036  | 0.001       |
| 18   | 2    | 16   | 17    | 1     | 15    | 1125.8302 | 1125.8301  | 0.0001   | 0.001       |
| 18   | 2    | 17   | 17    | 1     | 16    | 1125.8376 | 1125.838   | -0.00039 | 0.001       |
| 18   | 2    | 18   | 17    | 1     | 17    | 1125.8446 | 1125.8457  | -0.00111 | 0.001       |
| 18   | 2    | 19   | 17    | 1     | 18    | 1125.8506 | 1125.8533  | -0.00266 | 0.001       |
| 18   | 2    | 20   | 17    | 1     | 19    | 1125.8571 | 1125.8606  | -0.00354 | 0.001       |
| 18   | 2    | 21   | 17    | 1     | 20    | 1125.8635 | 1125.8679  | -0.00435 | 0.001       |
| 21   | 2    | 18   | 20    | 1     | 17    | 1134.5236 | 1134.5221  | 0.00154  | 0.001       |
| 21   | 2    | 19   | 20    | 1     | 18    | 1134.5287 | 1134.5285  | 0.00024  | 0.001       |
| 21   | 2    | 20   | 20    | 1     | 19    | 1134.5349 | 1134.5347  | 0.00023  | 0.001       |
| 21   | 2    | 21   | 20    | 1     | 20    | 1134.5406 | 1134.5407  | -0.00009 | 0.001       |
| 21   | 2    | 22   | 20    | 1     | 21    | 1134.5468 | 1134.5465  | 0.00028  | 0.001       |
| 21   | 2    | 23   | 20    | 1     | 22    | 1134.5529 | 1134.5522  | 0.00072  | 0.001       |
| 21   | 2    | 24   | 20    | 1     | 23    | 1134.558  | 1134.5577  | 0.00033  | 0.001       |
| 2    | 3    | 5    | 3     | 2     | 6     | 1000.0382 | 1000.0416  | -0.00339 | 0.001       |
| 2    | 3    | 4    | 3     | 2     | 5     | 1000.0589 | 1000.0569  | 0.00205  | 0.001       |
| 2    | 3    | 3    | 3     | 2     | 4     | 1000.0776 | 1000.0776  | 0.00001  | 0.001       |
| 2    | 3    | 2    | 3     | 2     | 3     | 1000.0961 | 1000.0992  | -0.00311 | 0.001       |
| 2    | 3    | 1    | 3     | 2     | 2     | 1000.1134 | 1000.1186  | -0.0052  | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 4    | 3    | 7    | 5     | 2     | 8     | 988.2227  | 988.22351  | -0.00081 | 0.001       |
| 4    | 3    | 6    | 5     | 2     | 7     | 988.2404  | 988.24001  | 0.00039  | 0.001       |
| 4    | 3    | 5    | 5     | 2     | 6     | 988.2596  | 988.25805  | 0.00155  | 0.001       |
| 5    | 3    | 3    | 6     | 2     | 4     | 982.2374  | 982.2358   | 0.0016   | 0.001       |
| 5    | 3    | 4    | 6     | 2     | 5     | 982.2194  | 982.21866  | 0.00074  | 0.001       |
| 5    | 3    | 5    | 6     | 2     | 6     | 982.2021  | 982.20076  | 0.00134  | 0.001       |
| 5    | 3    | 6    | 6     | 2     | 7     | 982.1829  | 982.18254  | 0.00036  | 0.001       |
| 5    | 3    | 8    | 6     | 2     | 9     | 982.1472  | 982.14767  | -0.00047 | 0.001       |
| 5    | 3    | 7    | 6     | 2     | 8     | 982.16537 | 982.16459  | 0.00078  | 0.001       |
| 7    | 3    | 4    | 6     | 2     | 3     | 1051.9775 | 1051.9789  | -0.0014  | 0.001       |
| 7    | 3    | 5    | 6     | 2     | 4     | 1051.9891 | 1051.9915  | -0.00235 | 0.001       |
| 7    | 3    | 6    | 6     | 2     | 5     | 1052.0015 | 1052.0042  | -0.00268 | 0.001       |
| 7    | 3    | 7    | 6     | 2     | 6     | 1052.0153 | 1052.017   | -0.00172 | 0.001       |
| 7    | 3    | 8    | 6     | 2     | 7     | 1052.0283 | 1052.0298  | -0.00151 | 0.001       |
| 7    | 3    | 9    | 6     | 2     | 8     | 1052.0421 | 1052.0423  | -0.00023 | 0.001       |
| 7    | 3    | 10   | 6     | 2     | 9     | 1052.0546 | 1052.0543  | 0.00028  | 0.001       |
| 6    | 3    | 9    | 7     | 2     | 10    | 975.9629  | 975.96318  | -0.00028 | 0.001       |
| 6    | 3    | 8    | 7     | 2     | 9     | 975.9805  | 975.98047  | 0.00003  | 0.001       |
| 6    | 3    | 7    | 7     | 2     | 8     | 975.9983  | 975.99849  | -0.00019 | 0.001       |
| 6    | 3    | 6    | 7     | 2     | 7     | 976.0165  | 976.01672  | -0.00022 | 0.001       |
| 6    | 3    | 5    | 7     | 2     | 6     | 976.0344  | 976.03471  | -0.00031 | 0.001       |
| 6    | 3    | 4    | 7     | 2     | 5     | 976.0526  | 976.05212  | 0.00048  | 0.001       |
| 6    | 3    | 3    | 7     | 2     | 4     | 976.069   | 976.06872  | 0.00028  | 0.001       |
| 8    | 3    | 5    | 7     | 2     | 4     | 1056.4712 | 1056.4708  | 0.00042  | 0.001       |
| 8    | 3    | 6    | 7     | 2     | 5     | 1056.4832 | 1056.483   | 0.0002   | 0.001       |
| 8    | 3    | 7    | 7     | 2     | 6     | 1056.4948 | 1056.4953  | -0.00049 | 0.001       |
| 8    | 3    | 8    | 7     | 2     | 7     | 1056.5079 | 1056.5076  | 0.00029  | 0.001       |
| 8    | 3    | 9    | 7     | 2     | 8     | 1056.5208 | 1056.5198  | 0.00097  | 0.001       |
| 8    | 3    | 10   | 7     | 2     | 9     | 1056.5326 | 1056.5318  | 0.00077  | 0.001       |
| 8    | 3    | 11   | 7     | 2     | 10    | 1056.5449 | 1056.5434  | 0.0015   | 0.001       |
| 9    | 3    | 6    | 8     | 2     | 5     | 1060.8289 | 1060.8273  | 0.00164  | 0.001       |
| 9    | 3    | 7    | 8     | 2     | 6     | 1060.8394 | 1060.8391  | 0.0003   | 0.001       |
| 9    | 3    | 8    | 8     | 2     | 7     | 1060.8514 | 1060.8509  | 0.00046  | 0.001       |
| 9    | 3    | 9    | 8     | 2     | 8     | 1060.8621 | 1060.8628  | -0.00065 | 0.001       |
| 9    | 3    | 10   | 8     | 2     | 9     | 1060.8739 | 1060.8745  | -0.00055 | 0.001       |
| 9    | 3    | 11   | 8     | 2     | 10    | 1060.8875 | 1060.8859  | 0.00156  | 0.001       |
| 9    | 3    | 12   | 8     | 2     | 11    | 1060.8986 | 1060.8971  | 0.00152  | 0.001       |
| 10   | 3    | 7    | 9     | 2     | 6     | 1065.0474 | 1065.0464  | 0.00098  | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 10   | 3    | 8    | 9     | 2     | 7     | 1065.0582 | 1065.0578  | 0.00036  | 0.001       |
| 10   | 3    | 9    | 9     | 2     | 8     | 1065.0693 | 1065.0692  | 0.00007  | 0.001       |
| 10   | 3    | 10   | 9     | 2     | 9     | 1065.0802 | 1065.0805  | -0.00033 | 0.001       |
| 10   | 3    | 12   | 9     | 2     | 11    | 1065.1045 | 1065.1027  | 0.0018   | 0.001       |
| 10   | 3    | 13   | 9     | 2     | 12    | 1065.1152 | 1065.1134  | 0.00182  | 0.001       |
| 10   | 3    | 11   | 9     | 2     | 10    | 1065.092  | 1065.0917  | 0.00028  | 0.001       |
| 11   | 3    | 8    | 10    | 2     | 7     | 1069.1285 | 1069.1263  | 0.00219  | 0.001       |
| 11   | 3    | 9    | 10    | 2     | 8     | 1069.1377 | 1069.1373  | 0.0004   | 0.001       |
| 11   | 3    | 12   | 10    | 2     | 11    | 1069.1693 | 1069.1697  | -0.00038 | 0.001       |
| 11   | 3    | 13   | 10    | 2     | 12    | 1069.1816 | 1069.1802  | 0.00144  | 0.001       |
| 11   | 3    | 14   | 10    | 2     | 13    | 1069.1929 | 1069.1904  | 0.00253  | 0.001       |
| 15   | 3    | 12   | 14    | 2     | 11    | 1084.0146 | 1084.0143  | 0.00029  | 0.001       |
| 15   | 3    | 13   | 14    | 2     | 12    | 1084.0237 | 1084.0234  | 0.00034  | 0.001       |
| 15   | 3    | 14   | 14    | 2     | 13    | 1084.0319 | 1084.0323  | -0.00036 | 0.001       |
| 15   | 3    | 15   | 14    | 2     | 14    | 1084.0396 | 1084.041   | -0.0014  | 0.001       |
| 15   | 3    | 16   | 14    | 2     | 15    | 1084.0472 | 1084.0496  | -0.00237 | 0.001       |
| 15   | 3    | 17   | 14    | 2     | 16    | 1084.0549 | 1084.058   | -0.00306 | 0.001       |
| 15   | 3    | 18   | 14    | 2     | 17    | 1084.0623 | 1084.0661  | -0.00384 | 0.001       |
| 16   | 3    | 13   | 15    | 2     | 12    | 1087.3688 | 1087.3687  | 0.00014  | 0.001       |
| 16   | 3    | 14   | 15    | 2     | 13    | 1087.3774 | 1087.3772  | 0.0002   | 0.001       |
| 16   | 3    | 15   | 15    | 2     | 14    | 1087.385  | 1087.3856  | -0.00057 | 0.001       |
| 16   | 3    | 16   | 15    | 2     | 15    | 1087.3928 | 1087.3938  | -0.00097 | 0.001       |
| 16   | 3    | 17   | 15    | 2     | 16    | 1087.4001 | 1087.4018  | -0.00169 | 0.001       |
| 16   | 3    | 18   | 15    | 2     | 17    | 1087.4081 | 1087.4096  | -0.00153 | 0.001       |
| 16   | 3    | 19   | 15    | 2     | 18    | 1087.4152 | 1087.4173  | -0.00207 | 0.001       |
| 18   | 3    | 15   | 17    | 2     | 14    | 1093.6241 | 1093.6225  | 0.00157  | 0.001       |
| 18   | 3    | 16   | 17    | 2     | 15    | 1093.631  | 1093.63    | 0.00101  | 0.001       |
| 18   | 3    | 17   | 17    | 2     | 16    | 1093.6373 | 1093.6373  | 0.00003  | 0.001       |
| 18   | 3    | 18   | 17    | 2     | 17    | 1093.6438 | 1093.6444  | -0.00055 | 0.001       |
| 18   | 3    | 19   | 17    | 2     | 18    | 1093.6495 | 1093.6513  | -0.00176 | 0.001       |
| 18   | 3    | 20   | 17    | 2     | 19    | 1093.6552 | 1093.658   | -0.00277 | 0.001       |
| 18   | 3    | 21   | 17    | 2     | 20    | 1093.6616 | 1093.6645  | -0.00289 | 0.001       |
| 19   | 3    | 17   | 18    | 2     | 16    | 1096.5259 | 1096.525   | 0.00086  | 0.001       |
| 19   | 3    | 18   | 18    | 2     | 17    | 1096.5315 | 1096.5318  | -0.00025 | 0.001       |
| 19   | 3    | 19   | 18    | 2     | 18    | 1096.5382 | 1096.5383  | -0.00006 | 0.001       |
| 19   | 3    | 20   | 18    | 2     | 19    | 1096.5458 | 1096.5446  | 0.00121  | 0.001       |
| 19   | 3    | 21   | 18    | 2     | 20    | 1096.5537 | 1096.5507  | 0.00298  | 0.001       |

| $N'$ | $v'$ | $J'$ | $N''$ | $v''$ | $J''$ | Observed  | Calculated | Obs-Calc | Uncertainty |
|------|------|------|-------|-------|-------|-----------|------------|----------|-------------|
| 19   | 3    | 22   | 18    | 2     | 21    | 1096.5601 | 1096.5567  | 0.00343  | 0.001       |

## Appendix B

# Line lists for CoH and CoD

Line lists for CoH and CoD, together with uncertainties assigned to these lines and differences between calculated and observed wavenumbers. The calculated lines in these tables were obtained from the band constant fits, where we fitted the severely perturbed upper states to individual term values, while the ground state was fitted with Eq. 5.1. The data of Heimer (Ref. [1], Chapter 5), and Klynning and Kronekvist (Ref. [4,5], Chapter 5) are included.

### B.1 Line list for CoH

Table B.1: Line list for CoH.

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Lines from A. Heimer, Z. Physik 104, 448-457 (1937)

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| $A^3\Phi_4 - X^3\Phi_4$ |      |         |       |       |          |          |
|-------------------------|------|---------|-------|-------|----------|----------|
| $v'$                    | $J'$ | parity' | $v''$ | $J''$ | parity'' |          |
| 0                       | 5    | e       | 0     | 4     | e        | 22305.84 |
| 0                       | 6    | e       | 0     | 5     | e        | 22312.58 |
| 0                       | 7    | e       | 0     | 6     | e        | 22318.02 |
| 0                       | 8    | e       | 0     | 7     | e        | 22322.02 |
| 0                       | 9    | e       | 0     | 8     | e        | 22324.43 |
| 0                       | 10   | e       | 0     | 9     | e        | 22325.53 |
| 0                       | 11   | e       | 0     | 10    | e        | 22324.83 |
| 0                       | 12   | e       | 0     | 11    | e        | 22322.30 |

Observed      Uncertainty      calc-obs

---

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|----------|-------------|----------|
| 0    | 13   | e       | 0     | 12    | e        | 22325.58 | 0.04        | -0.0100  |
| 0    | 14   | e       | 0     | 13    | e        | 22316.35 | 0.04        | -0.0243  |
| 0    | 15   | e       | 0     | 14    | e        | 22308.44 | 0.04        | -0.0665  |
| 0    | 16   | e       | 0     | 15    | e        | 22299.28 | 0.04        | -0.0009  |
| 0    | 17   | e       | 0     | 16    | e        | 22288.24 | 0.04        | -0.0243  |
| 0    | 18   | e       | 0     | 17    | e        | 22276.87 | 0.04        | 0.0145   |
| 0    | 19   | e       | 0     | 18    | e        | 22261.79 | 0.04        | 0.0863   |
| 0    | 20   | e       | 0     | 19    | e        | 22245.31 | 0.04        | 0.0073   |
| 0    | 21   | e       | 0     | 20    | e        | 22227.12 | 0.04        | -0.0893  |
| 0    | 22   | e       | 0     | 21    | e        | 22206.78 | 0.04        | -0.0630  |
| 0    | 23   | e       | 0     | 22    | e        | 22184.48 | 0.5         | -0.2666  |
| 0    | 24   | e       | 0     | 23    | e        | 22260.07 | 0.04        | 0.0002   |
| 0    | 25   | e       | 0     | 24    | e        | 22133.93 | 0.04        | 0.0007   |
| 0    | 4    | e       | 0     | 5     | e        | 22169.45 | 0.04        | -0.0217  |
| 0    | 5    | e       | 0     | 6     | e        | 22149.08 | 0.04        | 0.0006   |
| 0    | 6    | e       | 0     | 7     | e        | 22127.57 | 0.04        | -0.0005  |
| 0    | 7    | e       | 0     | 8     | e        | 22104.89 | 0.04        | -0.0139  |
| 0    | 8    | e       | 0     | 9     | e        | 22080.89 | 0.04        | -0.0117  |
| 0    | 9    | e       | 0     | 10    | e        | 22055.55 | 0.04        | 0.0053   |
| 0    | 10   | e       | 0     | 11    | e        | 22028.95 | 0.04        | 0.0070   |
| 0    | 11   | e       | 0     | 12    | e        | 22000.89 | 0.04        | -0.0240  |
| 0    | 12   | e       | 0     | 13    | e        | 21971.18 | 0.04        | -0.0593  |
| 0    | 13   | e       | 0     | 14    | e        | 21947.40 | 0.04        | 0.0105   |
| 0    | 14   | e       | 0     | 15    | e        | 21911.46 | 0.04        | -0.0039  |
| 0    | 15   | e       | 0     | 16    | e        | 21877.00 | 0.04        | 0.0757   |
| 0    | 16   | e       | 0     | 17    | e        | 21841.78 | 0.04        | 0.0765   |
| 0    | 17   | e       | 0     | 18    | e        | 21804.97 | 0.04        | 0.0243   |
| 0    | 18   | e       | 0     | 19    | e        | 21768.23 | 0.04        | -0.0157  |
| 0    | 19   | e       | 0     | 20    | e        | 21728.22 | 0.04        | -0.0873  |
| 0    | 20   | e       | 0     | 21    | e        | 21686.91 | 0.04        | -0.0070  |
| 0    | 21   | e       | 0     | 22    | e        | 21644.29 | 0.04        | 0.0884   |
| 0    | 22   | e       | 0     | 23    | e        | 21600.23 | 0.04        | 0.0622   |
| 0    | 23   | e       | 0     | 24    | e        | 21554.25 | 0.5         | 0.2677   |
| 0    | 4    | e       | 0     | 4     | f        | 22240.70 | 0.04        | 0.0221   |
| 0    | 5    | e       | 0     | 5     | f        | 22234.51 | 0.04        | 0.0173   |
| 0    | 6    | e       | 0     | 6     | f        | 22227.09 | 0.04        | 0.0215   |
| 0    | 7    | e       | 0     | 7     | f        | 22218.40 | 0.04        | 0.0463   |
| 0    | 8    | e       | 0     | 8     | f        | 22208.34 | 0.04        | 0.0598   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|----------|-------------|----------|
| 0    | 9    | e       | 0     | 9     | f        | 22196.98 | 0.04        | -0.0385  |
| 0    | 10   | e       | 0     | 10    | f        | 22184.09 | 0.04        | 0.0215   |
| 0    | 11   | e       | 0     | 11    | f        | 22169.67 | 0.04        | 0.0122   |
| 0    | 12   | e       | 0     | 12    | f        | 22153.43 | 0.04        | 0.0514   |
| 0    | 14   | e       | 0     | 14    | f        | 22120.48 | 0.04        | 0.0285   |
| 0    | 15   | e       | 0     | 15    | f        | 22099.26 | 0.04        | -0.0101  |
| 0    | 16   | e       | 0     | 16    | f        | 22077.06 | 0.04        | -0.0764  |
| 0    | 4    | f       | 0     | 4     | e        | 22240.70 | 0.04        | 0.0221   |
| 0    | 5    | f       | 0     | 5     | e        | 22234.51 | 0.04        | 0.0173   |
| 0    | 6    | f       | 0     | 6     | e        | 22227.09 | 0.04        | 0.0216   |
| 0    | 7    | f       | 0     | 7     | e        | 22218.40 | 0.04        | 0.0465   |
| 0    | 8    | f       | 0     | 8     | e        | 22208.34 | 0.04        | 0.0611   |
| 0    | 9    | f       | 0     | 9     | e        | 22196.98 | 0.04        | -0.0377  |
| 0    | 10   | f       | 0     | 10    | e        | 22184.09 | 0.04        | 0.0243   |
| 0    | 11   | f       | 0     | 11    | e        | 22169.67 | 0.04        | 0.0030   |
| 0    | 14   | f       | 0     | 14    | e        | 22120.02 | 0.04        | 0.0325   |
| 0    | 15   | f       | 0     | 15    | e        | 22098.84 | 0.5         | 0.2311   |
| 0    | 16   | f       | 0     | 16    | e        | 22076.58 | 0.04        | 0.1207   |
| 0    | 5    | f       | 0     | 4     | f        | 22305.84 | 0.04        | -0.0190  |
| 0    | 6    | f       | 0     | 5     | f        | 22312.58 | 0.04        | -0.0217  |
| 0    | 7    | f       | 0     | 6     | f        | 22318.02 | 0.04        | -0.0315  |
| 0    | 8    | f       | 0     | 7     | f        | 22322.02 | 0.04        | -0.0487  |
| 0    | 9    | f       | 0     | 8     | f        | 22324.43 | 0.04        | 0.0338   |
| 0    | 10   | f       | 0     | 9     | f        | 22325.53 | 0.04        | -0.0295  |
| 0    | 11   | f       | 0     | 10    | f        | 22324.83 | 0.04        | -0.0025  |
| 0    | 12   | f       | 0     | 11    | f        | 22322.30 | 0.04        | 0.0002   |
| 0    | 13   | f       | 0     | 12    | f        | 22316.10 | 0.04        | -0.0216  |
| 0    | 14   | f       | 0     | 13    | f        | 22315.84 | 0.04        | -0.0107  |
| 0    | 15   | f       | 0     | 14    | f        | 22308.15 | 0.04        | -0.0265  |
| 0    | 16   | f       | 0     | 15    | f        | 22298.89 | 0.04        | -0.0151  |
| 0    | 17   | f       | 0     | 16    | f        | 22287.36 | 0.04        | 0.0666   |
| 0    | 4    | f       | 0     | 5     | f        | 22169.45 | 0.04        | -0.0217  |
| 0    | 5    | f       | 0     | 6     | f        | 22149.08 | 0.04        | 0.0005   |
| 0    | 6    | f       | 0     | 7     | f        | 22127.57 | 0.04        | -0.0007  |
| 0    | 7    | f       | 0     | 8     | f        | 22104.89 | 0.04        | -0.0142  |
| 0    | 8    | f       | 0     | 9     | f        | 22080.89 | 0.04        | -0.0115  |
| 0    | 9    | f       | 0     | 10    | f        | 22055.55 | 0.04        | 0.0035   |
| 0    | 10   | f       | 0     | 11    | f        | 22028.95 | 0.04        | 0.0042   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|----------|-------------|----------|
| 0    | 13   | f       | 0     | 14    | f        | 21937.88 | 0.04        | 0.0205   |
| 0    | 14   | f       | 0     | 15    | f        | 21910.95 | 0.04        | -0.0211  |
| 0    | 15   | f       | 0     | 16    | f        | 21876.75 | 0.04        | 0.0256   |
| 0    | 16   | f       | 0     | 17    | f        | 21841.48 | 0.04        | -0.1070  |
| 0    | 17   | f       | 0     | 18    | f        | 21804.15 | 0.04        | -0.0671  |

