

Experimental Stress State-Dependent Void Nucleation Behaviour for Two 800 MPa Advanced High Strength Steels

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Abstract: The influence of microstructure and stress state, as defined by the stress triaxiality and Lode parameter, on micro-void nucleation was evaluated experimentally for two 800 MPa Advanced High Strength Steels (AHSS), one a Complex-Phase CP800 alloy, with a ferritic-bainitic microstructure, and the other a Dual-Phase DP780 ferritic-martensitic steel. Four plane stress specimen geometries (simple shear, hole tension, v-bend and biaxial Nakazima) were adopted, providing stress triaxiality and Lode parameter values ranging from in-plane shear to biaxial tension under approximately constant stress states until failure. This approach facilitated determination of the relationship between void nucleation and macroscopic stress state. Damage histories were developed from interrupted samples using 3D micro-tomography and quantitative stereology measurement of void nucleation paired with *in situ* digital image correlation (DIC) strain measurements during the mechanical testing. The trends in damage evolution are strongly linked to the stress state, with very little void nucleation under shear deformation but extensive void damage under biaxial tension for both materials. A dependency of the nucleation rate on Lode parameter was also demonstrated. A higher rate of damage accumulation was observed for the DP780 steel compared to damage in the CP800 steel for all loading conditions highlighting the strong influence of initial microstructure. An analytical framework is proposed to obtain the local stress-state and equivalent plastic strain history from direction integration of the measured DIC strain histories, using a measured hardening law and assumed anisotropic yield function (Yld91) to develop the link between nucleation and the macroscopic stress state. A stress-state dependent nucleation model is proposed by introducing a nucleation strain surface as a function of stress-triaxiality and Lode parameter using a modified form of the strain-based Chu and Needleman nucleation criterion.

1. Introduction

Advanced high strength steels (AHSS), in particular dual-phase (DP) steels, have gained widespread popularity in automotive applications to produce lighter, thinner-gauge components while retaining high strength and good formability. New variants of DP steels rely upon a multi-phase microstructure which comprises a high-strength martensitic phase within a soft ferritic matrix to provide an excellent combination of strength and ductility [1]. However, one of the major concerns associated with DP steels is that they can be susceptible to abrupt cracking during sheared edge stretching operations such as stretch flanging [2,3]. As an alternative, ferritic-bainitic

complex phase (CP) steels have been reported to offer improved edge stretchability [4-6]. The microstructure of DP steel consists of a significant fraction of martensite that has a large strength differential with the ferrite matrix, resulting in an accelerated damage evolution in comparison to the ferritic-bainitic CP steel that has a lower strength differential between phases [7]. Consequently, this difference in microstructural properties leads to lower resistance to sheared edge cracking for the DP steel compared to the CP steel. For steel producers seeking to optimize the microstructures of AHSS alloys to improve performance in industrial forming operations, there is considerable interest in further understanding the influence of microstructure on damage evolution and subsequent failure.

The fracture mechanism of ductile materials generally involves the nucleation, growth and coalescence of microscopic voids [8]. During plastic deformation, voids nucleate and grow until they coalesce with neighboring voids to create micro-cracks [9]. Extensive work has been done to characterize damage in the DP steels [10-13]. Avramovic-Cingara *et al.* [10] conducted optical microscopy and scanning electron microscopy to quantify damage during tensile loading. X-ray tomography techniques have been used to observe damage evolution in DP steel by the 3-D reconstruction of 2-D images [11-13]. Kahziz *et al.* [14] assessed damage evolution during deformation of a DP600 sheared edge using laminography. Pathak *et al.* [7] conducted void measurements using optical microscopy and DIC strain measurement during the edge stretching of the CP800 and DP780 steels. To-date, studies on 3D quantification of damage processes within ferritic-bainitic steels have not been reported to the authors' knowledge. Moreover, the available studies on AHSS grades have mostly focused on failure mechanism under tensile stress states.

The stress-state is often defined in terms of the stress triaxiality and the Lode parameter in models of fracture. The influence of stress-triaxiality on damage evolution has been inferred experimentally and analytically [11, 15, 16]. Landron *et al.* [11] quantified the nucleation of voids for two different specimens: tensile and higher triaxiality notch specimens and observed the influence of stress state on damage evolution. To quantify the influence of stress triaxiality on ductility, Hancock and Mackenzie [17] carried out experiments on smooth and notched round bars in three different low-alloy steels and observed increasing ductility with decreasing stress triaxiality. Barsoum and Faleskog [18] observed experimentally that the rupture mechanism shifts from internal necking at high stress triaxiality to internal shear localization at low stress triaxiality.

Needleman [19] studied the effect of different loading conditions on nucleation and correlated the onset of nucleation to stress triaxiality level. Xu and Needleman [20] reported that the stress triaxiality determines whether decohesion or cracking occurs first. Recently, Yu [21] performed 3D unit cell simulation to investigate the effect of stress triaxiality and Lode angle on nucleation at the particle-matrix interface. The results reveal that both the stress triaxiality and Lode angle parameter affects the nucleation process.

There is a wide variety of models available to capture void growth and coalescence as a function of stress state and these have been successfully implemented in finite element models to simulate the ductile fracture process [9, 22, 23]. In contrast, studies on void nucleation are less common due to the complexity of the required experimental measurements and strong dependence on microstructure. Void nucleation occurs at the second-phase particles and inclusions due to the cracking or debonding from the matrix material [10, 24]. Nucleation occurs earlier for larger particles due to cracking because they contain more surface internal defects, have a large interface and often are irregularly shaped [25]. An elongated particle is more susceptible to debonding if aligned transversely to the principal loading direction and exhibits cracking if aligned in the loading direction [19]. Ultimately, whether a particle will crack or debond depends on the size, shape, distribution, strength of the particle and interface [19, 26-28]. A strong correlation between the void nucleation and the orientation of the particle cluster with respect to the first principal strain direction was reported by Thomson *et al.* [29]. Overall, void nucleation is a complex process which is difficult to predict. Moreover, the void nucleation in AHSS steels was found to be more complex than in homogeneous materials, such as aluminum or, conventional and mild steels, due to their multiphase microstructure [10, 24]. The potential nucleation sites in a multi-phase microstructure are randomly distributed within or around different phases and particles [7], [30-32]. The modeling of nucleation mechanism would require capturing deformation of each particle and phases and their subsequent cracking and debonding.

Void nucleation can be modeled using an energy criterion [25, 33], and be stress-controlled [34, 35] or strain-controlled [36]. The void nucleation based on critical stress conditions have more physical relevance, but are difficult to implement due to intricacies of the void nucleation mechanism arising from the microstructure of a material. As an alternative approach, continuum void nucleation models have been developed. Chu and Needleman [36] proposed a continuum

approach to model void nucleation and postulated that the stress or strain required to nucleate a void follows a normal distribution. The strain-controlled Chu and Needleman model has been widely used in the literature to predict void nucleation in aluminium and steels [37, 38]. Butcher *et al.* [39, 40] successfully implemented a stress-based nucleation rule to predict void nucleation in aluminum and advanced high strength steels. Despite overwhelming evidence that damage evolution is sensitive to the stress state [11, 15], the effect of stress state on void nucleation has received limited attention to-date. Landron *et al.* [11] formulated the nucleation of voids as a function of stress triaxiality by modifying the Argon [41] criterion. However, the influence of Lode parameter has not been considered in the nucleation models. It is interesting that extensive work has been done to account for the influence of stress-state on void growth and coalescence, yet the effect of stress state on nucleation rate has been largely overlooked.

The first objective of the current work is to determine the influence of loading condition (stress state) on void nucleation and develop a nucleation rule as a function of stress triaxiality and Lode parameter for two different AHSS grades: DP780 and CP800 steels. The second objective is to consider the effect of microstructure on nucleation rate and for this, two different microstructure-types, ferritic-martensitic DP780 and ferritic-bainitic CP800 steels, are considered. The stress state is varied by considering four key experiments to characterize the strain to fracture for simple shear, uniaxial tension, plane strain tension and equi-biaxial tension. An attempt was made to select experiments that minimize necking and provide a nearly constant stress state throughout the experiments; these are the hemispherical dome test, hole tension test, v-bend test and a shear test. An analytical framework is presented to experimentally estimate the local stress and strain history at the fracture location using the Swift hardening law, Yld91 [42] anisotropic yield function and measured strain components using digital image correlation (DIC). A series of interrupted tests using stereoscopic DIC was conducted to determine the local strain field and then used to correlate the equivalent strain with void measurements using 3D tomography. A specimen was extracted from the maximum deformed region of each interrupted sample and an *ex-situ* 3D tomography was conducted on each specimen to quantify voids at each level of deformation and for the different proportional loading conditions. The experimental investigation of the influence of stress state on void nucleation was used to develop an experimental stress state dependent nucleation rule for each material. A modified strain-controlled Chu and Needleman [36] nucleation criterion

is proposed to account for the stress states by introducing a nucleation strain surface as a function of stress triaxiality and Lode parameter.

2. Experiment

2.1. Material Characterization

The mechanical properties of the two materials investigated herein, CP800 and DP780 steels, have been characterized by the authors in previous work [6]. The relevant mechanical properties of the CP and DP steels such as yield strength (YS), ultimate tensile strength (UTS), percentage total elongation ($\% TE$), strain hardening exponent (n) and Lankford coefficients (r) are listed in Table 1. The UTS reported for the TD is the highest for both materials; thus, the experiments in the current work were oriented to ensure the maximum principal stress directions were aligned with the TD.

Table 1: Mechanical properties of the CP and DP steels in the rolling direction (RD), transverse direction (TD) and diagonal direction (DD). The value in the brackets is the standard deviation after three tests [6].

Material	Thickness (mm)	Direction	YS (MPa)	UTS (MPa)	TE (%)	n (5-UE%)	r
CP800	2.90	RD	710 (6)	810 (3)	19.6 (1.7)	0.08 (0.00)	0.70 (0.04)
		TD	788 (5)	850 (5)	18.8 (1.0)	0.06 (0.00)	0.95 (0.04)
		DD	726 (8)	800 (5)	20.5 (2.0)	0.07 (0.00)	1.33 (0.03)
DP780	1.56	RD	509 (8)	800 (6)	22.8 (2.2)	0.16 (0.00)	0.72 (0.02)
		TD	522 (4)	806 (5)	21.6 (1.8)	0.15 (0.00)	0.92 (0.03)
		DD	533 (6)	815 (8)	25.5 (1.8)	0.15 (0.00)	0.98 (0.01)

2.2. Biaxial Stress State Experiments

A stress state corresponding to biaxial tension was obtained by conducting a Nakazima hemispherical dome test [43]. The experiment set up consists of a die, a blank holder and a punch of diameter 101.6 mm, with a die-entry radius of 6.35 mm. The biaxial specimen consisted of a 200 mm by 200 mm sheet blank that was clamped prior to punch movement using a blank holder force of 650 kN. A punch speed of 0.25 mm/s was used to achieve a quasi-static strain rate. The test and tooling conforms to ISO12004-2, aside from using the lower punch speed of 0.25 mm/s which is less than the lower limit in the standard of 0.5 mm/s. The punch force and displacement was recorded during testing while stereo DIC was used to measure the strain field using a camera

frame rate of 6 images per second. The DIC software was provided by Correlated Solutions Inc. and the incremental correlation option was activated to account for severe local strains. For post-processing of the captured images, the logarithmic strain was computed using DIC step and filter sizes of 3 and 6 pixels, respectively and a resolution of 0.03 mm/pixel. In order to quantify the effects of step size and the strain filter size in the DIC analysis, the Virtual Strain Gauge Length (VSGL) was calculated using following equation.

$$\text{VSGL} = \text{Resolution of the area of interest} \times \text{Step size} \times \text{Filter size} \quad (1)$$

The VSGL is not directly used within the DIC software algorithm to calculate the strains, but is considered to be a metric to report the DIC analysis settings used in the experiments. A VSGL of 0.5 mm was obtained using the current DIC setting.

2.3. Hole Tension Experiment

Ebnoether and Mohr (2013) [44] demonstrated that stress triaxiality in a conventional tensile specimen can vary from 0.33 at onset of necking to 0.8 prior to failure. Bao *et al.* [45] reported that a tensile specimen with a central hole located at its center exhibits approximately uniaxial tension at the intersection of the hole and the transverse symmetry plane (the normal location of failure onset) since deformation of a free edge is one of uniaxial tension. Given this desirable near-constant triaxiality, this test was used in the present work to acquire failure strains corresponding to a uniaxial tension stress state. A tensile specimen with a gauge length of 35 mm was fabricated with a central hole of diameter 10 mm, as shown in Figure 1. The width of the ligament on either side of the hole was selected to be four times larger than the sheet thickness for the two materials investigated. The holes were processed by first drilling a pilot hole of 9.5 mm diameter, followed by reaming to a diameter of 10 mm and lightly polishing with 300 grit SiC paper to remove any surface roughness or drill-burr at the edge. The specimen was subjected to tension in a 100 kN servo-hydraulic Instron testing apparatus at a cross-head displacement of 0.075 mm/s and strain rate corresponding to 0.003 s⁻¹. The full-field strain was recorded during the experiment using stereo DIC at an acquisition rate of 4 images per second. The DIC images were analyzed using a resolution of 0.02 mm/pixel, a step size and filter size of 3 and 9 pixels, respectively, to obtain VSGL of 0.5 mm.

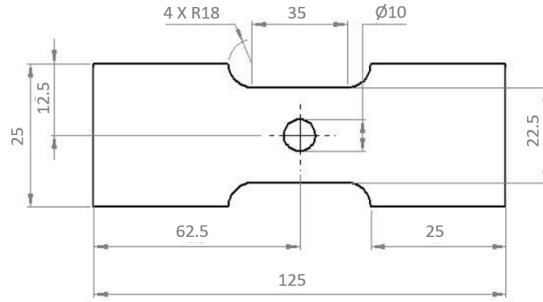


Figure 1: Specimen geometry used for the DP780 hole tension test. All units are in mm

2.4. V- Bend Experiment

The fracture strain in plane strain tension was characterized by conducting tight radius bending (v-bend) tests, illustrated in Figure 2. The mechanical arrangement was developed by Cheong *et al.* [46] and was designed to be compatible with stereographic DIC imaging by keeping the punch stationary and forcing the rollers to move downwards to perform the bending. The rollers are chamfered to provide a 65° viewing angle thereby enabling full field DIC of the tensile side of the bend specimen during the entire test. In addition, the bend region remains stationary on the fixed punch and hence enables higher DIC resolution. The 30 mm X 30 mm DP780 specimens and 58 mm X 58 mm CP800 specimens were electric discharge machined (EDM) instead of shearing to avoid edge cracking. A punch with 0.4 mm radius of curvature was used and the 30 mm diameter rollers moved downwards at 20 mm/minute. The rollers were spaced such that the gap between the cylindrical surfaces of the rollers was 2.5 times the thickness of material, in accordance with the VDA 238-100 specification [47]. The post processing of the DIC images was performed at a subset size of 37, a step size of 5 pixels, a strain filter size of 10 pixels and a resolution of 0.01 mm/pixel that corresponds to an approximate virtual strain gauge length of 0.5 mm.

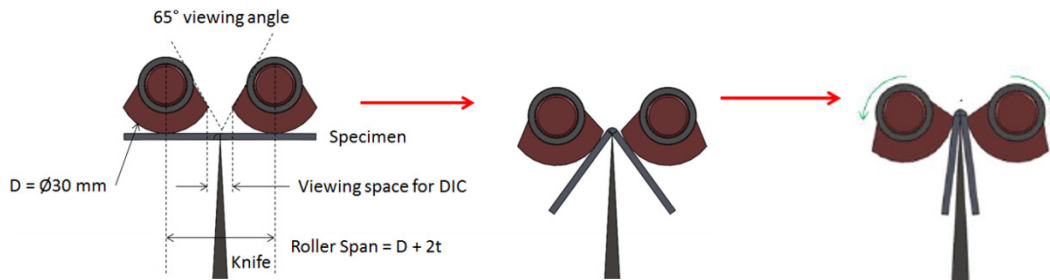


Figure 2: Concept of Cheong *et al.* [46] for the tight radius v-bend process with DIC strain measurement

μA with a Cu filter to obtain a voxel size of $1\ \mu\text{m}$. Reconstructed volumes were first median filtered with a radius of two voxels to reduce the noise associated with the scan acquisition. The volumes were thresholded to differentiate the void phase from the steel phase. The edge surface was detected using an ImageJ plugin [51] based on a Sobel edge detector that highlights sharp changes in intensity in 3D binarized volumes. The 3D visualization was done using the ImageJ 3D volume viewer. In the 3D views of the reconstructed slices presented herein, voids appear in red and the material bulk in white. A similar void measurement technique was used by Landron *et al.* [52]. A set of pixels has to be statistically significant in three dimensions to be registered as a void; therefore, a void is included in the analysis only when the diameter of the void exceeds twice the voxel size i.e. $2.0\ \mu\text{m}$. The void quantification was conducted using ImageJ to provide measurements of individual voids within a specimen.

3. Locally Proportional Loading Histories

A key aspect of the ductile fracture experiments was to obtain proportional loading; *i.e.* a constant strain path and stress state during deformation up to the point of fracture initiation. This section examines the strain paths achieved during testing and also introduces a technique to extract the stress state histories through direct integration of the constitutive laws using only the measured DIC strains at the points of interest.

3.1. Experimental Strain Paths

The equivalent strain, ε_{eq} , in the DIC software was calculated based on von Mises plasticity theory and plastic volume conservation by integrating Eq. (2),

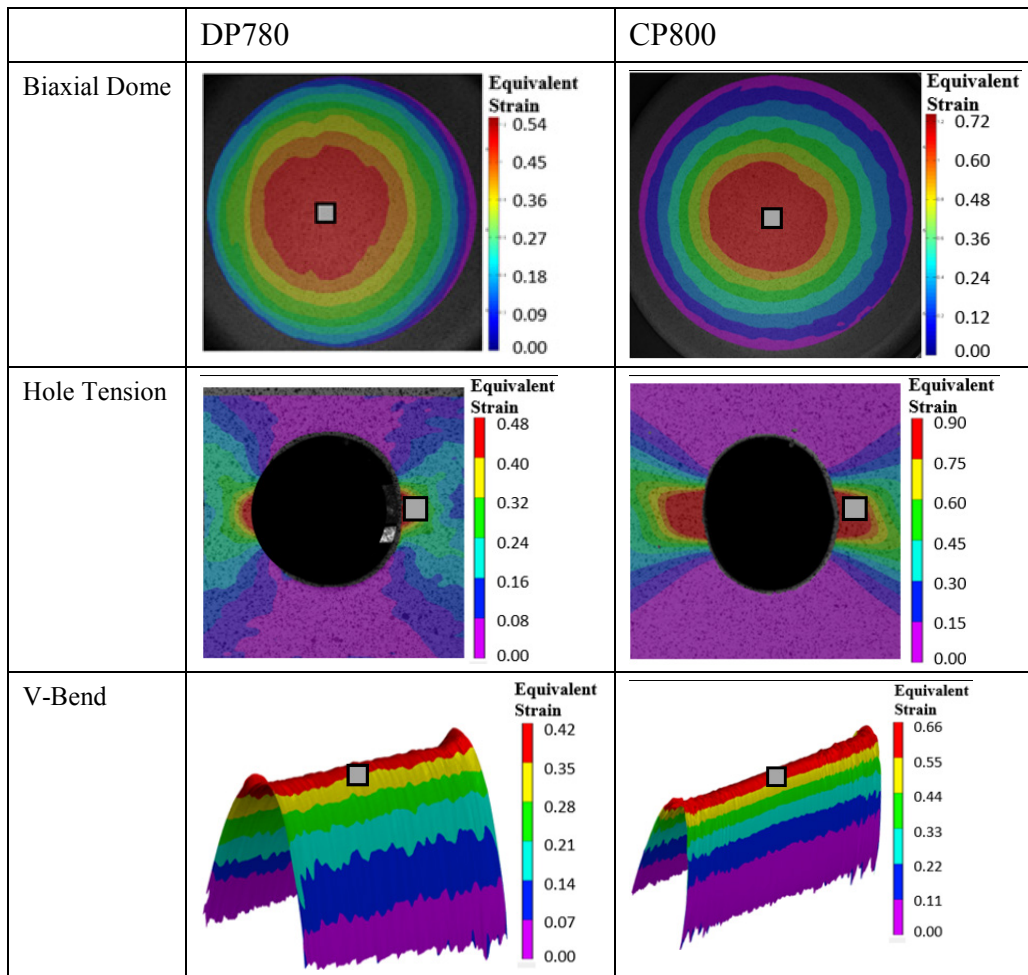
$$d\varepsilon_{eq} = \frac{2}{\sqrt{3}} \sqrt{(d\varepsilon_1^2 + d\varepsilon_2^2 + d\varepsilon_1 d\varepsilon_2)} \quad (2)$$

Jonas *et al.* [53] and Shrivastava *et al.* [54] stated that for simple shear, the rotation of principal strain with respect to the principal stresses must be accounted for. Butcher and Abedini [55] derived the von-Mises work-conjugate equivalent plastic strain for finite shear of a plastically deforming material that accounts for misalignment of the principal frames as a function of the major strain, as

$$\varepsilon_{eq} = \frac{2}{\sqrt{3}} \sinh \varepsilon_1 \quad (3)$$

where ε_1 is a major strain For simple shear conditions, the finite strain calculation shown in Eq. (3) is used to determine the equivalent strain and for the rest of stress states, Eq. (2) is used.

Figure 4 shows the measured contours of equivalent strain for the different test specimens: biaxial dome, v-bend, hole tension and shear for the CP800 and DP780 steels just prior to failure. The tomography specimens were extracted from the maximum deformation region with the location highlighted in Figure 4 for each specimen using a grey colored square.



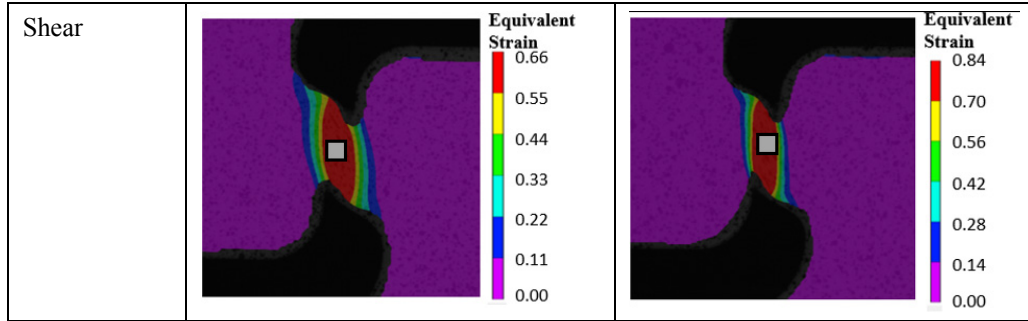


Figure 4: Measured contours of equivalent strain during the biaxial dome, hole tension, v-bend and shear tests for the (a) CP800 and (b) DP780 steels prior to failure. The location of tomography specimen is highlighted using a square for each specimen.