This work

 $A'^3\Phi_4 - X^3\Phi_4$ 

|   |    |   |   |    |   |            |       |         |
|---|----|---|---|----|---|------------|-------|---------|
| 0 | 5  | e | 0 | 4  | e | 12406.6643 | 0.007 | -0.0095 |
| 0 | 6  | e | 0 | 5  | e | 12401.3396 | 0.007 | 0.0029  |
| 0 | 7  | e | 0 | 6  | e | 12393.0810 | 0.007 | 0.0047  |
| 0 | 8  | e | 0 | 7  | e | 12382.0822 | 0.007 | 0.0065  |
| 0 | 9  | e | 0 | 8  | e | 12368.5191 | 0.007 | 0.0051  |
| 0 | 10 | e | 0 | 9  | e | 12352.6798 | 0.007 | 0.0074  |
| 0 | 11 | e | 0 | 10 | e | 12335.0318 | 0.007 | -0.0009 |
| 0 | 12 | e | 0 | 11 | e | 12317.8105 | 0.007 | -0.0055 |
| 0 | 13 | e | 0 | 12 | e | 12292.4629 | 0.007 | -0.0090 |
| 0 | 14 | e | 0 | 13 | e | 12276.3352 | 0.007 | 0.0012  |
| 0 | 15 | e | 0 | 14 | e | 12263.4408 | 0.007 | -0.0011 |
| 0 | 16 | e | 0 | 15 | e | 12166.0577 | 0.007 | -0.0037 |
| 0 | 17 | e | 0 | 16 | e | 12135.7314 | 0.007 | -0.0049 |
| 0 | 18 | e | 0 | 17 | e | 12102.0925 | 0.007 | -0.0050 |
| 0 | 19 | e | 0 | 18 | e | 12066.6945 | 0.007 | -0.0036 |
| 0 | 20 | e | 0 | 19 | e | 12024.8942 | 0.05  | -0.0571 |
| 0 | 21 | e | 0 | 20 | e | 11986.1773 | 0.007 | -0.0027 |
| 0 | 22 | e | 0 | 21 | e | 11949.8154 | 0.007 | -0.0013 |
| 0 | 23 | e | 0 | 22 | e | 11907.5716 | 10    | 0.0155  |
| 0 | 24 | e | 0 | 23 | e | 11867.9272 | 10    | 0.0626  |
| 0 | 25 | e | 0 | 24 | e | 11832.0079 | 10    | 0.0988  |
| 0 | 4  | e | 0 | 5  | e | 12280.5272 | 0.007 | -0.0025 |
| 0 | 5  | e | 0 | 6  | e | 12249.9227 | 0.007 | -0.0085 |
| 0 | 6  | e | 0 | 7  | e | 12216.3597 | 0.007 | -0.0060 |
| 0 | 7  | e | 0 | 8  | e | 12179.9710 | 0.007 | 0.0022  |
| 0 | 8  | e | 0 | 9  | e | 12140.9930 | 0.007 | 0.0036  |
| 0 | 9  | e | 0 | 10 | e | 12099.6120 | 0.007 | 0.0033  |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 0    | 10   | e       | 0     | 11    | e        | 12056.1356 | 0.007       | 0.0083   |
| 0    | 11   | e       | 0     | 12    | e        | 12011.0538 | 0.007       | 0.0008   |
| 0    | 12   | e       | 0     | 13    | e        | 11966.6183 | 0.007       | -0.0016  |
| 0    | 13   | e       | 0     | 14    | e        | 11914.2849 | 0.007       | 0.0096   |
| 0    | 14   | e       | 0     | 15    | e        | 11871.4789 | 0.007       | -0.0120  |
| 0    | 15   | e       | 0     | 16    | e        | 11832.1440 | 0.007       | -0.0022  |
| 0    | 16   | e       | 0     | 17    | e        | 11708.6319 | 0.007       | -0.0005  |
| 0    | 17   | e       | 0     | 18    | e        | 11652.5051 | 0.007       | 0.0000   |
| 0    | 18   | e       | 0     | 19    | e        | 11593.4173 | 0.007       | 0.0001   |
| 0    | 19   | e       | 0     | 20    | e        | 11532.9469 | 0.007       | 0.0004   |
| 0    | 20   | e       | 0     | 21    | e        | 11466.4710 | 0.05        | -0.0482  |
| 0    | 21   | e       | 0     | 22    | e        | 11403.5184 | 0.007       | 0.0040   |
| 0    | 22   | e       | 0     | 23    | e        | 11343.3875 | 0.007       | 0.0018   |
| 0    | 23   | e       | 0     | 24    | e        | 11277.8945 | 0.007       | -0.0031  |
| 0    | 24   | e       | 0     | 25    | e        | 11215.5628 | 0.007       | 0.0026   |
| 0    | 25   | e       | 0     | 26    | e        | 11157.6210 | 10          | -0.0797  |
| 0    | 4    | f       | 0     | 4     | e        | 12351.8160 | 0.007       | 0.0025   |
| 0    | 5    | f       | 0     | 5     | e        | 12335.3550 | 0.007       | 0.0060   |
| 0    | 6    | f       | 0     | 6     | e        | 12315.8900 | 0.007       | 0.0058   |
| 0    | 7    | f       | 0     | 7     | e        | 12293.4460 | 0.007       | 0.0040   |
| 0    | 8    | f       | 0     | 8     | e        | 12268.2290 | 0.007       | 0.0027   |
| 0    | 9    | f       | 0     | 9     | e        | 12240.7420 | 0.007       | 0.0037   |
| 0    | 10   | f       | 0     | 10    | e        | 12211.0600 | 0.007       | 0.0047   |
| 0    | 4    | e       | 0     | 4     | f        | 12351.8160 | 0.007       | 0.0025   |
| 0    | 5    | e       | 0     | 5     | f        | 12335.3550 | 0.007       | 0.0060   |
| 0    | 6    | e       | 0     | 6     | f        | 12315.8900 | 0.007       | 0.0057   |
| 0    | 7    | e       | 0     | 7     | f        | 12293.5230 | 0.007       | 0.0204   |
| 0    | 8    | e       | 0     | 8     | f        | 12268.5110 | 0.007       | 0.0070   |
| 0    | 9    | e       | 0     | 9     | f        | 12240.9900 | 0.007       | 0.0115   |
| 0    | 10   | e       | 0     | 10    | f        | 12211.3020 | 0.007       | -0.0036  |
| 0    | 5    | f       | 0     | 4     | f        | 12406.6643 | 0.007       | -0.0095  |
| 0    | 6    | f       | 0     | 5     | f        | 12401.3396 | 0.007       | 0.0029   |
| 0    | 7    | f       | 0     | 6     | f        | 12392.9960 | 0.007       | -0.0040  |
| 0    | 8    | f       | 0     | 7     | f        | 12381.7993 | 0.007       | 0.0026   |
| 0    | 9    | f       | 0     | 8     | f        | 12368.2658 | 0.007       | 0.0015   |
| 0    | 10   | f       | 0     | 9     | f        | 12352.4564 | 0.007       | -0.0055  |
| 0    | 11   | f       | 0     | 10    | f        | 12334.9036 | 0.007       | 0.0026   |
| 0    | 12   | f       | 0     | 11    | f        | 12315.3381 | 0.007       | 0.0040   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 0    | 13   | f       | 0     | 12    | f        | 12291.2482 | 0.007       | 0.0056   |
| 0    | 14   | f       | 0     | 13    | f        | 12261.7713 | 0.007       | 0.0034   |
| 0    | 15   | f       | 0     | 14    | f        | 12224.8669 | 0.007       | -0.0022  |
| 0    | 16   | f       | 0     | 15    | f        | 12186.3966 | 0.007       | 0.0007   |
| 0    | 17   | f       | 0     | 16    | f        | 12148.0711 | 0.007       | 0.0031   |
| 0    | 18   | f       | 0     | 17    | f        | 12109.6290 | 0.007       | 0.0012   |
| 0    | 19   | f       | 0     | 18    | f        | 12050.2228 | 0.007       | 0.0013   |
| 0    | 20   | f       | 0     | 19    | f        | 12007.1657 | 0.007       | 0.0080   |
| 0    | 21   | f       | 0     | 20    | f        | 11962.5128 | 0.007       | 0.0083   |
| 0    | 22   | f       | 0     | 21    | f        | 11916.0772 | 0.007       | 0.0095   |
| 0    | 23   | f       | 0     | 22    | f        | 11867.1602 | 0.007       | 0.0064   |
| 0    | 24   | f       | 0     | 23    | f        | 11817.6957 | 0.007       | -0.0081  |
| 0    | 25   | f       | 0     | 24    | f        | 11764.8521 | 0.007       | -0.0003  |
| 0    | 26   | f       | 0     | 25    | f        | 11710.3209 | 0.007       | -0.0089  |
| 0    | 27   | f       | 0     | 26    | f        | 11654.1484 | 0.007       | -0.0135  |
| 0    | 28   | f       | 0     | 27    | f        | 11598.0765 | 0.007       | -0.0027  |
| 0    | 29   | f       | 0     | 28    | f        | 11534.6100 | 0.007       | -0.0034  |
| 0    | 30   | f       | 0     | 29    | f        | 11473.7459 | 0.03        | 0.0354   |
| 0    | 31   | f       | 0     | 30    | f        | 11411.1191 | 0.05        | 0.0941   |
| 0    | 32   | f       | 0     | 31    | f        | 11347.1088 | 0.007       | -0.0031  |
| 0    | 4    | f       | 0     | 5     | f        | 12280.5272 | 0.007       | -0.0025  |
| 0    | 5    | f       | 0     | 6     | f        | 12249.9227 | 0.007       | -0.0085  |
| 0    | 6    | f       | 0     | 7     | f        | 12216.3597 | 0.007       | -0.0061  |
| 0    | 7    | f       | 0     | 8     | f        | 12179.8820 | 0.007       | -0.0027  |
| 0    | 8    | f       | 0     | 9     | f        | 12140.7110 | 0.007       | -0.0019  |
| 0    | 9    | f       | 0     | 10    | f        | 12099.3573 | 0.007       | -0.0004  |
| 0    | 10   | f       | 0     | 11    | f        | 12055.9083 | 0.007       | -0.0038  |
| 0    | 11   | f       | 0     | 12    | f        | 12010.9184 | 0.007       | 0.0057   |
| 0    | 12   | f       | 0     | 13    | f        | 11964.1388 | 0.007       | 0.0045   |
| 0    | 13   | f       | 0     | 14    | f        | 11913.0861 | 0.007       | -0.0102  |
| 0    | 14   | f       | 0     | 15    | f        | 11856.8670 | 0.007       | 0.0073   |
| 0    | 15   | f       | 0     | 16    | f        | 11793.5176 | 0.007       | -0.0008  |
| 0    | 16   | f       | 0     | 17    | f        | 11728.8968 | 0.007       | -0.0015  |
| 0    | 17   | f       | 0     | 18    | f        | 11664.7276 | 0.007       | 0.0029   |
| 0    | 18   | f       | 0     | 19    | f        | 11600.7749 | 0.007       | 0.0002   |
| 0    | 19   | f       | 0     | 20    | f        | 11516.2082 | 0.007       | -0.0019  |
| 0    | 20   | f       | 0     | 21    | f        | 11448.3618 | 0.007       | -0.0014  |
| 0    | 21   | f       | 0     | 22    | f        | 11379.3022 | 0.007       | -0.0053  |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 0    | 22   | f       | 0     | 23    | f        | 11308.8494 | 0.007       | 0.0044   |
| 0    | 23   | f       | 0     | 24    | f        | 11236.3441 | 0.007       | 0.0004   |
| 0    | 24   | f       | 0     | 25    | f        | 11163.7200 | 0.007       | -0.0080  |
| 0    | 25   | f       | 0     | 26    | f        | 11088.1730 | 0.007       | 0.0008   |
| 0    | 26   | f       | 0     | 27    | f        | 11011.3964 | 0.007       | 0.0007   |
| 0    | 27   | f       | 0     | 28    | f        | 10933.4577 | 0.007       | 0.0037   |
| 0    | 28   | f       | 0     | 29    | f        | 10856.1153 | 0.007       | 0.0158   |
| 0    | 29   | f       | 0     | 30    | f        | 10771.8858 | 0.007       | 0.0065   |
| 0    | 30   | f       | 0     | 31    | f        | 10690.7978 | 0.007       | 0.0010   |
| 0    | 31   | f       | 0     | 32    | f        | 10608.4685 | 0.007       | -0.0010  |
| 0    | 32   | f       | 0     | 33    | f        | 10525.3015 | 10          | -0.2022  |
| 0    | 5    | e       | 1     | 4     | e        | 10552.1272 | 0.007       | 0.0016   |
| 0    | 6    | e       | 1     | 5     | e        | 10548.9276 | 0.007       | 0.0047   |
| 0    | 7    | e       | 1     | 6     | e        | 10543.2180 | 0.007       | -0.0024  |
| 0    | 8    | e       | 1     | 7     | e        | 10535.1854 | 0.007       | -0.0020  |
| 0    | 9    | e       | 1     | 8     | e        | 10525.0139 | 0.007       | -0.0055  |
| 0    | 10   | e       | 1     | 9     | e        | 10512.9882 | 0.007       | -0.0025  |
| 0    | 11   | e       | 1     | 10    | e        | 10499.5716 | 0.007       | -0.0043  |
| 0    | 12   | e       | 1     | 11    | e        | 10487.0002 | 0.007       | 0.0016   |
| 0    | 13   | e       | 1     | 12    | e        | 10466.7647 | 0.05        | -0.0328  |
| 0    | 14   | e       | 1     | 13    | e        | 10456.0945 | 0.01        | 0.0189   |
| 0    | 15   | e       | 1     | 14    | e        | 10449.0747 | 0.05        | 0.0553   |
| 0    | 16   | e       | 1     | 15    | e        | 10357.9926 | 0.05        | 0.0753   |
| 0    | 17   | e       | 1     | 16    | e        | 10334.3702 | 0.05        | 0.0990   |
| 0    | 18   | e       | 1     | 17    | e        | 10307.8459 | 0.05        | 0.1133   |
| 0    | 19   | e       | 1     | 18    | e        | 10279.9657 | 0.05        | 0.1209   |
| 0    | 20   | e       | 1     | 19    | e        | 10246.0862 | 0.05        | 0.0614   |
| 0    | 21   | e       | 1     | 20    | e        | 10215.7026 | 0.07        | 0.0860   |
| 0    | 22   | e       | 1     | 21    | e        | 10188.0774 | 0.07        | 0.0434   |
| 0    | 23   | e       | 1     | 22    | e        | 10154.9759 | 0.007       | 0.0059   |
| 0    | 24   | e       | 1     | 23    | e        | 10124.8783 | 0.007       | 0.0029   |
| 0    | 25   | e       | 1     | 24    | e        | 10098.9314 | 0.007       | -0.0038  |
| 0    | 4    | e       | 1     | 5     | e        | 10428.1144 | 0.007       | 0.0001   |
| 0    | 5    | e       | 1     | 6     | e        | 10400.0498 | 0.007       | -0.0056  |
| 0    | 6    | e       | 1     | 7     | e        | 10369.4554 | 0.007       | -0.0070  |
| 0    | 7    | e       | 1     | 8     | e        | 10336.4810 | 0.007       | -0.0235  |
| 0    | 8    | e       | 1     | 9     | e        | 10301.3034 | 0.007       | -0.0084  |
| 0    | 9    | e       | 1     | 10    | e        | 10264.1644 | 0.007       | -0.0127  |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 0    | 10   | e       | 1     | 11    | e        | 10225.3502 | 0.007       | -0.0094  |
| 0    | 11   | e       | 1     | 12    | e        | 10185.2968 | 0.02        | 0.0358   |
| 0    | 12   | e       | 1     | 13    | e        | 10146.3500 | 0.02        | 0.0437   |
| 0    | 13   | e       | 1     | 14    | e        | 10100.0314 | 0.15        | -0.0466  |
| 0    | 14   | e       | 1     | 15    | e        | 10063.4122 | 0.05        | 0.0686   |
| 0    | 15   | e       | 1     | 16    | e        | 10030.7832 | 0.05        | 0.1013   |
| 0    | 16   | e       | 1     | 17    | e        | 9914.3846  | 0.05        | 0.1185   |
| 0    | 17   | e       | 1     | 18    | e        | 9865.7768  | 0.05        | 0.1240   |
| 0    | 18   | e       | 1     | 19    | e        | 9814.6122  | 0.05        | 0.1158   |
| 0    | 19   | e       | 1     | 20    | e        | 9762.4691  | 0.1         | 0.0921   |
| 0    | 20   | e       | 1     | 21    | e        | 9704.7283  | 0.007       | 0.0012   |
| 0    | 21   | e       | 1     | 22    | e        | 9650.9192  | 0.007       | -0.0021  |
| 0    | 22   | e       | 1     | 23    | e        | 9600.3349  | 0.05        | -0.0542  |
| 0    | 23   | e       | 1     | 24    | e        | 9544.8224  | 0.05        | -0.1101  |
| 0    | 24   | e       | 1     | 25    | e        | 9492.8759  | 0.03        | -0.0887  |
| 0    | 25   | e       | 1     | 26    | e        | 9445.6904  | 0.007       | 0.0031   |
| 0    | 5    | f       | 1     | 4     | f        | 10552.1272 | 0.007       | 0.0016   |
| 0    | 6    | f       | 1     | 5     | f        | 10548.9276 | 0.007       | 0.0047   |
| 0    | 7    | f       | 1     | 6     | f        | 10543.1180 | 0.007       | 0.0040   |
| 0    | 8    | f       | 1     | 7     | f        | 10534.8994 | 0.007       | -0.0024  |
| 0    | 9    | f       | 1     | 8     | f        | 10524.7506 | 0.007       | 0.0018   |
| 0    | 10   | f       | 1     | 9     | f        | 10512.7571 | 0.007       | -0.0056  |
| 0    | 11   | f       | 1     | 10    | f        | 10499.4561 | 0.007       | -0.0090  |
| 0    | 12   | f       | 1     | 11    | f        | 10484.5569 | 0.007       | -0.0086  |
| 0    | 13   | f       | 1     | 12    | f        | 10465.5023 | 0.03        | 0.0469   |
| 0    | 14   | f       | 1     | 13    | f        | 10441.5947 | 0.007       | -0.0119  |
| 0    | 15   | f       | 1     | 14    | f        | 10410.6155 | 0.007       | -0.0075  |
| 0    | 16   | f       | 1     | 15    | f        | 10378.4995 | 0.007       | -0.0024  |
| 0    | 17   | f       | 1     | 16    | f        | 10346.9519 | 0.007       | -0.0005  |
| 0    | 18   | f       | 1     | 17    | f        | 10315.6983 | 0.007       | 0.0064   |
| 0    | 19   | f       | 1     | 18    | f        | 10263.9016 | 0.007       | 0.0138   |
| 0    | 20   | f       | 1     | 19    | f        | 10228.8972 | 0.007       | 0.0043   |
| 0    | 21   | f       | 1     | 20    | f        | 10192.7087 | 0.007       | -0.0034  |
| 0    | 22   | f       | 1     | 21    | f        | 10155.1534 | 0.007       | -0.0061  |
| 0    | 23   | f       | 1     | 22    | f        | 10115.5253 | 0.007       | -0.0009  |
| 0    | 24   | f       | 1     | 23    | f        | 10075.7516 | 0.007       | 0.0113   |
| 0    | 25   | f       | 1     | 24    | f        | 10033.0638 | 0.007       | -0.0011  |
| 0    | 26   | f       | 1     | 25    | f        | 9989.0750  | 0.007       | -0.0033  |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 0    | 27   | f       | 1     | 26    | f        | 9943.8460  | 0.007       | 0.0004   |
| 0    | 28   | f       | 1     | 27    | f        | 9899.1097  | 0.02        | 0.0133   |
| 0    | 29   | f       | 1     | 28    | f        | 9847.3446  | 0.007       | 0.0058   |
| 0    | 30   | f       | 1     | 29    | f        | 9798.5333  | 0.007       | -0.0003  |
| 0    | 31   | f       | 1     | 30    | f        | 9748.1962  | 0.03        | 0.0240   |
| 0    | 32   | f       | 1     | 31    | f        | 9696.5162  | 0.007       | 0.0060   |
| 0    | 4    | f       | 1     | 5     | f        | 10428.1144 | 0.007       | 0.0001   |
| 0    | 5    | f       | 1     | 6     | f        | 10400.0498 | 0.007       | -0.0055  |
| 0    | 6    | f       | 1     | 7     | f        | 10369.4554 | 0.007       | -0.0068  |
| 0    | 7    | f       | 1     | 8     | f        | 10336.3630 | 0.007       | 0.0015   |
| 0    | 8    | f       | 1     | 9     | f        | 10301.0126 | 0.007       | -0.0029  |
| 0    | 9    | f       | 1     | 10    | f        | 10263.9016 | 0.007       | -0.0038  |
| 0    | 10   | f       | 1     | 11    | f        | 10225.1006 | 0.007       | 0.0101   |
| 0    | 11   | f       | 1     | 12    | f        | 10185.2187 | 0.007       | 0.0008   |
| 0    | 12   | f       | 1     | 13    | f        | 10143.9514 | 0.007       | 0.0000   |
| 0    | 13   | f       | 1     | 14    | f        | 10098.7223 | 0.05        | 0.0969   |
| 0    | 14   | f       | 1     | 15    | f        | 10048.9734 | 0.007       | 0.0008   |
| 0    | 15   | f       | 1     | 16    | f        | 9992.3842  | 0.007       | 0.0098   |
| 0    | 16   | f       | 1     | 17    | f        | 9934.9673  | 0.007       | 0.0026   |
| 0    | 17   | f       | 1     | 18    | f        | 9878.4279  | 0.007       | -0.0061  |
| 0    | 18   | f       | 1     | 19    | f        | 9822.5116  | 0.007       | -0.0087  |
| 0    | 19   | f       | 1     | 20    | f        | 9746.4042  | 0.007       | -0.0138  |
| 0    | 20   | f       | 1     | 21    | f        | 9687.4327  | 0.007       | -0.0117  |
| 0    | 21   | f       | 1     | 22    | f        | 9627.6682  | 0.07        | -0.0135  |
| 0    | 22   | f       | 1     | 23    | f        | 9566.9377  | 0.007       | -0.0086  |
| 0    | 23   | f       | 1     | 24    | f        | 9504.5619  | 0.007       | -0.0065  |
| 0    | 24   | f       | 1     | 25    | f        | 9442.4677  | 0.007       | 0.0039   |
| 0    | 25   | f       | 1     | 26    | f        | 9377.8853  | 0.007       | 0.0000   |
| 0    | 26   | f       | 1     | 27    | f        | 9312.4351  | 0.007       | 0.0111   |
| 0    | 27   | f       | 1     | 28    | f        | 9246.1959  | 0.007       | 0.0093   |
| 0    | 28   | f       | 1     | 29    | f        | 9180.8967  | 0.007       | -0.0140  |
| 0    | 29   | f       | 1     | 30    | f        | 9108.9599  | 0.02        | -0.0605  |
| 0    | 30   | f       | 1     | 31    | f        | 9040.2626  | 0.05        | -0.0472  |
| 0    | 4    | f       | 1     | 4     | e        | 10497.2641 | 0.07        | 0.0283   |
| 0    | 5    | f       | 1     | 5     | e        | 10482.9337 | 0.007       | 0.0171   |
| 0    | 6    | f       | 1     | 6     | e        | 10466.0252 | 0.007       | 0.0005   |
| 0    | 7    | f       | 1     | 7     | e        | 10446.5470 | 0.007       | -0.0023  |
| 0    | 8    | f       | 1     | 8     | e        | 10424.7135 | 0.007       | 0.0025   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 0    | 9    | f       | 1     | 9     | e        | 10401.0467 | 0.007       | -0.0025  |
| 0    | 4    | e       | 1     | 4     | f        | 10497.2641 | 0.07        | 0.0283   |
| 0    | 5    | e       | 1     | 5     | f        | 10482.9337 | 0.007       | 0.0171   |
| 0    | 6    | e       | 1     | 6     | f        | 10466.0252 | 0.007       | 0.0006   |
| 0    | 7    | e       | 1     | 7     | f        | 10446.6390 | 0.007       | -0.0005  |
| 0    | 8    | e       | 1     | 8     | f        | 10425.0096 | 0.007       | -0.0064  |
| 0    | 9    | e       | 1     | 9     | f        | 10401.3036 | 0.007       | -0.0015  |
| 1    | 5    | e       | 2     | 4     | e        | 10202.2810 | 0.007       | -0.0062  |
| 1    | 6    | e       | 2     | 5     | e        | 10199.0070 | 0.007       | -0.0031  |
| 1    | 7    | e       | 2     | 6     | e        | 10193.3484 | 0.007       | -0.0048  |
| 1    | 8    | e       | 2     | 7     | e        | 10185.7312 | 0.007       | 0.0040   |
| 1    | 9    | e       | 2     | 8     | e        | 10178.5422 | 0.007       | 0.0009   |
| 1    | 10   | e       | 2     | 9     | e        | 10163.9680 | 0.007       | -0.0027  |
| 1    | 11   | e       | 2     | 10    | e        | 10149.9973 | 0.007       | 0.0042   |
| 1    | 12   | e       | 2     | 11    | e        | 10138.5684 | 0.007       | 0.0009   |
| 1    | 13   | e       | 2     | 12    | e        | 10093.2007 | 0.07        | -0.1186  |
| 1    | 14   | e       | 2     | 13    | e        | 10071.1249 | 0.007       | -0.0057  |
| 1    | 15   | e       | 2     | 14    | e        | 10059.2072 | 0.007       | -0.0057  |
| 1    | 16   | e       | 2     | 15    | e        | 10053.6818 | 0.007       | 0.0088   |
| 1    | 17   | e       | 2     | 16    | e        | 9990.3645  | 10          | -0.3641  |
| 1    | 18   | e       | 2     | 17    | e        | 9947.5223  | 0.007       | 0.0107   |
| 1    | 19   | e       | 2     | 18    | e        | 9922.6187  | 0.007       | 0.0166   |
| 1    | 20   | e       | 2     | 19    | e        | 9896.7191  | 0.007       | 0.0012   |
| 1    | 21   | e       | 2     | 20    | e        | 9860.0746  | 0.007       | -0.0071  |
| 1    | 22   | e       | 2     | 21    | e        | 9834.2850  | 0.007       | 0.0031   |
| 1    | 4    | e       | 2     | 5     | e        | 10082.2445 | 0.007       | 0.0051   |
| 1    | 5    | e       | 2     | 6     | e        | 10054.8811 | 0.007       | -0.0037  |
| 1    | 6    | e       | 2     | 7     | e        | 10025.0438 | 0.007       | 0.0073   |
| 1    | 7    | e       | 2     | 8     | e        | 9992.9517  | 0.007       | 0.0044   |
| 1    | 8    | e       | 2     | 9     | e        | 9959.0513  | 0.007       | 0.0004   |
| 1    | 9    | e       | 2     | 10    | e        | 9925.7136  | 0.007       | 0.0062   |
| 1    | 10   | e       | 2     | 11    | e        | 9885.2380  | 0.07        | -0.0612  |
| 1    | 11   | e       | 2     | 12    | e        | 9845.4401  | 0.007       | 0.0006   |
| 1    | 12   | e       | 2     | 13    | e        | 9808.4491  | 0.007       | -0.0007  |
| 1    | 13   | e       | 2     | 14    | e        | 9737.9046  | 10          | -0.2720  |
| 1    | 14   | e       | 2     | 15    | e        | 9690.5869  | 0.007       | 0.0061   |
| 1    | 15   | e       | 2     | 16    | e        | 9653.8621  | 0.007       | 0.0088   |
| 1    | 16   | e       | 2     | 17    | e        | 9623.8618  | 0.007       | -0.0135  |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 1    | 18   | e       | 2     | 19    | e        | 9469.6304  | 0.007       | -0.0099  |
| 1    | 19   | e       | 2     | 20    | e        | 9421.2051  | 0.007       | -0.0109  |
| 1    | 20   | e       | 2     | 21    | e        | 9372.0946  | 0.007       | 0.0035   |
| 1    | 5    | f       | 2     | 4     | f        | 10202.2810 | 0.007       | -0.0077  |
| 1    | 6    | f       | 2     | 5     | f        | 10199.0070 | 0.007       | -0.0055  |
| 1    | 7    | f       | 2     | 6     | f        | 10193.3484 | 0.007       | -0.0042  |
| 1    | 9    | f       | 2     | 8     | f        | 10175.5845 | 0.007       | 0.0083   |
| 1    | 10   | f       | 2     | 9     | f        | 10161.8427 | 0.007       | 0.0063   |
| 1    | 11   | f       | 2     | 10    | f        | 10147.9095 | 0.007       | -0.0106  |
| 1    | 12   | f       | 2     | 11    | f        | 10146.3500 | 0.07        | -0.0871  |
| 1    | 13   | f       | 2     | 12    | f        | 10131.8817 | 0.07        | -0.0905  |
| 1    | 14   | f       | 2     | 13    | f        | 10072.6552 | 0.07        | -0.1039  |
| 1    | 15   | f       | 2     | 14    | f        | 10057.2615 | 0.07        | 0.0485   |
| 1    | 16   | f       | 2     | 15    | f        | 10048.4962 | 0.07        | -0.1034  |
| 1    | 17   | f       | 2     | 16    | f        | 10044.6286 | 0.007       | -0.0012  |
| 1    | 4    | f       | 2     | 5     | f        | 10082.2445 | 0.007       | 0.0063   |
| 1    | 5    | f       | 2     | 6     | f        | 10054.8811 | 0.007       | -0.0052  |
| 1    | 6    | f       | 2     | 7     | f        | 10025.0438 | 0.007       | 0.0052   |
| 1    | 7    | f       | 2     | 8     | f        | 9992.9517  | 0.007       | 0.0057   |
| 1    | 8    | f       | 2     | 9     | f        | 9958.8064  | 0.07        | -0.0663  |
| 1    | 9    | f       | 2     | 10    | f        | 9922.7874  | 0.007       | -0.0125  |
| 1    | 10   | f       | 2     | 11    | f        | 9883.0679  | 0.007       | 0.0051   |
| 1    | 11   | f       | 2     | 12    | f        | 9843.4390  | 0.07        | -0.0736  |
| 1    | 12   | f       | 2     | 13    | f        | 9816.2988  | 0.07        | -0.1011  |
| 1    | 13   | f       | 2     | 14    | f        | 9776.2907  | 10          | 0.1599   |
| 1    | 14   | f       | 2     | 15    | f        | 9692.3321  | 10          | -0.1041  |
| 1    | 15   | f       | 2     | 16    | f        | 9652.3432  | 0.007       | -0.0006  |
| 1    | 16   | f       | 2     | 17    | f        | 9618.9359  | 10          | 0.2431   |
| 1    | 17   | f       | 2     | 18    | f        | 9591.6380  | 0.007       | 0.0024   |
| 1    | 4    | f       | 2     | 4     | e        | 10149.2993 | 0.007       | -0.0026  |
| 1    | 5    | f       | 2     | 5     | e        | 10135.2301 | 0.007       | -0.0027  |
| 1    | 6    | f       | 2     | 6     | e        | 10118.6374 | 0.007       | 0.0126   |
| 1    | 7    | f       | 2     | 7     | e        | 10099.7786 | 0.05        | -0.0358  |
| 1    | 5    | e       | 0     | 4     | e        | 13842.1714 | 0.007       | 0.0068   |
| 1    | 6    | e       | 0     | 5     | e        | 13834.6542 | 0.007       | 0.0053   |
| 1    | 7    | e       | 0     | 6     | e        | 13823.9007 | 0.007       | 0.0033   |
| 1    | 8    | e       | 0     | 7     | e        | 13810.3544 | 0.007       | 0.0003   |
| 1    | 9    | e       | 0     | 8     | e        | 13796.3799 | 0.007       | -0.0014  |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 1    | 10   | e       | 0     | 9     | e        | 13774.1762 | 0.007       | 0.0002   |
| 1    | 11   | e       | 0     | 10    | e        | 13751.7532 | 0.007       | -0.0018  |
| 1    | 12   | e       | 0     | 11    | e        | 13731.0239 | 0.007       | 0.0017   |
| 1    | 13   | e       | 0     | 12    | e        | 13675.4254 | 0.007       | -0.0089  |
| 1    | 14   | e       | 0     | 13    | e        | 13642.5073 | 0.007       | 0.0008   |
| 1    | 15   | e       | 0     | 14    | e        | 13618.8286 | 0.007       | -0.0027  |
| 1    | 16   | e       | 0     | 15    | e        | 13600.7327 | 0.007       | 0.0034   |
| 1    | 17   | e       | 0     | 16    | e        | 13523.6622 | 0.007       | -0.0046  |
| 1    | 18   | e       | 0     | 17    | e        | 13466.9997 | 0.007       | -0.0015  |
| 1    | 19   | e       | 0     | 18    | e        | 13427.1218 | 0.007       | -0.0088  |
| 1    | 20   | e       | 0     | 19    | e        | 13385.4346 | 0.007       | -0.0068  |
| 1    | 21   | e       | 0     | 20    | e        | 13332.2533 | 0.007       | -0.0106  |
| 1    | 22   | e       | 0     | 21    | e        | 13289.2108 | 0.007       | -0.0073  |
| 1    | 23   | e       | 0     | 22    | e        | 13196.8415 | 0.007       | 0.0102   |
| 1    | 24   | e       | 0     | 23    | e        | 13123.4806 | 0.007       | 0.0034   |
| 1    | 4    | e       | 0     | 5     | e        | 13717.9109 | 0.007       | -0.0057  |
| 1    | 5    | e       | 0     | 6     | e        | 13685.4360 | 0.007       | 0.0018   |
| 1    | 6    | e       | 0     | 7     | e        | 13649.6807 | 0.007       | -0.0100  |
| 1    | 7    | e       | 0     | 8     | e        | 13610.7945 | 0.007       | -0.0030  |
| 1    | 8    | e       | 0     | 9     | e        | 13569.2664 | 0.007       | -0.0038  |
| 1    | 9    | e       | 0     | 10    | e        | 13527.4741 | 0.007       | -0.0044  |
| 1    | 10   | e       | 0     | 11    | e        | 13477.6290 | 0.007       | 0.0040   |
| 1    | 11   | e       | 0     | 12    | e        | 13427.7753 | 0.007       | -0.0002  |
| 1    | 12   | e       | 0     | 13    | e        | 13379.8363 | 0.007       | 0.0010   |
| 1    | 13   | e       | 0     | 14    | e        | 13297.2471 | 0.007       | 0.0099   |
| 1    | 14   | e       | 0     | 15    | e        | 13237.6370 | 0.007       | 0.0015   |
| 1    | 15   | e       | 0     | 16    | e        | 13187.5263 | 0.007       | 0.0018   |
| 1    | 16   | e       | 0     | 17    | e        | 13143.3108 | 0.007       | 0.0027   |
| 1    | 17   | e       | 0     | 18    | e        | 13040.4319 | 0.007       | 0.0043   |
| 1    | 18   | e       | 0     | 19    | e        | 12958.3275 | 0.007       | 0.0005   |
| 1    | 19   | e       | 0     | 20    | e        | 12893.3678 | 0.007       | 0.0016   |
| 1    | 20   | e       | 0     | 21    | e        | 12827.0135 | 0.007       | 0.0000   |
| 1    | 21   | e       | 0     | 22    | e        | 12749.5739 | 0.007       | 0.0165   |
| 1    | 22   | e       | 0     | 23    | e        | 12682.7759 | 0.007       | 0.0027   |
| 1    | 23   | e       | 0     | 24    | e        | 12567.1661 | 0.007       | -0.0101  |
| 1    | 24   | e       | 0     | 25    | e        | 12471.0626 | 0.007       | -0.0029  |
| 1    | 4    | f       | 0     | 4     | e        | 13789.2009 | 0.007       | -0.0007  |
| 1    | 5    | f       | 0     | 5     | e        | 13770.8746 | 0.007       | 0.0084   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 1    | 6    | f       | 0     | 6     | e        | 13749.2141 | 0.007       | -0.0037  |
| 1    | 7    | f       | 0     | 7     | e        | 13724.3639 | 0.007       | -0.0016  |
| 1    | 5    | f       | 0     | 4     | f        | 13842.1714 | 0.007       | 0.0053   |
| 1    | 6    | f       | 0     | 5     | f        | 13834.6542 | 0.007       | 0.0029   |
| 1    | 7    | f       | 0     | 6     | f        | 13823.9007 | 0.007       | 0.0038   |
| 1    | 8    | f       | 0     | 7     | f        | 13810.0392 | 0.007       | 0.0016   |
| 1    | 9    | f       | 0     | 8     | f        | 13793.4222 | 0.007       | 0.0049   |
| 1    | 10   | f       | 0     | 9     | f        | 13772.0607 | 0.007       | -0.0038  |
| 1    | 11   | f       | 0     | 10    | f        | 13749.6388 | 0.007       | 0.0021   |
| 1    | 12   | f       | 0     | 11    | f        | 13738.6998 | 0.007       | 0.0006   |
| 1    | 13   | f       | 0     | 12    | f        | 13714.0771 | 0.007       | 0.0075   |
| 1    | 14   | f       | 0     | 13    | f        | 13643.8548 | 0.007       | 0.0003   |
| 1    | 15   | f       | 0     | 14    | f        | 13616.7660 | 0.007       | 0.0001   |
| 1    | 16   | f       | 0     | 15    | f        | 13595.1189 | 0.007       | 0.0006   |
| 1    | 17   | f       | 0     | 16    | f        | 13577.7014 | 0.007       | 0.0016   |
| 1    | 4    | f       | 0     | 5     | f        | 13717.9109 | 0.007       | -0.0046  |
| 1    | 5    | f       | 0     | 6     | f        | 13685.4360 | 0.007       | 0.0002   |
| 1    | 6    | f       | 0     | 7     | f        | 13649.6807 | 0.007       | -0.0125  |
| 1    | 7    | f       | 0     | 8     | f        | 13610.7945 | 0.007       | -0.0028  |
| 1    | 8    | f       | 0     | 9     | f        | 13568.9490 | 0.007       | -0.0010  |
| 1    | 9    | f       | 0     | 10    | f        | 13524.5163 | 0.007       | 0.0004   |
| 1    | 10   | f       | 0     | 11    | f        | 13475.5164 | 0.007       | -0.0058  |
| 1    | 11   | f       | 0     | 12    | f        | 13425.6488 | 0.007       | 0.0100   |
| 1    | 12   | f       | 0     | 13    | f        | 13387.5003 | 0.007       | 0.0013   |
| 1    | 13   | f       | 0     | 14    | f        | 13335.9135 | 0.007       | -0.0068  |
| 1    | 14   | f       | 0     | 15    | f        | 13238.9542 | 0.007       | 0.0005   |
| 1    | 15   | f       | 0     | 16    | f        | 13185.4188 | 0.007       | -0.0006  |
| 1    | 16   | f       | 0     | 17    | f        | 13137.6177 | 0.007       | -0.0001  |
| 1    | 17   | f       | 0     | 18    | f        | 13094.3615 | 0.007       | -0.0022  |
| 2    | 9    | e       | 0     | 8     | e        | 15117.0796 | 0.007       | 0.0016   |
| 2    | 10   | e       | 0     | 9     | e        | 15093.6455 | 0.007       | 0.0009   |
| 2    | 11   | e       | 0     | 10    | e        | 15065.3443 | 0.007       | -0.0052  |
| 2    | 12   | e       | 0     | 11    | e        | 15036.0993 | 0.007       | -0.0070  |
| 2    | 13   | e       | 0     | 12    | e        | 15005.8933 | 0.007       | -0.0086  |
| 2    | 14   | e       | 0     | 13    | e        | 14977.3235 | 0.007       | -0.0192  |
| 2    | 15   | e       | 0     | 14    | e        | 14947.5975 | 0.02        | -0.0298  |
| 2    | 16   | e       | 0     | 15    | e        | 14917.8163 | 0.03        | -0.0333  |
| 2    | 8    | e       | 0     | 9     | e        | 14897.2603 | 0.007       | 0.0000   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 2    | 9    | e       | 0     | 10    | e        | 14848.1739 | 0.007       | -0.0016  |
| 2    | 10   | e       | 0     | 11    | e        | 14797.1041 | 0.007       | -0.0010  |
| 2    | 11   | e       | 0     | 12    | e        | 14741.3578 | 0.007       | 0.0050   |
| 2    | 12   | e       | 0     | 13    | e        | 14684.8972 | 0.007       | 0.0068   |
| 2    | 13   | e       | 0     | 14    | e        | 14627.7167 | 0.007       | 0.0085   |
| 2    | 14   | e       | 0     | 15    | e        | 14572.4156 | 0.007       | 0.0191   |
| 2    | 15   | e       | 0     | 16    | e        | 14516.2534 | 0.015       | 0.0165   |
| 2    | 16   | e       | 0     | 17    | e        | 14460.3275 | 0.03        | 0.0329   |
| 2    | 9    | f       | 0     | 8     | f        | 15117.0796 | 0.007       | 0.0023   |
| 2    | 10   | f       | 0     | 9     | f        | 15092.5806 | 0.007       | -0.0030  |
| 2    | 11   | f       | 0     | 10    | f        | 15064.6088 | 0.007       | -0.0028  |
| 2    | 12   | f       | 0     | 11    | f        | 15034.9730 | 0.007       | 0.0047   |
| 2    | 13   | f       | 0     | 12    | f        | 15004.2208 | 0.007       | 0.0112   |
| 2    | 14   | f       | 0     | 13    | f        | 14974.3107 | 0.007       | 0.0143   |
| 2    | 8    | f       | 0     | 9     | f        | 14897.2603 | 0.007       | 0.0000   |
| 2    | 9    | f       | 0     | 10    | f        | 14848.1739 | 0.007       | -0.0023  |
| 2    | 10   | f       | 0     | 11    | f        | 14796.0284 | 0.007       | 0.0029   |
| 2    | 11   | f       | 0     | 12    | f        | 14740.6212 | 0.007       | 0.0027   |
| 2    | 12   | f       | 0     | 13    | f        | 14683.7835 | 0.007       | -0.0047  |
| 2    | 13   | f       | 0     | 14    | f        | 14626.0656 | 0.007       | -0.0114  |
| 2    | 14   | f       | 0     | 15    | f        | 14569.4392 | 0.007       | -0.0146  |