Figure 5 shows the strain-path for each test geometry extracted from the region of maximum deformation, corresponding to the 0.5 mm regions indicated in Figure 4, for both materials. The DIC strains were averaged over the square of size 0.50 mm to match the size of the tomography specimens to provide an appropriate macroscopic strain to correlate with void nucleation. The dashed lines plotted in Figure 5 indicate the theoretical strain paths for an isotropic material with principal strain ratios (slopes) of -1, -0.5, 0 and 1 corresponding to shear, uniaxial tension, plane-strain and equal-biaxial tension, respectively. During the shear and v-bend testing, the principal strain path followed is linear and proportional throughout the deformation. The strain path followed during the dome test is biaxial until close to failure at which point the path transitions towards plane-strain. Similarly the principal strain ratio during the hole tension test is uniaxial throughout the deformation for the DP780 and deviates to plane-strain for the CP800 steel due to necking or strain localization. Roth and Mohr [56] reported that altering the hole tension specimen geometry (i.e. decreasing hole size) can shift the onset of localization to higher strain, thus, further delay in the onset of necking may have been possible in the CP800 experiments by modifying the hole tension specimen geometry. Such modifications were not considered in the current research since the onset of necking is already considerably delayed relative to that seen in a uniaxial tensile specimen.

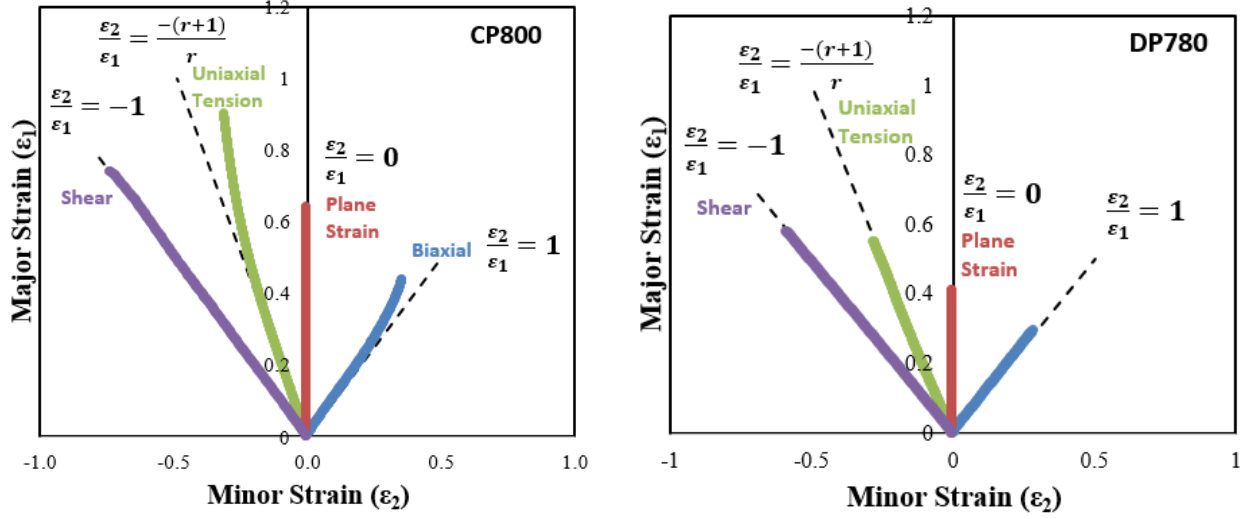


Figure 5: Major and minor strains paths in the region of maximum deformation subjected to different loading conditions for the (a) CP800 and (b) DP780 steels

3.2. Stress Integration using DIC-Based Measured Strains

In this section, an analytical approach is presented to calculate local stress using (a) DIC strain measurements, (b) a suitable yield function and (c) an appropriate hardening law. A brief description of the material model is presented, followed by the algorithm to integrate the stress components from the strain measurements.

3.2.1. Material Model

In 1991, Barlat [42] proposed a 3D yield function (called Yld91) which can provide a good representation of the variation in the yield stress and r -values for steel and aluminum alloys. More advanced yield criteria such as Yld2004 are available, but require more extensive experimental characterization to calibrate the yield function. Consequently, the Yld91 criterion was adopted to model anisotropy of the CP800 and DP780 steels and can be expressed as

$$\sigma = \left(0.5(|S_1 - S_2|^m + |S_2 - S_3|^m + |S_3 - S_1|^m)\right)^{1/m} \quad (4a)$$

where m is chosen based on the crystallographic structure. S_1 , S_2 and S_3 are eigenvalues of the symmetric transformed stress tensor \mathbf{S}

$$\mathbf{S} = \begin{bmatrix} S_{11} & S_{12} & S_{13} \\ S_{12} & S_{22} & S_{23} \\ S_{13} & S_{23} & S_{33} \end{bmatrix} \quad (4b)$$

where

$$S_{11} = \frac{c(\sigma_{xx} - \sigma_{yy}) - b(\sigma_{zz} - \sigma_{xx})}{3} \quad (4c)$$

$$S_{22} = \frac{a(\sigma_{yy} - \sigma_{zz}) - c(\sigma_{xx} - \sigma_{yy})}{3} \quad (4d)$$

$$S_{33} = \frac{b(\sigma_{zz} - \sigma_{xx}) - a(\sigma_{yy} - \sigma_{zz})}{3} \quad (4e)$$

$$S_{12} = h\sigma_{xy} \quad (4f)$$

$$S_{23} = g\sigma_{xz} \quad (4g)$$

$$S_{31} = f\sigma_{yz} \quad (4h)$$

and a , b , c , h , g , f are calibration parameters. In the current work, an equivalent plastic work methodology was adopted to calibrate the Yld91 function for both steels. The plastic work, w^p , was calculated from the tensile test along the rolling, transverse and diagonal directions and the shear test using the following equation.

$$dw^p = \sigma_1 d\varepsilon_1^p + \sigma_2 d\varepsilon_2^p + \sigma_3 d\varepsilon_3^p = \sigma_{eq} d\varepsilon_{eq}^p \quad (5a)$$

$$w^p = \int dw^p \quad (5b)$$

For a given plastic work level, the stress anisotropy is determined as a ratio of the stress in a particular material orientation divided by the corresponding tensile stress along the rolling direction at the same plastic work. . These “stress ratios” are plotted in Figure 6 and the values corresponding to the plastic work at UTS in the rolling direction (55.2 MPa) are listed in Table 2 for the CP800 and DP780 steels. The r -values used in the calibration of yield function are listed in Table 1.

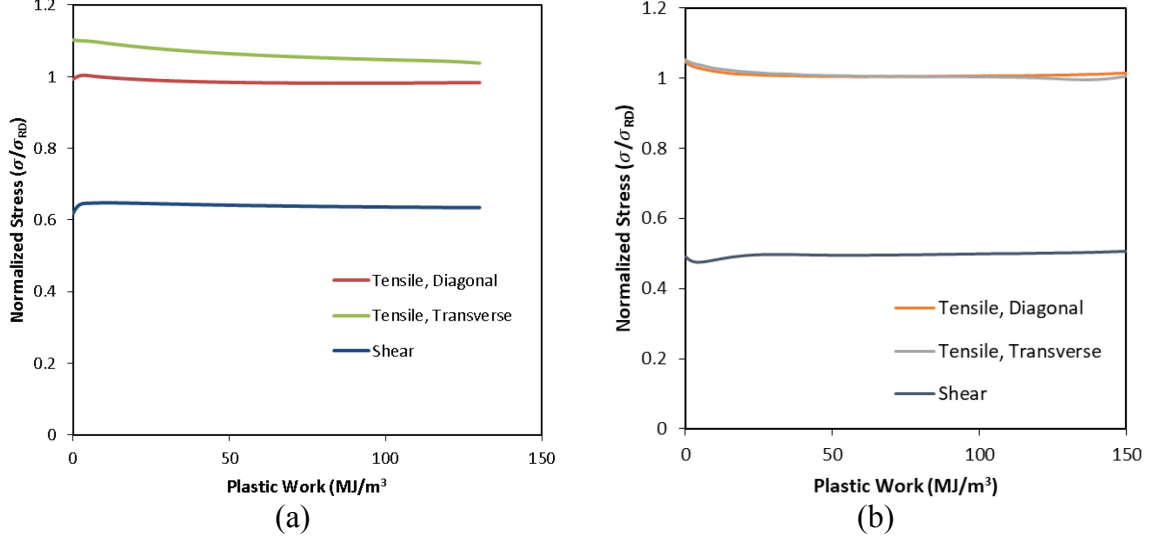


Figure 6: Stress ratios with respect to rolling direction for (a) CP800 and (b) DP780 materials.

Table 2: Stress-ratios at a plastic work of 55.2 MPa for the tension test along the diagonal and transverse directions and shear test for the CP800 and DP780 steels

Material	σ_D/σ_R	σ_T/σ_R	τ/σ_R
CP800	0.98	1.08	0.63
DP780	1.00	1.00	0.50

The Yld91 parameters (plane stress assumption) were determined using an optimization approach in which a least squares error minimization was performed to reduce error between the experimental data and the values predicted by the yield function. In the present study, the genetic algorithm, which is a global optimization subroutine available in Matlab, was selected to perform minimization for the following “Error” function:

$$Error = w_\sigma \sum_{i=1}^t \left(\left(\frac{\sigma_{model}}{\sigma_{exp}} \right)_i - 1 \right)^2 + w_r \sum_{i=1}^t \left(\left(\frac{r_{model}}{r_{exp}} \right)_i - 1 \right)^2 \quad (6)$$

The superscripts “exp” and “model” in Eq. (6) represents measured values and predicted values from the yield function, respectively. w_σ and w_r are weights applied to values of stress and r -value, respectively, and t is the number of available experimental data points. A shear constraint, introduced by Abedini [57], was also implemented to enforce normality in the shear regions of anisotropic yield function. For both materials, an exponent of $m = 6$ was used for the anisotropic model, as recommended for bcc materials [42], and the resulting coefficients for the yield function are listed in Table 3.

Table 3: The parameters of Yld91 yield function for the CP800 and DP780 steels

Material	a	b	c	h	g	f
CP800	-0.81	0.85	0.12	1.00	1.00	-1.04
DP780	-1.00	0.60	0.47	1.00	1.00	0.99

The hardening behavior of the CP800 and DP780 materials was defined using the Swift law,

$$\sigma = K(\varepsilon_0 + \varepsilon^p)^n \quad (7)$$

where ε_0 is the initial strain, ε^p is the plastic strain, and K and n are the material parameters that describe the rate of hardening. In conventional practice, Eq. (7) is fit to the true stress versus effective plastic strain response determined from uniaxial tensile samples; however the range of available hardening data prior to onset of necking is relatively low, as can be seen in Figure 7. Instead, the calculated stress-ratios from the shear test, τ/σ_R (Table 2), was applied to extend the hardening curve using data from the shear experiments following the methodology described by Rahman *et al.* [50]. Figure 7 shows the resulting hardening response as well as the Swift law fits (Table 4) which capture the measured data rather well.