 $A'^3\Phi_3 - X^3\Phi_4$ 

|   |    |   |   |    |   |            |       |         |
|---|----|---|---|----|---|------------|-------|---------|
| 0 | 5  | f | 0 | 4  | f | 12749.5739 | 0.1   | 0.0572  |
| 0 | 7  | f | 0 | 6  | f | 12756.6590 | 0.1   | -0.0953 |
| 0 | 8  | f | 0 | 7  | f | 12757.1450 | 0.1   | -0.0928 |
| 0 | 9  | f | 0 | 8  | f | 12755.5038 | 0.007 | 0.0079  |
| 0 | 10 | f | 0 | 9  | f | 12751.8543 | 0.007 | -0.0013 |
| 0 | 11 | f | 0 | 10 | f | 12745.9934 | 0.007 | 0.0022  |
| 0 | 12 | f | 0 | 11 | f | 12737.8831 | 0.007 | 0.0043  |
| 0 | 13 | f | 0 | 12 | f | 12727.4799 | 0.007 | -0.0078 |
| 0 | 14 | f | 0 | 13 | f | 12714.7307 | 0.007 | 0.0003  |
| 0 | 15 | f | 0 | 14 | f | 12699.6199 | 0.007 | -0.0034 |
| 0 | 16 | f | 0 | 15 | f | 12682.0789 | 0.007 | -0.0017 |
| 0 | 17 | f | 0 | 16 | f | 12661.4772 | 0.007 | 0.0007  |
| 0 | 18 | f | 0 | 17 | f | 12639.7991 | 0.007 | -0.0042 |
| 0 | 19 | f | 0 | 18 | f | 12614.7708 | 0.007 | 0.0056  |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 0    | 20   | f       | 0     | 19    | f        | 12587.8996 | 0.007       | 0.0013   |
| 0    | 6    | f       | 0     | 7     | f        | 12569.0703 | 0.07        | -0.0355  |
| 0    | 7    | f       | 0     | 8     | f        | 12543.4619 | 0.007       | -0.0110  |
| 0    | 4    | f       | 0     | 4     | e        | 12686.0263 | 0.1         | 0.0870   |
| 0    | 5    | f       | 0     | 5     | e        | 12678.3331 | 0.1         | 0.0042   |
| 0    | 6    | f       | 0     | 6     | e        | 12668.7777 | 0.1         | -0.2008  |
| 0    | 7    | f       | 0     | 7     | e        | 12657.0096 | 0.02        | 0.0120   |
| 0    | 8    | f       | 0     | 8     | e        | 12643.5724 | 0.1         | -0.0905  |
| 0    | 9    | f       | 0     | 9     | e        | 12627.9945 | 0.007       | -0.0042  |
| 0    | 10   | f       | 0     | 10    | e        | 12610.4735 | 0.007       | -0.0067  |
| 0    | 11   | f       | 0     | 11    | e        | 12590.8461 | 0.007       | -0.0050  |
| 0    | 12   | f       | 0     | 12    | e        | 12569.0703 | 0.007       | 0.0010   |
| 0    | 13   | f       | 0     | 13    | e        | 12545.0988 | 0.007       | 0.0127   |
| 0    | 14   | f       | 0     | 14    | e        | 12518.9520 | 0.007       | 0.0022   |
| 0    | 5    | e       | 0     | 5     | f        | 12678.2646 | 0.007       | 0.0090   |
| 0    | 6    | e       | 0     | 6     | f        | 12668.3296 | 0.007       | 0.0054   |
| 0    | 7    | e       | 0     | 7     | f        | 12657.1811 | 0.03        | -0.0739  |
| 0    | 8    | e       | 0     | 8     | f        | 12643.5724 | 0.007       | 0.0044   |
| 0    | 9    | e       | 0     | 9     | f        | 12627.9945 | 0.02        | -0.0093  |
| 0    | 10   | e       | 0     | 10    | f        | 12610.1200 | 0.007       | 0.0102   |
| 0    | 11   | e       | 0     | 11    | f        | 12589.8252 | 0.007       | -0.0026  |
| 0    | 12   | e       | 0     | 12    | f        | 12568.1216 | 0.007       | -0.0162  |
| 0    | 13   | e       | 0     | 13    | f        | 12543.5024 | 0.007       | -0.0065  |
| 0    | 14   | e       | 0     | 14    | f        | 12516.8748 | 0.05        | -0.0648  |
| 0    | 5    | e       | 0     | 4     | e        | 12749.5739 | 0.007       | -0.0065  |
| 0    | 6    | e       | 0     | 5     | e        | 12753.7929 | 0.01        | -0.0111  |
| 0    | 7    | e       | 0     | 6     | e        | 12756.6590 | 0.01        | -0.0095  |
| 0    | 8    | e       | 0     | 7     | e        | 12757.1450 | 0.007       | 0.0025   |
| 0    | 9    | e       | 0     | 8     | e        | 12755.5038 | 0.007       | 0.0040   |
| 0    | 10   | e       | 0     | 9     | e        | 12751.5267 | 0.007       | -0.0077  |
| 0    | 11   | e       | 0     | 10    | e        | 12744.9990 | 0.007       | -0.0163  |
| 0    | 12   | e       | 0     | 11    | e        | 12736.9328 | 0.007       | 0.0003   |
| 0    | 13   | e       | 0     | 12    | e        | 12725.8853 | 0.007       | -0.0067  |
| 0    | 14   | e       | 0     | 13    | e        | 12712.6289 | 0.007       | -0.0017  |
| 0    | 15   | e       | 0     | 14    | e        | 12697.2013 | 0.007       | 0.0070   |
| 0    | 5    | e       | 0     | 6     | e        | 12592.8366 | 0.007       | -0.0097  |
| 0    | 8    | e       | 0     | 9     | e        | 12516.0619 | 0.007       | -0.0066  |
| 0    | 7    | f       | 1     | 6     | f        | 10906.7327 | 0.1         | -0.0391  |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 0    | 8    | f       | 1     | 7     | f        | 10910.2271 | 0.1         | -0.0799  |
| 0    | 9    | f       | 1     | 8     | f        | 10912.0786 | 0.1         | -0.0817  |
| 0    | 10   | f       | 1     | 9     | f        | 10912.0786 | 0.1         | 0.0749   |
| 0    | 11   | f       | 1     | 10    | f        | 10910.5290 | 0.007       | 0.0075   |
| 0    | 12   | f       | 1     | 11    | f        | 10907.0933 | 0.007       | 0.0003   |
| 0    | 13   | f       | 1     | 12    | f        | 10901.7797 | 0.007       | -0.0121  |
| 0    | 14   | f       | 1     | 13    | f        | 10894.5414 | 0.07        | -0.0023  |
| 0    | 15   | f       | 1     | 14    | f        | 10885.3679 | 0.007       | -0.0082  |
| 0    | 16   | f       | 1     | 15    | f        | 10874.1696 | 0.007       | 0.0075   |
| 0    | 17   | f       | 1     | 16    | f        | 10860.3496 | 0.007       | 0.0055   |
| 0    | 18   | f       | 1     | 17    | f        | 10845.8654 | 0.007       | 0.0039   |
| 0    | 19   | f       | 1     | 18    | f        | 10828.4721 | 0.007       | -0.0042  |
| 0    | 20   | f       | 1     | 19    | f        | 10809.6317 | 0.007       | -0.0030  |
| 0    | 10   | f       | 1     | 11    | f        | 10624.5279 | 0.007       | -0.0151  |
| 0    | 5    | f       | 1     | 5     | e        | 10825.9258 | 0.007       | 0.0013   |
| 0    | 6    | f       | 1     | 6     | e        | 10818.7078 | 0.007       | -0.0009  |
| 0    | 7    | f       | 1     | 7     | e        | 10810.1902 | 1           | -0.0739  |
| 0    | 8    | f       | 1     | 8     | e        | 10800.1036 | 1           | -0.1373  |
| 0    | 9    | f       | 1     | 9     | e        | 10788.2863 | 0.007       | 0.0023   |
| 0    | 10   | f       | 1     | 10    | e        | 10774.9907 | 0.007       | 0.0125   |
| 0    | 11   | f       | 1     | 11    | e        | 10760.0301 | 0.007       | 0.0079   |
| 0    | 12   | f       | 1     | 12    | e        | 10743.2873 | 0.07        | 0.0619   |
| 0    | 13   | f       | 1     | 13    | e        | 10724.8631 | 0.07        | 0.0254   |
| 0    | 14   | f       | 1     | 14    | e        | 10704.5925 | 0.07        | 0.0521   |
| 0    | 15   | f       | 1     | 15    | e        | 10682.5205 | 0.07        | 0.0575   |
| 0    | 7    | e       | 1     | 7     | f        | 10810.1902 | 0.007       | 0.0121   |
| 0    | 8    | e       | 1     | 8     | f        | 10800.1036 | 0.07        | -0.0416  |
| 0    | 9    | e       | 1     | 9     | f        | 10788.2863 | 0.007       | -0.0006  |
| 0    | 10   | e       | 1     | 10    | f        | 10774.6744 | 0.007       | -0.0033  |
| 0    | 11   | e       | 1     | 11    | f        | 10759.0248 | 0.007       | 0.0039   |
| 0    | 12   | e       | 1     | 12    | f        | 10742.4330 | 0.07        | -0.0321  |
| 0    | 13   | e       | 1     | 13    | f        | 10723.2994 | 0.007       | 0.0047   |
| 0    | 14   | e       | 1     | 14    | f        | 10702.5487 | 0.007       | 0.0046   |
| 0    | 15   | e       | 1     | 15    | f        | 10680.1926 | 0.007       | -0.0080  |
| 0    | 5    | e       | 1     | 4     | e        | 10895.0331 | 0.007       | 0.0082   |
| 0    | 9    | e       | 1     | 8     | e        | 10912.0786 | 0.07        | -0.0865  |
| 0    | 11   | e       | 1     | 10    | e        | 10909.5152 | 0.007       | 0.0038   |
| 0    | 12   | e       | 1     | 11    | e        | 10906.1160 | 0.007       | 0.0140   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 0    | 13   | e       | 1     | 12    | e        | 10900.1483 | 0.007       | 0.0083   |
| 0    | 14   | e       | 1     | 13    | e        | 10892.3694 | 0.07        | 0.0348   |
| 0    | 15   | e       | 1     | 14    | e        | 10882.8273 | 0.07        | 0.0714   |
| 0    | 5    | e       | 1     | 6     | e        | 10743.0039 | 0.07        | -0.0471  |
| 0    | 7    | e       | 1     | 8     | e        | 10700.0244 | 0.007       | -0.0030  |
| 0    | 9    | e       | 1     | 10    | e        | 10651.2637 | 0.07        | -0.1284  |
| 0    | 10   | e       | 1     | 11    | e        | 10624.0954 | 0.07        | 0.0772   |
| 0    | 11   | e       | 1     | 12    | e        | 10595.2732 | 0.007       | 0.0112   |

 $A'^3\Phi_4 - X^3\Phi_3$ 

|   |    |   |   |    |   |            |       |         |
|---|----|---|---|----|---|------------|-------|---------|
| 0 | 5  | f | 1 | 4  | f | 12022.6392 | 0.007 | -0.0109 |
| 0 | 6  | f | 0 | 5  | f | 12025.6986 | 0.007 | 0.0158  |
| 0 | 7  | f | 0 | 6  | f | 12026.7225 | 0.007 | -0.0068 |
| 0 | 8  | f | 0 | 7  | f | 12025.4484 | 0.007 | 0.0011  |
| 0 | 9  | f | 0 | 8  | f | 12021.9650 | 0.007 | -0.0075 |
| 0 | 10 | f | 0 | 9  | f | 12016.1790 | 0.007 | -0.0065 |
| 0 | 11 | f | 0 | 10 | f | 12008.0582 | 0.007 | -0.0187 |
| 0 | 12 | f | 0 | 11 | f | 11997.5437 | 0.007 | -0.0083 |
| 0 | 13 | f | 0 | 12 | f | 11984.6319 | 0.007 | 0.0038  |
| 0 | 14 | f | 0 | 13 | f | 11969.3208 | 0.07  | 0.0368  |
| 0 | 15 | f | 0 | 14 | f | 11951.6828 | 0.007 | 0.0107  |
| 0 | 16 | f | 0 | 15 | f | 11931.6385 | 0.007 | -0.0031 |
| 0 | 17 | f | 0 | 16 | f | 11908.6010 | 0.007 | -0.0053 |
| 0 | 18 | f | 0 | 17 | f | 11884.6155 | 0.007 | -0.0123 |
| 0 | 19 | f | 0 | 18 | f | 11857.4260 | 0.07  | 0.0367  |
| 0 | 20 | f | 0 | 19 | f | 11828.7263 | 0.007 | -0.0121 |
| 0 | 21 | f | 0 | 20 | f | 11797.3040 | 0.007 | 0.0054  |
| 0 | 22 | f | 0 | 21 | f | 11763.6648 | 0.007 | 0.0085  |
| 0 | 23 | f | 0 | 22 | f | 11726.8736 | 0.007 | 0.0125  |
| 0 | 24 | f | 0 | 23 | f | 11691.9993 | 0.007 | -0.0094 |
| 0 | 3  | f | 0 | 4  | f | 11908.7414 | 0.007 | -0.0004 |
| 0 | 4  | f | 0 | 5  | f | 11886.5126 | 0.007 | -0.0023 |
| 0 | 5  | f | 0 | 6  | f | 11863.0353 | 0.007 | 0.0073  |
| 0 | 6  | f | 0 | 7  | f | 11837.4475 | 0.007 | -0.0154 |
| 0 | 7  | f | 0 | 8  | f | 11809.8826 | 0.007 | 0.0141  |
| 0 | 8  | f | 0 | 9  | f | 11780.2807 | 0.007 | -0.0019 |
| 0 | 9  | f | 0 | 10 | f | 11748.6450 | 0.007 | 0.0003  |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 0    | 10   | f       | 0     | 11    | f        | 11714.9394 | 0.007       | 0.0151   |
| 0    | 11   | f       | 0     | 12    | f        | 11679.1721 | 0.007       | 0.0048   |
| 0    | 12   | f       | 0     | 13    | f        | 11641.3145 | 0.007       | 0.0007   |
| 0    | 13   | f       | 0     | 14    | f        | 11601.3690 | 0.007       | 0.0023   |
| 0    | 14   | f       | 0     | 15    | f        | 11559.3924 | 0.007       | -0.0037  |
| 0    | 15   | f       | 0     | 16    | f        | 11515.3868 | 0.007       | -0.0003  |
| 0    | 16   | f       | 0     | 17    | f        | 11469.3866 | 0.007       | -0.0030  |
| 0    | 17   | f       | 0     | 18    | f        | 11420.8216 | 0.007       | -0.0012  |
| 0    | 18   | f       | 0     | 19    | f        | 11371.7400 | 0.007       | 0.0131   |
| 0    | 19   | f       | 0     | 20    | f        | 11320.0163 | 0.007       | -0.0015  |
| 0    | 20   | f       | 0     | 21    | f        | 11267.1596 | 0.007       | 0.0147   |
| 0    | 21   | f       | 0     | 22    | f        | 11212.2162 | 0.007       | -0.0040  |
| 0    | 22   | f       | 0     | 23    | f        | 11155.5904 | 0.007       | -0.0069  |
| 0    | 23   | f       | 0     | 24    | f        | 11096.4089 | 0.007       | -0.0105  |
| 0    | 24   | f       | 0     | 25    | f        | 11039.7181 | 0.007       | 0.0114   |
| 0    | 3    | f       | 0     | 3     | e        | 11966.8995 | 0.007       | -0.0019  |
| 0    | 4    | f       | 0     | 4     | e        | 11959.0570 | 0.07        | 0.0671   |
| 0    | 5    | f       | 0     | 5     | e        | 11950.0609 | 0.07        | 0.0128   |
| 0    | 6    | f       | 0     | 6     | e        | 11938.8586 | 0.07        | -0.0042  |
| 0    | 7    | f       | 0     | 7     | e        | 11925.5321 | 0.1         | 0.1841   |
| 0    | 8    | f       | 0     | 8     | e        | 11910.0915 | 0.5         | 0.4678   |
| 0    | 5    | e       | 0     | 4     | e        | 12022.6392 | 0.5         | -0.0611  |
| 0    | 6    | e       | 0     | 5     | e        | 12025.6986 | 10          | -0.1804  |
| 0    | 7    | e       | 0     | 6     | e        | 12026.7225 | 10          | 0.2044   |
| 0    | 8    | e       | 0     | 7     | e        | 12025.4484 | 10          | 0.3936   |
| 0    | 9    | e       | 0     | 8     | e        | 12021.9650 | 10          | 0.6203   |
| 0    | 10   | e       | 0     | 9     | e        | 12016.1790 | 10          | 0.8930   |
| 0    | 11   | e       | 0     | 10    | e        | 12008.0582 | 10          | 1.2203   |
| 0    | 14   | e       | 0     | 13    | e        | 11977.4499 | 0.007       | -0.0029  |
| 0    | 16   | e       | 0     | 15    | e        | 11942.8805 | 0.007       | -0.0009  |
| 0    | 17   | e       | 0     | 16    | e        | 11925.5321 | 0.007       | -0.0011  |
| 0    | 3    | e       | 0     | 4     | e        | 11908.7414 | 10          | -0.0012  |
| 0    | 4    | e       | 0     | 5     | e        | 11886.5126 | 10          | -0.0011  |
| 0    | 5    | e       | 0     | 6     | e        | 11863.3069 | 10          | -0.2025  |
| 0    | 6    | e       | 0     | 7     | e        | 11837.7463 | 10          | -0.2587  |
| 0    | 7    | e       | 0     | 8     | e        | 11810.2829 | 10          | 0.3316   |
| 0    | 8    | e       | 0     | 9     | e        | 11780.9184 | 10          | 0.6900   |
| 0    | 9    | e       | 0     | 10    | e        | 11749.6956 | 10          | 1.1992   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 0    | 10   | e       | 0     | 11    | e        | 11716.8787 | 10          | 1.6354   |
| 0    | 11   | e       | 0     | 12    | e        | 11682.9216 | 10          | 1.6687   |
| 0    | 12   | e       | 0     | 13    | e        | 11650.5633 | 0.007       | 0.0013   |

## B.2 Line list for CoD

Table B.2: Line list for CoD.