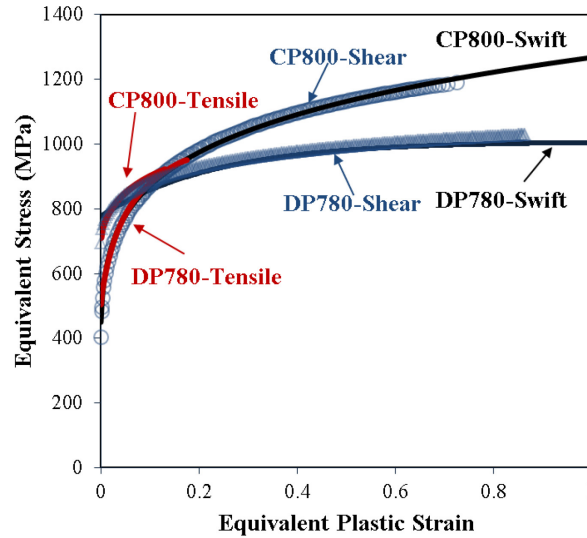


Figure 7: Comparison between experimental true stress versus true plastic strain obtained from the tensile (RD) and shear tests for the CP800 and DP780 steels and the best fit curve based on Swift's hardening law

Table 4: Swift's hardening law parameters for the CP800 and DP780 steels

Material	K	ε_0	n	R^2
CP800	1024	0.0067	0.07	0.99
DP780	1267	0.0018	0.16	0.98

3.2.2. Algorithm for Stress Integration from Measured Strains

The principal strains $(\varepsilon_1, \varepsilon_2)$ under proportional loading can be expressed as, $(\varepsilon_1, \beta\varepsilon_1)$, where β is a variable in the range $[-1, 1]$ that represents ratio of the plastic strain increments in the two principal directions. The stress ratio, α , is defined as the ratio of minor principal stress, σ_2 , to major principal stress, σ_1 . The strain ratios corresponding to stress ratios in the range $\alpha = [-2, 2]$ are determined using the Yld 91 yield function (Eq. 4). For proportional loading, β is a constant that is defined by the normal to the yield surface at a particular stress ratio, α . To save computational time during the stress integration period, values of the stress ratios (α and $\gamma = \frac{\sigma_1}{\sigma}$) in the range $\alpha = [-2, 2]$ are tabulated along with the corresponding strain ratio determined using derivatives of the yield function. This range is selected to cover the stress states ranging from shear to biaxial tension to determine the typical stress ratios corresponding to strain paths in forming operations.

The plastic work increment is defined as, $dw^p = \sigma d\varepsilon^p$, where $d\varepsilon^p$ is the plastic strain increment

$$dw^p = \sigma d\varepsilon^p = \sigma_1 d\varepsilon_1 + \sigma_2 d\varepsilon_2 = (1 + \alpha\beta)\sigma_1 d\varepsilon_1 \quad (8a)$$

$$\text{or} \quad d\varepsilon^p = (1 + \alpha\beta) \frac{\sigma_1}{\sigma} d\varepsilon_1 = (1 + \alpha\beta)\gamma d\varepsilon_1, \text{ where } \gamma = \frac{\sigma_1}{\sigma} \quad (8b)$$

The ε^p can be calculated by summing plastic strain increments. Using the hardening law, the equivalent stress, σ , corresponding to ε^p can be determined.

The framework to determine stress-components from the major and minor strains is summarized as:

- i. Tabulate the values of $\beta = f(\alpha)$ and $\gamma = f(\alpha)$ using Yld91.
- ii. The strain ratio β_i is calculated at each experimental data point, i .
- iii. The stress ratios γ_i and α_i corresponding to β_i are determined from the database.
- iv. The equivalent plastic strain is calculated at each increment using Eq. (8b).
- v. The hardening law is updated to obtain the anisotropic equivalent stress, σ .
- vi. Major and minor stresses are calculated using γ_i, α_i i.e. $\sigma_1 = \gamma\sigma$ and $\sigma_2 = \alpha\sigma_1$.

3.3. Calculated Stress Triaxiality and Lode parameter

In this section, the evolution of equivalent plastic strain as a function of the stress triaxiality and the Lode parameter during the experiments is determined for plane stress conditions. To determine the stress states during deformation, the stress triaxiality and Lode parameter are determined using following equations

$$T = \frac{\sigma_m}{\sigma_{eq}} \quad (9)$$

$$L = -\frac{27}{2} \frac{(\sigma_1 - \sigma_m)(\sigma_2 - \sigma_m)(\sigma_3 - \sigma_m)}{\sigma_{eq}^3} \quad (10)$$

where $\sigma_m = \frac{\sigma_1 + \sigma_2 + \sigma_3}{3}$ is the mean stress and σ_{eq} is the von Mises effective stress. Figures 8 and 9 show the equivalent strain as a function of stress triaxiality and Lode angle parameter, respectively, for the CP800 and DP780 samples during the biaxial dome, hole tension, v-bend and simple shear experiments. The average stress triaxiality and Lode parameter reported for both materials is indicated in Table 5 for all four loading conditions. It is important to state that for plane stress states, as assumed here in the analytical integration, the stress triaxiality and Lode parameter are not independent. As shown by Bai and Wierzbicki [58], only the triaxiality or the Lode parameter is sufficient to define the plane stress state.

Table 5: Average stress triaxiality (T) and Lode parameter (L) determined for biaxial tension, plane strain, uniaxial tension and simple shear deformation of the CP800 and DP780 steels

Material	Biaxial Tension		Plane Strain		Uniaxial Tension		Shear	
	T	L	T	L	T	L	T	L
CP800	0.66	0.97	0.55	-0.01	0.30	-0.92	0.00	0.01
DP780	0.66	0.98	0.55	0.01	0.30	-0.98	0.00	0.02

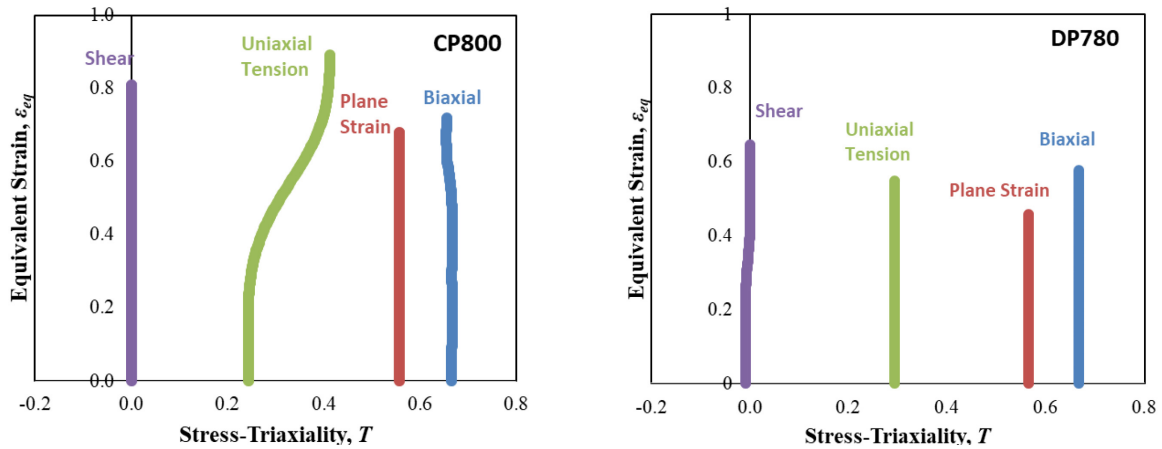


Figure 8: Stress triaxiality history for biaxial tension, plane strain, uniaxial tension and shear deformation of the CP800 and DP780 steels

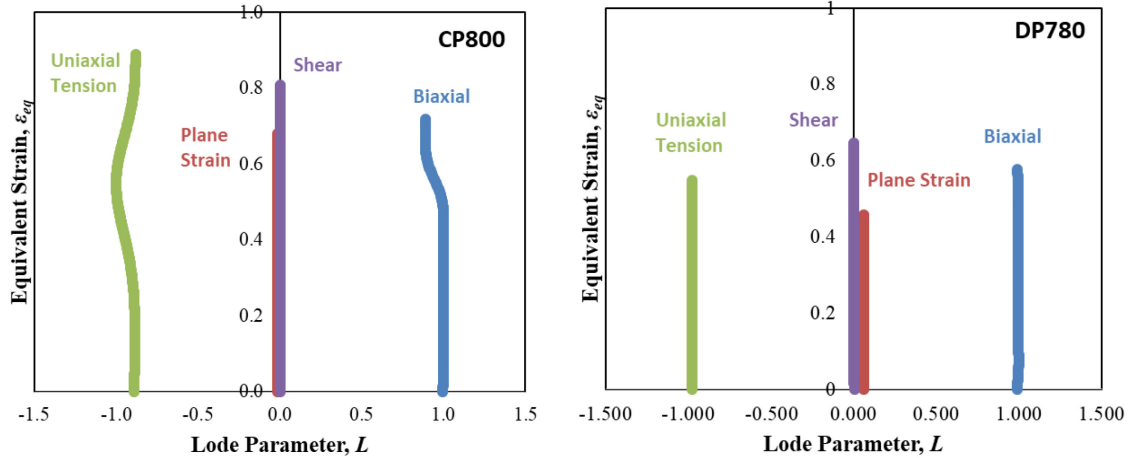


Figure 9: Lode parameter history for biaxial tension, plane strain, uniaxial tension and shear deformation of the CP800 and DP780 steels

4. Damage Evolution under Proportional Loading

To systematically characterize damage accumulation, interrupted testing was conducted at four levels of displacement for the four different stress states: biaxial tension, uniaxial tension, plane-strain and simple shear. The four displacement levels were selected such that each specimen was deformed to approximately 50%, 70%, 85% and 95% of the failure strain. Figure 10 shows the load displacement response for the biaxial samples tested to failure as well as the interrupted samples that exhibit good repeatability up to the final strain level considered in each experiment. The repeatability was similar for the other geometries (not shown for brevity).

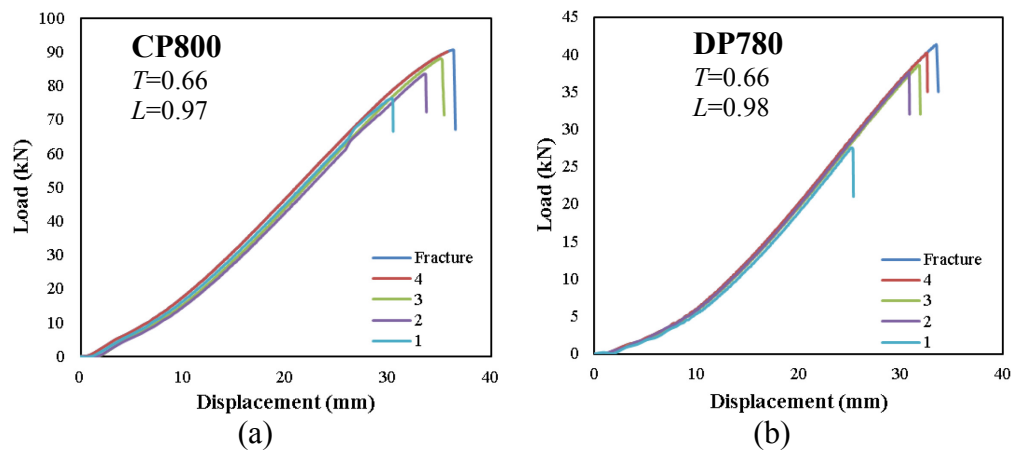


Figure 10: Histories of load versus displacement strain for the (a) CP800 and (b) DP780 biaxial specimens interrupted at different strain levels

3D tomography was performed on the interrupted specimens to quantify the number of voids nucleated at the different stages of deformation and loading conditions. The effect of stress state on void nucleation is discussed for the two materials, CP800 and DP780 steel, by comparing the number of voids nucleated (N) as a function of equivalent plastic strain (ϵ) for each loading condition.

The tomograms of the undeformed CP800 and DP780 steels are shown in Figure 11 and the number of cavities per unit volume (N) measured for each specimen is specified.