| Lines from Refs. [4,5] of Chapter 5 |      |         |       |       |          |          |             |          |
|-------------------------------------|------|---------|-------|-------|----------|----------|-------------|----------|
| $A^3\Phi_4 - X^3\Phi_4$             |      |         |       |       |          |          |             |          |
| $v'$                                | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed | Uncertainty | calc-obs |
| 0                                   | 5    | e       | 0     | 4     | e        | 22299.23 | 0.03        | 0.074    |
| 0                                   | 6    | e       | 0     | 5     | e        | 22302.21 | 0.03        | 0.005    |
| 0                                   | 7    | e       | 0     | 6     | e        | 22304.29 | 0.03        | 0.002    |
| 0                                   | 8    | e       | 0     | 7     | e        | 22305.61 | 0.03        | -0.030   |
| 0                                   | 9    | e       | 0     | 8     | e        | 22306.18 | 0.03        | -0.065   |
| 0                                   | 10   | e       | 0     | 9     | e        | 22305.82 | 0.03        | -0.001   |
| 0                                   | 11   | e       | 0     | 10    | e        | 22304.71 | 0.03        | 0.032    |
| 0                                   | 12   | e       | 0     | 11    | e        | 22302.81 | 0.03        | -0.010   |
| 0                                   | 13   | e       | 0     | 12    | e        | 22300.27 | 0.03        | -0.017   |
| 0                                   | 14   | e       | 0     | 13    | e        | 22297.04 | 0.03        | 0.033    |
| 0                                   | 15   | e       | 0     | 14    | e        | 22292.40 | 0.03        | -0.005   |
| 0                                   | 16   | e       | 0     | 15    | e        | 22287.21 | 0.03        | 0.021    |
| 0                                   | 17   | e       | 0     | 16    | e        | 22281.17 | 0.03        | 0.007    |
| 0                                   | 18   | e       | 0     | 17    | e        | 22274.23 | 0.03        | 0.018    |
| 0                                   | 19   | e       | 0     | 18    | e        | 22266.45 | 0.03        | -0.026   |
| 0                                   | 20   | e       | 0     | 19    | e        | 22257.75 | 0.03        | 0.015    |
| 0                                   | 21   | e       | 0     | 20    | e        | 22248.24 | 0.03        | 0.016    |
| 0                                   | 22   | e       | 0     | 21    | e        | 22237.66 | 0.03        | 0.064    |
| 0                                   | 23   | e       | 0     | 22    | e        | 22225.86 | 0.03        | 0.039    |
| 0                                   | 24   | e       | 0     | 23    | e        | 22211.96 | 0.03        | -0.050   |
| 0                                   | 25   | e       | 0     | 24    | e        | 22204.58 | 0.03        | 0.012    |
| 0                                   | 26   | e       | 0     | 25    | e        | 22189.91 | 0.03        | 0.021    |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|----------|-------------|----------|
| 0    | 27   | e       | 0     | 26    | e        | 22174.80 | 0.03        | 0.007    |
| 0    | 28   | e       | 0     | 27    | e        | 22158.91 | 0.03        | 0.009    |
| 0    | 29   | e       | 0     | 28    | e        | 22142.14 | 0.03        | -0.006   |
| 0    | 30   | e       | 0     | 29    | e        | 22124.45 | 0.03        | -0.016   |
| 0    | 31   | e       | 0     | 30    | e        | 22105.72 | 0.03        | 0.000    |
| 0    | 4    | e       | 0     | 5     | e        | 22228.79 | 0.03        | -0.017   |
| 0    | 5    | e       | 0     | 6     | e        | 22217.59 | 0.03        | -0.041   |
| 0    | 6    | e       | 0     | 7     | e        | 22205.63 | 0.03        | 0.035    |
| 0    | 7    | e       | 0     | 8     | e        | 22192.99 | 0.03        | -0.009   |
| 0    | 8    | e       | 0     | 9     | e        | 22179.56 | 0.03        | -0.011   |
| 0    | 9    | e       | 0     | 10    | e        | 22165.41 | 0.03        | -0.001   |
| 0    | 10   | e       | 0     | 11    | e        | 22150.50 | 0.03        | -0.012   |
| 0    | 11   | e       | 0     | 12    | e        | 22134.85 | 0.03        | -0.009   |
| 0    | 12   | e       | 0     | 13    | e        | 22118.40 | 0.03        | -0.009   |
| 0    | 13   | e       | 0     | 14    | e        | 22101.45 | 0.03        | -0.048   |
| 0    | 14   | e       | 0     | 15    | e        | 22083.86 | 0.03        | -0.009   |
| 0    | 15   | e       | 0     | 16    | e        | 22064.85 | 0.03        | 0.028    |
| 0    | 16   | e       | 0     | 17    | e        | 22045.46 | 0.03        | 0.041    |
| 0    | 17   | e       | 0     | 18    | e        | 22025.31 | 0.03        | 0.011    |
| 0    | 18   | e       | 0     | 19    | e        | 22004.34 | 0.03        | 0.016    |
| 0    | 19   | e       | 0     | 20    | e        | 21982.62 | 0.03        | -0.027   |
| 0    | 20   | e       | 0     | 21    | e        | 21960.11 | 0.03        | -0.013   |
| 0    | 21   | e       | 0     | 22    | e        | 21936.88 | 0.03        | -0.023   |
| 0    | 22   | e       | 0     | 23    | e        | 21912.71 | 0.03        | -0.005   |
| 0    | 23   | e       | 0     | 24    | e        | 21887.39 | 0.03        | -0.014   |
| 0    | 24   | e       | 0     | 25    | e        | 21860.04 | 0.03        | -0.036   |
| 0    | 25   | e       | 0     | 26    | e        | 21839.44 | 0.03        | -0.011   |
| 0    | 26   | e       | 0     | 27    | e        | 21811.66 | 0.03        | -0.020   |
| 0    | 27   | e       | 0     | 28    | e        | 21783.53 | 0.03        | -0.007   |
| 0    | 28   | e       | 0     | 29    | e        | 21754.79 | 0.03        | -0.009   |
| 0    | 29   | e       | 0     | 30    | e        | 21725.28 | 0.03        | 0.006    |
| 0    | 30   | e       | 0     | 31    | e        | 21695.01 | 0.03        | 0.015    |
| 0    | 4    | f       | 0     | 4     | e        | 22265.94 | 0.03        | 0.011    |
| 0    | 5    | f       | 0     | 5     | e        | 22262.17 | 0.03        | -0.029   |
| 0    | 6    | f       | 0     | 6     | e        | 22257.64 | 0.03        | 0.001    |
| 0    | 7    | f       | 0     | 7     | e        | 22252.33 | 0.03        | -0.009   |
| 0    | 8    | f       | 0     | 8     | e        | 22246.22 | 0.03        | 0.004    |
| 0    | 9    | f       | 0     | 9     | e        | 22239.45 | 0.03        | -0.024   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|----------|-------------|----------|
| 0    | 10   | f       | 0     | 10    | e        | 22231.79 | 0.03        | 0.014    |
| 0    | 11   | f       | 0     | 11    | e        | 22223.40 | 0.03        | 0.027    |
| 0    | 12   | f       | 0     | 12    | e        | 22214.27 | 0.03        | -0.027   |
| 0    | 13   | f       | 0     | 13    | e        | 22204.58 | 0.03        | -0.065   |
| 0    | 14   | f       | 0     | 14    | e        | 22194.00 | 0.03        | 0.031    |
| 0    | 15   | f       | 0     | 15    | e        | 22182.20 | 0.03        | 0.001    |
| 0    | 16   | f       | 0     | 16    | e        | 22169.83 | 0.03        | 0.062    |
| 0    | 17   | f       | 0     | 17    | e        | 22156.79 | 0.03        | -0.012   |
| 0    | 18   | f       | 0     | 18    | e        | 22142.86 | 0.03        | 0.012    |
| 0    | 4    | f       | 0     | 4     | e        | 22265.94 | 0.03        | 0.011    |
| 0    | 5    | f       | 0     | 5     | e        | 22262.17 | 0.03        | -0.029   |
| 0    | 6    | f       | 0     | 6     | e        | 22257.64 | 0.03        | 0.001    |
| 0    | 7    | f       | 0     | 7     | e        | 22252.33 | 0.03        | -0.009   |
| 0    | 8    | f       | 0     | 8     | e        | 22246.22 | 0.03        | 0.004    |
| 0    | 9    | f       | 0     | 9     | e        | 22239.45 | 0.03        | -0.024   |
| 0    | 10   | f       | 0     | 10    | e        | 22231.79 | 0.03        | 0.014    |
| 0    | 11   | f       | 0     | 11    | e        | 22223.40 | 0.03        | 0.027    |
| 0    | 12   | f       | 0     | 12    | e        | 22214.27 | 0.03        | -0.027   |
| 0    | 13   | f       | 0     | 13    | e        | 22204.58 | 0.03        | -0.065   |
| 0    | 14   | f       | 0     | 14    | e        | 22194.00 | 0.03        | 0.031    |
| 0    | 15   | f       | 0     | 15    | e        | 22182.20 | 0.03        | 0.001    |
| 0    | 16   | f       | 0     | 16    | e        | 22169.83 | 0.03        | 0.062    |
| 0    | 17   | f       | 0     | 17    | e        | 22156.79 | 0.03        | -0.012   |
| 0    | 18   | f       | 0     | 18    | e        | 22142.86 | 0.03        | 0.012    |
| 0    | 5    | f       | 0     | 4     | f        | 22299.23 | 0.03        | 0.086    |
| 0    | 6    | f       | 0     | 5     | f        | 22302.21 | 0.03        | 0.011    |
| 0    | 7    | f       | 0     | 6     | f        | 22304.29 | 0.03        | 0.001    |
| 0    | 8    | f       | 0     | 7     | f        | 22305.61 | 0.03        | -0.045   |
| 0    | 9    | f       | 0     | 8     | f        | 22306.18 | 0.03        | -0.064   |
| 0    | 10   | f       | 0     | 9     | f        | 22305.82 | 0.03        | 0.000    |
| 0    | 11   | f       | 0     | 10    | f        | 22304.71 | 0.03        | 0.032    |
| 0    | 12   | f       | 0     | 11    | f        | 22302.81 | 0.03        | 0.018    |
| 0    | 13   | f       | 0     | 12    | f        | 22300.27 | 0.03        | 0.068    |
| 0    | 14   | f       | 0     | 13    | f        | 22297.04 | 0.03        | 0.019    |
| 0    | 15   | f       | 0     | 14    | f        | 22292.40 | 0.03        | -0.005   |
| 0    | 16   | f       | 0     | 15    | f        | 22287.21 | 0.03        | 0.004    |
| 0    | 17   | f       | 0     | 16    | f        | 22281.17 | 0.03        | 0.015    |
| 0    | 18   | f       | 0     | 17    | f        | 22274.32 | 0.03        | 0.000    |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|----------|-------------|----------|
| 0    | 19   | f       | 0     | 18    | f        | 22266.61 | 0.03        | 0.003    |
| 0    | 20   | f       | 0     | 19    | f        | 22257.96 | 0.03        | 0.049    |
| 0    | 21   | f       | 0     | 20    | f        | 22248.49 | 0.03        | -0.003   |
| 0    | 22   | f       | 0     | 21    | f        | 22238.05 | 0.03        | 0.054    |
| 0    | 23   | f       | 0     | 22    | f        | 22226.70 | 0.03        | 0.004    |
| 0    | 24   | f       | 0     | 23    | f        | 22214.27 | 0.03        | 0.030    |
| 0    | 25   | f       | 0     | 24    | f        | 22200.74 | 0.03        | 0.043    |
| 0    | 26   | f       | 0     | 25    | f        | 22185.53 | 0.03        | 0.046    |
| 0    | 27   | f       | 0     | 26    | f        | 22178.28 | 0.03        | -0.009   |
| 0    | 28   | f       | 0     | 27    | f        | 22160.43 | 0.03        | 0.064    |
| 0    | 29   | f       | 0     | 28    | f        | 22142.86 | 0.03        | 0.022    |
| 0    | 30   | f       | 0     | 29    | f        | 22124.63 | 0.03        | -0.024   |
| 0    | 4    | f       | 0     | 5     | f        | 22228.79 | 0.03        | -0.014   |
| 0    | 5    | f       | 0     | 6     | f        | 22217.59 | 0.03        | -0.029   |
| 0    | 6    | f       | 0     | 7     | f        | 22205.63 | 0.03        | 0.041    |
| 0    | 7    | f       | 0     | 8     | f        | 22192.99 | 0.03        | -0.010   |
| 0    | 8    | f       | 0     | 9     | f        | 22179.56 | 0.03        | -0.026   |
| 0    | 9    | f       | 0     | 10    | f        | 22165.41 | 0.03        | 0.000    |
| 0    | 10   | f       | 0     | 11    | f        | 22150.50 | 0.03        | -0.012   |
| 0    | 11   | f       | 0     | 12    | f        | 22134.85 | 0.03        | -0.009   |
| 0    | 12   | f       | 0     | 13    | f        | 22118.40 | 0.03        | 0.020    |
| 0    | 13   | f       | 0     | 14    | f        | 22101.45 | 0.03        | 0.037    |
| 0    | 14   | f       | 0     | 15    | f        | 22083.86 | 0.03        | -0.024   |
| 0    | 15   | f       | 0     | 16    | f        | 22064.85 | 0.03        | 0.028    |
| 0    | 16   | f       | 0     | 17    | f        | 22045.46 | 0.03        | 0.024    |
| 0    | 17   | f       | 0     | 18    | f        | 22025.31 | 0.03        | 0.017    |
| 0    | 18   | f       | 0     | 19    | f        | 22004.45 | 0.03        | -0.023   |
| 0    | 19   | f       | 0     | 20    | f        | 21982.78 | 0.03        | 0.001    |
| 0    | 20   | f       | 0     | 21    | f        | 21960.38 | 0.03        | -0.042   |
| 0    | 21   | f       | 0     | 22    | f        | 21937.10 | 0.03        | -0.015   |
| 0    | 22   | f       | 0     | 23    | f        | 21913.09 | 0.03        | -0.009   |
| 0    | 23   | f       | 0     | 24    | f        | 21888.20 | 0.03        | -0.025   |
| 0    | 24   | f       | 0     | 25    | f        | 21862.37 | 0.03        | 0.017    |
| 0    | 25   | f       | 0     | 26    | f        | 21835.58 | 0.03        | 0.030    |
| 0    | 26   | f       | 0     | 27    | f        | 21807.29 | 0.03        | -0.019   |
| 0    | 27   | f       | 0     | 28    | f        | 21786.96 | 0.03        | 0.009    |
| 0    | 28   | f       | 0     | 29    | f        | 21756.40 | 0.03        | -0.066   |
| 0    | 29   | f       | 0     | 30    | f        | 21726.03 | 0.03        | -0.023   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|----------|-------------|----------|
| 0    | 30   | f       | 0     | 31    | f        | 21695.14 | 0.03        | 0.022    |
| 1    | 5    | e       | 0     | 4     | e        | 23413.63 | 0.03        | 0.031    |
| 1    | 6    | e       | 0     | 5     | e        | 23415.29 | 0.03        | -0.003   |
| 1    | 7    | e       | 0     | 6     | e        | 23415.94 | 0.03        | 0.006    |
| 1    | 8    | e       | 0     | 7     | e        | 23415.61 | 0.03        | 0.001    |
| 1    | 9    | e       | 0     | 8     | e        | 23414.30 | 0.03        | 0.006    |
| 1    | 10   | e       | 0     | 9     | e        | 23411.98 | 0.03        | -0.029   |
| 1    | 11   | e       | 0     | 10    | e        | 23408.64 | 0.03        | -0.006   |
| 1    | 12   | e       | 0     | 11    | e        | 23404.33 | 0.03        | -0.030   |
| 1    | 13   | e       | 0     | 12    | e        | 23399.85 | 0.03        | -0.012   |
| 1    | 14   | e       | 0     | 13    | e        | 23392.84 | 0.03        | 0.014    |
| 1    | 15   | e       | 0     | 14    | e        | 23385.31 | 0.03        | 0.017    |
| 1    | 16   | e       | 0     | 15    | e        | 23376.79 | 0.03        | 0.024    |
| 1    | 17   | e       | 0     | 16    | e        | 23367.23 | 0.03        | -0.034   |
| 1    | 18   | e       | 0     | 17    | e        | 23356.56 | 0.03        | 0.010    |
| 1    | 19   | e       | 0     | 18    | e        | 23344.80 | 0.03        | 0.024    |
| 1    | 20   | e       | 0     | 19    | e        | 23331.91 | 0.03        | 0.013    |
| 1    | 21   | e       | 0     | 20    | e        | 23317.87 | 0.03        | 0.051    |
| 1    | 22   | e       | 0     | 21    | e        | 23302.69 | 0.03        | 0.022    |
| 1    | 23   | e       | 0     | 22    | e        | 23286.30 | 0.03        | 0.000    |
| 1    | 24   | e       | 0     | 23    | e        | 23268.66 | 0.03        | 0.018    |
| 1    | 4    | e       | 0     | 5     | e        | 23343.97 | 0.03        | 0.017    |
| 1    | 5    | e       | 0     | 6     | e        | 23331.91 | 0.03        | -0.004   |
| 1    | 6    | e       | 0     | 7     | e        | 23318.66 | 0.03        | 0.077    |
| 1    | 7    | e       | 0     | 8     | e        | 23304.60 | 0.03        | 0.035    |
| 1    | 8    | e       | 0     | 9     | e        | 23289.57 | 0.03        | 0.010    |
| 1    | 9    | e       | 0     | 10    | e        | 23273.55 | 0.03        | 0.050    |
| 1    | 10   | e       | 0     | 11    | e        | 23256.60 | 0.03        | 0.020    |
| 1    | 11   | e       | 0     | 12    | e        | 23238.72 | 0.03        | 0.013    |
| 1    | 12   | e       | 0     | 13    | e        | 23219.84 | 0.03        | 0.051    |
| 1    | 13   | e       | 0     | 14    | e        | 23200.96 | 0.03        | 0.027    |
| 1    | 14   | e       | 0     | 15    | e        | 23179.63 | 0.03        | 0.002    |
| 1    | 15   | e       | 0     | 16    | e        | 23157.78 | 0.03        | 0.030    |
| 1    | 16   | e       | 0     | 17    | e        | 23135.06 | 0.03        | 0.024    |
| 1    | 17   | e       | 0     | 18    | e        | 23111.33 | 0.03        | 0.010    |
| 1    | 18   | e       | 0     | 19    | e        | 23086.72 | 0.03        | -0.042   |
| 1    | 19   | e       | 0     | 20    | e        | 23060.98 | 0.03        | 0.013    |
| 1    | 20   | e       | 0     | 21    | e        | 23034.28 | 0.03        | -0.025   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|----------|-------------|----------|
| 1    | 21   | e       | 0     | 22    | e        | 23006.56 | 0.03        | -0.038   |
| 1    | 22   | e       | 0     | 23    | e        | 22977.72 | 0.03        | -0.027   |
| 1    | 23   | e       | 0     | 24    | e        | 22947.81 | 0.03        | -0.033   |
| 1    | 24   | e       | 0     | 25    | e        | 22916.79 | 0.03        | -0.018   |
| 1    | 4    | f       | 0     | 4     | e        | 23381.17 | 0.03        | 0.020    |
| 1    | 5    | f       | 0     | 5     | e        | 23376.50 | 0.03        | -0.007   |
| 1    | 6    | f       | 0     | 6     | e        | 23370.70 | 0.03        | 0.006    |
| 1    | 7    | f       | 0     | 7     | e        | 23363.97 | 0.03        | -0.006   |
| 1    | 8    | f       | 0     | 8     | e        | 23356.29 | 0.03        | -0.011   |
| 1    | 9    | f       | 0     | 9     | e        | 23347.64 | 0.03        | -0.016   |
| 1    | 10   | f       | 0     | 10    | e        | 23337.94 | 0.03        | 0.003    |
| 1    | 11   | f       | 0     | 11    | e        | 23327.33 | 0.03        | -0.019   |
| 1    | 12   | f       | 0     | 12    | e        | 23315.68 | 0.03        | 0.001    |
| 1    | 5    | f       | 0     | 4     | f        | 23413.63 | 0.03        | 0.038    |
| 1    | 6    | f       | 0     | 5     | f        | 23415.29 | 0.03        | -0.004   |
| 1    | 7    | f       | 0     | 6     | f        | 23415.94 | 0.03        | -0.006   |
| 1    | 8    | f       | 0     | 7     | f        | 23415.61 | 0.03        | 0.010    |
| 1    | 9    | f       | 0     | 8     | f        | 23414.30 | 0.03        | 0.014    |
| 1    | 10   | f       | 0     | 9     | f        | 23411.98 | 0.03        | -0.021   |
| 1    | 11   | f       | 0     | 10    | f        | 23408.64 | 0.03        | -0.014   |
| 1    | 12   | f       | 0     | 11    | f        | 23404.33 | 0.03        | -0.064   |
| 1    | 13   | f       | 0     | 12    | f        | 23398.91 | 0.03        | -0.019   |
| 1    | 14   | f       | 0     | 13    | f        | 23392.48 | 0.03        | 0.007    |
| 1    | 15   | f       | 0     | 14    | f        | 23384.97 | 0.03        | 0.009    |
| 1    | 16   | f       | 0     | 15    | f        | 23376.37 | 0.03        | -0.013   |
| 1    | 17   | f       | 0     | 16    | f        | 23366.51 | 0.03        | 0.032    |
| 1    | 18   | f       | 0     | 17    | f        | 23354.97 | 0.03        | -0.017   |
| 1    | 20   | f       | 0     | 19    | f        | 23332.91 | 0.03        | -0.003   |
| 1    | 21   | f       | 0     | 20    | f        | 23318.66 | 0.03        | -0.026   |
| 1    | 22   | f       | 0     | 21    | f        | 23303.23 | 0.03        | 0.047    |
| 1    | 23   | f       | 0     | 22    | f        | 23286.80 | 0.03        | 0.020    |
| 1    | 4    | f       | 0     | 5     | f        | 23343.97 | 0.03        | 0.045    |
| 1    | 5    | f       | 0     | 6     | f        | 23331.91 | 0.03        | 0.003    |
| 1    | 6    | f       | 0     | 7     | f        | 23318.66 | 0.03        | 0.076    |
| 1    | 7    | f       | 0     | 8     | f        | 23304.60 | 0.03        | 0.023    |
| 1    | 8    | f       | 0     | 9     | f        | 23289.57 | 0.03        | 0.019    |
| 1    | 9    | f       | 0     | 10    | f        | 23273.55 | 0.03        | 0.058    |
| 1    | 10   | f       | 0     | 11    | f        | 23256.60 | 0.03        | 0.027    |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|----------|-------------|----------|
| 1    | 11   | f       | 0     | 12    | f        | 23238.72 | 0.03        | 0.005    |
| 1    | 12   | f       | 0     | 13    | f        | 23219.84 | 0.03        | 0.018    |
| 1    | 13   | f       | 0     | 14    | f        | 23200.05 | 0.03        | -0.010   |
| 1    | 14   | f       | 0     | 15    | f        | 23179.23 | 0.03        | 0.034    |
| 1    | 15   | f       | 0     | 16    | f        | 23157.47 | 0.03        | -0.008   |
| 1    | 16   | f       | 0     | 17    | f        | 23134.61 | 0.03        | 0.017    |
| 1    | 17   | f       | 0     | 18    | f        | 23110.78 | 0.03        | -0.096   |
| 1    | 18   | f       | 0     | 19    | f        | 23085.05 | 0.03        | 0.010    |
| 1    | 20   | f       | 0     | 21    | f        | 23035.28 | 0.03        | -0.044   |
| 1    | 21   | f       | 0     | 22    | f        | 23007.26 | 0.03        | -0.028   |
| 1    | 22   | f       | 0     | 23    | f        | 22978.29 | 0.03        | -0.036   |
| 1    | 23   | f       | 0     | 24    | f        | 22948.32 | 0.03        | -0.029   |
| 0    | 5    | e       | 1     | 4     | e        | 20961.53 | 0.03        | -0.006   |
| 0    | 6    | e       | 1     | 5     | e        | 20965.29 | 0.03        | -0.071   |
| 0    | 7    | e       | 1     | 6     | e        | 20968.21 | 0.03        | 0.027    |
| 0    | 8    | e       | 1     | 7     | e        | 20970.65 | 0.03        | -0.027   |
| 0    | 9    | e       | 1     | 8     | e        | 20972.38 | 0.03        | 0.032    |
| 0    | 10   | e       | 1     | 9     | e        | 20973.50 | 0.03        | 0.027    |
| 0    | 11   | e       | 1     | 10    | e        | 20973.88 | 10          | 0.137    |
| 0    | 12   | e       | 1     | 11    | e        | 20973.78 | 0.03        | 0.018    |
| 0    | 13   | e       | 1     | 12    | e        | 20973.15 | 10          | -0.019   |
| 0    | 14   | e       | 1     | 13    | e        | 20972.00 | 0.03        | -0.015   |
| 0    | 15   | e       | 1     | 14    | e        | 20969.50 | 0.03        | -0.001   |
| 0    | 16   | e       | 1     | 15    | e        | 20966.71 | 0.03        | -0.029   |
| 0    | 17   | e       | 1     | 16    | e        | 20963.12 | 0.03        | 0.009    |
| 0    | 18   | e       | 1     | 17    | e        | 20958.89 | 0.03        | -0.033   |
| 0    | 19   | e       | 1     | 18    | e        | 20953.79 | 0.03        | 0.055    |
| 0    | 20   | e       | 1     | 19    | e        | 20948.34 | 10          | -0.188   |
| 0    | 21   | e       | 1     | 20    | e        | 20941.68 | 0.03        | 0.085    |
| 0    | 22   | e       | 1     | 21    | e        | 20934.53 | 0.03        | -0.022   |
| 0    | 23   | e       | 1     | 22    | e        | 20926.07 | 0.03        | 0.043    |
| 0    | 24   | e       | 1     | 23    | e        | 20915.68 | 0.03        | 0.027    |
| 0    | 4    | e       | 1     | 5     | e        | 20891.59 | 0.1         | 0.187    |
| 0    | 5    | e       | 1     | 6     | e        | 20881.52 | 0.03        | -0.026   |
| 0    | 6    | e       | 1     | 7     | e        | 20870.68 | 0.03        | 0.028    |
| 0    | 7    | e       | 1     | 8     | e        | 20859.30 | 0.03        | -0.022   |
| 0    | 8    | e       | 1     | 9     | e        | 20847.19 | 0.03        | 0.067    |
| 0    | 9    | e       | 1     | 10    | e        | 20834.65 | 0.03        | 0.034    |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|----------|-------------|----------|
| 0    | 10   | e       | 1     | 11    | e        | 20821.50 | 0.03        | -0.014   |
| 0    | 11   | e       | 1     | 12    | e        | 20807.74 | 0.03        | -0.021   |
| 0    | 12   | e       | 1     | 13    | e        | 20793.30 | 0.03        | 0.003    |
| 0    | 13   | e       | 1     | 14    | e        | 20778.44 | 0.03        | 0.066    |
| 0    | 14   | e       | 1     | 15    | e        | 20763.31 | 0.03        | -0.009   |
| 0    | 15   | e       | 1     | 16    | e        | 20746.85 | 0.03        | -0.020   |
| 0    | 16   | e       | 1     | 17    | e        | 20730.14 | 0.03        | -0.030   |
| 0    | 17   | e       | 1     | 18    | e        | 20712.77 | 0.03        | -0.028   |
| 0    | 18   | e       | 1     | 19    | e        | 20694.85 | 10          | -0.107   |
| 0    | 19   | e       | 1     | 20    | e        | 20676.29 | 10          | -0.188   |
| 0    | 20   | e       | 1     | 21    | e        | 20657.01 | 10          | -0.129   |
| 0    | 21   | e       | 1     | 22    | e        | 20637.15 | 0.03        | -0.079   |
| 0    | 22   | e       | 1     | 23    | e        | 20616.54 | 0.03        | -0.038   |
| 0    | 23   | e       | 1     | 24    | e        | 20594.98 | 0.03        | -0.069   |
| 0    | 24   | e       | 1     | 25    | e        | 20571.37 | 0.03        | 0.059    |
| 0    | 4    | f       | 1     | 4     | e        | 20928.18 | 0.03        | -0.009   |
| 0    | 5    | f       | 1     | 5     | e        | 20925.14 | 0.03        | 0.005    |
| 0    | 6    | f       | 1     | 6     | e        | 20921.61 | 0.03        | -0.024   |
| 0    | 7    | f       | 1     | 7     | e        | 20917.34 | 0.03        | 0.024    |
| 0    | 8    | f       | 1     | 8     | e        | 20912.47 | 0.03        | 0.051    |
| 0    | 9    | f       | 1     | 9     | e        | 20907.09 | 0.03        | 0.044    |
| 0    | 10   | f       | 1     | 10    | e        | 20901.11 | 0.03        | -0.031   |
| 0    | 11   | f       | 1     | 11    | e        | 20894.48 | 0.03        | -0.055   |
| 0    | 12   | f       | 1     | 12    | e        | 20887.18 | 0.03        | -0.059   |
| 0    | 13   | f       | 1     | 13    | e        | 20879.47 | 0.03        | -0.043   |
| 0    | 14   | f       | 1     | 14    | e        | 20871.27 | 10          | -0.135   |
| 0    | 15   | f       | 1     | 15    | e        | 20861.50 | 10          | 0.151    |
| 0    | 16   | f       | 1     | 16    | e        | 20851.90 | 0.03        | -0.056   |
| 0    | 5    | f       | 1     | 4     | f        | 20961.53 | 0.03        | 0.006    |
| 0    | 6    | f       | 1     | 5     | f        | 20965.29 | 0.03        | -0.065   |
| 0    | 7    | f       | 1     | 6     | f        | 20968.21 | 0.03        | 0.026    |
| 0    | 8    | f       | 1     | 7     | f        | 20970.65 | 0.03        | -0.042   |
| 0    | 9    | f       | 1     | 8     | f        | 20972.38 | 0.03        | 0.033    |
| 0    | 10   | f       | 1     | 9     | f        | 20973.50 | 0.03        | 0.028    |
| 0    | 11   | f       | 1     | 10    | f        | 20973.88 | 10          | 0.137    |
| 0    | 12   | f       | 1     | 11    | f        | 20973.78 | 0.03        | 0.047    |
| 0    | 13   | f       | 1     | 12    | f        | 20973.15 | 0.03        | 0.065    |
| 0    | 14   | f       | 1     | 13    | f        | 20972.00 | 0.03        | -0.029   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|----------|-------------|----------|
| 0    | 15   | f       | 1     | 14    | f        | 20969.50 | 0.03        | -0.002   |
| 0    | 16   | f       | 1     | 15    | f        | 20966.71 | 0.03        | -0.046   |
| 0    | 17   | f       | 1     | 16    | f        | 20963.12 | 0.03        | 0.016    |
| 0    | 18   | f       | 1     | 17    | f        | 20958.89 | 0.03        | 0.038    |
| 0    | 19   | f       | 1     | 18    | f        | 20953.79 | 10          | 0.243    |
| 0    | 20   | f       | 1     | 19    | f        | 20948.34 | 0.03        | 0.055    |
| 0    | 21   | f       | 1     | 20    | f        | 20941.93 | 0.03        | 0.063    |
| 0    | 22   | f       | 1     | 21    | f        | 20934.87 | 0.03        | 0.015    |
| 0    | 23   | f       | 1     | 22    | f        | 20926.88 | 0.03        | 0.032    |
| 0    | 24   | f       | 1     | 23    | f        | 20918.11 | 0.03        | -0.021   |
| 0    | 25   | f       | 1     | 24    | f        | 20908.38 | 0.03        | -0.074   |
| 0    | 26   | f       | 1     | 25    | f        | 20897.01 | 0.03        | -0.027   |
| 0    | 4    | f       | 1     | 5     | f        | 20891.59 | 10          | 0.190    |
| 0    | 5    | f       | 1     | 6     | f        | 20881.52 | 0.03        | -0.014   |
| 0    | 6    | f       | 1     | 7     | f        | 20870.68 | 0.03        | 0.034    |
| 0    | 7    | f       | 1     | 8     | f        | 20859.30 | 0.03        | -0.023   |
| 0    | 8    | f       | 1     | 9     | f        | 20847.19 | 0.03        | 0.052    |
| 0    | 9    | f       | 1     | 10    | f        | 20834.65 | 0.03        | 0.035    |
| 0    | 10   | f       | 1     | 11    | f        | 20821.50 | 0.03        | -0.013   |
| 0    | 11   | f       | 1     | 12    | f        | 20807.74 | 0.03        | -0.022   |
| 0    | 12   | f       | 1     | 13    | f        | 20793.30 | 0.03        | 0.032    |
| 0    | 13   | f       | 1     | 14    | f        | 20778.44 | 0.15        | 0.150    |
| 0    | 14   | f       | 1     | 15    | f        | 20763.31 | 0.03        | -0.024   |
| 0    | 15   | f       | 1     | 16    | f        | 20746.85 | 0.03        | -0.021   |
| 0    | 16   | f       | 1     | 17    | f        | 20730.14 | 0.03        | -0.048   |
| 0    | 17   | f       | 1     | 18    | f        | 20712.77 | 0.03        | -0.023   |
| 0    | 18   | f       | 1     | 19    | f        | 20694.85 | 0.03        | -0.037   |
| 0    | 19   | f       | 1     | 20    | f        | 20676.29 | 0.03        | -0.003   |
| 0    | 20   | f       | 1     | 21    | f        | 20657.18 | 0.03        | -0.061   |
| 0    | 21   | f       | 1     | 22    | f        | 20637.34 | 0.03        | -0.047   |
| 0    | 22   | f       | 1     | 23    | f        | 20616.93 | 0.03        | -0.060   |
| 0    | 23   | f       | 1     | 24    | f        | 20595.81 | 0.1         | -0.112   |
| 0    | 24   | f       | 1     | 25    | f        | 20573.82 | 0.03        | -0.026   |
| 1    | 5    | e       | 1     | 4     | e        | 22075.92 | 0.03        | -0.039   |
| 1    | 6    | e       | 1     | 5     | e        | 22078.31 | 0.03        | -0.019   |
| 1    | 7    | e       | 1     | 6     | e        | 22079.86 | 0.03        | 0.031    |
| 1    | 8    | e       | 1     | 7     | e        | 22080.83 | 10          | -0.176   |
| 1    | 9    | e       | 1     | 8     | e        | 22080.61 | 0.03        | -0.007   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|----------|-------------|----------|
| 1    | 10   | e       | 1     | 9     | e        | 22079.64 | 0.03        | 0.019    |
| 1    | 11   | e       | 1     | 10    | e        | 22077.86 | 0.03        | 0.049    |
| 1    | 12   | e       | 1     | 11    | e        | 22075.17 | 10          | 0.128    |
| 1    | 13   | e       | 1     | 12    | e        | 22072.72 | 0.03        | -0.004   |
| 1    | 14   | e       | 1     | 13    | e        | 22067.71 | 0.03        | 0.056    |
| 1    | 15   | e       | 1     | 14    | e        | 22062.38 | 0.03        | 0.051    |
| 1    | 16   | e       | 1     | 15    | e        | 22056.22 | 0.03        | 0.044    |
| 1    | 17   | e       | 1     | 16    | e        | 22049.10 | 0.03        | 0.048    |
| 1    | 18   | e       | 1     | 17    | e        | 22041.16 | 0.03        | 0.019    |
| 1    | 19   | e       | 1     | 18    | e        | 22032.24 | 0.03        | 0.005    |
| 1    | 20   | e       | 1     | 19    | e        | 22022.26 | 0.03        | 0.050    |
| 1    | 21   | e       | 1     | 20    | e        | 22011.41 | 0.03        | 0.020    |
| 1    | 22   | e       | 1     | 21    | e        | 21999.49 | 0.03        | 0.006    |
| 1    | 23   | e       | 1     | 22    | e        | 21986.48 | 0.03        | 0.034    |
| 1    | 4    | e       | 1     | 5     | e        | 22007.18 | 0.1         | -0.189   |
| 1    | 5    | e       | 1     | 6     | e        | 21995.93 | 0.1         | -0.079   |
| 1    | 6    | e       | 1     | 7     | e        | 21983.80 | 0.03        | -0.020   |
| 1    | 7    | e       | 1     | 8     | e        | 21971.09 | 10          | -0.158   |
| 1    | 8    | e       | 1     | 9     | e        | 21957.24 | 0.03        | 0.048    |
| 1    | 9    | e       | 1     | 10    | e        | 21942.87 | 0.03        | 0.005    |
| 1    | 10   | e       | 1     | 11    | e        | 21927.60 | 0.03        | 0.018    |
| 1    | 11   | e       | 1     | 12    | e        | 21911.60 | 0.03        | 0.011    |
| 1    | 12   | e       | 1     | 13    | e        | 21894.85 | 0.03        | -0.047   |
| 1    | 13   | e       | 1     | 14    | e        | 21878.10 | 0.03        | -0.009   |
| 1    | 14   | e       | 1     | 15    | e        | 21859.07 | 0.03        | 0.012    |
| 1    | 15   | e       | 1     | 16    | e        | 21839.75 | 0.03        | 0.012    |
| 1    | 16   | e       | 1     | 17    | e        | 21819.69 | 0.03        | 0.003    |
| 1    | 17   | e       | 1     | 18    | e        | 21798.70 | 0.03        | 0.061    |
| 1    | 18   | e       | 1     | 19    | e        | 21777.01 | 0.03        | 0.055    |
| 1    | 20   | e       | 1     | 21    | e        | 21731.04 | 0.03        | -0.001   |
| 1    | 21   | e       | 1     | 22    | e        | 21706.72 | 0.03        | 0.016    |
| 1    | 4    | f       | 1     | 4     | e        | 22043.42 | 0.03        | -0.010   |
| 1    | 5    | f       | 1     | 5     | e        | 22039.43 | 0.03        | 0.067    |
| 1    | 6    | f       | 1     | 6     | e        | 22034.62 | 0.03        | 0.031    |
| 1    | 7    | f       | 1     | 7     | e        | 22028.96 | 0.03        | 0.047    |
| 1    | 8    | f       | 1     | 8     | e        | 22022.57 | 0.03        | 0.006    |
| 1    | 9    | f       | 1     | 9     | e        | 22015.35 | 0.03        | -0.018   |
| 1    | 10   | f       | 1     | 10    | e        | 22007.18 | 0.03        | 0.038    |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|----------|-------------|----------|
| 1    | 11   | f       | 1     | 11    | e        | 21998.24 | 0.03        | 0.069    |
| 1    | 12   | f       | 1     | 12    | e        | 21988.49 | 0.03        | 0.069    |
| 1    | 5    | f       | 1     | 4     | f        | 22075.92 | 0.03        | -0.032   |
| 1    | 6    | f       | 1     | 5     | f        | 22078.31 | 0.03        | -0.020   |
| 1    | 7    | f       | 1     | 6     | f        | 22079.86 | 0.03        | 0.019    |
| 1    | 8    | f       | 1     | 7     | f        | 22080.83 | 10          | -0.167   |
| 1    | 9    | f       | 1     | 8     | f        | 22080.61 | 0.03        | 0.001    |
| 1    | 10   | f       | 1     | 9     | f        | 22079.64 | 0.03        | 0.027    |
| 1    | 11   | f       | 1     | 10    | f        | 22077.86 | 0.03        | 0.041    |
| 1    | 12   | f       | 1     | 11    | f        | 22075.17 | 0.03        | 0.095    |
| 1    | 13   | f       | 1     | 12    | f        | 22071.72 | 0.03        | 0.048    |
| 1    | 14   | f       | 1     | 13    | f        | 22067.38 | 0.03        | 0.019    |
| 1    | 15   | f       | 1     | 14    | f        | 22062.04 | 0.03        | 0.042    |
| 1    | 16   | f       | 1     | 15    | f        | 22055.74 | 0.03        | 0.067    |
| 1    | 17   | f       | 1     | 16    | f        | 22048.44 | 0.03        | 0.053    |
| 1    | 18   | f       | 1     | 17    | f        | 22039.43 | 10          | 0.131    |
| 1    | 20   | f       | 1     | 19    | f        | 22023.28 | 0.03        | 0.013    |
| 1    | 21   | f       | 1     | 20    | f        | 22012.06 | 0.03        | 0.080    |
| 1    | 22   | f       | 1     | 21    | f        | 22000.07 | 0.03        | -0.012   |
| 1    | 23   | f       | 1     | 22    | f        | 21987.02 | 0.03        | 0.008    |
| 1    | 4    | f       | 1     | 5     | f        | 22007.18 | 0.15        | -0.161   |
| 1    | 5    | f       | 1     | 6     | f        | 21995.93 | 0.03        | -0.072   |
| 1    | 6    | f       | 1     | 7     | f        | 21983.80 | 0.03        | -0.021   |
| 1    | 7    | f       | 1     | 8     | f        | 21971.09 | 10          | -0.170   |
| 1    | 8    | f       | 1     | 9     | f        | 21957.24 | 0.03        | 0.057    |
| 1    | 9    | f       | 1     | 10    | f        | 21942.87 | 0.03        | 0.013    |
| 1    | 10   | f       | 1     | 11    | f        | 21927.60 | 0.03        | 0.026    |
| 1    | 11   | f       | 1     | 12    | f        | 21911.60 | 0.03        | 0.002    |
| 1    | 12   | f       | 1     | 13    | f        | 21894.85 | 0.03        | -0.080   |
| 1    | 13   | f       | 1     | 14    | f        | 21877.11 | 0.03        | 0.033    |
| 1    | 14   | f       | 1     | 15    | f        | 21858.65 | 0.03        | 0.064    |
| 1    | 15   | f       | 1     | 16    | f        | 21839.44 | 0.03        | -0.027   |
| 1    | 16   | f       | 1     | 17    | f        | 21819.23 | 0.03        | 0.005    |
| 1    | 17   | f       | 1     | 18    | f        | 21798.07 | 0.03        | 0.034    |
| 1    | 18   | f       | 1     | 19    | f        | 21775.34 | 0.1         | 0.106    |
| 1    | 20   | f       | 1     | 21    | f        | 21732.13 | 0.1         | -0.113   |
| 1    | 21   | f       | 1     | 22    | f        | 21707.26 | 10          | 0.180    |
| 2    | 5    | e       | 1     | 4     | e        | 23124.56 | 0.03        | -0.060   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|----------|-------------|----------|
| 2    | 6    | e       | 1     | 5     | e        | 23125.43 | 0.03        | -0.005   |
| 2    | 7    | e       | 1     | 6     | e        | 23125.43 | 0.03        | 0.004    |
| 2    | 8    | e       | 1     | 7     | e        | 23124.25 | 0.03        | -0.007   |
| 2    | 9    | e       | 1     | 8     | e        | 23121.88 | 0.03        | -0.011   |
| 2    | 10   | e       | 1     | 9     | e        | 23118.57 | 0.03        | -0.024   |
| 2    | 11   | e       | 1     | 10    | e        | 23114.14 | 0.03        | -0.016   |
| 2    | 12   | e       | 1     | 11    | e        | 23108.37 | 0.03        | 0.047    |
| 2    | 13   | e       | 1     | 12    | e        | 23101.19 | 0.03        | -0.062   |
| 2    | 4    | e       | 1     | 5     | e        | 23056.75 | 0.03        | -0.001   |
| 2    | 5    | e       | 1     | 6     | e        | 23044.41 | 0.03        | 0.060    |
| 2    | 6    | e       | 1     | 7     | e        | 23030.91 | 0.03        | 0.004    |
| 2    | 7    | e       | 1     | 8     | e        | 23016.48 | 0.03        | -0.005   |
| 2    | 8    | e       | 1     | 9     | e        | 23000.87 | 0.03        | 0.007    |
| 2    | 9    | e       | 1     | 10    | e        | 22984.13 | 0.03        | 0.011    |
| 2    | 10   | e       | 1     | 11    | e        | 22966.48 | 0.03        | 0.025    |
| 2    | 11   | e       | 1     | 12    | e        | 22947.81 | 0.03        | 0.016    |
| 2    | 12   | e       | 1     | 13    | e        | 22927.97 | 0.03        | -0.048   |
| 2    | 13   | e       | 1     | 14    | e        | 22906.44 | 0.03        | 0.063    |
| 2    | 4    | f       | 1     | 4     | e        | 23093.38 | 0.03        | 0.000    |
| 2    | 5    | f       | 1     | 5     | e        | 23088.02 | 0.03        | -0.001   |
| 2    | 6    | f       | 1     | 6     | e        | 23081.82 | 0.03        | 0.000    |
| 2    | 7    | f       | 1     | 7     | e        | 23074.57 | 0.03        | 0.000    |
| 2    | 8    | f       | 1     | 8     | e        | 23066.10 | 0.03        | -0.001   |
| 1    | 5    | e       | 2     | 4     | e        | 20773.34 | 0.03        | 0.022    |
| 1    | 6    | e       | 2     | 5     | e        | 20776.56 | 0.03        | -0.003   |
| 1    | 7    | e       | 2     | 6     | e        | 20779.12 | 0.03        | -0.021   |
| 1    | 8    | e       | 2     | 7     | e        | 20780.99 | 0.03        | -0.031   |
| 1    | 9    | e       | 2     | 8     | e        | 20782.13 | 0.03        | 0.032    |
| 1    | 10   | e       | 2     | 9     | e        | 20782.59 | 0.03        | 0.035    |
| 1    | 11   | e       | 2     | 10    | e        | 20782.59 | 10          | -0.151   |
| 1    | 12   | e       | 2     | 11    | e        | 20781.50 | 0.03        | 0.046    |
| 1    | 13   | e       | 2     | 12    | e        | 20780.99 | 10          | -0.153   |
| 1    | 14   | e       | 2     | 13    | e        | 20777.92 | 0.03        | -0.006   |
| 1    | 15   | e       | 2     | 14    | e        | 20774.78 | 0.03        | -0.022   |
| 1    | 16   | e       | 2     | 15    | e        | 20770.99 | 0.03        | -0.065   |
| 1    | 17   | e       | 2     | 16    | e        | 20766.36 | 0.03        | -0.063   |
| 1    | 18   | e       | 2     | 17    | e        | 20760.94 | 0.03        | 0.029    |
| 1    | 19   | e       | 2     | 18    | e        | 20754.87 | 0.03        | -0.040   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|----------|-------------|----------|
| 1    | 20   | e       | 2     | 19    | e        | 20747.88 | 0.03        | -0.034   |
| 1    | 21   | e       | 2     | 20    | e        | 20740.12 | 0.03        | -0.049   |
| 1    | 6    | e       | 2     | 7     | e        | 20684.12 | 0.03        | -0.035   |
| 1    | 7    | e       | 2     | 8     | e        | 20672.54 | 0.03        | -0.049   |
| 1    | 8    | e       | 2     | 9     | e        | 20660.28 | 0.03        | -0.026   |
| 1    | 9    | e       | 2     | 10    | e        | 20647.49 | 0.03        | -0.085   |
| 1    | 10   | e       | 2     | 11    | e        | 20633.93 | 0.03        | -0.064   |
| 1    | 11   | e       | 2     | 12    | e        | 20619.80 | 0.03        | -0.068   |
| 1    | 12   | e       | 2     | 13    | e        | 20604.97 | 0.03        | -0.019   |
| 1    | 14   | e       | 2     | 15    | e        | 20573.82 | 0.03        | -0.077   |
| 1    | 15   | e       | 2     | 16    | e        | 20557.00 | 0.03        | -0.089   |
| 1    | 16   | e       | 2     | 17    | e        | 20539.51 | 0.03        | -0.027   |
| 1    | 17   | e       | 2     | 18    | e        | 20521.37 | 0.03        | -0.024   |
| 1    | 18   | e       | 2     | 19    | e        | 20502.67 | 0.03        | -0.069   |
| 1    | 19   | e       | 2     | 20    | e        | 20483.35 | 10          | -0.207   |
| 1    | 4    | f       | 2     | 4     | e        | 20740.94 | 0.03        | -0.049   |
| 1    | 5    | f       | 2     | 5     | e        | 20737.79 | 0.03        | -0.027   |
| 1    | 6    | f       | 2     | 6     | e        | 20733.89 | 0.03        | -0.031   |
| 1    | 7    | f       | 2     | 7     | e        | 20729.29 | 0.03        | 0.022    |
| 1    | 8    | f       | 2     | 8     | e        | 20724.18 | 0.03        | -0.045   |
| 1    | 9    | f       | 2     | 9     | e        | 20718.31 | 0.03        | -0.012   |
| 1    | 10   | f       | 2     | 10    | e        | 20711.79 | 0.03        | -0.042   |
| 1    | 11   | f       | 2     | 11    | e        | 20704.56 | 0.03        | -0.003   |
| 1    | 5    | f       | 2     | 4     | f        | 20773.34 | 0.03        | 0.029    |
| 1    | 6    | f       | 2     | 5     | f        | 20776.56 | 0.03        | -0.004   |
| 1    | 7    | f       | 2     | 6     | f        | 20779.12 | 0.03        | -0.033   |
| 1    | 8    | f       | 2     | 7     | f        | 20780.99 | 0.03        | -0.022   |
| 1    | 9    | f       | 2     | 8     | f        | 20782.13 | 0.03        | 0.039    |
| 1    | 10   | f       | 2     | 9     | f        | 20782.59 | 10          | 0.043    |
| 1    | 11   | f       | 2     | 10    | f        | 20782.59 | 10          | -0.159   |
| 1    | 12   | f       | 2     | 11    | f        | 20781.50 | 0.03        | 0.013    |
| 1    | 13   | f       | 2     | 12    | f        | 20779.94 | 0.03        | -0.051   |
| 1    | 14   | f       | 2     | 13    | f        | 20777.61 | 0.03        | -0.065   |
| 1    | 15   | f       | 2     | 14    | f        | 20774.40 | 0.03        | 0.007    |
| 1    | 16   | f       | 2     | 15    | f        | 20770.50 | 0.03        | -0.037   |
| 1    | 17   | f       | 2     | 16    | f        | 20765.62 | 0.03        | 0.014    |
| 1    | 18   | f       | 2     | 17    | f        | 20759.34 | 0.03        | -0.002   |
| 1    | 20   | f       | 2     | 19    | f        | 20748.75 | 0.03        | 0.046    |