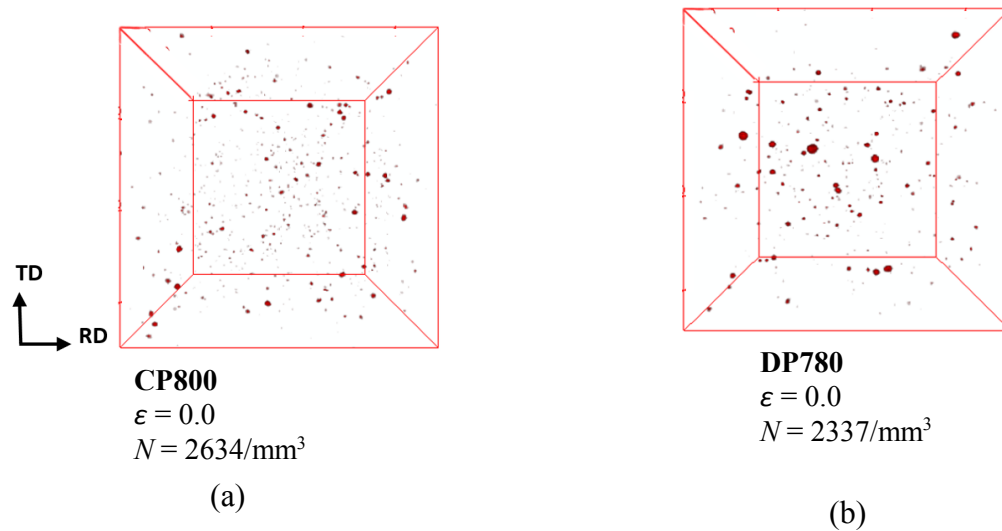


Figure 11: 3D views of damage within the undeformed (a) CP800 and (b) DP780 specimens

4.1. Tomography

The tomographs acquired from the biaxial loaded samples interrupted at a Mises effective strain of 0.95% of the failure strain are shown in Figure 12. The two biaxial loading directions corresponds to the rolling and transverse directions (RD and TD) and the tomographs are projected such that the plane of the figure corresponds to the sheet RD and through-thickness (TT) directions. The DP800 sample exhibits significant numbers of regions of local void coalescence that represents precursors to formation of macro-cracks. The DP780 sample exhibits extensive coalescence along the sheet mid-plane which corresponds to martensitic bands in the as-received sheet [7]. The number of cavities per unit volume (N) measured for each specimen is also indicated in Figure 12.

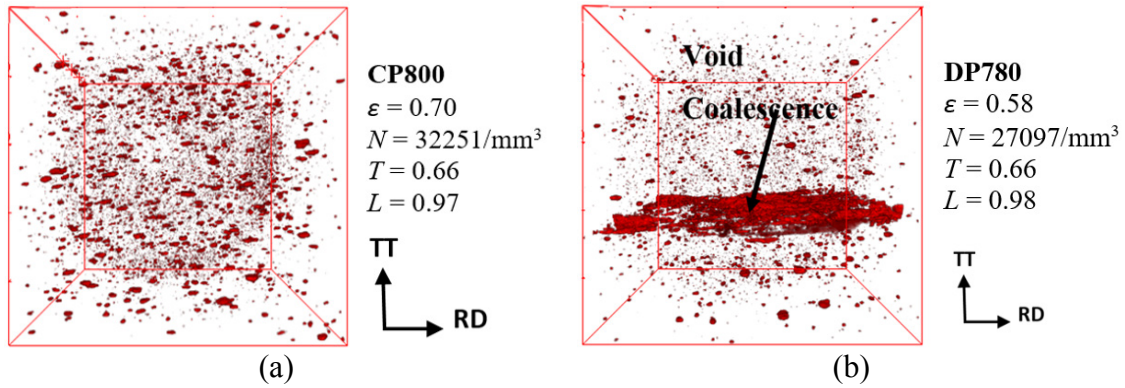


Figure 12: 3D views of damage within the specimen deformed under biaxial tension loading near failure. The horizontal axis in the figure corresponds to the sheet RD while the vertical axis is the through-thickness (TT) direction.

Void coalescence is the final stage of ductile failure and occurs through the localization of the ligament between neighboring voids. Coalescence is generally favoured along the ligament perpendicular to the loading direction and is difficult along ligaments which are not perpendicular to the loading direction [59]. Horstemeyer and Gokhale [60] demonstrated experimentally that under biaxial deformation the coalescence path is activated in two directions because the specimen is subjected to loading in the two directions and consequently the crack propagates along both directions. The plan-view projection of the coalescence plane indicated in Figure 12 is shown in Figure 13 and illustrates crack formation through coalescence of voids in the DP780 specimen deformed close to the failure strain. Since the DP780 specimen is deformed under a biaxial stress state, the void growth and subsequent coalescence occur in the two directions and consequently crack propagates along the two loading directions. This behavior could not be captured in the CP800 specimen because the experiment was terminated before the initiation of coalescence.

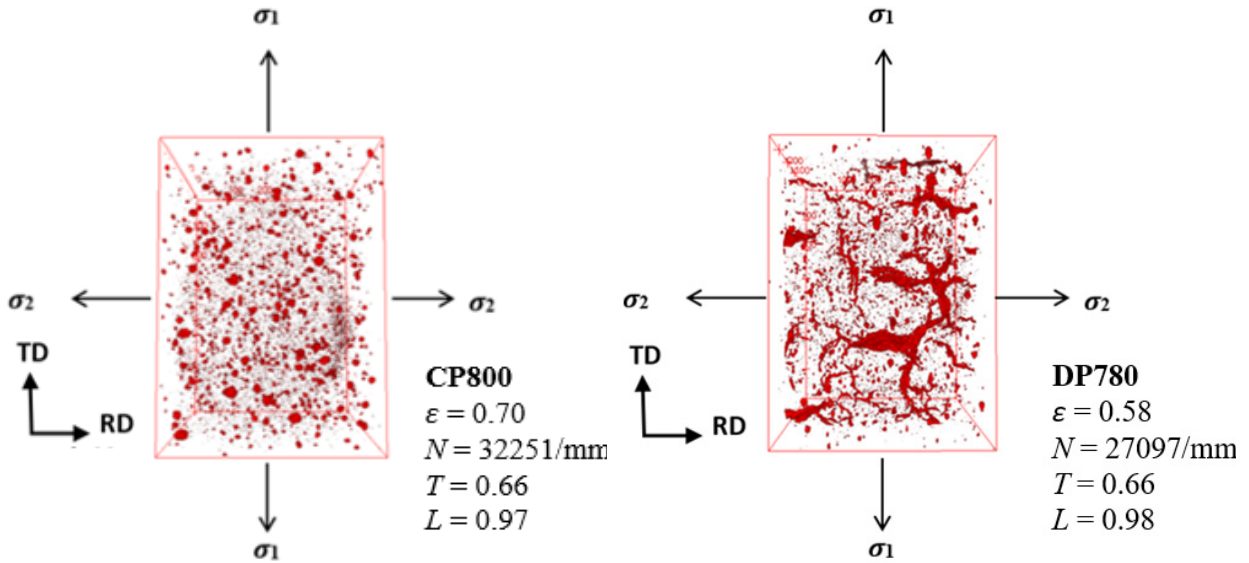


Figure 13: 3D views of damage within the CP800 and DP780 specimens deformed under biaxial tension loading near failure. The horizontal axis in the figure corresponds to the sheet RD while the vertical axis is the transverse direction (TD).

The hole tension specimens were loaded along the TD. The deformation of the reamed hole tension specimens follows uniaxial tension and the tomographs were acquired on the CP800 and DP780 reamed edges interrupted prior to fracture. Tomographs from the most deformed CP800 and DP780 specimens are shown in Figure 14.

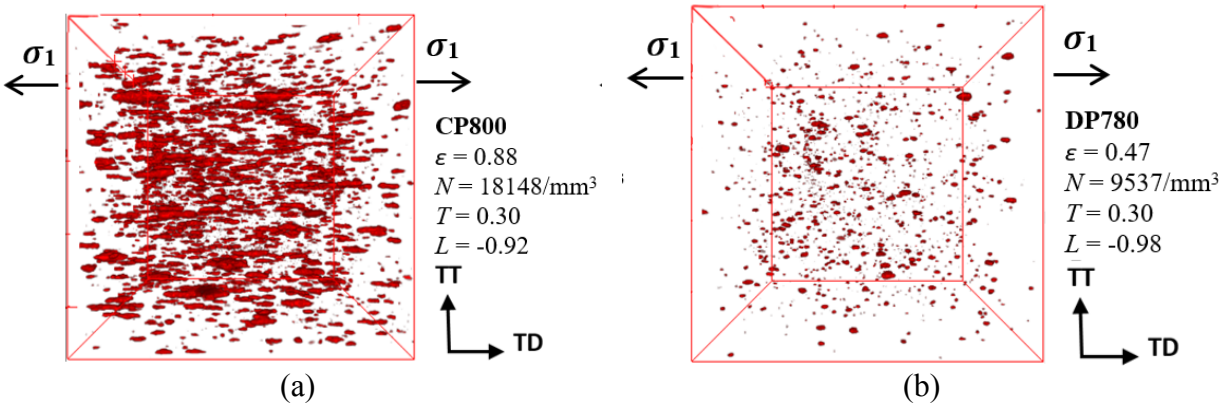


Figure 14: 3D views of damage within the (a) CP800 and (b) DP780 hole tension specimens deformed near failure. The horizontal axis in the figure corresponds to the sheet TD while the vertical axis is the through-thickness (TT) direction.

The comparison of the CP800 and DP780 tomographs deformed near failure (Figure 14) suggests that the amount of damage developed near the failure strain is significantly higher in the

CP800 specimen compared to the DP780 specimen. This difference in the damage evolution is attributed to the difference in microstructure of the two steels. The ferritic-bainitic CP800 microstructure can sustain deformation up to a larger strain due to lower strength-differential between the phases and exhibits more damage accumulation near the failure strain compared to the DP780 steel.

In contrast with the biaxial loading which exhibits void growth along the two loading directions, void growth is only significant in one direction under uniaxial tension, especially for the CP800 hole tension specimen. A similar trend was observed by Landron *et al.* [12] and Weck *et al.* [61] using 3D tomography. As to be expected, in biaxial tension the voids will elongate in two directions that was also shown in the unit cell models of by Potirniche *et al.* [62]

Figure 15 shows the damage during the deformation under plane-strain in the CP800 and DP780 plane strain v-bend specimens deformed to strains near failure. The void growth is not significant under plane-strain deformation. Pardoen and Brechet [63] reported two distinct coalescence mechanisms (1) internal necking of ligaments between voids that have enlarged their sizes significantly and (2) internal shear localization involving limited void growth. Ductility typically is less for plane strain specimens because a plane strain specimen is more susceptible to plastic shear localization due to the kinematic constraints [64]. A cluster of voids is however observed in the vicinity of a crack (shown in Figure 15) presumably due to the enhanced stress triaxiality. Subsequent growth of the crack tip occurs by interaction of multiple voids along the crack front and leads to propagation of the crack.