| $v'$                    | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed | Uncertainty | calc-obs |
|-------------------------|------|---------|-------|-------|----------|----------|-------------|----------|
| 1                       | 21   | f       | 2     | 20    | f        | 20740.76 | 0.03        | -0.026   |
| 1                       | 6    | f       | 2     | 7     | f        | 20684.12 | 0.03        | -0.036   |
| 1                       | 7    | f       | 2     | 8     | f        | 20672.54 | 0.03        | -0.062   |
| 1                       | 8    | f       | 2     | 9     | f        | 20660.28 | 0.03        | -0.017   |
| 1                       | 9    | f       | 2     | 10    | f        | 20647.49 | 0.03        | -0.077   |
| 1                       | 10   | f       | 2     | 11    | f        | 20633.93 | 0.03        | -0.056   |
| 1                       | 11   | f       | 2     | 12    | f        | 20619.80 | 0.03        | -0.077   |
| 1                       | 12   | f       | 2     | 13    | f        | 20604.97 | 0.03        | -0.054   |
| 1                       | 13   | f       | 2     | 14    | f        | 20589.66 | 10          | -0.192   |
| 1                       | 14   | f       | 2     | 15    | f        | 20573.43 | 0.03        | -0.060   |
| 1                       | 15   | f       | 2     | 16    | f        | 20556.58 | 0.03        | -0.026   |
| 1                       | 16   | f       | 2     | 17    | f        | 20539.05 | 0.03        | -0.038   |
| 1                       | 17   | f       | 2     | 18    | f        | 20520.71 | 0.03        | -0.041   |
| 1                       | 18   | f       | 2     | 19    | f        | 20501.07 | 10          | -0.121   |
| $A^3\Phi_3 - X^3\Phi_3$ |      |         |       |       |          |          |             |          |
| 0                       | 4    | f       | 1     | 3     | f        | 21955.15 | 0.03        | -0.0600  |
| 0                       | 5    | f       | 1     | 4     | f        | 21958.77 | 0.03        | 0.0013   |
| 0                       | 6    | f       | 1     | 5     | f        | 21961.73 | 0.03        | -0.0025  |
| 0                       | 7    | f       | 1     | 6     | f        | 21963.89 | 0.03        | 0.0058   |
| 0                       | 8    | f       | 1     | 7     | f        | 21965.30 | 0.03        | -0.0105  |
| 0                       | 9    | f       | 1     | 8     | f        | 21965.90 | 0.03        | -0.0160  |
| 0                       | 10   | f       | 1     | 9     | f        | 21965.72 | 0.03        | -0.0079  |
| 0                       | 11   | f       | 1     | 10    | f        | 21964.72 | 0.03        | 0.0110   |
| 0                       | 12   | f       | 1     | 11    | f        | 21962.96 | 0.03        | 0.0392   |
| 0                       | 13   | f       | 1     | 12    | f        | 21960.38 | 0.03        | -0.0195  |
| 0                       | 14   | f       | 1     | 13    | f        | 21957.06 | 0.03        | 0.0353   |
| 0                       | 15   | f       | 1     | 14    | f        | 21952.92 | 0.03        | 0.0311   |
| 0                       | 16   | f       | 1     | 15    | f        | 21948.03 | 0.03        | 0.0116   |
| 0                       | 17   | f       | 1     | 16    | f        | 21942.34 | 0.03        | 0.0168   |
| 0                       | 18   | f       | 1     | 17    | f        | 21935.94 | 0.03        | -0.0271  |
| 0                       | 19   | f       | 1     | 18    | f        | 21928.75 | 0.03        | -0.0086  |
| 0                       | 20   | f       | 1     | 19    | f        | 21920.93 | 0.03        | -0.0063  |
| 0                       | 21   | f       | 1     | 20    | f        | 21912.49 | 0.3         | 0.1391   |
| 0                       | 23   | f       | 1     | 22    | f        | 21894.39 | 0.03        | 0.0031   |
| 0                       | 24   | f       | 1     | 23    | f        | 21885.45 | 0.03        | 0.0059   |
| 0                       | 3    | f       | 1     | 4     | f        | 21898.02 | 0.03        | -0.0167  |
| 0                       | 4    | f       | 1     | 5     | f        | 21887.50 | 0.03        | 0.0445   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|----------|-------------|----------|
| 0    | 5    | f       | 1     | 6     | f        | 21876.25 | 0.03        | 0.0178   |
| 0    | 6    | f       | 1     | 7     | f        | 21864.28 | 0.03        | 0.0175   |
| 0    | 7    | f       | 1     | 8     | f        | 21851.61 | 0.03        | -0.0330  |
| 0    | 8    | f       | 1     | 9     | f        | 21838.15 | 0.03        | -0.0239  |
| 0    | 9    | f       | 1     | 10    | f        | 21823.92 | 0.03        | 0.0070   |
| 0    | 10   | f       | 1     | 11    | f        | 21809.02 | 0.03        | 0.0002   |
| 0    | 11   | f       | 1     | 12    | f        | 21793.39 | 0.03        | -0.0185  |
| 0    | 12   | f       | 1     | 13    | f        | 21777.01 | 0.03        | 0.0393   |
| 0    | 13   | f       | 1     | 14    | f        | 21759.89 | 0.03        | 0.0191   |
| 0    | 14   | f       | 1     | 15    | f        | 21742.28 | 0.03        | -0.0354  |
| 0    | 15   | f       | 1     | 16    | f        | 21723.85 | 0.03        | -0.0302  |
| 0    | 16   | f       | 1     | 17    | f        | 21704.78 | 0.03        | -0.0121  |
| 0    | 17   | f       | 1     | 18    | f        | 21685.12 | 0.03        | -0.0176  |
| 0    | 18   | f       | 1     | 19    | f        | 21664.84 | 0.03        | 0.0277   |
| 0    | 19   | f       | 1     | 20    | f        | 21644.12 | 0.03        | 0.0091   |
| 0    | 20   | f       | 1     | 21    | f        | 21623.00 | 0.03        | 0.0087   |
| 0    | 21   | f       | 1     | 22    | f        | 21601.86 | 0.3         | -0.1359  |
| 0    | 3    | e       | 1     | 3     | f        | 21928.02 | 0.03        | 0.0130   |
| 0    | 4    | e       | 1     | 4     | f        | 21925.05 | 0.03        | 0.0103   |
| 0    | 5    | e       | 1     | 5     | f        | 21921.28 | 0.03        | -0.0245  |
| 0    | 6    | e       | 1     | 6     | f        | 21916.76 | 0.03        | -0.0202  |
| 0    | 7    | e       | 1     | 7     | f        | 21911.43 | 0.03        | 0.0235   |
| 0    | 8    | e       | 1     | 8     | f        | 21905.38 | 0.03        | 0.0330   |
| 0    | 9    | e       | 1     | 9     | f        | 21898.59 | 0.03        | 0.0091   |
| 0    | 10   | e       | 1     | 10    | f        | 21891.03 | 0.03        | 0.0150   |
| 0    | 11   | e       | 1     | 11    | f        | 21882.69 | 0.03        | 0.0262   |
| 0    | 12   | e       | 1     | 12    | f        | 21873.71 | 0.03        | -0.0345  |
| 0    | 3    | f       | 1     | 3     | e        | 21928.02 | 0.03        | 0.0130   |
| 0    | 4    | f       | 1     | 4     | e        | 21925.05 | 0.03        | 0.0103   |
| 0    | 5    | f       | 1     | 5     | e        | 21921.28 | 0.03        | -0.0244  |
| 0    | 6    | f       | 1     | 6     | e        | 21916.76 | 0.03        | -0.0201  |
| 0    | 7    | f       | 1     | 7     | e        | 21911.43 | 0.03        | 0.0236   |
| 0    | 8    | f       | 1     | 8     | e        | 21905.38 | 0.03        | 0.0327   |
| 0    | 9    | f       | 1     | 9     | e        | 21898.59 | 0.03        | 0.0054   |
| 0    | 10   | f       | 1     | 10    | e        | 21891.03 | 0.03        | 0.0068   |
| 0    | 11   | f       | 1     | 11    | e        | 21882.69 | 0.03        | 0.0060   |
| 0    | 12   | f       | 1     | 12    | e        | 21873.71 | 0.03        | -0.0777  |
| 0    | 4    | e       | 1     | 3     | e        | 21955.15 | 0.03        | -0.0600  |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|----------|-------------|----------|
| 0    | 5    | e       | 1     | 4     | e        | 21958.77 | 0.03        | 0.0013   |
| 0    | 6    | e       | 1     | 5     | e        | 21961.73 | 0.03        | -0.0024  |
| 0    | 7    | e       | 1     | 6     | e        | 21963.89 | 0.03        | 0.0059   |
| 0    | 8    | e       | 1     | 7     | e        | 21965.30 | 0.03        | -0.0104  |
| 0    | 9    | e       | 1     | 8     | e        | 21965.90 | 0.03        | -0.0143  |
| 0    | 10   | e       | 1     | 9     | e        | 21965.72 | 0.03        | -0.0066  |
| 0    | 11   | e       | 1     | 10    | e        | 21964.72 | 0.03        | 0.0128   |
| 0    | 12   | e       | 1     | 11    | e        | 21962.96 | 0.03        | 0.0400   |
| 0    | 13   | e       | 1     | 12    | e        | 21960.38 | 0.03        | 0.0223   |
| 0    | 14   | e       | 1     | 13    | e        | 21957.06 | 0.03        | 0.0122   |
| 0    | 15   | e       | 1     | 14    | e        | 21952.92 | 0.03        | -0.0171  |
| 0    | 16   | e       | 1     | 15    | e        | 21947.94 | 0.03        | -0.0168  |
| 0    | 17   | e       | 1     | 16    | e        | 21942.12 | 0.03        | -0.0163  |
| 0    | 18   | e       | 1     | 17    | e        | 21935.50 | 0.03        | -0.0026  |
| 0    | 19   | e       | 1     | 18    | e        | 21928.02 | 0.03        | 0.0099   |
| 0    | 20   | e       | 1     | 19    | e        | 21919.80 | 0.03        | -0.0108  |
| 0    | 21   | e       | 1     | 20    | e        | 21910.70 | 0.03        | -0.0711  |
| 0    | 22   | e       | 1     | 21    | e        | 21900.76 | 0.03        | -0.0204  |
| 0    | 23   | e       | 1     | 22    | e        | 21889.99 | 0.03        | 0.0044   |
| 0    | 24   | e       | 1     | 23    | e        | 21878.38 | 0.03        | -0.0082  |
| 0    | 25   | e       | 1     | 24    | e        | 21865.98 | 0.03        | 0.0104   |
| 0    | 26   | e       | 1     | 25    | e        | 21852.65 | 0.03        | -0.0013  |
| 0    | 27   | e       | 1     | 26    | e        | 21838.52 | 0.03        | -0.0151  |
| 0    | 28   | e       | 1     | 27    | e        | 21823.46 | 0.03        | -0.0349  |
| 0    | 30   | e       | 1     | 29    | e        | 21790.88 | 0.03        | 0.0272   |
| 0    | 3    | e       | 1     | 4     | e        | 21898.02 | 0.03        | -0.0167  |
| 0    | 4    | e       | 1     | 5     | e        | 21887.50 | 0.03        | 0.0446   |
| 0    | 5    | e       | 1     | 6     | e        | 21876.25 | 0.03        | 0.0179   |
| 0    | 6    | e       | 1     | 7     | e        | 21864.28 | 0.03        | 0.0176   |
| 0    | 7    | e       | 1     | 8     | e        | 21851.61 | 0.03        | -0.0333  |
| 0    | 8    | e       | 1     | 9     | e        | 21838.15 | 0.03        | -0.0256  |
| 0    | 9    | e       | 1     | 10    | e        | 21823.92 | 0.03        | 0.0038   |
| 0    | 10   | e       | 1     | 11    | e        | 21809.02 | 0.03        | -0.0100  |
| 0    | 11   | e       | 1     | 12    | e        | 21793.39 | 0.03        | -0.0407  |
| 0    | 12   | e       | 1     | 13    | e        | 21777.01 | 0.03        | -0.0058  |
| 0    | 13   | e       | 1     | 14    | e        | 21759.89 | 0.03        | -0.0221  |
| 0    | 14   | e       | 1     | 15    | e        | 21742.09 | 0.03        | -0.0108  |
| 0    | 15   | e       | 1     | 16    | e        | 21723.52 | 0.03        | 0.0177   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|----------|-------------|----------|
| 0    | 16   | e       | 1     | 17    | e        | 21704.26 | 0.03        | 0.0184   |
| 0    | 17   | e       | 1     | 18    | e        | 21684.26 | 0.03        | 0.0179   |
| 0    | 18   | e       | 1     | 19    | e        | 21663.59 | 0.03        | 0.0052   |
| 0    | 19   | e       | 1     | 20    | e        | 21642.17 | 0.03        | -0.0081  |
| 0    | 20   | e       | 1     | 21    | e        | 21620.06 | 0.03        | 0.0117   |
| 0    | 21   | e       | 1     | 22    | e        | 21597.11 | 0.03        | 0.0734   |
| 0    | 22   | e       | 1     | 23    | e        | 21573.67 | 0.03        | 0.0228   |
| 0    | 23   | e       | 1     | 24    | e        | 21549.48 | 0.03        | -0.0026  |
| 0    | 24   | e       | 1     | 25    | e        | 21524.51 | 0.03        | 0.0097   |
| 0    | 25   | e       | 1     | 26    | e        | 21498.95 | 0.03        | -0.0081  |
| 0    | 26   | e       | 1     | 27    | e        | 21472.54 | 0.03        | 0.0051   |
| 0    | 27   | e       | 1     | 28    | e        | 21445.47 | 0.03        | 0.0193   |
| 0    | 28   | e       | 1     | 29    | e        | 21417.60 | 0.03        | 0.0412   |
| 0    | 30   | e       | 1     | 31    | e        | 21360.03 | 0.03        | -0.0144  |
| 1    | 4    | e       | 1     | 3     | e        | 23064.19 | 0.03        | 0.0770   |
| 1    | 5    | e       | 1     | 4     | e        | 23066.93 | 0.03        | 0.0143   |
| 1    | 6    | e       | 1     | 5     | e        | 23068.60 | 0.03        | 0.0016   |
| 1    | 7    | e       | 1     | 6     | e        | 23069.26 | 0.03        | 0.0229   |
| 1    | 8    | e       | 1     | 7     | e        | 23068.97 | 0.03        | -0.0134  |
| 1    | 9    | e       | 1     | 8     | e        | 23067.66 | 0.03        | -0.0013  |
| 1    | 10   | e       | 1     | 9     | e        | 23065.34 | 0.03        | -0.0036  |
| 1    | 11   | e       | 1     | 10    | e        | 23062.00 | 0.03        | 0.0028   |
| 1    | 12   | e       | 1     | 11    | e        | 23057.67 | 0.03        | 0.0270   |
| 1    | 13   | e       | 1     | 12    | e        | 23052.33 | 0.03        | -0.0177  |
| 1    | 14   | e       | 1     | 13    | e        | 23045.93 | 0.03        | 0.0412   |
| 1    | 15   | e       | 1     | 14    | e        | 23038.56 | 0.03        | -0.0121  |
| 1    | 16   | e       | 1     | 15    | e        | 23030.04 | 0.03        | 0.0132   |
| 1    | 17   | e       | 1     | 16    | e        | 23020.55 | 0.03        | 0.0187   |
| 1    | 18   | e       | 1     | 17    | e        | 23010.01 | 0.03        | -0.0026  |
| 1    | 19   | e       | 1     | 18    | e        | 22998.42 | 0.03        | -0.0001  |
| 1    | 20   | e       | 1     | 19    | e        | 22985.70 | 0.03        | 0.0142   |
| 1    | 21   | e       | 1     | 20    | e        | 22972.00 | 0.1         | -0.0561  |
| 1    | 3    | e       | 1     | 4     | e        | 23008.15 | 0.03        | -0.0417  |
| 1    | 4    | e       | 1     | 5     | e        | 22996.76 | 0.03        | -0.0384  |
| 1    | 5    | e       | 1     | 6     | e        | 22984.44 | 0.03        | 0.0009   |
| 1    | 6    | e       | 1     | 7     | e        | 22971.20 | 0.03        | -0.0284  |
| 1    | 7    | e       | 1     | 8     | e        | 22956.98 | 0.03        | -0.0163  |
| 1    | 8    | e       | 1     | 9     | e        | 22941.80 | 0.03        | -0.0086  |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|----------|-------------|----------|
| 1    | 9    | e       | 1     | 10    | e        | 22925.69 | 0.03        | 0.0068   |
| 1    | 10   | e       | 1     | 11    | e        | 22908.65 | 0.03        | -0.0170  |
| 1    | 11   | e       | 1     | 12    | e        | 22890.69 | 0.03        | -0.0707  |
| 1    | 12   | e       | 1     | 13    | e        | 22871.73 | 0.03        | -0.0288  |
| 1    | 13   | e       | 1     | 14    | e        | 22851.83 | 0.03        | -0.0521  |
| 1    | 14   | e       | 1     | 15    | e        | 22830.96 | 0.03        | 0.0182   |
| 1    | 15   | e       | 1     | 16    | e        | 22809.17 | 0.03        | 0.0127   |
| 1    | 16   | e       | 1     | 17    | e        | 22786.42 | 0.03        | -0.0116  |
| 1    | 17   | e       | 1     | 18    | e        | 22762.76 | 0.03        | -0.0171  |
| 1    | 18   | e       | 1     | 19    | e        | 22738.10 | 0.03        | 0.0052   |
| 1    | 19   | e       | 1     | 20    | e        | 22712.55 | 0.03        | 0.0019   |
| 1    | 20   | e       | 1     | 21    | e        | 22686.01 | 0.03        | -0.0134  |
| 1    | 21   | e       | 1     | 22    | e        | 22658.44 | 0.1         | 0.0584   |
| 1    | 3    | e       | 1     | 3     | f        | 23038.10 | 0.03        | 0.0380   |
| 1    | 4    | e       | 1     | 4     | f        | 23034.28 | 0.03        | -0.0427  |
| 1    | 5    | e       | 1     | 5     | f        | 23029.45 | 0.03        | -0.0215  |
| 1    | 6    | e       | 1     | 6     | f        | 23023.59 | 0.03        | 0.0238   |
| 1    | 7    | e       | 1     | 7     | f        | 23016.85 | 0.03        | -0.0095  |
| 1    | 8    | e       | 1     | 8     | f        | 23009.06 | 0.03        | 0.0200   |
| 1    | 9    | e       | 1     | 9     | f        | 23000.38 | 0.03        | -0.0079  |
| 1    | 10   | e       | 1     | 10    | f        | 22990.65 | 0.03        | 0.0180   |
| 1    | 11   | e       | 1     | 11    | f        | 22979.92 | 0.03        | 0.0662   |
| 1    | 12   | e       | 1     | 12    | f        | 22968.37 | 0.03        | 0.0025   |
| 1    | 13   | e       | 1     | 13    | f        | 22955.66 | 0.03        | 0.0693   |
| 1    | 14   | e       | 1     | 14    | f        | 22942.25 | 0.03        | -0.0589  |
| 1    | 4    | f       | 1     | 3     | f        | 23064.19 | 0.03        | 0.0560   |
| 1    | 5    | f       | 1     | 4     | f        | 23066.93 | 0.03        | 0.0053   |
| 1    | 6    | f       | 1     | 5     | f        | 23068.60 | 0.03        | 0.0135   |
| 1    | 7    | f       | 1     | 6     | f        | 23069.26 | 0.03        | 0.0178   |
| 1    | 8    | f       | 1     | 7     | f        | 23068.97 | 0.03        | -0.0045  |
| 1    | 9    | f       | 1     | 8     | f        | 23067.66 | 0.03        | -0.0070  |
| 1    | 10   | f       | 1     | 9     | f        | 23065.34 | 0.03        | 0.0001   |
| 1    | 11   | f       | 1     | 10    | f        | 23062.00 | 0.03        | 0.0240   |
| 1    | 12   | f       | 1     | 11    | f        | 23057.67 | 0.03        | 0.0052   |
| 1    | 13   | f       | 1     | 12    | f        | 23052.33 | 0.03        | -0.0245  |
| 1    | 14   | f       | 1     | 13    | f        | 23045.93 | 0.03        | 0.0503   |
| 1    | 15   | f       | 1     | 14    | f        | 23038.56 | 0.03        | 0.0361   |
| 1    | 16   | f       | 1     | 15    | f        | 23030.21 | 0.03        | 0.0066   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|----------|-------------|----------|
| 1    | 17   | f       | 1     | 16    | f        | 23020.81 | 0.03        | -0.0182  |
| 1    | 18   | f       | 1     | 17    | f        | 23010.47 | 0.03        | -0.0421  |
| 1    | 19   | f       | 1     | 18    | f        | 22999.09 | 0.03        | -0.0286  |
| 1    | 20   | f       | 1     | 19    | f        | 22986.86 | 0.03        | 0.0137   |
| 1    | 21   | f       | 1     | 20    | f        | 22973.75 | 0.1         | 0.1341   |
| 1    | 3    | f       | 1     | 4     | f        | 23008.15 | 0.03        | -0.0017  |
| 1    | 4    | f       | 1     | 5     | f        | 22996.76 | 0.03        | -0.0595  |
| 1    | 5    | f       | 1     | 6     | f        | 22984.44 | 0.03        | -0.0082  |
| 1    | 6    | f       | 1     | 7     | f        | 22971.20 | 0.03        | -0.0165  |
| 1    | 7    | f       | 1     | 8     | f        | 22956.98 | 0.03        | -0.0210  |
| 1    | 8    | f       | 1     | 9     | f        | 22941.80 | 0.03        | 0.0021   |
| 1    | 9    | f       | 1     | 10    | f        | 22925.69 | 0.03        | 0.0060   |
| 1    | 10   | f       | 1     | 11    | f        | 22908.65 | 0.03        | -0.0018  |
| 1    | 11   | f       | 1     | 12    | f        | 22890.69 | 0.03        | -0.0255  |
| 1    | 12   | f       | 1     | 13    | f        | 22871.73 | 0.03        | -0.0047  |
| 1    | 13   | f       | 1     | 14    | f        | 22851.83 | 0.03        | 0.0241   |
| 1    | 14   | f       | 1     | 15    | f        | 22831.18 | 0.03        | -0.0504  |
| 1    | 15   | f       | 1     | 16    | f        | 22809.50 | 0.03        | -0.0352  |
| 1    | 16   | f       | 1     | 17    | f        | 22786.95 | 0.03        | -0.0071  |
| 1    | 17   | f       | 1     | 18    | f        | 22763.52 | 0.03        | 0.0174   |
| 1    | 18   | f       | 1     | 19    | f        | 22739.34 | 0.03        | 0.0427   |
| 1    | 19   | f       | 1     | 20    | f        | 22714.42 | 0.03        | 0.0291   |
| 1    | 20   | f       | 1     | 21    | f        | 22688.97 | 0.03        | -0.0113  |
| 1    | 21   | f       | 1     | 22    | f        | 22663.11 | 0.1         | -0.1309  |

This work

| $A'^3\Phi_4 - X^3\Phi_4$ |    |   |   |    |   |            |       |         |
|--------------------------|----|---|---|----|---|------------|-------|---------|
| 0                        | 5  | e | 0 | 4  | e | 12441.8781 | 0.007 | 0.0007  |
| 0                        | 6  | e | 0 | 5  | e | 12439.9182 | 0.007 | -0.0039 |
| 0                        | 7  | e | 0 | 6  | e | 12436.4031 | 0.007 | -0.0024 |
| 0                        | 8  | e | 0 | 7  | e | 12431.3429 | 0.007 | -0.0015 |
| 0                        | 9  | e | 0 | 8  | e | 12424.7522 | 0.007 | 0.0012  |
| 0                        | 10 | e | 0 | 9  | e | 12416.6451 | 0.007 | -0.0028 |
| 0                        | 11 | e | 0 | 10 | e | 12407.0289 | 0.007 | -0.0003 |
| 0                        | 12 | e | 0 | 11 | e | 12395.8563 | 0.007 | 0.0017  |
| 0                        | 13 | e | 0 | 12 | e | 12383.2904 | 0.007 | -0.0040 |
| 0                        | 14 | e | 0 | 13 | e | 12369.2242 | 0.007 | 0.0003  |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 0    | 15   | e       | 0     | 14    | e        | 12353.7110 | 0.007       | 0.0008   |
| 0    | 16   | e       | 0     | 15    | e        | 12337.0895 | 0.007       | 0.0056   |
| 0    | 17   | e       | 0     | 16    | e        | 12318.3053 | 0.007       | 0.0022   |
| 0    | 18   | e       | 0     | 17    | e        | 12298.5293 | 0.007       | -0.0024  |
| 0    | 19   | e       | 0     | 18    | e        | 12277.3528 | 0.007       | 0.0033   |
| 0    | 20   | e       | 0     | 19    | e        | 12254.9036 | 0.007       | 0.0034   |
| 0    | 21   | e       | 0     | 20    | e        | 12230.8069 | 0.007       | -0.0044  |
| 0    | 22   | e       | 0     | 21    | e        | 12205.5396 | 0.007       | -0.0059  |
| 0    | 23   | e       | 0     | 22    | e        | 12179.0098 | 0.007       | -0.0058  |
| 0    | 24   | e       | 0     | 23    | e        | 12151.1560 | 0.05        | 0.0642   |
| 0    | 25   | e       | 0     | 24    | e        | 12122.1046 | 0.007       | 0.0078   |
| 0    | 26   | e       | 0     | 25    | e        | 12091.7580 | 0.007       | 0.0042   |
| 0    | 27   | e       | 0     | 26    | e        | 12060.1948 | 0.007       | 0.0058   |
| 0    | 28   | e       | 0     | 27    | e        | 12027.4486 | 0.007       | 0.0015   |
| 0    | 29   | e       | 0     | 28    | e        | 11993.7157 | 0.007       | -0.0006  |
| 0    | 30   | e       | 0     | 29    | e        | 11958.6446 | 0.007       | 0.0097   |
| 0    | 31   | e       | 0     | 30    | e        | 11922.6286 | 0.007       | 0.0021   |
| 0    | 32   | e       | 0     | 31    | e        | 11885.6612 | 0.007       | 0.0009   |
| 0    | 33   | e       | 0     | 32    | e        | 11847.8318 | 0.007       | 0.0017   |
| 0    | 34   | e       | 0     | 33    | e        | 11809.2692 | 0.007       | 0.0022   |
| 0    | 35   | e       | 0     | 34    | e        | 11770.0096 | 0.007       | 0.0023   |
| 0    | 4    | e       | 0     | 5     | e        | 12375.3616 | 0.007       | 0.0116   |
| 0    | 5    | e       | 0     | 6     | e        | 12360.1163 | 0.007       | 0.0076   |
| 0    | 6    | e       | 0     | 7     | e        | 12343.3622 | 0.007       | 0.0021   |
| 0    | 7    | e       | 0     | 8     | e        | 12325.0885 | 0.007       | 0.0015   |
| 0    | 8    | e       | 0     | 9     | e        | 12305.3122 | 0.007       | -0.0020  |
| 0    | 9    | e       | 0     | 10    | e        | 12284.0461 | 0.007       | 0.0008   |
| 0    | 10   | e       | 0     | 11    | e        | 12261.3140 | 0.007       | -0.0030  |
| 0    | 11   | e       | 0     | 12    | e        | 12237.1257 | 0.007       | 0.0023   |
| 0    | 12   | e       | 0     | 13    | e        | 12211.4479 | 0.007       | 0.0012   |
| 0    | 13   | e       | 0     | 14    | e        | 12184.4384 | 0.007       | -0.0031  |
| 0    | 14   | e       | 0     | 15    | e        | 12156.0046 | 0.007       | -0.0023  |
| 0    | 15   | e       | 0     | 16    | e        | 12126.1957 | 0.007       | -0.0006  |
| 0    | 16   | e       | 0     | 17    | e        | 12095.3601 | 0.007       | 0.0050   |
| 0    | 17   | e       | 0     | 18    | e        | 12062.4502 | 0.007       | 0.0007   |
| 0    | 18   | e       | 0     | 19    | e        | 12028.6377 | 0.007       | -0.0028  |
| 0    | 19   | e       | 0     | 20    | e        | 11993.5110 | 0.007       | 0.0145   |
| 0    | 20   | e       | 0     | 21    | e        | 11957.2372 | 0.007       | 0.0017   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 0    | 21   | e       | 0     | 22    | e        | 11919.4073 | 0.007       | -0.0038  |
| 0    | 22   | e       | 0     | 23    | e        | 11880.5197 | 0.007       | -0.0049  |
| 0    | 23   | e       | 0     | 24    | e        | 11840.4822 | 0.007       | -0.0010  |
| 0    | 24   | e       | 0     | 25    | e        | 11799.3230 | 0.007       | -0.0087  |
| 0    | 25   | e       | 0     | 26    | e        | 11756.9430 | 0.007       | 0.0058   |
| 0    | 26   | e       | 0     | 27    | e        | 11713.4640 | 0.007       | 0.0071   |
| 0    | 27   | e       | 0     | 28    | e        | 11668.9117 | 0.007       | 0.0049   |
| 0    | 28   | e       | 0     | 29    | e        | 11623.3045 | 0.007       | 0.0080   |
| 0    | 29   | e       | 0     | 30    | e        | 11576.8653 | 0.007       | 0.0024   |
| 0    | 30   | e       | 0     | 31    | e        | 11529.2693 | 0.02        | -0.0238  |
| 0    | 31   | e       | 0     | 32    | e        | 11480.8081 | 0.007       | 0.0049   |
| 0    | 32   | e       | 0     | 33    | e        | 11431.5864 | 0.007       | 0.0062   |
| 0    | 33   | e       | 0     | 34    | e        | 11381.6705 | 0.007       | 0.0028   |
| 0    | 34   | e       | 0     | 35    | e        | 11331.1879 | 0.007       | -0.0016  |
| 0    | 35   | e       | 0     | 36    | e        | 11280.1791 | 0.007       | -0.0077  |
| 0    | 4    | f       | 0     | 4     | e        | 12412.5613 | 0.007       | -0.0125  |
| 0    | 5    | f       | 0     | 5     | e        | 12404.6982 | 0.007       | -0.0002  |
| 0    | 6    | f       | 0     | 6     | e        | 12395.3340 | 0.007       | -0.0011  |
| 0    | 7    | f       | 0     | 7     | e        | 12384.4285 | 0.007       | 0.0026   |
| 0    | 8    | f       | 0     | 8     | e        | 12371.9974 | 0.007       | 0.0041   |
| 0    | 9    | f       | 0     | 9     | e        | 12358.0600 | 0.007       | 0.0019   |
| 0    | 10   | f       | 0     | 10    | e        | 12342.6248 | 0.007       | 0.0035   |
| 0    | 11   | f       | 0     | 11    | e        | 12325.7086 | 0.007       | 0.0048   |
| 0    | 12   | f       | 0     | 12    | e        | 12307.2713 | 0.007       | 0.0005   |
| 0    | 13   | f       | 0     | 13    | e        | 12287.4454 | 0.1         | 0.0212   |
| 0    | 14   | f       | 0     | 14    | e        | 12266.1897 | 0.007       | 0.0061   |
| 0    | 5    | f       | 0     | 4     | f        | 12441.8781 | 0.007       | -0.0054  |
| 0    | 6    | f       | 0     | 5     | f        | 12439.9182 | 0.007       | -0.0051  |
| 0    | 7    | f       | 0     | 6     | f        | 12436.4031 | 0.007       | -0.0020  |
| 0    | 8    | f       | 0     | 7     | f        | 12431.3429 | 0.007       | -0.0006  |
| 0    | 9    | f       | 0     | 8     | f        | 12424.7522 | 0.007       | 0.0001   |
| 0    | 10   | f       | 0     | 9     | f        | 12416.6451 | 0.007       | -0.0007  |
| 0    | 11   | f       | 0     | 10    | f        | 12407.0289 | 0.007       | -0.0002  |
| 0    | 12   | f       | 0     | 11    | f        | 12395.8563 | 0.007       | 0.0008   |
| 0    | 13   | f       | 0     | 12    | f        | 12383.2904 | 0.007       | -0.0002  |
| 0    | 14   | f       | 0     | 13    | f        | 12369.2242 | 0.007       | -0.0009  |
| 0    | 15   | f       | 0     | 14    | f        | 12353.7110 | 0.007       | 0.0022   |
| 0    | 16   | f       | 0     | 15    | f        | 12336.7099 | 0.007       | -0.0007  |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 0    | 17   | f       | 0     | 16    | f        | 12318.3053 | 0.007       | 0.0023   |
| 0    | 18   | f       | 0     | 17    | f        | 12298.5293 | 0.007       | 0.0016   |
| 0    | 19   | f       | 0     | 18    | f        | 12277.3528 | 0.007       | 0.0021   |
| 0    | 20   | f       | 0     | 19    | f        | 12254.7591 | 0.007       | -0.0076  |
| 0    | 21   | f       | 0     | 20    | f        | 12230.8069 | 0.007       | 0.0007   |
| 0    | 22   | f       | 0     | 21    | f        | 12205.5396 | 0.007       | -0.0003  |
| 0    | 23   | f       | 0     | 22    | f        | 12179.0098 | 0.007       | 0.0018   |
| 0    | 24   | f       | 0     | 23    | f        | 12151.1570 | 0.02        | -0.0269  |
| 0    | 25   | f       | 0     | 24    | f        | 12121.9471 | 0.007       | -0.0049  |
| 0    | 26   | f       | 0     | 25    | f        | 12091.5286 | 0.007       | -0.0043  |
| 0    | 27   | f       | 0     | 26    | f        | 12059.8732 | 0.007       | -0.0046  |
| 0    | 28   | f       | 0     | 27    | f        | 12026.9448 | 0.007       | -0.0050  |
| 0    | 29   | f       | 0     | 28    | f        | 11993.6098 | 1           | -0.1904  |
| 0    | 30   | f       | 0     | 29    | f        | 11958.6446 | 0.1         | 0.0744   |
| 0    | 31   | f       | 0     | 30    | f        | 11923.0570 | 0.007       | -0.0121  |
| 0    | 32   | f       | 0     | 31    | f        | 11885.4860 | 0.007       | -0.0111  |
| 0    | 33   | f       | 0     | 32    | f        | 11847.1602 | 0.007       | 0.0071   |
| 0    | 34   | f       | 0     | 33    | f        | 11808.2386 | 0.007       | -0.0034  |
| 0    | 35   | f       | 0     | 34    | f        | 11768.7792 | 0.007       | 0.0005   |
| 0    | 4    | f       | 0     | 5     | f        | 12375.3616 | 0.007       | 0.0125   |
| 0    | 5    | f       | 0     | 6     | f        | 12360.1163 | 0.007       | 0.0015   |
| 0    | 6    | f       | 0     | 7     | f        | 12343.3622 | 0.007       | 0.0009   |
| 0    | 7    | f       | 0     | 8     | f        | 12325.0885 | 0.007       | 0.0019   |
| 0    | 8    | f       | 0     | 9     | f        | 12305.3122 | 0.007       | -0.0011  |
| 0    | 9    | f       | 0     | 10    | f        | 12284.0461 | 0.007       | -0.0003  |
| 0    | 10   | f       | 0     | 11    | f        | 12261.3140 | 0.007       | -0.0010  |
| 0    | 11   | f       | 0     | 12    | f        | 12237.1257 | 0.007       | 0.0023   |
| 0    | 12   | f       | 0     | 13    | f        | 12211.4479 | 0.007       | 0.0002   |
| 0    | 13   | f       | 0     | 14    | f        | 12184.4384 | 0.007       | 0.0006   |
| 0    | 14   | f       | 0     | 15    | f        | 12156.0046 | 0.007       | -0.0037  |
| 0    | 15   | f       | 0     | 16    | f        | 12126.1957 | 0.007       | 0.0005   |
| 0    | 16   | f       | 0     | 17    | f        | 12094.9803 | 0.007       | -0.0017  |
| 0    | 17   | f       | 0     | 18    | f        | 12062.4502 | 0.007       | 0.0000   |
| 0    | 18   | f       | 0     | 19    | f        | 12028.6377 | 0.007       | 0.0002   |
| 0    | 19   | f       | 0     | 20    | f        | 11993.5110 | 0.007       | 0.0117   |
| 0    | 20   | f       | 0     | 21    | f        | 11957.1286 | 0.05        | -0.0473  |
| 0    | 21   | f       | 0     | 22    | f        | 11919.4073 | 0.007       | -0.0018  |
| 0    | 22   | f       | 0     | 23    | f        | 11880.5197 | 0.007       | -0.0036  |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 0    | 23   | f       | 0     | 24    | f        | 11840.4822 | 0.007       | 0.0008   |
| 0    | 24   | f       | 0     | 25    | f        | 11799.2243 | 0.007       | -0.0078  |
| 0    | 25   | f       | 0     | 26    | f        | 11756.7691 | 0.007       | -0.0006  |
| 0    | 26   | f       | 0     | 27    | f        | 11713.2219 | 0.007       | -0.0022  |
| 0    | 27   | f       | 0     | 28    | f        | 11668.5695 | 0.007       | -0.0022  |
| 0    | 28   | f       | 0     | 29    | f        | 11622.7825 | 0.007       | -0.0025  |
| 0    | 29   | f       | 0     | 30    | f        | 11576.5860 | 0.1         | -0.0422  |
| 0    | 30   | f       | 0     | 31    | f        | 11529.2693 | 0.007       | 0.0052   |
| 0    | 31   | f       | 0     | 32    | f        | 11481.1896 | 0.007       | -0.0070  |
| 0    | 32   | f       | 0     | 33    | f        | 11431.3587 | 0.007       | -0.0089  |
| 0    | 33   | f       | 0     | 34    | f        | 11380.9421 | 0.007       | -0.0035  |
| 0    | 34   | f       | 0     | 35    | f        | 11330.0623 | 0.007       | 0.0036   |
| 0    | 35   | f       | 0     | 36    | f        | 11278.8356 | 0.007       | 0.0007   |
| 0    | 36   | f       | 0     | 37    | f        | 11227.4269 | 0.007       | 0.0106   |
| 0    | 5    | e       | 1     | 4     | e        | 11104.1082 | 0.007       | -0.0097  |
| 0    | 6    | e       | 1     | 5     | e        | 11102.9232 | 0.007       | -0.0048  |
| 0    | 7    | e       | 1     | 6     | e        | 11100.3464 | 0.007       | -0.0007  |
| 0    | 8    | e       | 1     | 7     | e        | 11096.3866 | 0.007       | -0.0024  |
| 0    | 9    | e       | 1     | 8     | e        | 11091.0500 | 0.007       | 0.0005   |
| 0    | 10   | e       | 1     | 9     | e        | 11084.3523 | 0.007       | -0.0022  |
| 0    | 11   | e       | 1     | 10    | e        | 11076.3079 | 0.007       | -0.0045  |
| 0    | 12   | e       | 1     | 11    | e        | 11066.8530 | 0.007       | 0.0031   |
| 0    | 13   | e       | 1     | 12    | e        | 11056.1664 | 0.007       | -0.0026  |
| 0    | 14   | e       | 1     | 13    | e        | 11044.1386 | 0.007       | -0.0016  |
| 0    | 15   | e       | 1     | 14    | e        | 11030.8153 | 0.007       | 0.0000   |
| 0    | 16   | e       | 1     | 15    | e        | 11016.5405 | 0.007       | 0.0046   |
| 0    | 17   | e       | 1     | 16    | e        | 11000.2580 | 0.007       | 0.0015   |
| 0    | 18   | e       | 1     | 17    | e        | 10983.1409 | 0.007       | -0.0050  |
| 0    | 19   | e       | 1     | 18    | e        | 10964.7795 | 0.007       | -0.0022  |
| 0    | 20   | e       | 1     | 19    | e        | 10945.3004 | 0.007       | -0.0055  |
| 0    | 21   | e       | 1     | 20    | e        | 10924.3114 | 0.007       | 0.0001   |
| 0    | 22   | e       | 1     | 21    | e        | 10902.3167 | 0.007       | 0.0017   |
| 0    | 23   | e       | 1     | 22    | e        | 10879.2175 | 0.007       | 0.0008   |
| 0    | 24   | e       | 1     | 23    | e        | 10855.0112 | 0.007       | 0.0066   |
| 0    | 25   | e       | 1     | 24    | e        | 10829.6591 | 0.007       | -0.0121  |
| 0    | 26   | e       | 1     | 25    | e        | 10803.1942 | 0.007       | -0.0070  |
| 0    | 27   | e       | 1     | 26    | e        | 10775.6754 | 0.007       | -0.0063  |
| 0    | 28   | e       | 1     | 27    | e        | 10747.1214 | 0.007       | -0.0065  |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 0    | 29   | e       | 1     | 28    | e        | 10717.7267 | 0.007       | 0.0025   |
| 0    | 30   | e       | 1     | 29    | e        | 10687.1812 | 0.007       | -0.0110  |
| 0    | 31   | e       | 1     | 30    | e        | 10655.8086 | 0.007       | -0.0078  |
| 0    | 32   | e       | 1     | 31    | e        | 10623.6482 | 0.007       | -0.0094  |
| 0    | 33   | e       | 1     | 32    | e        | 10590.7736 | 0.007       | -0.0044  |
| 0    | 34   | e       | 1     | 33    | e        | 10557.3210 | 0.007       | -0.0024  |
| 0    | 35   | e       | 1     | 34    | e        | 10523.3236 | 0.007       | -0.0008  |
| 0    | 36   | e       | 1     | 35    | e        | 10491.2224 | 0.007       | -0.0007  |
| 0    | 37   | e       | 1     | 36    | e        | 10457.6534 | 0.007       | -0.0003  |
| 0    | 5    | e       | 1     | 6     | e        | 11024.0248 | 0.07        | 0.0441   |
| 0    | 6    | e       | 1     | 7     | e        | 11008.3955 | 0.007       | 0.0116   |
| 0    | 7    | e       | 1     | 8     | e        | 10991.3902 | 0.007       | -0.0032  |
| 0    | 8    | e       | 1     | 9     | e        | 10973.0203 | 0.007       | -0.0023  |
| 0    | 9    | e       | 1     | 10    | e        | 10953.3216 | 0.007       | 0.0001   |
| 0    | 10   | e       | 1     | 11    | e        | 10932.3127 | 0.007       | -0.0037  |
| 0    | 11   | e       | 1     | 12    | e        | 10910.0075 | 0.007       | -0.0022  |
| 0    | 12   | e       | 1     | 13    | e        | 10886.3641 | 0.007       | -0.0024  |
| 0    | 13   | e       | 1     | 14    | e        | 10861.5436 | 0.007       | -0.0047  |
| 0    | 14   | e       | 1     | 15    | e        | 10835.4486 | 0.007       | 0.0039   |
| 0    | 15   | e       | 1     | 16    | e        | 10808.1510 | 0.007       | -0.0039  |
| 0    | 16   | e       | 1     | 17    | e        | 10779.9765 | 0.007       | -0.0024  |
| 0    | 17   | e       | 1     | 18    | e        | 10749.8727 | 0.007       | -0.0008  |
| 0    | 18   | e       | 1     | 19    | e        | 10719.0232 | 0.007       | -0.0004  |
| 0    | 19   | e       | 1     | 20    | e        | 10687.0373 | 0.007       | -0.0028  |
| 0    | 20   | e       | 1     | 21    | e        | 10654.0280 | 0.007       | -0.0044  |
| 0    | 21   | e       | 1     | 22    | e        | 10619.6140 | 0.007       | 0.0036   |
| 0    | 22   | e       | 1     | 23    | e        | 10584.3040 | 0.007       | 0.0085   |
| 0    | 23   | e       | 1     | 24    | e        | 10548.0101 | 0.007       | 0.0058   |
| 0    | 24   | e       | 1     | 25    | e        | 10510.7389 | 0.007       | 0.0004   |
| 0    | 25   | e       | 1     | 26    | e        | 10472.4192 | 0.007       | -0.0019  |
| 0    | 26   | e       | 1     | 27    | e        | 10433.1413 | 0.007       | -0.0053  |
| 0    | 27   | e       | 1     | 28    | e        | 10392.9360 | 0.007       | -0.0053  |
| 0    | 28   | e       | 1     | 29    | e        | 10351.8327 | 0.007       | -0.0044  |
| 0    | 29   | e       | 1     | 30    | e        | 10310.0433 | 0.007       | -0.0055  |
| 0    | 30   | e       | 1     | 31    | e        | 10267.1950 | 0.02        | 0.0272   |
| 0    | 31   | e       | 1     | 32    | e        | 10223.7494 | 0.007       | -0.0006  |
| 0    | 32   | e       | 1     | 33    | e        | 10179.6384 | 0.007       | 0.0013   |
| 0    | 33   | e       | 1     | 34    | e        | 10134.9851 | 0.007       | -0.0007  |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 0    | 34   | e       | 1     | 35    | e        | 10089.9115 | 0.007       | 0.0023   |
| 0    | 35   | e       | 1     | 36    | e        | 10044.4607 | 0.007       | 0.0075   |
| 0    | 36   | e       | 1     | 37    | e        | 10001.0915 | 0.007       | 0.0003   |
| 0    | 5    | f       | 1     | 4     | f        | 11104.1082 | 0.05        | -0.0158  |
| 0    | 6    | f       | 1     | 5     | f        | 11102.9232 | 0.007       | -0.0060  |
| 0    | 7    | f       | 1     | 6     | f        | 11100.3464 | 0.007       | -0.0003  |
| 0    | 8    | f       | 1     | 7     | f        | 11096.3866 | 0.007       | -0.0015  |
| 0    | 9    | f       | 1     | 8     | f        | 11091.0500 | 0.007       | -0.0006  |
| 0    | 10   | f       | 1     | 9     | f        | 11084.3523 | 0.007       | -0.0001  |
| 0    | 11   | f       | 1     | 10    | f        | 11076.3079 | 0.007       | -0.0045  |
| 0    | 12   | f       | 1     | 11    | f        | 11066.8530 | 0.007       | 0.0022   |
| 0    | 13   | f       | 1     | 12    | f        | 11056.1664 | 0.007       | 0.0011   |
| 0    | 14   | f       | 1     | 13    | f        | 11044.1386 | 0.007       | -0.0029  |
| 0    | 15   | f       | 1     | 14    | f        | 11030.8153 | 0.007       | 0.0013   |
| 0    | 16   | f       | 1     | 15    | f        | 11016.1591 | 0.007       | -0.0002  |
| 0    | 17   | f       | 1     | 16    | f        | 11000.2580 | 0.007       | 0.0011   |
| 0    | 18   | f       | 1     | 17    | f        | 10983.1409 | 0.007       | -0.0018  |
| 0    | 19   | f       | 1     | 18    | f        | 10964.7795 | 0.007       | -0.0048  |
| 0    | 20   | f       | 1     | 19    | f        | 10945.1326 | 0.007       | 0.0048   |
| 0    | 21   | f       | 1     | 20    | f        | 10924.3114 | 0.007       | 0.0022   |
| 0    | 22   | f       | 1     | 21    | f        | 10902.3167 | 0.007       | 0.0028   |
| 0    | 23   | f       | 1     | 22    | f        | 10879.2175 | 0.007       | 0.0020   |
| 0    | 24   | f       | 1     | 23    | f        | 10854.8777 | 0.02        | 0.0411   |
| 0    | 25   | f       | 1     | 24    | f        | 10829.4456 | 0.02        | 0.0187   |
| 0    | 26   | f       | 1     | 25    | f        | 10802.9094 | 0.02        | 0.0225   |
| 0    | 27   | f       | 1     | 26    | f        | 10775.2907 | 0.02        | 0.0229   |
| 0    | 28   | f       | 1     | 27    | f        | 10746.5458 | 0.02        | 0.0271   |
| 0    | 29   | f       | 1     | 28    | f        | 10717.3911 | 0.007       | 0.0002   |
| 0    | 30   | f       | 1     | 29    | f        | 10687.1812 | 0.007       | -0.0020  |
| 0    | 31   | f       | 1     | 30    | f        | 10656.1248 | 0.02        | 0.0177   |
| 0    | 32   | f       | 1     | 31    | f        | 10623.3451 | 0.007       | 0.0126   |
| 0    | 33   | f       | 1     | 32    | f        | 10589.9820 | 0.007       | 0.0004   |
| 0    | 34   | f       | 1     | 33    | f        | 10556.1196 | 0.007       | 0.0090   |
| 0    | 35   | f       | 1     | 34    | f        | 10521.8968 | 0.007       | -0.0006  |
| 0    | 36   | f       | 1     | 35    | f        | 10487.4763 | 0.007       | -0.0090  |
| 0    | 37   | f       | 1     | 36    | f        | 10442.0488 | 0.007       | -0.0001  |
| 0    | 5    | f       | 1     | 6     | f        | 11024.0248 | 0.02        | 0.0380   |
| 0    | 6    | f       | 1     | 7     | f        | 11008.3955 | 0.007       | 0.0104   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 0    | 7    | f       | 1     | 8     | f        | 10991.3902 | 0.007       | -0.0028  |
| 0    | 8    | f       | 1     | 9     | f        | 10973.0203 | 0.007       | -0.0014  |
| 0    | 9    | f       | 1     | 10    | f        | 10953.3216 | 0.007       | -0.0010  |
| 0    | 10   | f       | 1     | 11    | f        | 10932.3127 | 0.007       | -0.0017  |
| 0    | 11   | f       | 1     | 12    | f        | 10910.0075 | 0.007       | -0.0022  |
| 0    | 12   | f       | 1     | 13    | f        | 10886.3641 | 0.007       | -0.0035  |
| 0    | 13   | f       | 1     | 14    | f        | 10861.5436 | 0.007       | -0.0013  |
| 0    | 14   | f       | 1     | 15    | f        | 10835.4486 | 0.007       | 0.0021   |
| 0    | 15   | f       | 1     | 16    | f        | 10808.1510 | 0.007       | -0.0033  |
| 0    | 16   | f       | 1     | 17    | f        | 10779.5836 | 0.007       | 0.0032   |
| 0    | 17   | f       | 1     | 18    | f        | 10749.8727 | 0.007       | -0.0028  |
| 0    | 18   | f       | 1     | 19    | f        | 10719.0232 | 0.007       | 0.0005   |
| 0    | 19   | f       | 1     | 20    | f        | 10687.0373 | 0.007       | -0.0086  |
| 0    | 20   | f       | 1     | 21    | f        | 10653.8576 | 0.007       | 0.0040   |
| 0    | 21   | f       | 1     | 22    | f        | 10619.6140 | 0.007       | -0.0007  |
| 0    | 22   | f       | 1     | 23    | f        | 10584.3040 | 0.007       | 0.0008   |
| 0    | 23   | f       | 1     | 24    | f        | 10548.0101 | 0.007       | -0.0049  |
| 0    | 24   | f       | 1     | 25    | f        | 10510.5764 | 0.02        | 0.0478   |
| 0    | 25   | f       | 1     | 26    | f        | 10472.1900 | 0.02        | 0.0234   |
| 0    | 26   | f       | 1     | 27    | f        | 10432.8252 | 0.02        | 0.0277   |
| 0    | 27   | f       | 1     | 28    | f        | 10392.5102 | 0.02        | 0.0290   |
| 0    | 28   | f       | 1     | 29    | f        | 10351.2104 | 0.02        | 0.0298   |
| 0    | 29   | f       | 1     | 30    | f        | 10309.6473 | 0.02        | -0.0059  |
| 0    | 30   | f       | 1     | 31    | f        | 10267.1950 | 0.02        | -0.0377  |
| 0    | 31   | f       | 1     | 32    | f        | 10223.9821 | 0.007       | 0.0157   |
| 0    | 32   | f       | 1     | 33    | f        | 10179.2377 | 0.007       | 0.0056   |
| 0    | 33   | f       | 1     | 34    | f        | 10134.0609 | 0.007       | -0.0058  |
| 0    | 34   | f       | 1     | 35    | f        | 10088.5592 | 0.007       | -0.0103  |
| 0    | 35   | f       | 1     | 36    | f        | 10042.8667 | 0.05        | -0.0389  |
| 0    | 36   | f       | 1     | 37    | f        | 9997.1382  | 0.05        | -0.0603  |
| 0    | 4    | e       | 1     | 4     | f        | 11074.7801 | 0.007       | -0.0125  |
| 0    | 5    | e       | 1     | 5     | f        | 11067.7133 | 0.007       | -0.0051  |
| 0    | 6    | e       | 1     | 6     | f        | 11059.2825 | 0.007       | -0.0032  |
| 0    | 7    | e       | 1     | 7     | f        | 11049.4742 | 0.007       | -0.0006  |
| 0    | 8    | e       | 1     | 8     | f        | 11038.3027 | 0.007       | -0.0051  |
| 0    | 9    | e       | 1     | 9     | f        | 11025.7787 | 0.007       | -0.0079  |
| 0    | 10   | e       | 1     | 10    | f        | 11011.9059 | 0.007       | -0.0049  |
| 0    | 11   | e       | 1     | 11    | f        | 10996.7070 | 0.007       | 0.0044   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 0    | 12   | e       | 1     | 12    | f        | 10980.1603 | 0.007       | -0.0103  |
| 1    | 5    | e       | 2     | 4     | e        | 10846.0822 | 0.007       | -0.0010  |
| 1    | 6    | e       | 2     | 5     | e        | 10845.3315 | 0.007       | -0.0043  |
| 1    | 7    | e       | 2     | 6     | e        | 10843.3074 | 0.007       | -0.0092  |
| 1    | 8    | e       | 2     | 7     | e        | 10839.9849 | 0.007       | 0.0043   |
| 1    | 9    | e       | 2     | 8     | e        | 10835.4486 | 0.007       | -0.0113  |
| 1    | 10   | e       | 2     | 9     | e        | 10829.6591 | 0.007       | 0.0101   |
| 1    | 11   | e       | 2     | 10    | e        | 10822.7321 | 0.007       | 0.0031   |
| 1    | 12   | e       | 2     | 11    | e        | 10814.6796 | 0.007       | 0.0065   |
| 1    | 13   | e       | 2     | 12    | e        | 10805.6926 | 0.007       | 0.0028   |
| 1    | 14   | e       | 2     | 13    | e        | 10795.9246 | 0.007       | 0.0068   |
| 1    | 15   | e       | 2     | 14    | e        | 10786.4225 | 0.007       | 0.0031   |
| 1    | 16   | e       | 2     | 15    | e        | 10766.5840 | 0.007       | 0.0035   |
| 1    | 17   | e       | 2     | 16    | e        | 10756.8221 | 0.007       | -0.0036  |
| 1    | 18   | e       | 2     | 17    | e        | 10744.3775 | 0.007       | -0.0090  |
| 1    | 19   | e       | 2     | 18    | e        | 10731.2049 | 0.007       | -0.0160  |
| 1    | 20   | e       | 2     | 19    | e        | 10717.7267 | 0.02        | -0.0243  |
| 1    | 5    | e       | 2     | 6     | e        | 10767.7808 | 0.007       | -0.0028  |
| 1    | 6    | e       | 2     | 7     | e        | 10752.8534 | 0.007       | 0.0013   |
| 1    | 7    | e       | 2     | 8     | e        | 10736.6826 | 0.007       | 0.0076   |
| 1    | 8    | e       | 2     | 9     | e        | 10719.2965 | 0.007       | -0.0118  |
| 1    | 9    | e       | 2     | 10    | e        | 10700.6766 | 0.007       | 0.0040   |
| 1    | 10   | e       | 2     | 11    | e        | 10680.9072 | 0.007       | 0.0027   |
| 1    | 11   | e       | 2     | 12    | e        | 10660.0252 | 0.007       | 0.0026   |
| 1    | 12   | e       | 2     | 13    | e        | 10638.0886 | 0.007       | 0.0021   |
| 1    | 13   | e       | 2     | 14    | e        | 10615.2787 | 0.007       | -0.0016  |
| 1    | 14   | e       | 2     | 15    | e        | 10591.7544 | 0.007       | 0.0065   |
| 1    | 15   | e       | 2     | 16    | e        | 10568.5772 | 0.007       | 0.0013   |
| 1    | 16   | e       | 2     | 17    | e        | 10535.1544 | 0.007       | -0.0092  |
| 1    | 17   | e       | 2     | 18    | e        | 10511.8769 | 0.007       | -0.0096  |
| 1    | 18   | e       | 2     | 19    | e        | 10486.0038 | 0.007       | -0.0032  |
| 1    | 19   | e       | 2     | 20    | e        | 10459.4779 | 0.007       | 0.0239   |
| 1    | 20   | e       | 2     | 21    | e        | 10432.6135 | 10          | 0.1856   |
| 1    | 4    | f       | 2     | 4     | e        | 10817.0173 | 0.007       | 0.0051   |
| 1    | 5    | f       | 2     | 5     | e        | 10810.4745 | 0.007       | 0.0005   |
| 1    | 6    | f       | 2     | 6     | e        | 10802.6340 | 0.007       | -0.0041  |
| 1    | 7    | f       | 2     | 7     | e        | 10793.5275 | 0.007       | -0.0040  |
| 1    | 8    | f       | 2     | 8     | e        | 10783.1488 | 0.007       | 0.0062   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 1    | 9    | f       | 2     | 9     | e        | 10771.5658 | 0.007       | 0.0007   |
| 1    | 10   | f       | 2     | 10    | e        | 10758.7773 | 0.007       | 0.0063   |
| 1    | 11   | f       | 2     | 11    | e        | 10744.8535 | 0.007       | 0.0081   |
| 1    | 12   | f       | 2     | 12    | e        | 10729.8598 | 0.007       | -0.0056  |
| 1    | 13   | f       | 2     | 13    | e        | 10713.9334 | 0.007       | 0.0018   |
| 1    | 5    | f       | 2     | 4     | f        | 10846.0822 | 0.007       | -0.0018  |
| 1    | 6    | f       | 2     | 5     | f        | 10845.3315 | 0.007       | -0.0038  |
| 1    | 7    | f       | 2     | 6     | f        | 10843.3074 | 0.007       | -0.0093  |
| 1    | 8    | f       | 2     | 7     | f        | 10839.9849 | 0.007       | 0.0034   |
| 1    | 9    | f       | 2     | 8     | f        | 10835.4486 | 0.007       | -0.0110  |
| 1    | 10   | f       | 2     | 9     | f        | 10829.6591 | 0.007       | 0.0099   |
| 1    | 11   | f       | 2     | 10    | f        | 10822.7321 | 0.007       | 0.0032   |
| 1    | 12   | f       | 2     | 11    | f        | 10814.6796 | 0.007       | 0.0076   |
| 1    | 13   | f       | 2     | 12    | f        | 10805.6926 | 0.007       | 0.0035   |
| 1    | 14   | f       | 2     | 13    | f        | 10795.8423 | 0.007       | 0.0044   |
| 1    | 15   | f       | 2     | 14    | f        | 10786.1172 | 0.007       | 0.0015   |
| 1    | 16   | f       | 2     | 15    | f        | 10766.1283 | 0.007       | 0.0044   |
| 1    | 17   | f       | 2     | 16    | f        | 10756.5434 | 0.007       | 0.0030   |
| 1    | 18   | f       | 2     | 17    | f        | 10744.1203 | 0.007       | -0.0019  |
| 1    | 19   | f       | 2     | 18    | f        | 10730.9264 | 0.007       | -0.0024  |
| 1    | 20   | f       | 2     | 19    | f        | 10717.3911 | 0.007       | -0.0042  |
| 1    | 5    | f       | 2     | 6     | f        | 10767.7808 | 0.007       | -0.0036  |
| 1    | 6    | f       | 2     | 7     | f        | 10752.8534 | 0.007       | 0.0018   |
| 1    | 7    | f       | 2     | 8     | f        | 10736.6826 | 0.007       | 0.0074   |
| 1    | 8    | f       | 2     | 9     | f        | 10719.2965 | 0.007       | -0.0128  |
| 1    | 9    | f       | 2     | 10    | f        | 10700.6766 | 0.007       | 0.0041   |
| 1    | 10   | f       | 2     | 11    | f        | 10680.9072 | 0.007       | 0.0020   |
| 1    | 11   | f       | 2     | 12    | f        | 10660.0252 | 0.007       | 0.0019   |
| 1    | 12   | f       | 2     | 13    | f        | 10638.0886 | 0.007       | 0.0018   |
| 1    | 13   | f       | 2     | 14    | f        | 10615.2787 | 0.007       | -0.0032  |
| 1    | 14   | f       | 2     | 15    | f        | 10591.6783 | 0.007       | -0.0059  |
| 1    | 15   | f       | 2     | 16    | f        | 10568.2802 | 0.007       | -0.0146  |
| 1    | 16   | f       | 2     | 17    | f        | 10534.6826 | 0.007       | -0.0016  |
| 1    | 17   | f       | 2     | 18    | f        | 10511.5839 | 0.007       | -0.0026  |
| 1    | 18   | f       | 2     | 19    | f        | 10485.7277 | 0.007       | 0.0023   |
| 1    | 19   | f       | 2     | 20    | f        | 10459.1917 | 0.007       | 0.0155   |
| 1    | 20   | f       | 2     | 21    | f        | 10432.5077 | 0.1         | -0.0660  |
| 0    | 5    | e       | 2     | 4     | e        | 9801.6141  | 0.1         | -0.0344  |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed  | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|-----------|-------------|----------|
| 0    | 6    | e       | 2     | 5     | e        | 9801.1905 | 0.007       | -0.0059  |
| 0    | 7    | e       | 2     | 6     | e        | 9799.5602 | 0.007       | -0.0069  |
| 0    | 8    | e       | 2     | 7     | e        | 9796.6804 | 0.007       | 0.0087   |
| 0    | 9    | e       | 2     | 8     | e        | 9792.6088 | 0.007       | -0.0002  |
| 0    | 10   | e       | 2     | 9     | e        | 9787.3089 | 0.007       | 0.0079   |
| 0    | 11   | e       | 2     | 10    | e        | 9780.8374 | 0.007       | -0.0037  |
| 0    | 12   | e       | 2     | 11    | e        | 9773.1001 | 0.007       | 0.0044   |
| 0    | 13   | e       | 2     | 12    | e        | 9764.2776 | 0.007       | 0.0072   |
| 0    | 14   | e       | 2     | 13    | e        | 9754.2846 | 0.007       | -0.0001  |
| 0    | 15   | e       | 2     | 14    | e        | 9743.1402 | 0.007       | 0.0028   |
| 0    | 16   | e       | 2     | 15    | e        | 9731.2102 | 0.007       | -0.0036  |
| 0    | 17   | e       | 2     | 16    | e        | 9717.4437 | 0.02        | -0.0352  |
| 0    | 18   | e       | 2     | 17    | e        | 9702.9317 | 0.007       | -0.0056  |
| 0    | 19   | e       | 2     | 18    | e        | 9687.3760 | 0.007       | -0.0133  |
| 0    | 20   | e       | 2     | 19    | e        | 9670.8249 | 0.007       | 0.0054   |
| 0    | 21   | e       | 2     | 20    | e        | 9652.9132 | 0.02        | 0.0394   |
| 0    | 22   | e       | 2     | 21    | e        | 9634.0636 | 0.1         | 0.1581   |
| 0    | 23   | e       | 2     | 22    | e        | 9614.1311 | 10          | 0.4115   |
| 0    | 5    | e       | 2     | 6     | e        | 9723.3544 | 0.1         | -0.0779  |
| 0    | 6    | e       | 2     | 7     | e        | 9708.7062 | 0.007       | 0.0059   |
| 0    | 7    | e       | 2     | 8     | e        | 9692.9335 | 0.007       | 0.0118   |
| 0    | 8    | e       | 2     | 9     | e        | 9675.9811 | 0.007       | 0.0036   |
| 0    | 9    | e       | 2     | 10    | e        | 9657.8473 | 0.007       | 0.0047   |
| 0    | 10   | e       | 2     | 11    | e        | 9638.5499 | 0.007       | 0.0075   |
| 0    | 11   | e       | 2     | 12    | e        | 9618.1232 | 0.007       | 0.0031   |
| 0    | 12   | e       | 2     | 13    | e        | 9596.5086 | 0.007       | 0.0005   |
| 0    | 13   | e       | 2     | 14    | e        | 9573.8607 | 0.007       | 0.0059   |
| 0    | 14   | e       | 2     | 15    | e        | 9550.1152 | 0.007       | -0.0013  |
| 0    | 15   | e       | 2     | 16    | e        | 9525.2963 | 0.007       | -0.0003  |
| 0    | 16   | e       | 2     | 17    | e        | 9499.7744 | 0.007       | -0.0101  |
| 0    | 17   | e       | 2     | 18    | e        | 9472.4568 | 0.007       | 0.0006   |
| 0    | 18   | e       | 2     | 19    | e        | 9444.5418 | 0.007       | 0.0164   |
| 0    | 19   | e       | 2     | 20    | e        | 9415.6337 | 0.05        | 0.0419   |
| 0    | 20   | e       | 2     | 21    | e        | 9385.6958 | 10          | 0.2313   |
| 0    | 21   | e       | 2     | 22    | e        | 9354.5544 | 10          | 0.3876   |
| 0    | 4    | e       | 2     | 4     | f        | 9772.1705 | 0.1         | 0.0783   |
| 0    | 5    | e       | 2     | 5     | f        | 9765.9677 | 0.007       | 0.0066   |
| 0    | 6    | e       | 2     | 6     | f        | 9758.4877 | 0.007       | -0.0010  |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 0    | 7    | e       | 2     | 7     | f        | 9749.7514  | 0.05        | 0.0271   |
| 0    | 8    | e       | 2     | 8     | f        | 9739.8194  | 0.05        | 0.0364   |
| 1    | 5    | e       | 0     | 4     | e        | 13486.3790 | 0.007       | 0.0012   |
| 1    | 6    | e       | 0     | 5     | e        | 13484.0574 | 0.007       | -0.0004  |
| 1    | 7    | e       | 0     | 6     | e        | 13480.1440 | 0.007       | 0.0016   |
| 1    | 8    | e       | 0     | 7     | e        | 13474.6390 | 0.007       | 0.0023   |
| 1    | 9    | e       | 0     | 8     | e        | 13467.5809 | 0.007       | 0.0011   |
| 1    | 10   | e       | 0     | 9     | e        | 13458.9999 | 0.007       | -0.0052  |
| 1    | 11   | e       | 0     | 10    | e        | 13448.9305 | 0.007       | -0.0004  |
| 1    | 12   | e       | 0     | 11    | e        | 13437.4454 | 0.007       | -0.0059  |
| 1    | 13   | e       | 0     | 12    | e        | 13424.7025 | 0.007       | -0.0055  |
| 1    | 14   | e       | 0     | 13    | e        | 13410.8803 | 0.007       | -0.0089  |
| 1    | 15   | e       | 0     | 14    | e        | 13397.0034 | 0.007       | -0.0091  |
| 1    | 16   | e       | 0     | 15    | e        | 13372.4702 | 0.007       | 0.0057   |
| 1    | 17   | e       | 0     | 16    | e        | 13357.7112 | 0.007       | 0.0063   |
| 1    | 18   | e       | 0     | 17    | e        | 13339.9614 | 0.007       | 0.0079   |
| 1    | 19   | e       | 0     | 18    | e        | 13321.1862 | 0.007       | -0.0038  |
| 1    | 4    | e       | 0     | 5     | e        | 13420.1150 | 0.007       | 0.0000   |
| 1    | 5    | e       | 0     | 6     | e        | 13404.6238 | 0.007       | 0.0015   |
| 1    | 6    | e       | 0     | 7     | e        | 13387.5018 | 0.007       | 0.0051   |
| 1    | 7    | e       | 0     | 8     | e        | 13368.8293 | 0.007       | 0.0057   |
| 1    | 8    | e       | 0     | 9     | e        | 13348.6074 | 0.007       | 0.0028   |
| 1    | 9    | e       | 0     | 10    | e        | 13326.8774 | 0.007       | -0.0019  |
| 1    | 10   | e       | 0     | 11    | e        | 13303.6684 | 0.007       | -0.0050  |
| 1    | 11   | e       | 0     | 12    | e        | 13279.0359 | 0.007       | -0.0064  |
| 1    | 12   | e       | 0     | 13    | e        | 13253.0344 | 0.007       | -0.0038  |
| 1    | 13   | e       | 0     | 14    | e        | 13225.8375 | 0.007       | 0.0084   |
| 1    | 14   | e       | 0     | 15    | e        | 13197.6584 | 0.007       | -0.0091  |
| 1    | 15   | e       | 0     | 16    | e        | 13169.4878 | 0.007       | -0.0103  |
| 1    | 16   | e       | 0     | 17    | e        | 13130.7362 | 0.007       | 0.0097   |
| 1    | 17   | e       | 0     | 18    | e        | 13101.8533 | 0.007       | 0.0074   |
| 1    | 18   | e       | 0     | 19    | e        | 13070.0728 | 0.007       | 0.0045   |
| 1    | 19   | e       | 0     | 20    | e        | 13037.3548 | 0.007       | -0.0031  |
| 1    | 20   | e       | 0     | 21    | e        | 13004.1077 | 0.007       | 0.0033   |
| 1    | 5    | f       | 0     | 4     | f        | 13486.3790 | 0.007       | 0.0004   |
| 1    | 6    | f       | 0     | 5     | f        | 13484.0574 | 0.007       | 0.0001   |
| 1    | 7    | f       | 0     | 6     | f        | 13480.1440 | 0.007       | 0.0015   |
| 1    | 8    | f       | 0     | 7     | f        | 13474.6390 | 0.007       | 0.0015   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 1    | 9    | f       | 0     | 8     | f        | 13467.5809 | 0.007       | 0.0015   |
| 1    | 10   | f       | 0     | 9     | f        | 13458.9999 | 0.007       | -0.0053  |
| 1    | 11   | f       | 0     | 10    | f        | 13448.9305 | 0.007       | -0.0001  |
| 1    | 12   | f       | 0     | 11    | f        | 13437.4454 | 0.007       | -0.0043  |
| 1    | 13   | f       | 0     | 12    | f        | 13424.7025 | 0.007       | -0.0038  |
| 1    | 14   | f       | 0     | 13    | f        | 13410.7863 | 0.007       | 0.0021   |
| 1    | 15   | f       | 0     | 14    | f        | 13396.6818 | 0.007       | 0.0087   |
| 1    | 16   | f       | 0     | 15    | f        | 13372.0287 | 0.007       | -0.0023  |
| 1    | 17   | f       | 0     | 16    | f        | 13357.4559 | 0.007       | -0.0017  |
| 1    | 18   | f       | 0     | 17    | f        | 13339.7339 | 0.007       | -0.0006  |
| 1    | 19   | f       | 0     | 18    | f        | 13320.9453 | 0.007       | -0.0059  |
| 1    | 4    | f       | 0     | 5     | f        | 13420.1150 | 0.05        | 0.0318   |
| 1    | 5    | f       | 0     | 6     | f        | 13404.6238 | 0.007       | 0.0007   |
| 1    | 6    | f       | 0     | 7     | f        | 13387.5018 | 0.007       | 0.0056   |
| 1    | 7    | f       | 0     | 8     | f        | 13368.8293 | 0.007       | 0.0056   |
| 1    | 8    | f       | 0     | 9     | f        | 13348.6074 | 0.007       | 0.0020   |
| 1    | 9    | f       | 0     | 10    | f        | 13326.8774 | 0.007       | -0.0016  |
| 1    | 10   | f       | 0     | 11    | f        | 13303.6684 | 0.007       | -0.0052  |
| 1    | 11   | f       | 0     | 12    | f        | 13279.0359 | 0.007       | -0.0061  |
| 1    | 12   | f       | 0     | 13    | f        | 13253.0344 | 0.007       | -0.0023  |
| 1    | 13   | f       | 0     | 14    | f        | 13225.8375 | 0.007       | 0.0099   |
| 1    | 14   | f       | 0     | 15    | f        | 13197.5660 | 0.007       | 0.0001   |
| 1    | 15   | f       | 0     | 16    | f        | 13169.1693 | 0.007       | 0.0042   |
| 1    | 16   | f       | 0     | 17    | f        | 13130.2993 | 0.007       | -0.0033  |
| 1    | 17   | f       | 0     | 18    | f        | 13101.6026 | 0.007       | -0.0058  |
| 1    | 19   | f       | 0     | 20    | f        | 13037.1132 | 0.007       | -0.0060  |
| 1    | 20   | f       | 0     | 21    | f        | 13003.8219 | 0.007       | 0.0050   |
| 1    | 4    | f       | 0     | 4     | e        | 13457.3263 | 0.007       | -0.0048  |
| 1    | 5    | f       | 0     | 5     | e        | 13449.1996 | 0.007       | 0.0052   |
| 1    | 6    | f       | 0     | 6     | e        | 13439.4748 | 0.007       | 0.0024   |
| 1    | 7    | f       | 0     | 7     | e        | 13428.1704 | 0.007       | 0.0053   |
| 1    | 8    | f       | 0     | 8     | e        | 13415.3007 | 0.007       | -0.0009  |
| 1    | 9    | f       | 0     | 9     | e        | 13400.8936 | 0.007       | -0.0016  |
| 1    | 10   | f       | 0     | 10    | e        | 13384.9825 | 0.007       | -0.0040  |
| 1    | 11   | f       | 0     | 11    | e        | 13367.6220 | 0.007       | -0.0069  |
| 1    | 12   | f       | 0     | 12    | e        | 13348.8535 | 0.007       | 0.0023   |
| 1    | 7    | e       | 3     | 6     | e        | 9577.6638  | 0.007       | -0.0056  |
| 1    | 8    | e       | 3     | 7     | e        | 9575.4406  | 0.007       | 0.0023   |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed  | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|-----------|-------------|----------|
| 1    | 9    | e       | 3     | 8     | e        | 9572.1423 | 0.007       | -0.0019  |
| 1    | 10   | e       | 3     | 9     | e        | 9567.7811 | 0.007       | -0.0041  |
| 1    | 11   | e       | 3     | 10    | e        | 9562.4000 | 0.007       | 0.0027   |
| 1    | 12   | e       | 3     | 11    | e        | 9556.0641 | 0.007       | 0.0037   |
| 1    | 13   | e       | 3     | 12    | e        | 9548.9451 | 0.007       | 0.0005   |
| 1    | 14   | e       | 3     | 13    | e        | 9541.1651 | 0.03        | 0.0389   |
| 1    | 15   | e       | 3     | 14    | e        | 9533.8686 | 0.007       | 0.0054   |
| 1    | 16   | e       | 3     | 15    | e        | 9516.3766 | 0.007       | -0.0117  |
| 1    | 17   | e       | 3     | 16    | e        | 9509.0997 | 0.03        | -0.0221  |
| 1    | 5    | e       | 3     | 6     | e        | 9502.0895 | 0.03        | 0.0484   |
| 1    | 6    | e       | 3     | 7     | e        | 9488.3084 | 0.007       | 0.0001   |
| 1    | 7    | e       | 3     | 8     | e        | 9473.3917 | 0.007       | 0.0017   |
| 1    | 8    | e       | 3     | 9     | e        | 9457.3910 | 0.007       | 0.0016   |
| 1    | 9    | e       | 3     | 10    | e        | 9440.3373 | 0.007       | 0.0108   |
| 1    | 10   | e       | 3     | 11    | e        | 9422.2897 | 0.007       | 0.0018   |
| 1    | 11   | e       | 3     | 12    | e        | 9403.2798 | 0.007       | -0.0017  |
| 1    | 12   | e       | 3     | 13    | e        | 9383.3664 | 0.007       | -0.0032  |
| 1    | 13   | e       | 3     | 14    | e        | 9362.7316 | 0.007       | -0.0060  |
| 1    | 14   | e       | 3     | 15    | e        | 9341.5004 | 0.04        | 0.0380   |
| 1    | 15   | e       | 3     | 16    | e        | 9320.8306 | 0.007       | 0.0070   |
| 1    | 7    | f       | 3     | 6     | f        | 9577.6638 | 0.007       | -0.0057  |
| 1    | 8    | f       | 3     | 7     | f        | 9575.4406 | 0.007       | 0.0015   |
| 1    | 9    | f       | 3     | 8     | f        | 9572.1423 | 0.007       | -0.0016  |
| 1    | 10   | f       | 3     | 9     | f        | 9567.7811 | 0.007       | -0.0044  |
| 1    | 11   | f       | 3     | 10    | f        | 9562.4000 | 0.007       | 0.0025   |
| 1    | 12   | f       | 3     | 11    | f        | 9556.0641 | 0.007       | 0.0043   |
| 1    | 13   | f       | 3     | 12    | f        | 9548.9451 | 0.007       | 0.0004   |
| 1    | 14   | f       | 3     | 13    | f        | 9541.1651 | 0.05        | -0.0473  |
| 1    | 15   | f       | 3     | 14    | f        | 9533.5772 | 0.05        | -0.0126  |
| 1    | 16   | f       | 3     | 15    | f        | 9515.9039 | 0.007       | 0.0019   |
| 1    | 17   | f       | 3     | 16    | f        | 9508.7920 | 0.007       | 0.0065   |
| 1    | 5    | f       | 3     | 6     | f        | 9502.0895 | 0.05        | 0.0476   |
| 1    | 6    | f       | 3     | 7     | f        | 9488.3084 | 0.007       | 0.0005   |
| 1    | 7    | f       | 3     | 8     | f        | 9473.3917 | 0.007       | 0.0015   |
| 1    | 8    | f       | 3     | 9     | f        | 9457.3910 | 0.007       | 0.0006   |
| 1    | 9    | f       | 3     | 10    | f        | 9440.3373 | 0.007       | 0.0107   |
| 1    | 10   | f       | 3     | 11    | f        | 9422.2897 | 0.007       | 0.0008   |
| 1    | 11   | f       | 3     | 12    | f        | 9403.2798 | 0.007       | -0.0032  |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 1    | 12   | f       | 3     | 13    | f        | 9383.3664  | 0.007       | -0.0049  |
| 1    | 13   | f       | 3     | 14    | f        | 9362.7316  | 0.007       | -0.0101  |
| 1    | 14   | f       | 3     | 15    | f        | 9341.5004  | 0.05        | -0.0549  |
| 1    | 15   | f       | 3     | 16    | f        | 9320.5568  | 0.05        | -0.0392  |
| 2    | 5    | e       | 0     | 4     | e        | 14484.5800 | 0.007       | 0.0017   |
| 2    | 6    | e       | 0     | 5     | e        | 14481.9514 | 0.007       | -0.0236  |
| 2    | 7    | e       | 0     | 6     | e        | 14477.6506 | 0.007       | -0.0066  |
| 2    | 8    | e       | 0     | 7     | e        | 14471.7577 | 0.007       | 0.0018   |
| 2    | 9    | e       | 0     | 8     | e        | 14464.3192 | 0.007       | 0.0050   |
| 2    | 10   | e       | 0     | 9     | e        | 14455.3629 | 0.007       | 0.0039   |
| 2    | 11   | e       | 0     | 10    | e        | 14444.9601 | 0.007       | 0.0068   |
| 2    | 12   | e       | 0     | 11    | e        | 14433.1781 | 0.007       | -0.0037  |
| 2    | 13   | e       | 0     | 12    | e        | 14420.0601 | 0.007       | 0.0112   |
| 2    | 14   | e       | 0     | 13    | e        | 14405.8225 | 0.007       | -0.0075  |
| 2    | 15   | e       | 0     | 14    | e        | 14390.4582 | 0.05        | -0.0601  |
| 2    | 4    | e       | 0     | 5     | e        | 14418.3674 | 10          | 0.1415   |
| 2    | 5    | e       | 0     | 6     | e        | 14402.8285 | 0.007       | -0.0018  |
| 2    | 6    | e       | 0     | 7     | e        | 14385.3813 | 0.007       | -0.0036  |
| 2    | 7    | e       | 0     | 8     | e        | 14366.3419 | 0.007       | -0.0085  |
| 2    | 8    | e       | 0     | 9     | e        | 14345.7313 | 0.007       | -0.0030  |
| 2    | 9    | e       | 0     | 10    | e        | 14323.6224 | 0.007       | -0.0047  |
| 2    | 10   | e       | 0     | 11    | e        | 14300.0350 | 0.007       | 0.0004   |
| 2    | 11   | e       | 0     | 12    | e        | 14275.0734 | 0.007       | -0.0071  |
| 2    | 12   | e       | 0     | 13    | e        | 14248.7664 | 0.007       | -0.0010  |
| 2    | 13   | e       | 0     | 14    | e        | 14221.2147 | 0.007       | 0.0054   |
| 2    | 14   | e       | 0     | 15    | e        | 14192.5973 | 0.007       | -0.0044  |
| 2    | 15   | e       | 0     | 16    | e        | 14162.8686 | 0.05        | 0.0127   |
| 2    | 5    | f       | 0     | 4     | f        | 14484.5800 | 0.007       | 0.0037   |
| 2    | 6    | f       | 0     | 5     | f        | 14481.9514 | 0.007       | -0.0219  |
| 2    | 7    | f       | 0     | 6     | f        | 14477.6506 | 0.007       | -0.0038  |
| 2    | 8    | f       | 0     | 7     | f        | 14471.7577 | 0.007       | 0.0055   |
| 2    | 9    | f       | 0     | 8     | f        | 14464.3192 | 0.007       | 0.0076   |
| 2    | 10   | f       | 0     | 9     | f        | 14455.3629 | 0.007       | 0.0021   |
| 2    | 11   | f       | 0     | 10    | f        | 14444.9601 | 0.007       | 0.0051   |
| 2    | 12   | f       | 0     | 11    | f        | 14433.1781 | 0.007       | -0.0030  |
| 2    | 13   | f       | 0     | 12    | f        | 14420.0601 | 0.007       | 0.0165   |
| 2    | 14   | f       | 0     | 13    | f        | 14405.8225 | 0.007       | -0.0073  |
| 2    | 15   | f       | 0     | 14    | f        | 14390.4582 | 0.05        | -0.0637  |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 2    | 5    | f       | 0     | 6     | f        | 14402.8285 | 0.007       | 0.0002   |
| 2    | 6    | f       | 0     | 7     | f        | 14385.3813 | 0.007       | -0.0019  |
| 2    | 7    | f       | 0     | 8     | f        | 14366.3419 | 0.007       | -0.0057  |
| 2    | 8    | f       | 0     | 9     | f        | 14345.7313 | 0.007       | 0.0007   |
| 2    | 9    | f       | 0     | 10    | f        | 14323.6224 | 0.007       | -0.0021  |
| 2    | 10   | f       | 0     | 11    | f        | 14300.0350 | 0.007       | -0.0014  |
| 2    | 11   | f       | 0     | 12    | f        | 14275.0734 | 0.007       | -0.0088  |
| 2    | 12   | f       | 0     | 13    | f        | 14248.7664 | 0.007       | -0.0003  |
| 2    | 13   | f       | 0     | 14    | f        | 14221.2147 | 0.007       | 0.0106   |
| 2    | 14   | f       | 0     | 15    | f        | 14192.5973 | 0.007       | -0.0044  |
| 2    | 15   | f       | 0     | 16    | f        | 14162.8686 | 0.007       | 0.0088   |
| 2    | 4    | e       | 0     | 4     | f        | 14455.8250 | 10          | -0.1414  |
| 2    | 5    | e       | 0     | 5     | f        | 14447.4004 | 0.007       | 0.0066   |
| 2    | 6    | e       | 0     | 6     | f        | 14437.3396 | 0.007       | 0.0079   |
| 2    | 7    | e       | 0     | 7     | f        | 14425.6562 | 0.007       | 0.0179   |
| 2    | 8    | e       | 0     | 8     | f        | 14412.3835 | 0.1         | 0.0352   |
| 2    | 6    | e       | 1     | 5     | e        | 13144.9384 | 0.007       | -0.0065  |
| 2    | 7    | e       | 1     | 6     | e        | 13141.5859 | 0.007       | 0.0032   |
| 2    | 8    | e       | 1     | 7     | e        | 13136.8012 | 0.007       | 0.0011   |
| 2    | 9    | e       | 1     | 8     | e        | 13130.6169 | 0.007       | 0.0044   |
| 2    | 10   | e       | 1     | 9     | e        | 13123.0746 | 0.007       | 0.0000   |
| 2    | 11   | e       | 1     | 10    | e        | 13114.2419 | 0.007       | -0.0002  |
| 2    | 12   | e       | 1     | 11    | e        | 13104.1701 | 0.007       | 0.0023   |
| 2    | 13   | e       | 1     | 12    | e        | 13092.9566 | 0.007       | -0.0080  |
| 2    | 14   | e       | 1     | 13    | e        | 13080.7187 | 0.007       | 0.0089   |
| 2    | 15   | e       | 1     | 14    | e        | 13067.4881 | 0.007       | 0.0135   |
| 2    | 16   | e       | 1     | 15    | e        | 13053.3417 | 0.007       | -0.0001  |
| 2    | 17   | e       | 1     | 16    | e        | 13039.0326 | 0.007       | -0.0001  |
| 2    | 5    | e       | 1     | 6     | e        | 13066.7788 | 0.007       | -0.0070  |
| 2    | 6    | e       | 1     | 7     | e        | 13050.3953 | 0.007       | 0.0252   |
| 2    | 7    | e       | 1     | 8     | e        | 13032.6372 | 0.007       | -0.0067  |
| 2    | 8    | e       | 1     | 9     | e        | 13013.4367 | 0.007       | -0.0006  |
| 2    | 9    | e       | 1     | 10    | e        | 12992.8973 | 0.007       | -0.0048  |
| 2    | 10   | e       | 1     | 11    | e        | 12971.0379 | 0.007       | -0.0044  |
| 2    | 11   | e       | 1     | 12    | e        | 12947.9431 | 0.007       | 0.0005   |
| 2    | 12   | e       | 1     | 13    | e        | 12923.6753 | 0.007       | 0.0027   |
| 2    | 13   | e       | 1     | 14    | e        | 12898.3320 | 0.007       | -0.0084  |
| 2    | 14   | e       | 1     | 15    | e        | 12872.0397 | 0.007       | 0.0033   |