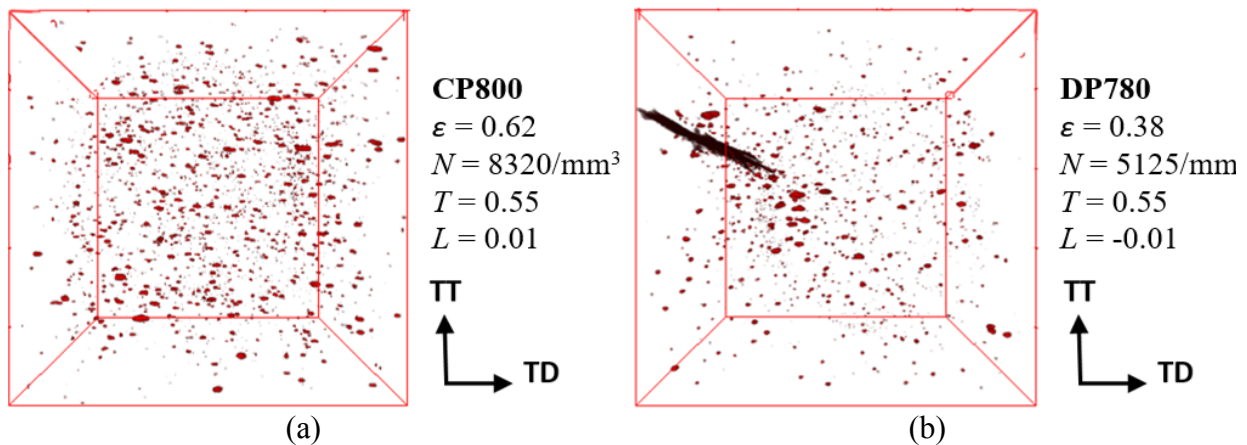


Figure 15: 3D views of damage within the (a) CP800 and (b) DP780 specimens deformed under plane-strain loading at various steps of deformation. The horizontal axis in the figure corresponds to the sheet TD while the vertical axis is the through-thickness (TT) direction.

For the shear specimens, the maximum deformation occurs at the center of the specimen due to rotation of the shear band as indicated in the contour plots of the CP800 and DP780 steels (Figure 4). The tomography specimen of cross-section 0.5 mm X 0.5 mm was therefore extracted from the center of the shear band of each interrupted specimen. The shear tests were performed with the applied load in the diagonal direction of the sheet which results in principal stresses in the rolling and transverse directions (RD and TD). Tomographs of the CP800 and DP780 shear specimens deformed to near failure are shown in Figure 16. The extent of void nucleation increases with the equivalent strain for both the materials. Void growth however is not significant during the shear loading of the CP800 and DP780 steels which is to be expected since due to absence of a hydrostatic stress to expand the void volume [22], [59], [65].

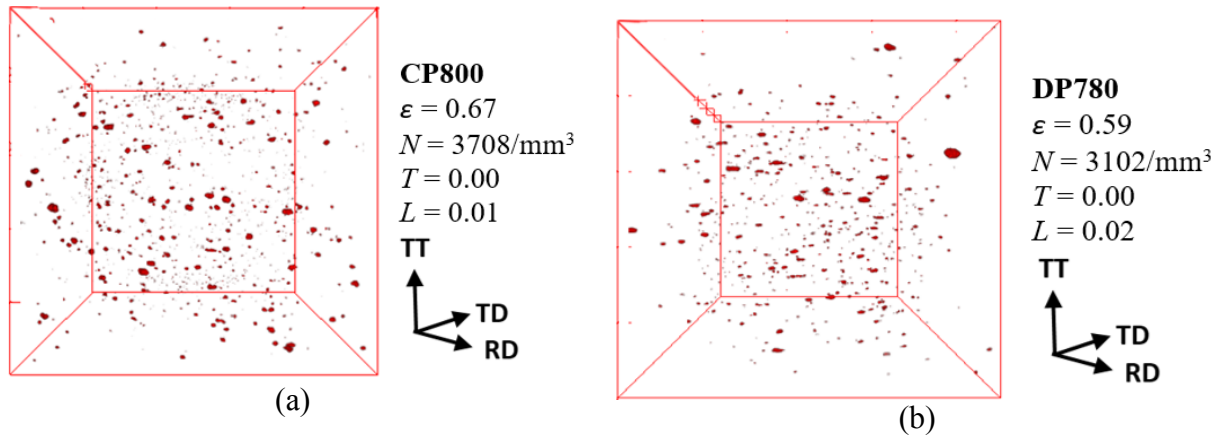


Figure 16: 3D views of damage within the CP800 and DP780 specimens deformed under shear loading at various steps of deformation.

A second view or orientation of the tomographs for the most deformed shear specimens (Figure 16) are shown in Figure 17. For the simple shear loading type, normal stresses are almost negligible relative to the shear stress (τ_{xy}) so that principal plane is oriented 45° to the loading directions [49]. In the current shear loading condition, the location of principal stresses (σ_1 and σ_2) are aligned along the rolling and transverse directions and the shear stresses (τ_{xy}) are 45° to the rolling and transverse directions as indicated in Figure 17. The voids have a tendency to rotate and align along the principal normal stresses and therefore are oriented along the rolling direction as shown in Figure 17 for both the alloys.

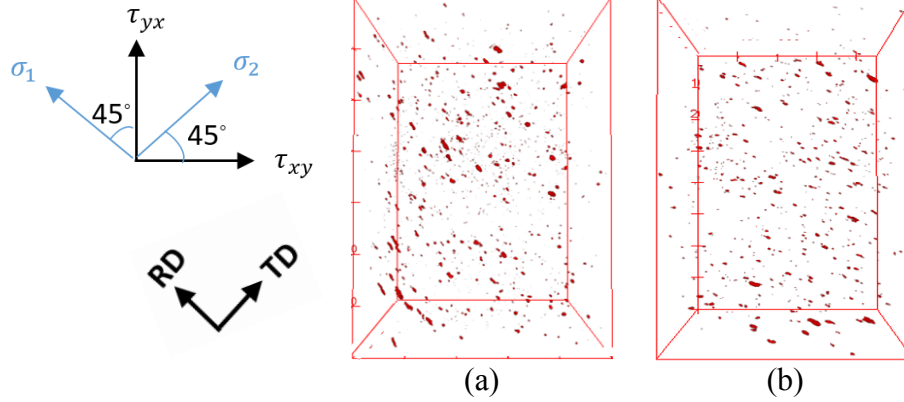


Figure 17: 3D views of damage within the (a) CP800 and (b) DP780 specimens deformed under shear loading at near failure.

4.2. Effect of Loading Condition on the Damage Evolution

Figure 18 shows the number of voids nucleated as a function of equivalent strain for the different loading conditions. Void nucleation is a continuous process and the maximum nucleation rate occurred under biaxial tension and the minimum rate was in simple shear for both materials. Void nucleation is clearly dependent upon the stress state for both materials. Similar results were observed by Landron *et al.* [11] and Needleman [19] which reported that the stress triaxiality has an impact on void nucleation rate.

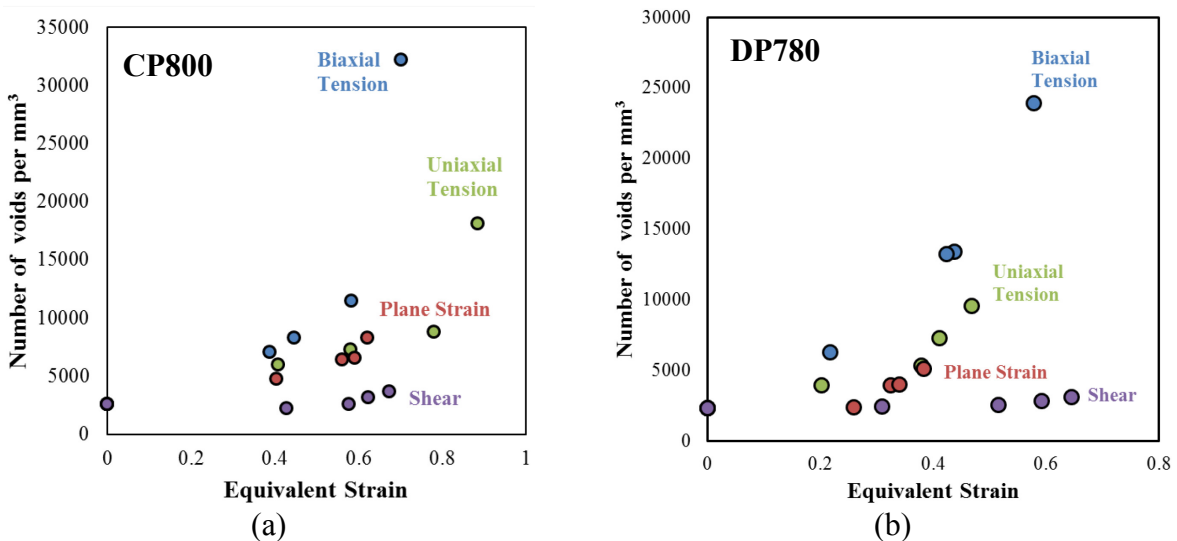


Figure 18: Average void density versus equivalent strain for (a) CP800 and (b) DP780 steels

Figure 19 shows the evolution of the porosity with the equivalent strain for the two materials subjected to different stress states. As deformation progresses, more voids are nucleated while the existing cavities grow and the void volume fraction increases. Since the number of nucleated voids and growth of voids under the plane-strain and shear stress states are less than that for biaxial tension and uniaxial tension at a given strain, the accumulation of damage is lower within the specimens subjected to shear and plane-strain loading.

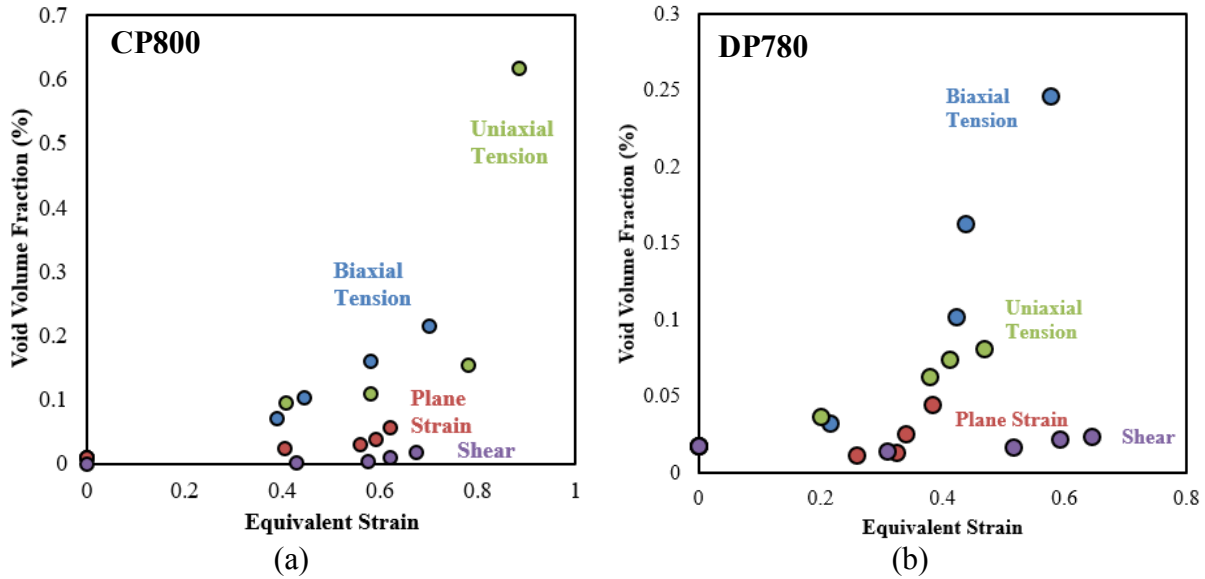


Figure 19: Evolution of the void volume fraction with respect to equivalent strain for (a) CP800 and (b) DP780

5. Void Nucleation Model

The results presented in the previous section have demonstrated the influence of loading condition on the nucleation mechanism. To predict ductile failure accurately, the modeling of void nucleation is critical and therefore it is critical to account for the effect of stress state on the nucleation mechanism. In this section, modifications to the Chu and Needleman [36] nucleation models are presented to predict the nucleation process for a wide range of loading conditions using two criteria: strain-based and stress-based nucleation models. The efficacy of these two approaches is assessed.

5.1. Strain-Based Nucleation Model

Chu and Needleman [36] postulated that the strain required to nucleate voids follows a normal distribution and can be expressed as:

$$\dot{N} = \frac{N_n}{s_N \sqrt{2\pi}} \exp \left[\frac{-1}{2} \left(\frac{\varepsilon^p - \varepsilon_N}{s_N} \right)^2 \right] \dot{\varepsilon}_p \quad (11a)$$

$$s_N = c_v * \varepsilon_N \quad (11b)$$

where \dot{N} is the void nucleation rate, N_n is the maximum number of voids per unit volume available to nucleation voids, ε_N and s_N are the mean and standard deviation of the nucleation strain, c_v is the coefficient of variance of the nucleation strain and N_n represents the number of potential void nucleation sites in a material and therefore is a material-dependent parameter. For a homogeneous material, N_n can be determined from metallurgical analysis of the volume fraction of second-phase particles and inclusions in the material. Chu and Needleman [36] and Søvik [66], assumed ε_N and s_N to be material-specific parameters that were constant for all stress states. To assess the strain-controlled nucleation assumption, the predicted numbers of nucleated voids within CP800 based on a strain-controlled nucleation assumption (Eq. (11a)) was calculated using the following values of nucleation strain, $\varepsilon_N = 1.0, 1.2, 1.4, 1.6, 1.8$ and 2.0 , an assumed value of c_v equal to 0.24 and s_N was calculated using Eq. (11b). N_n was taken as $397,942$ per mm^3 for CP800. These predictions are plotted in Figure 20, along with the observed number of voids per unit volume as a function of strain for the different stress state experiments on CP800. It is evident from the figure that the nucleation rates differ dramatically between stress states; therefore, the adoption of a simple strain-controlled nucleation model with ε_N as a material parameter cannot predict the nucleation behaviour for such a wide range of stress states. To capture the nucleation behaviour for different stress states, ε_N could be determined individually for each loading condition, but such an approach has not been investigated thus far.

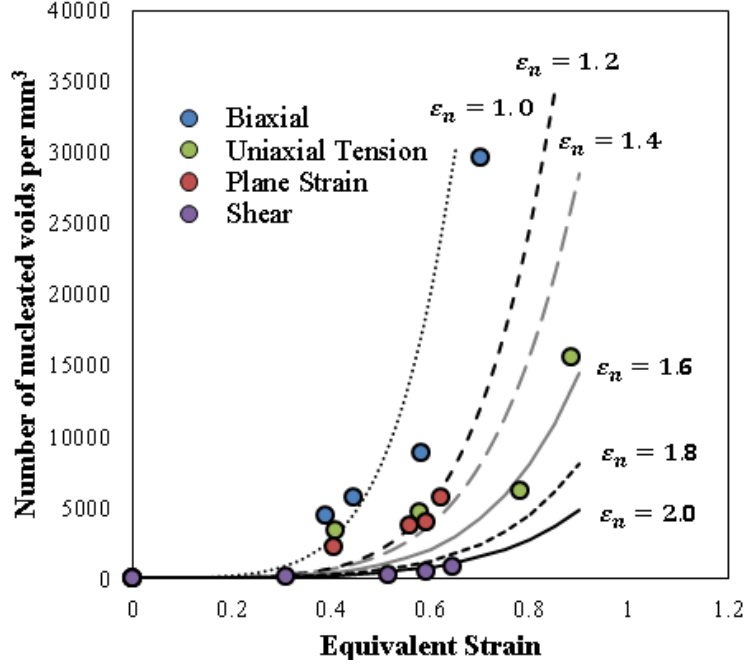


Figure 20: Predictions using Chu and Needleman's strain-based nucleation rule for CP800 using various nucleation strain assumptions. Solid curves are predictions using Eq. (11), while symbols are measurements from interrupted samples.

5.2. Stress-Based Nucleation Model

Nucleation rules based on critical stress and stress concentrations are available in the literature [41], [35], [67]. For practical applications, the stress-based Chu and Needleman [36] nucleation criterion has been used extensively in past work [39], [68], [69] and can be expressed as

$$\dot{N} = \frac{N_n}{s_n \sqrt{2\pi}} \exp \left[\frac{-1}{2} \left(\frac{\sigma_n - \sigma_N}{s_n} \right)^2 \right] \dot{\sigma}_n \quad (12a)$$

$$s_n = C_v * \sigma_N \quad (12b)$$

where σ_n is the nucleation stress, σ_N and s_n are the average and standard deviation of the nucleation stress and C_v is the coefficient of variance of the nucleation stress. Fowler *et al.* [68] examined Argon's nucleation stress criterion to estimate nucleation stress for Chu and Needleman's stress-controlled nucleation model and reported that the stress-controlled nucleation model can capture the experimentally observed dependence of nucleation strain on stress triaxiality. Shabrov and Needleman [70] extended Argon's criterion that relates the nucleation stress to the stress in the matrix material as given by the following relation:

$$\sigma_n = c\sigma_{eq} + \sigma_{hyd} , \text{ where } \sigma_{hyd} = \frac{\sigma_1 + \sigma_2 + \sigma_3}{3} \quad (13)$$

For periodically distributed particles, $c \approx 0.44$ for cubic particles and $c \approx 0.35$ for spherical particles [70]. To illustrate the use of a stress-controlled nucleation criterion, Similar to the strain-controlled nucleation model, N_n and C_v are considered material-specific properties and held constant for all the loading conditions. C_v was taken as 0.04 and 0.10 for the CP800 and DP780 steels respectively. The stress components, unlike the strain components, cannot be obtained from experiments and the stress integrator described in Section 3 is used to determine stress components (σ_1, σ_2) from the strain components ($\varepsilon_1, \varepsilon_2$) derived from the experimental data. The predicted nucleation response is plotted in Figure 21, along with the measured data from the interrupted samples. With $\sigma_N = 1070$ and 746 MPa, the predicted nucleation mechanism agrees with the measured values only for the biaxial stress state and uniaxial tension loading, respectively. The predicted number of nucleated voids for the other stress states is either higher compared to the measured value or lower. This observation suggests that despite the stress-based nucleation model being dependent on the stress triaxiality, the adoption of single σ_N to predict nucleation for all the stress states is not achievable using the current definition of the nucleation stress of Eq. (13) that is based upon particle debonding. It is possible that other forms for the nucleation stress such as that of Beremin [35] could provide a better description.

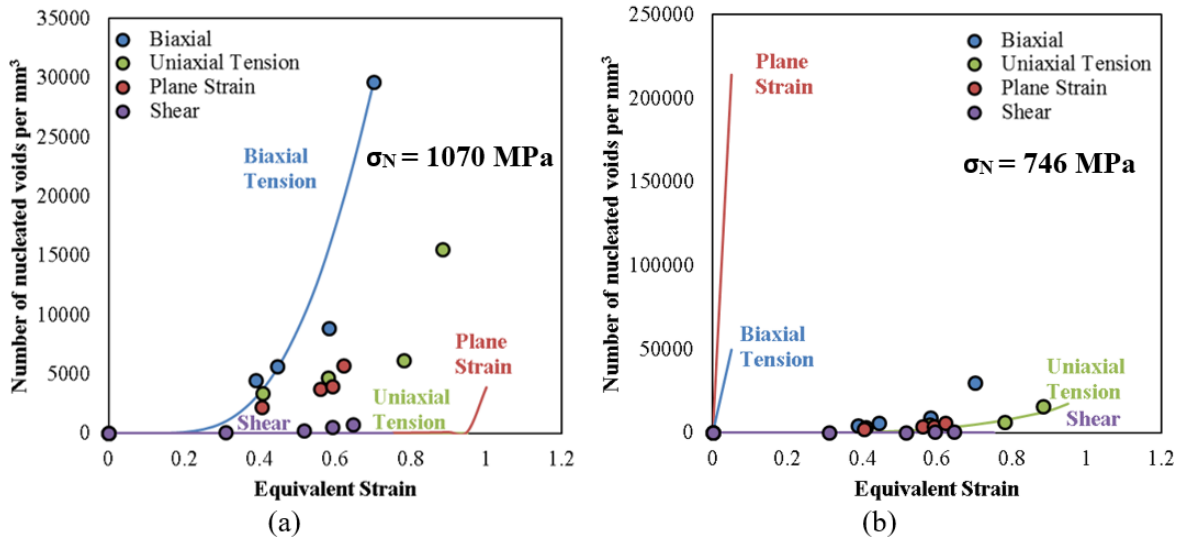


Figure 21: Predictions using Chu and Needleman's stress-based nucleation rule using various assumed nucleation stress levels: (a) 1070 MPa and (b) 746 MPa. Solid curves are predictions using Eq. (12), while symbols are measurements from interrupted samples.

5.3 Introduction of Lode-Dependence of Nucleation Strain

The major limitation of Chu and Needleman's nucleation model is that it does not fully account for the effect of stress state. The experimental results presented in Section 4 and the work done by [11] suggests that the nucleation mechanism varies with the loading condition. To account for this behavior, a modification to Chu and Needleman's criteria is proposed in which nucleation strain becomes a function of both stress triaxiality and Lode parameter. In the light of the proposed dependency of nucleation mechanism on stress state, the nucleation strain, ε_N , was first determined individually for each loading condition as a function of stress triaxiality as well as Lode parameter, and the modified nucleation model is expressed in following equation.

$$\dot{N} = \frac{N_n}{s_N \sqrt{2\pi}} \exp \left[\frac{-1}{2} \left(\frac{\varepsilon_p - \varepsilon_N(T,L)}{s_N} \right)^2 \right] \dot{\varepsilon}_p \quad (14)$$

As before, N_n and C_v are considered to be constant for all the stress states.

An optimization code was written in MATLAB to determine the parameters in Eq. (14) for both steels, using an assumed normal distribution of the observed void density versus strain data for the different stress states. The genetic algorithm global optimization subroutine, available in MATLAB, was used to minimize error between the experimental data points and the values predicted by the nucleation model. The Error function was defined as:

$$Error = \sum_{i=1}^4 w_i \left(\left(\frac{N_{model}}{N_{exp}} \right)_i - 1 \right)^2 \quad (15)$$

where the superscripts "exp" and "model" indicate either measured values or predicted nucleated void density from the nucleation model. w_i are weighting parameters for the number of experimental data points where $i=1$ corresponds to experimental data point acquired at the lowest strain, $i=2$, the data point obtained at the next strain level, and so on. In the present work, the weighting parameters were assigned in such a manner that a higher weighting is given to the experimental data points acquired at a higher strain level i.e. $w_1 = 0.125$, $w_2 = 0.25$, $w_3 = 0.5$, $w_4 = 1$ (recall that four tomography images (data points) were acquired for each stress state). The nucleation parameters determined for each loading condition using the optimization approach described above are listed in Table 6 for the CP800 and DP780 steels. The resulting nucleation

predictions are shown in Figure 22 from which it can be seen that the model predictions capture the trends in the measured data rather well.