| $v'$                     | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|--------------------------|------|---------|-------|-------|----------|------------|-------------|----------|
| 2                        | 15   | e       | 1     | 16    | e        | 12844.8460 | 0.007       | -0.0126  |
| 2                        | 6    | f       | 1     | 5     | f        | 13144.9384 | 0.007       | -0.0048  |
| 2                        | 7    | f       | 1     | 6     | f        | 13141.5859 | 0.007       | 0.0060   |
| 2                        | 8    | f       | 1     | 7     | f        | 13136.8012 | 0.007       | 0.0048   |
| 2                        | 9    | f       | 1     | 8     | f        | 13130.6169 | 0.007       | 0.0070   |
| 2                        | 10   | f       | 1     | 9     | f        | 13123.0746 | 0.007       | -0.0019  |
| 2                        | 11   | f       | 1     | 10    | f        | 13114.2419 | 0.007       | -0.0019  |
| 2                        | 12   | f       | 1     | 11    | f        | 13104.1701 | 0.007       | 0.0030   |
| 2                        | 13   | f       | 1     | 12    | f        | 13092.9566 | 0.007       | -0.0027  |
| 2                        | 14   | f       | 1     | 13    | f        | 13080.7187 | 0.007       | 0.0090   |
| 2                        | 15   | f       | 1     | 14    | f        | 13067.4881 | 0.007       | 0.0098   |
| 2                        | 16   | f       | 1     | 15    | f        | 13053.3417 | 0.007       | -0.0001  |
| 2                        | 17   | f       | 1     | 16    | f        | 13039.0326 | 0.007       | 0.0000   |
| 2                        | 5    | f       | 1     | 6     | f        | 13066.7788 | 0.007       | -0.0050  |
| 2                        | 6    | f       | 1     | 7     | f        | 13050.3953 | 0.007       | 0.0269   |
| 2                        | 7    | f       | 1     | 8     | f        | 13032.6372 | 0.007       | -0.0039  |
| 2                        | 8    | f       | 1     | 9     | f        | 13013.4367 | 0.007       | 0.0031   |
| 2                        | 9    | f       | 1     | 10    | f        | 12992.8973 | 0.007       | -0.0022  |
| 2                        | 10   | f       | 1     | 11    | f        | 12971.0379 | 0.007       | -0.0062  |
| 2                        | 11   | f       | 1     | 12    | f        | 12947.9431 | 0.007       | -0.0013  |
| 2                        | 12   | f       | 1     | 13    | f        | 12923.6753 | 0.007       | 0.0033   |
| 2                        | 13   | f       | 1     | 14    | f        | 12898.3320 | 0.007       | -0.0033  |
| 2                        | 14   | f       | 1     | 15    | f        | 12872.0397 | 0.007       | 0.0030   |
| 2                        | 15   | f       | 1     | 16    | f        | 12844.8460 | 0.007       | -0.0171  |
| 2                        | 5    | f       | 1     | 5     | e        | 13110.4128 | 0.007       | 0.0003   |
| 2                        | 6    | f       | 1     | 6     | e        | 13101.2413 | 0.05        | 0.0531   |
| 2                        | 7    | f       | 1     | 7     | e        | 13090.7134 | 0.007       | 0.0064   |
| 2                        | 8    | f       | 1     | 8     | e        | 13078.7344 | 0.007       | -0.0149  |
| 2                        | 9    | f       | 1     | 9     | e        | 13065.3549 | 0.007       | -0.0107  |
| 2                        | 10   | f       | 1     | 10    | e        | 13050.6165 | 0.007       | 0.0072   |
| 2                        | 11   | f       | 1     | 11    | e        | 13034.6412 | 0.007       | 0.0068   |
| 2                        | 12   | f       | 1     | 12    | e        | 13017.4702 | 0.007       | -0.0030  |
| 2                        | 13   | f       | 1     | 13    | e        | 12999.1863 | 0.007       | -0.0206  |
| $A'^3\Phi_3 - X^3\Phi_3$ |      |         |       |       |          |            |             |          |
| 0                        | 9    | f       | 0     | 8     | f        | 12038.5857 | 0.007       | -0.0067  |
| 0                        | 10   | f       | 0     | 9     | f        | 12033.6369 | 0.007       | -0.0068  |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 0    | 11   | f       | 0     | 10    | f        | 12027.4486 | 10          | 0.1844   |
| 0    | 12   | f       | 0     | 11    | f        | 12020.1671 | 0.007       | 0.0101   |
| 0    | 13   | f       | 0     | 12    | f        | 12010.8493 | 0.07        | 0.0632   |
| 0    | 14   | f       | 0     | 13    | f        | 12000.0652 | 0.007       | 0.0091   |
| 0    | 15   | f       | 0     | 14    | f        | 11988.4073 | 0.007       | -0.0102  |
| 0    | 16   | f       | 0     | 15    | f        | 11975.9427 | 0.007       | -0.0040  |
| 0    | 17   | f       | 0     | 16    | f        | 11962.5110 | 0.007       | -0.0153  |
| 0    | 18   | f       | 0     | 17    | f        | 11947.9947 | 0.015       | -0.0527  |
| 0    | 19   | f       | 0     | 18    | f        | 11932.2117 | 0.015       | -0.0344  |
| 0    | 20   | f       | 0     | 19    | f        | 11917.3223 | 0.007       | 0.0234   |
| 0    | 9    | f       | 0     | 10    | f        | 11896.6167 | 0.007       | 0.0053   |
| 0    | 10   | f       | 0     | 11    | f        | 11876.9321 | 0.007       | 0.0060   |
| 0    | 11   | f       | 0     | 12    | f        | 11856.2741 | 0.007       | -0.0005  |
| 0    | 12   | f       | 0     | 13    | f        | 11834.2152 | 0.007       | 0.0121   |
| 0    | 13   | f       | 0     | 14    | f        | 11810.4490 | 0.007       | 0.0120   |
| 0    | 14   | f       | 0     | 15    | f        | 11785.2327 | 0.007       | -0.0091  |
| 0    | 15   | f       | 0     | 16    | f        | 11759.2554 | 0.007       | 0.0104   |
| 0    | 16   | f       | 0     | 17    | f        | 11732.6613 | 0.007       | 0.0037   |
| 0    | 17   | f       | 0     | 18    | f        | 11705.2265 | 0.007       | 0.0149   |
| 0    | 18   | f       | 0     | 19    | f        | 11676.8848 | 0.007       | 0.0119   |
| 0    | 19   | f       | 0     | 20    | f        | 11647.5564 | 0.007       | 0.0087   |
| 0    | 20   | f       | 0     | 21    | f        | 11619.4517 | 0.007       | -0.0210  |
| 0    | 12   | e       | 0     | 11    | e        | 12013.2217 | 0.007       | -0.0047  |
| 0    | 13   | e       | 0     | 12    | e        | 12004.4712 | 0.007       | 0.0021   |
| 0    | 14   | e       | 0     | 13    | e        | 11997.5885 | 0.007       | -0.0004  |
| 0    | 15   | e       | 0     | 14    | e        | 11985.9062 | 0.007       | -0.0013  |
| 0    | 16   | e       | 0     | 15    | e        | 11979.8797 | 0.007       | 0.0095   |
| 0    | 17   | e       | 0     | 16    | e        | 11964.2326 | 0.007       | 0.0041   |
| 0    | 18   | e       | 0     | 17    | e        | 11947.7437 | 0.007       | 0.0027   |
| 0    | 19   | e       | 0     | 18    | e        | 11930.8335 | 0.02        | 0.0494   |
| 0    | 20   | e       | 0     | 19    | e        | 11914.2535 | 0.02        | 0.0007   |
| 0    | 12   | e       | 0     | 13    | e        | 11827.2160 | 0.007       | 0.0052   |
| 0    | 13   | e       | 0     | 14    | e        | 11803.9400 | 0.007       | -0.0011  |
| 0    | 14   | e       | 0     | 15    | e        | 11782.5947 | 0.007       | 0.0005   |
| 0    | 15   | e       | 0     | 16    | e        | 11756.5363 | 0.007       | 0.0034   |
| 0    | 16   | e       | 0     | 17    | e        | 11736.2523 | 0.007       | -0.0079  |
| 0    | 17   | e       | 0     | 18    | e        | 11706.4145 | 0.007       | -0.0036  |
| 0    | 18   | e       | 0     | 19    | e        | 11675.8452 | 0.007       | -0.0010  |

| $v'$                  | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|-----------------------|------|---------|-------|-------|----------|------------|-------------|----------|
| 0                     | 19   | e       | 0     | 20    | e        | 11645.0200 | 0.007       | -0.0050  |
| 0                     | 20   | e       | 0     | 21    | e        | 11614.6160 | 10          | -0.0793  |
| 0                     | 12   | f       | 0     | 12    | e        | 11930.8335 | 0.007       | -0.0231  |
| 0                     | 13   | f       | 0     | 13    | e        | 11914.2535 | 0.007       | -0.0123  |
| 0                     | 14   | f       | 0     | 14    | e        | 11895.9149 | 10          | 0.2080   |
| 0                     | 16   | f       | 0     | 16    | e        | 11858.1006 | 10          | -0.6279  |
| [13.3]4 – $X^3\Phi_4$ |      |         |       |       |          |            |             |          |
| 0                     | 14   | e       | 0     | 13    | e        | 13332.6685 | 0.01        | -0.0219  |
| 0                     | 15   | e       | 0     | 14    | e        | 13325.5972 | 0.007       | -0.0111  |
| 0                     | 16   | e       | 0     | 15    | e        | 13315.1554 | 0.007       | -0.0108  |
| 0                     | 17   | e       | 0     | 16    | e        | 13302.0365 | 0.007       | 0.0029   |
| 0                     | 18   | e       | 0     | 17    | e        | 13286.5101 | 0.007       | 0.0024   |
| 0                     | 19   | e       | 0     | 18    | e        | 13268.6273 | 0.007       | -0.0036  |
| 0                     | 20   | e       | 0     | 19    | e        | 13248.3690 | 0.007       | 0.0016   |
| 0                     | 21   | e       | 0     | 20    | e        | 13225.8375 | 0.05        | -0.0545  |
| 0                     | 22   | e       | 0     | 21    | e        | 13201.1174 | 0.007       | -0.0008  |
| 0                     | 23   | e       | 0     | 22    | e        | 13174.2910 | 0.007       | -0.0031  |
| 0                     | 24   | e       | 0     | 23    | e        | 13145.6175 | 0.007       | -0.0018  |
| 0                     | 25   | e       | 0     | 24    | e        | 13115.2558 | 0.007       | -0.0066  |
| 0                     | 26   | e       | 0     | 25    | e        | 13083.3183 | 0.007       | -0.0035  |
| 0                     | 27   | e       | 0     | 26    | e        | 13048.4269 | 0.007       | -0.0014  |
| 0                     | 28   | e       | 0     | 27    | e        | 13012.3167 | 0.007       | -0.0010  |
| 0                     | 29   | e       | 0     | 28    | e        | 12976.3927 | 0.007       | -0.0011  |
| 0                     | 30   | e       | 0     | 29    | e        | 12938.8007 | 0.007       | -0.0027  |
| 0                     | 31   | e       | 0     | 30    | e        | 12899.9828 | 0.007       | 0.0044   |
| 0                     | 32   | e       | 0     | 31    | e        | 12860.0772 | 0.007       | 0.0020   |
| 0                     | 33   | e       | 0     | 32    | e        | 12819.1898 | 0.007       | -0.0023  |
| 0                     | 34   | e       | 0     | 33    | e        | 12777.4329 | 0.007       | 0.0067   |
| 0                     | 35   | e       | 0     | 34    | e        | 12734.9819 | 0.007       | 0.0045   |
| 0                     | 36   | e       | 0     | 35    | e        | 12691.9910 | 0.007       | 0.0015   |
| 0                     | 37   | e       | 0     | 36    | e        | 12648.6592 | 0.007       | 0.0016   |
| 0                     | 38   | e       | 0     | 37    | e        | 12605.1349 | 0.007       | 0.0025   |
| 0                     | 39   | e       | 0     | 38    | e        | 12561.4992 | 0.007       | 0.0029   |
| 0                     | 17   | e       | 0     | 18    | e        | 13046.2000 | 0.007       | -0.0174  |
| 0                     | 18   | e       | 0     | 19    | e        | 13016.6177 | 0.007       | 0.0029   |
| 0                     | 20   | e       | 0     | 21    | e        | 12950.7038 | 0.007       | -0.0012  |