Table 6: Nucleation parameters for the different stress states of the CP800 and DP780 steels

Material	N_n (per mm^3)	c_v	Biaxial Tension			Plane Strain			Uniaxial Tension			Shear		
			ϵ_N	T	L	ϵ_N	T	L	ϵ_N	T	L	ϵ_N	T	L
CP800	397942	0.24	1.10	0.66	0.97	1.34	0.55	-0.01	1.58	0.30	-0.92	2.20	0.00	0.02
DP780	48000	0.31	0.50	0.66	0.98	0.80	0.55	0.01	0.70	0.30	-0.98	1.40	0.00	0.01

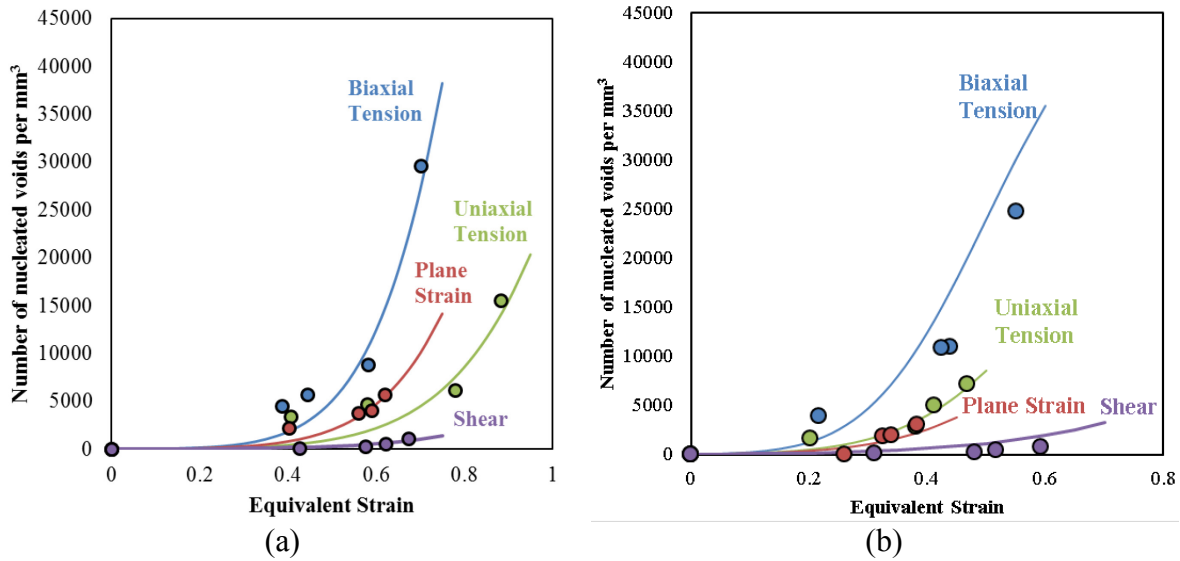


Figure 22: The implementation of Lode parameter-dependent strain-based Chu and Needleman nucleation rule using Eq. (14) for the various loading conditions of the (a) CP800 and (b) DP780 steels. Solid curves are predictions using Eq. (14), while symbols are measurements from interrupted samples.

The nucleation parameters listed in Table 6 predict the nucleation rates for the specific stress states corresponding to the measured damage histories. To develop a more comprehensive expression to predict nucleation under different loading conditions, a functional dependence of average nucleation strain on both stress triaxiality and Lode parameter is introduced. In this case, the functional form of the fracture *locus* proposed by Bai and Wierzbicki [58] is adopted to develop a “nucleation strain surface” that can be expressed as:

$$\epsilon_N = \left\{ \frac{c_1}{c_2} \left[C_3 + \frac{\sqrt{3}}{2-\sqrt{3}} (1 - C_3) \left(\sec\left(\frac{\pi L}{6}\right) - 1 \right) \right] \right\}^{\frac{-1}{c_5}} \times \left[\sqrt{\frac{1+C_4^2}{3}} \cos\left(\frac{\pi L}{6}\right) + C_4 \left(T + \frac{1}{3} \sin\left(\frac{\pi L}{6}\right) \right) \right] \quad (16)$$

where C_{1-5} are material parameters and are listed in Table 7 for the CP800 and DP780 steels. Note that c_v is independent of loading condition, as is N_n . The constants in Eq. (16) were identified using the genetic algorithm in MATLAB. Although the formulation shown in Eq. (16) has five coefficients, the number of coefficients can be reduced to four by replacing C_1/C_2 with a single variable. Subsequently, the four coefficients values can be determined by plugging in the four sets of experimental values. The error between the experimental data points and the values predicted by the nucleation model was minimized using the Error function defined as

$$Error = \sum_{i=1}^4 w_i \left(\left(\frac{\epsilon_{model}}{\epsilon_{exp}} \right)_i - 1 \right)^2 \quad (17)$$

where the superscripts “exp” and “model” indicate either measured values or predicted nucleated void density from the nucleation model. w_i are weighting parameters for the four loading conditions and assumed to be unity for all the cases.

Figure 23 shows the resulting nucleation surfaces for the CP800 and DP780 steels that cover a broad range of stress states. Also shown is the so-called plane stress locus corresponding to the stress states accessed in the current experiments (symbols). The nucleation rate for a given stress state can then be predicted by substituting the nucleation strain, from Eq. (16), corresponding to the loading condition, into Chu and Needleman’s nucleation criterion of Eq. (14) along with the respective material parameters, N_n and c_v . The predicted void density as a function of equivalent strain for the various loading conditions are shown in Figure 24 along with the experimental data.

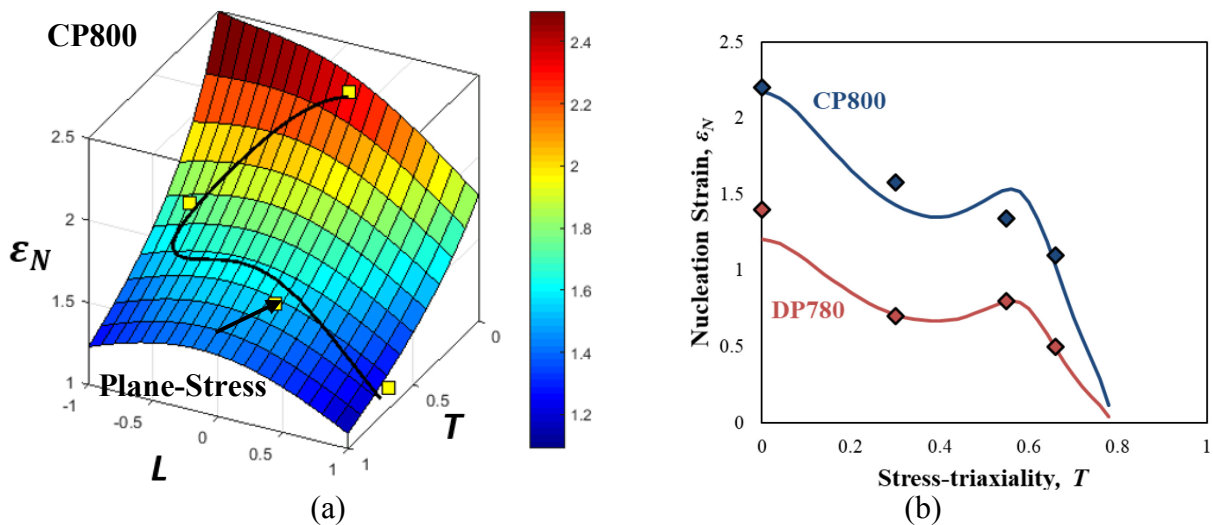


Figure 23: (a) Representation of nucleation strain (ϵ_N) surface as a function stress triaxiality (T) and Lode angle parameter (L) for the CP800 steel. (b) The plane stress curve locus corresponding to the stress states and experimental data points are indicated by black line and square symbols, respectively.

Table 7: Material parameters for the CP800 and DP780 steels listed in Eq. (16) and Error in Eq. (17)

Material	C_1	C_2	C_3	C_4	C_5	Error
CP800	0.44	1.7	0.7	2.2	1.8	0.03
DP780	1.80	901.5	0.7	1409.0	1.7	0.02

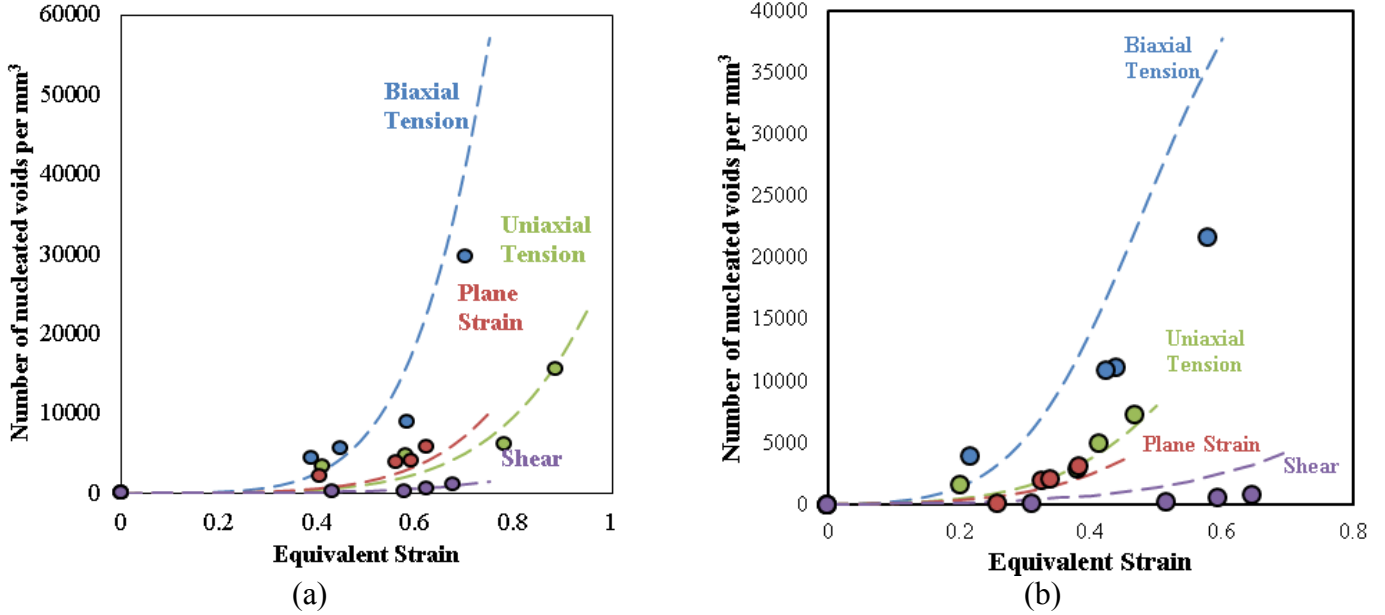


Figure 24: Predicted nucleated voids as a function of equivalent strain for the various loading conditions of the (a) CP800 and (b) DP780 steels. Solid curves are predictions using Eq. (14), while symbols are measurements from interrupted samples

6. Conclusions

1. The rate of damage nucleation is lower for the CP800 steel relative to DP780. This difference can be attributed to the lower strength differential between phases of the ferritic-bainitic CP800 steel [7], resulting in a higher nucleation strain and accelerated void nucleation in comparison to the ferritic-martensitic DP780 steel.
2. The influence of stress state, in terms of triaxiality and Lode parameter, on nucleation behaviour was characterized for the DP780 and CP800 steel sheet. At a given strain, the number of voids per unit volume observed during the biaxial dome test was highest while

the void nucleation was lowest under simple shear deformation for both materials considered.

3. Strain-based or stress-based nucleation criteria alone were unable to capture the measured dependency of nucleation rate on stress-state. The introduction of Lode parameter-dependency of nucleation rate, in addition to stress-triaxiality, accurately captured the measured nucleation behaviour. The use of a nucleation surface will enable application to three-dimensional stress states and will be evaluated in future work.

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