| $v'$ | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|------|------|---------|-------|-------|----------|------------|-------------|----------|
| 0    | 21   | e       | 0     | 22    | e        | 12914.3794 | 0.007       | 0.0045   |
| 0    | 22   | e       | 0     | 23    | e        | 12876.0955 | 0.007       | 0.0022   |
| 0    | 23   | e       | 0     | 24    | e        | 12835.7607 | 0.007       | 0.0044   |
| 0    | 24   | e       | 0     | 25    | e        | 12793.7069 | 0.007       | 0.0029   |
| 0    | 25   | e       | 0     | 26    | e        | 12750.0787 | 0.007       | 0.0069   |
| 0    | 26   | e       | 0     | 27    | e        | 12705.0193 | 0.007       | 0.0043   |
| 0    | 27   | e       | 0     | 28    | e        | 12657.1402 | 0.007       | 0.0014   |
| 0    | 28   | e       | 0     | 29    | e        | 12608.1764 | 0.007       | 0.0017   |
| 0    | 29   | e       | 0     | 30    | e        | 12559.5423 | 0.007       | 0.0019   |
| 0    | 30   | e       | 0     | 31    | e        | 12509.3867 | 0.007       | 0.0025   |
| 0    | 31   | e       | 0     | 32    | e        | 12458.1730 | 0.007       | -0.0035  |
| 0    | 32   | e       | 0     | 33    | e        | 12406.0107 | 0.007       | -0.0010  |
| 0    | 33   | e       | 0     | 34    | e        | 12353.0251 | 0.007       | 0.0022   |
| 0    | 34   | e       | 0     | 35    | e        | 12299.3602 | 0.007       | -0.0057  |
| 0    | 35   | e       | 0     | 36    | e        | 12245.1483 | 0.007       | -0.0025  |
| 0    | 15   | f       | 0     | 14    | f        | 13327.0826 | 0.01        | -0.0116  |
| 0    | 16   | f       | 0     | 15    | f        | 13316.4531 | 0.007       | 0.0061   |
| 0    | 17   | f       | 0     | 16    | f        | 13303.2497 | 0.007       | 0.0102   |
| 0    | 18   | f       | 0     | 17    | f        | 13287.8031 | 0.007       | 0.0076   |
| 0    | 19   | f       | 0     | 18    | f        | 13270.2620 | 0.007       | 0.0025   |
| 0    | 20   | f       | 0     | 19    | f        | 13250.9065 | 0.007       | -0.0028  |
| 0    | 21   | f       | 0     | 20    | f        | 13230.5498 | 0.007       | -0.0037  |
| 0    | 22   | f       | 0     | 21    | f        | 13195.9787 | 0.007       | 0.0018   |
| 0    | 23   | f       | 0     | 22    | f        | 13170.2520 | 0.007       | 0.0040   |
| 0    | 24   | f       | 0     | 23    | f        | 13141.5859 | 0.007       | 0.0004   |
| 0    | 25   | f       | 0     | 24    | f        | 13114.9985 | 0.007       | 0.0049   |
| 0    | 26   | f       | 0     | 25    | f        | 13083.3183 | 0.007       | 0.0025   |
| 0    | 16   | f       | 0     | 17    | f        | 13074.7096 | 0.007       | 0.0192   |
| 0    | 17   | f       | 0     | 18    | f        | 13047.3870 | 0.007       | 0.0154   |
| 0    | 18   | f       | 0     | 19    | f        | 13017.9140 | 0.007       | 0.0037   |
| 0    | 19   | f       | 0     | 20    | f        | 12986.4274 | 0.007       | 0.0047   |
| 0    | 20   | f       | 0     | 21    | f        | 12953.2377 | 0.007       | -0.0042  |
| 0    | 21   | f       | 0     | 22    | f        | 12919.1498 | 0.007       | -0.0058  |
| 0    | 22   | f       | 0     | 23    | f        | 12870.9586 | 0.007       | -0.0013  |
| 0    | 23   | f       | 0     | 24    | f        | 12831.7310 | 0.007       | -0.0036  |
| 0    | 24   | f       | 0     | 25    | f        | 12789.6722 | 0.007       | 0.0005   |
| 0    | 25   | f       | 0     | 26    | f        | 12749.8351 | 0.007       | -0.0054  |
| 0    | 26   | f       | 0     | 27    | f        | 12705.0193 | 0.007       | -0.0031  |

| $v'$                  | $J'$ | parity' | $v''$ | $J''$ | parity'' | Observed   | Uncertainty | calc-obs |
|-----------------------|------|---------|-------|-------|----------|------------|-------------|----------|
| [13.3]4 – $X^3\Phi_3$ |      |         |       |       |          |            |             |          |
| 0                     | 14   | e       | 1     | 13    | e        | 12631.8731 | 0.007       | -0.0039  |
| 0                     | 15   | e       | 0     | 14    | e        | 12623.9293 | 0.007       | 0.0146   |
| 0                     | 16   | e       | 0     | 15    | e        | 12612.5904 | 0.007       | 0.0058   |
| 0                     | 17   | e       | 0     | 16    | e        | 12598.5378 | 0.007       | 0.0109   |
| 0                     | 18   | e       | 0     | 17    | e        | 12582.0403 | 0.007       | 0.0090   |
| 0                     | 19   | e       | 0     | 18    | e        | 12563.1597 | 0.007       | 0.0042   |
| 0                     | 20   | e       | 0     | 19    | e        | 12541.8969 | 0.007       | 0.0003   |
| 0                     | 21   | e       | 0     | 20    | e        | 12518.2881 | 0.007       | -0.0022  |
| 0                     | 22   | e       | 0     | 21    | e        | 12492.6012 | 0.03        | -0.0076  |
| 0                     | 23   | e       | 0     | 22    | e        | 12464.7558 | 0.03        | -0.0113  |
| 0                     | 24   | e       | 0     | 23    | e        | 12435.0722 | 0.03        | -0.0074  |
| 0                     | 25   | e       | 0     | 24    | e        | 12403.7160 | 0.03        | -0.0047  |
| 0                     | 13   | e       | 0     | 14    | e        | 12436.8010 | 0.007       | 0.0009   |
| 0                     | 14   | e       | 0     | 15    | e        | 12416.8593 | 0.007       | 0.0169   |
| 0                     | 15   | e       | 0     | 16    | e        | 12394.5804 | 0.007       | -0.0016  |
| 0                     | 16   | e       | 0     | 17    | e        | 12368.9438 | 0.007       | 0.0076   |
| 0                     | 17   | e       | 0     | 18    | e        | 12340.7158 | 0.007       | 0.0071   |
| 0                     | 18   | e       | 0     | 19    | e        | 12310.1596 | 0.007       | -0.0124  |
| 0                     | 13   | f       | 0     | 12    | f        | 12639.4308 | 0.05        | -0.0643  |
| 0                     | 14   | f       | 0     | 13    | f        | 12633.4083 | 0.007       | 0.0020   |
| 0                     | 15   | f       | 0     | 14    | f        | 12625.5341 | 0.007       | 0.0070   |
| 0                     | 16   | f       | 0     | 15    | f        | 12614.1355 | 0.007       | -0.0228  |
| 0                     | 17   | f       | 0     | 16    | f        | 12600.1411 | 0.007       | -0.0253  |
| 0                     | 18   | f       | 0     | 17    | f        | 12583.9331 | 0.007       | -0.0121  |
| 0                     | 19   | f       | 0     | 18    | f        | 12565.7292 | 0.007       | -0.0058  |
| 0                     | 20   | f       | 0     | 19    | f        | 12545.8270 | 0.015       | 0.0347   |
| 0                     | 21   | f       | 0     | 20    | f        | 12525.2057 | 0.01        | 0.0194   |
| 0                     | 13   | f       | 0     | 14    | f        | 12438.9141 | 0.007       | 0.0010   |
| 0                     | 14   | f       | 0     | 15    | f        | 12418.5615 | 0.007       | -0.0019  |
| 0                     | 15   | f       | 0     | 16    | f        | 12396.4110 | 0.007       | -0.0012  |
| 0                     | 16   | f       | 0     | 17    | f        | 12370.8416 | 0.007       | -0.0026  |
| 0                     | 17   | f       | 0     | 18    | f        | 12342.7718 | 0.05        | 0.0896   |
| 0                     | 18   | f       | 0     | 19    | f        | 12312.8245 | 0.05        | 0.0512   |

# Appendix C

## Line list for YbO

Output from least-square fits for Systems 1, 2 and 3. All values are in  $\text{cm}^{-1}$ .

### C.1 Line list for YbO. System 1

Table C.1: Line list for System 1.

| $J'$ | Parity | $J''$ | Observed  | Obs.-Calc. | Uncertainty |
|------|--------|-------|-----------|------------|-------------|
| 8    | e      | 9     | 10249.502 | 0.00071    | 0.005       |
| 9    | e      | 10    | 10248.723 | 0.00172    | 0.005       |
| 10   | e      | 11    | 10247.924 | -0.00843   | 0.005       |
| 11   | e      | 12    | 10247.137 | 0.00228    | 0.005       |
| 12   | e      | 13    | 10246.304 | -0.02415   | 0.005       |
| 13   | e      | 14    | 10245.499 | -0.0137    | 0.005       |
| 14   | e      | 15    | 10244.679 | -0.00934   | 0.005       |
| 15   | e      | 16    | 10243.838 | -0.01705   | 0.005       |
| 16   | e      | 17    | 10243.015 | 0.00219    | 0.005       |
| 17   | e      | 18    | 10242.148 | -0.01357   | 0.005       |
| 18   | e      | 19    | 10241.317 | 0.01568    | 0.005       |
| 19   | e      | 20    | 10240.448 | 0.016      | 0.005       |
| 20   | e      | 21    | 10239.56  | 0.00642    | 0.005       |
| 21   | e      | 22    | 10238.674 | 0.00798    | 0.005       |
| 22   | e      | 23    | 10237.745 | -0.02426   | 0.005       |
| 23   | e      | 24    | 10236.872 | 0.00875    | 0.005       |

| $J'$ | Parity | $J''$ | Observed  | Obs.-Calc. | Uncertainty |
|------|--------|-------|-----------|------------|-------------|
| 24   | e      | 25    | 10235.946 | -0.00192   | 0.005       |
| 25   | e      | 26    | 10234.999 | -0.02422   | 0.005       |
| 26   | e      | 27    | 10234.074 | -0.01507   | 0.005       |
| 27   | e      | 28    | 10233.149 | 0.0036     | 0.005       |
| 28   | e      | 29    | 10232.208 | 0.01587    | 0.005       |
| 29   | e      | 30    | 10231.235 | 0.00583    | 0.005       |
| 30   | e      | 31    | 10230.268 | 0.01158    | 0.005       |
| 31   | e      | 32    | 10229.291 | 0.01722    | 0.005       |
| 32   | e      | 33    | 10228.289 | 0.00785    | 0.005       |
| 33   | e      | 34    | 10227.299 | 0.0206     | 0.005       |
| 34   | e      | 35    | 10226.278 | 0.01258    | 0.005       |
| 35   | e      | 36    | 10225.254 | 0.01192    | 0.005       |
| 36   | e      | 37    | 10224.215 | 0.00677    | 0.005       |
| 37   | e      | 38    | 10223.177 | 0.01328    | 0.005       |
| 38   | e      | 39    | 10222.121 | 0.0126     | 0.005       |
| 39   | e      | 40    | 10221.056 | 0.01391    | 0.005       |
| 40   | e      | 41    | 10219.983 | 0.01838    | 0.005       |
| 41   | e      | 42    | 10218.887 | 0.0112     | 0.005       |
| 42   | e      | 43    | 10217.771 | -0.00443   | 0.005       |
| 43   | e      | 44    | 10216.663 | -0.00029   | 0.005       |
| 44   | e      | 45    | 10215.549 | 0.00983    | 0.005       |
| 45   | e      | 46    | 10214.38  | -0.02281   | 0.005       |
| 46   | e      | 47    | 10213.266 | 0.01201    | 0.005       |
| 47   | e      | 48    | 10212.081 | -0.01143   | 0.005       |
| 48   | e      | 49    | 10210.928 | 0.01015    | 0.005       |
|      |        |       |           |            |             |
| 2    | e      | 1     | 10257.504 | 0.00463    | 0.005       |
| 3    | e      | 2     | 10258.179 | 0.00553    | 0.005       |
| 4    | e      | 3     | 10258.83  | -0.0087    | 0.005       |
| 5    | e      | 4     | 10259.511 | 0.01598    | 0.005       |
| 6    | e      | 5     | 10260.148 | 0.00556    | 0.005       |
| 7    | e      | 6     | 10260.781 | 0.00009    | 0.005       |
| 8    | e      | 7     | 10261.409 | -0.00143   | 0.005       |
| 9    | e      | 8     | 10262.037 | 0.00605    | 0.005       |
| 10   | e      | 9     | 10262.632 | -0.01046   | 0.005       |
| 11   | e      | 10    | 10263.244 | -0.00092   | 0.005       |
| 12   | e      | 11    | 10263.843 | 0.0047     | 0.005       |
| 13   | e      | 12    | 10264.423 | 0.00044    | 0.005       |

| $J'$ | Parity | $J''$ | Observed  | Obs.-Calc. | Uncertainty |
|------|--------|-------|-----------|------------|-------------|
| 14   | e      | 13    | 10264.997 | -0.00066   | 0.005       |
| 15   | e      | 14    | 10265.563 | -0.00056   | 0.005       |
| 16   | e      | 15    | 10266.116 | -0.00421   | 0.005       |
| 17   | e      | 16    | 10266.666 | -0.00156   | 0.005       |
| 18   | e      | 17    | 10267.205 | -0.00057   | 0.005       |
| 19   | e      | 18    | 10267.731 | -0.00316   | 0.005       |
| 20   | e      | 19    | 10268.254 | 0.00071    | 0.005       |
| 21   | e      | 20    | 10268.763 | 0.00011    | 0.005       |
| 22   | e      | 21    | 10269.259 | -0.00388   | 0.005       |
| 23   | e      | 22    | 10269.75  | -0.0032    | 0.005       |
| 24   | e      | 23    | 10270.23  | -0.00377   | 0.005       |
| 25   | e      | 24    | 10270.703 | -0.0015    | 0.005       |
| 26   | e      | 25    | 10271.158 | -0.00731   | 0.005       |
| 27   | e      | 26    | 10271.613 | -0.00309   | 0.005       |
| 28   | e      | 27    | 10272.056 | -0.00076   | 0.005       |
| 29   | e      | 28    | 10272.484 | -0.0032    | 0.005       |
| 30   | e      | 29    | 10272.906 | -0.0013    | 0.005       |
| 31   | e      | 30    | 10273.315 | -0.00194   | 0.005       |
| 32   | e      | 31    | 10273.709 | -0.00699   | 0.005       |
| 33   | e      | 32    | 10274.096 | -0.00832   | 0.005       |
| 34   | e      | 33    | 10274.474 | -0.00779   | 0.005       |
| 35   | e      | 34    | 10274.845 | -0.00325   | 0.005       |
| 36   | e      | 35    | 10275.197 | -0.00653   | 0.005       |
| 37   | e      | 36    | 10275.542 | -0.00547   | 0.005       |
| 38   | e      | 37    | 10275.883 | 0.00311    | 0.005       |
| 39   | e      | 38    | 10276.185 | -0.0156    | 0.005       |
| 40   | e      | 39    | 10276.501 | -0.00841   | 0.005       |
| 41   | e      | 40    | 10276.794 | -0.01211   | 0.005       |
| 42   | e      | 41    | 10277.085 | -0.00548   | 0.005       |
| 43   | e      | 42    | 10277.364 | 0.00172    | 0.005       |
| 44   | e      | 43    | 10277.616 | -0.00528   | 0.005       |
| 45   | e      | 44    | 10277.861 | -0.00621   | 0.005       |
| 46   | e      | 45    | 10278.087 | -0.01282   | 0.005       |
| 47   | e      | 46    | 10278.321 | 0.00218    | 0.005       |
| 48   | e      | 47    | 10278.501 | -0.02291   | 0.005       |
| 49   | e      | 48    | 10278.718 | 0.00322    | 0.005       |
| 50   | e      | 49    | 10278.895 | 0.00389    | 0.005       |
| 51   | e      | 50    | 10279.051 | -0.00156   | 0.005       |

| $J'$ | Parity | $J''$ | Observed  | Obs.-Calc. | Uncertainty |
|------|--------|-------|-----------|------------|-------------|
| 52   | e      | 51    | 10279.199 | 0.00023    | 0.005       |
| 53   | e      | 52    | 10279.329 | -0.00037   | 0.005       |
| 54   | e      | 53    | 10279.456 | 0.01204    | 0.005       |
| 5    | f      | 5     | 10256.037 | 0.01653    | 0.005       |
| 6    | f      | 6     | 10255.996 | 0.01725    | 0.005       |
| 7    | f      | 7     | 10255.936 | 0.00597    | 0.005       |
| 8    | f      | 8     | 10255.885 | 0.01071    | 0.005       |
| 9    | f      | 9     | 10255.817 | 0.0055     | 0.005       |
| 10   | f      | 10    | 10255.746 | 0.00437    | 0.005       |
| 11   | f      | 11    | 10255.668 | 0.00335    | 0.005       |
| 12   | f      | 12    | 10255.579 | -0.00152   | 0.005       |
| 13   | f      | 13    | 10255.484 | -0.0052    | 0.005       |
| 14   | f      | 14    | 10255.384 | -0.00664   | 0.005       |
| 15   | f      | 15    | 10255.278 | -0.00681   | 0.005       |
| 16   | f      | 16    | 10255.168 | -0.00363   | 0.005       |
| 17   | f      | 17    | 10255.049 | -0.00206   | 0.005       |
| 18   | f      | 18    | 10254.925 | 0.00196    | 0.005       |
| 19   | f      | 19    | 10254.783 | -0.00449   | 0.005       |
| 20   | f      | 20    | 10254.639 | -0.00535   | 0.005       |
| 21   | f      | 21    | 10254.493 | -0.00053   | 0.005       |
| 22   | f      | 22    | 10254.334 | -0.00096   | 0.005       |
| 23   | f      | 23    | 10254.17  | 0.00145    | 0.005       |
| 24   | f      | 24    | 10253.997 | 0.00281    | 0.005       |
| 25   | f      | 25    | 10253.814 | 0.0022     | 0.005       |
| 26   | f      | 26    | 10253.618 | -0.00326   | 0.005       |
| 27   | f      | 27    | 10253.417 | -0.00547   | 0.005       |
| 28   | f      | 28    | 10253.217 | 0.00171    | 0.005       |
| 29   | f      | 29    | 10252.991 | -0.00861   | 0.005       |
| 30   | f      | 30    | 10252.776 | 0.00072    | 0.005       |
| 31   | f      | 31    | 10252.544 | 0.00184    | 0.005       |
| 32   | f      | 32    | 10252.306 | 0.00589    | 0.005       |
| 33   | f      | 33    | 10252.059 | 0.01004    | 0.005       |
| 34   | f      | 34    | 10251.785 | -0.00354   | 0.005       |
| 35   | f      | 35    | 10251.524 | 0.00533    | 0.005       |
| 36   | f      | 36    | 10251.235 | -0.00416   | 0.005       |
| 37   | f      | 37    | 10250.951 | 0.00118    | 0.005       |
| 38   | f      | 38    | 10250.653 | 0.00256    | 0.005       |

| $J'$ | Parity | $J''$ | Observed  | Obs.-Calc. | Uncertainty |
|------|--------|-------|-----------|------------|-------------|
| 39   | f      | 39    | 10250.331 | -0.00979   | 0.005       |
| 40   | f      | 40    | 10250.031 | 0.01035    | 0.005       |
| 41   | f      | 41    | 10249.683 | -0.00678   | 0.005       |
| 42   | f      | 42    | 10249.354 | 0.00609    | 0.005       |
| 43   | f      | 43    | 10248.985 | -0.00978   | 0.005       |
| 44   | f      | 44    | 10248.632 | 0.00189    | 0.005       |
| 45   | f      | 45    | 10248.261 | 0.0074     | 0.005       |
| 47   | f      | 47    | 10247.474 | 0.01016    | 0.005       |
| 49   | f      | 49    | 10246.603 | -0.01984   | 0.005       |
| 50   | f      | 50    | 10246.179 | -0.00323   | 0.005       |
| 51   | f      | 51    | 10245.737 | 0.00929    | 0.005       |

## C.2 Line list for YbO. System 2

Table C.2: Line list for the System 2.

| $J'$ | $J''$ | Observed  | Obs.-Calc. | Uncertainty |
|------|-------|-----------|------------|-------------|
| 0    | 1     | 10942.334 | -0.00672   | 0.005       |
| 1    | 2     | 10941.638 | -0.00169   | 0.005       |
| 2    | 3     | 10940.937 | -0.00128   | 0.005       |
| 3    | 4     | 10940.234 | -0.00251   | 0.005       |
| 4    | 5     | 10939.531 | -0.00337   | 0.005       |
| 5    | 6     | 10938.832 | 0.00011    | 0.005       |
| 6    | 7     | 10938.127 | -0.00205   | 0.005       |
| 7    | 8     | 10937.426 | 0.00014    | 0.005       |
| 8    | 9     | 10936.722 | -0.00033   | 0.005       |
| 9    | 10    | 10936.017 | -0.00144   | 0.005       |
| 10   | 11    | 10935.316 | 0.00179    | 0.005       |
| 11   | 12    | 10934.611 | 0.00139    | 0.005       |
| 12   | 13    | 10933.907 | 0.00236    | 0.005       |
| 13   | 14    | 10933.202 | 0.00272    | 0.005       |
| 14   | 15    | 10932.496 | 0.00249    | 0.005       |
| 15   | 16    | 10931.793 | 0.00568    | 0.005       |
| 16   | 17    | 10931.084 | 0.00334    | 0.005       |
| 17   | 18    | 10930.377 | 0.0035     | 0.005       |
| 18   | 19    | 10929.672 | 0.00621    | 0.005       |

| $J'$ | $J''$ | Observed  | Obs.-Calc. | Uncertainty |
|------|-------|-----------|------------|-------------|
| 19   | 20    | 10928.961 | 0.00351    | 0.005       |
| 20   | 21    | 10928.254 | 0.00547    | 0.005       |
| 21   | 22    | 10927.542 | 0.00317    | 0.005       |
| 22   | 23    | 10926.83  | 0.00169    | 0.005       |
| 23   | 24    | 10926.119 | 0.00212    | 0.005       |
| 24   | 25    | 10925.406 | 0.00157    | 0.005       |
| 25   | 26    | 10924.689 | -0.00184   | 0.005       |
| 26   | 27    | 10923.976 | 0.00004    | 0.005       |
| 27   | 28    | 10923.257 | -0.00265   | 0.005       |
| 28   | 29    | 10922.538 | -0.00372   | 0.005       |
| 29   | 30    | 10921.814 | -0.00799   | 0.005       |
| 30   | 31    | 10921.092 | -0.00825   | 0.005       |
| 31   | 32    | 10920.369 | -0.00725   | 0.005       |
| 32   | 33    | 10919.64  | -0.00975   | 0.005       |
| 33   | 34    | 10918.907 | -0.01346   | 0.005       |
| 34   | 35    | 10918.175 | -0.01307   | 0.005       |
| 35   | 36    | 10917.441 | -0.01125   | 0.005       |
| 36   | 37    | 10916.699 | -0.01362   | 0.005       |
| 37   | 38    | 10915.962 | -0.00679   | 0.005       |
| 38   | 39    | 10915.209 | -0.01133   | 0.005       |
| 39   | 40    | 10914.452 | -0.01477   | 0.005       |
| 40   | 41    | 10913.696 | -0.01161   | 0.005       |
| 41   | 42    | 10912.949 | 0.00669    | 0.005       |
| 42   | 43    | 10912.173 | 0.00271    | 0.005       |
| 43   | 44    | 10911.395 | 0.00408    | 0.005       |
| 44   | 45    | 10910.592 | -0.01153   | 0.005       |
| 45   | 46    | 10909.811 | 0.00359    | 0.005       |
| 46   | 47    | 10908.987 | -0.0148    | 0.005       |
| 47   | 48    | 10908.16  | -0.02587   | 100         |
| 48   | 49    | 10907.302 | -0.05676   | 100         |
| 49   | 50    | 10906.467 | -0.05255   | 100         |
| 50   | 51    | 10905.475 | -0.19226   | 100         |
| 51   | 52    | 10904.447 | -0.35384   | 100         |
| 52   | 53    | 10903.235 | -0.68419   | 100         |
| 53   | 54    | 10901.826 | -1.19514   | 100         |
| 54   | 55    | 10899.896 | -2.20946   | 100         |
| 55   | 56    | 10896.939 | -4.23183   | 100         |
| 56   | 57    | 10892.851 | -7.36489   | 100         |

| $J'$ | $J''$ | Observed  | Obs.-Calc. | Uncertainty |
|------|-------|-----------|------------|-------------|
| 57   | 58    | 10911.557 | 12.31784   | 100         |
| 1    | 0     | 10943.728 | -0.01363   | 0.005       |
| 2    | 1     | 10944.435 | -0.00648   | 0.005       |
| 3    | 2     | 10945.131 | -0.00993   | 0.005       |
| 4    | 3     | 10945.837 | -0.00294   | 0.005       |
| 5    | 4     | 10946.535 | -0.00352   | 0.005       |
| 6    | 5     | 10947.237 | 0.00036    | 0.005       |
| 7    | 6     | 10947.933 | -0.0013    | 0.005       |
| 8    | 7     | 10948.631 | -0.00046   | 0.005       |
| 9    | 8     | 10949.328 | -0.00012   | 0.005       |
| 10   | 9     | 10950.026 | 0.00176    | 0.005       |
| 11   | 10    | 10950.723 | 0.00319    | 0.005       |
| 12   | 11    | 10951.417 | 0.00221    | 0.005       |
| 13   | 12    | 10952.111 | 0.00186    | 0.005       |
| 14   | 13    | 10952.808 | 0.00516    | 0.005       |
| 15   | 14    | 10953.5   | 0.00417    | 0.005       |
| 16   | 15    | 10954.193 | 0.00493    | 0.005       |
| 17   | 16    | 10954.885 | 0.00551    | 0.005       |
| 18   | 17    | 10955.576 | 0.00595    | 0.005       |
| 19   | 18    | 10956.266 | 0.00635    | 0.005       |
| 20   | 19    | 10956.954 | 0.00577    | 0.005       |
| 21   | 20    | 10957.641 | 0.0053     | 0.005       |
| 22   | 21    | 10958.326 | 0.00406    | 0.005       |
| 23   | 22    | 10959.01  | 0.00316    | 0.005       |
| 24   | 23    | 10959.693 | 0.00272    | 0.005       |
| 25   | 24    | 10960.375 | 0.00288    | 0.005       |
| 26   | 25    | 10961.056 | 0.0038     | 0.005       |
| 27   | 26    | 10961.733 | 0.00266    | 0.005       |
| 28   | 27    | 10962.408 | 0.00165    | 0.005       |
| 29   | 28    | 10963.078 | -0.00202   | 0.005       |
| 30   | 29    | 10963.75  | -0.00113   | 0.005       |
| 31   | 30    | 10964.418 | -0.00141   | 0.005       |
| 32   | 31    | 10965.083 | -0.0016    | 0.005       |
| 33   | 32    | 10965.744 | -0.00238   | 0.005       |
| 34   | 33    | 10966.402 | -0.00244   | 0.005       |
| 35   | 34    | 10967.058 | -0.00042   | 0.005       |
| 36   | 35    | 10967.707 | -0.00092   | 0.005       |

| $J'$ | $J''$ | Observed  | Obs.-Calc. | Uncertainty |
|------|-------|-----------|------------|-------------|
| 37   | 36    | 10968.354 | 0.00146    | 0.005       |
| 38   | 37    | 10968.997 | 0.00518    | 0.005       |
| 39   | 38    | 10969.632 | 0.00672    | 0.005       |
| 40   | 39    | 10970.262 | 0.0096     | 0.005       |
| 41   | 40    | 10970.887 | 0.01438    | 0.005       |
| 42   | 41    | 10971.503 | 0.01767    | 0.005       |
| 43   | 42    | 10972.113 | 0.0231     | 0.005       |
| 44   | 43    | 10972.707 | 0.02136    | 0.005       |
| 45   | 44    | 10973.292 | 0.02019    | 0.005       |
| 46   | 45    | 10973.86  | 0.01237    | 0.005       |
| 47   | 46    | 10974.409 | -0.00326   | 0.005       |
| 48   | 47    | 10974.932 | -0.03282   | 0.005       |
| 49   | 48    | 10975.436 | -0.06837   | 100         |
| 50   | 49    | 10975.866 | -0.16391   | 100         |
| 51   | 50    | 10976.229 | -0.31137   | 100         |
| 52   | 51    | 10976.421 | -0.61363   | 100         |
| 53   | 52    | 10976.421 | -1.09051   | 100         |
| 54   | 53    | 10975.778 | -2.19175   | 100         |
| 55   | 54    | 10974.182 | -4.22602   | 100         |
| 56   | 55    | 10971.503 | -7.32193   | 100         |

### C.3 Line list for YbO. System 3

Table C.3: Line list for the System 3.

| $J'$ | $J''$ | Observed  | Obs.-Calc. | Uncertainty |
|------|-------|-----------|------------|-------------|
| 5    | 6     | 11191.679 | -0.02778   | 0.05        |
| 6    | 7     | 11190.589 | -0.00189   | 0.005       |
| 7    | 8     | 11189.400 | -0.00449   | 0.005       |
| 8    | 9     | 11188.158 | 0.01037    | 0.005       |
| 9    | 10    | 11186.824 | 0.00367    | 0.005       |
| 11   | 12    | 11183.962 | 0.00741    | 0.005       |
| 12   | 13    | 11182.409 | -0.00721   | 0.005       |
| 13   | 14    | 11180.803 | -0.00452   | 0.005       |
| 14   | 15    | 11179.133 | 0.00445    | 0.005       |
| 15   | 16    | 11177.392 | 0.01271    | 0.005       |

| $J'$ | $J''$ | Observed  | Obs.-Calc. | Weight |
|------|-------|-----------|------------|--------|
| 16   | 17    | 11175.550 | -0.00975   | 0.005  |
| 17   | 18    | 11173.676 | 0.0061     | 0.005  |
| 18   | 19    | 11171.719 | 0.00929    | 0.005  |
| 19   | 20    | 11169.695 | 0.01588    | 0.05   |
| 20   | 21    | 11167.586 | 0.00795    | 0.005  |
| 21   | 22    | 11165.403 | -0.00339   | 0.005  |
| 22   | 23    | 11163.164 | -0.00001   | 0.005  |
| 23   | 24    | 11160.849 | -0.00174   | 0.005  |
| 24   | 25    | 11158.452 | -0.01437   | 0.005  |
| 25   | 26    | 11156.021 | 0.01034    | 0.05   |
| 26   | 27    | 11153.478 | -0.00532   | 0.005  |
| 27   | 28    | 11150.885 | 0.001      | 0.005  |
| 28   | 29    | 11148.196 | -0.01633   | 0.05   |
| 29   | 30    | 11145.447 | -0.02084   | 0.05   |
| 30   | 31    | 11142.633 | -0.01704   | 0.05   |
| 31   | 32    | 11139.755 | -0.00334   | 0.005  |
| 32   | 33    | 11136.782 | -0.0101    | 0.005  |
| 33   | 34    | 11133.749 | -0.00159   | 0.005  |
| 34   | 35    | 11130.630 | -0.00301   | 0.005  |
| 35   | 36    | 11127.433 | -0.00547   | 0.005  |
| 36   | 37    | 11124.176 | 0.01003    | 0.005  |
| 37   | 38    | 11120.819 | 0.00456    | 0.005  |
| 38   | 39    | 11117.396 | 0.01331    | 0.005  |
| 39   | 40    | 11113.888 | 0.01859    | 0.05   |
| 40   | 41    | 11110.279 | 0.0058     | 0.005  |
| 41   | 42    | 11106.614 | 0.02149    | 0.05   |
| 42   | 43    | 11102.853 | 0.02733    | 0.05   |
| 43   | 44    | 11098.961 | -0.00988   | 0.005  |
| 44   | 45    | 11094.968 | -0.05819   | 0.05   |
| 5    | 4     | 11199.311 | -0.00974   | 0.005  |
| 7    | 6     | 11199.775 | -0.01147   | 0.005  |
| 11   | 10    | 11199.874 | 0.0035     | 0.005  |
| 13   | 12    | 11199.476 | -0.01302   | 0.005  |
| 14   | 13    | 11199.193 | 0.00058    | 0.005  |
| 15   | 14    | 11198.828 | 0.00277    | 0.005  |
| 16   | 15    | 11198.393 | 0.00558    | 0.005  |
| 17   | 16    | 11197.866 | -0.01295   | 0.005  |

| $J'$ | $J''$ | Observed  | Obs.-Calc. | Weight |
|------|-------|-----------|------------|--------|
| 18   | 17    | 11197.309 | 0.00924    | 0.005  |
| 19   | 18    | 11196.660 | 0.01022    | 0.005  |
| 20   | 19    | 11195.937 | 0.0081     | 0.005  |
| 21   | 20    | 11195.136 | -0.001     | 0.005  |
| 22   | 21    | 11194.286 | 0.01208    | 0.005  |
| 23   | 22    | 11193.347 | 0.00754    | 0.005  |
| 24   | 23    | 11192.334 | 0.00059    | 0.005  |
| 25   | 24    | 11191.253 | -0.00249   | 0.005  |
| 26   | 25    | 11190.102 | -0.00339   | 0.005  |
| 27   | 26    | 11188.866 | -0.01676   | 0.05   |
| 28   | 27    | 11187.579 | -0.00818   | 0.005  |
| 29   | 28    | 11186.206 | -0.01218   | 0.005  |
| 30   | 29    | 11184.768 | -0.00723   | 0.005  |
| 31   | 30    | 11183.262 | 0.00426    | 0.005  |
| 32   | 31    | 11181.634 | -0.03103   | 0.05   |
| 33   | 32    | 11179.961 | -0.03536   | 0.05   |
| 34   | 33    | 11178.259 | 0.00809    | 0.005  |
| 35   | 34    | 11176.445 | 0.01725    | 0.05   |
| 36   | 35    | 11174.524 | -0.00189   | 0.005  |
| 37   | 36    | 11172.547 | 0.00279    | 0.005  |
| 38   | 37    | 11170.48  | -0.0015    | 0.005  |
| 39   | 38    | 11168.358 | 0.02154    | 0.05   |