

Evaluation of Polymeric Membranes for Gas
Separation Processes: Poly(ether-*b*-amide)
(PEBAX[®]2533) Block Copolymer

by

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Abstract

The development of polymeric membranes for gas separations has provided an alternative to traditional energy-intensive processes, especially for hydrocarbon separations. Material studies of the membrane can provide insights to its formation and modification. Gas permeation behaviour through two types of polymeric membrane material is investigated herein. Though the main objective of our investigation was to determine the hydrocarbon gas permeation properties of poly(ether-*b*-amide) PEBAX[®]2533 copolymer membranes over a range of operating temperatures and pressures, we first tested a poly(ethylene oxide) (PEO) membrane for permeability of ethane and ethylene. The screening results from the tests of PEO membranes containing silver salts, indicate that although PEO membranes may possess high olefin/paraffin selectivity through facilitated transport, difficult membrane preparation and unstable structure remain major obstacles to their commercial use. However, the knowledge acquired on preparation technique and permeability testing from these trials was carried over to our study of PEBAX[®]2533 membranes. Permeability coefficients were determined at temperatures ranging from 25°C to 75°C, and pressures from 25 psig to 200 psig for ethane, ethylene, nitrogen, propane, propylene, and carbon dioxide. The PEBAX[®]2533 membranes showed high organic gas permeabilities. Plasticization effects on the membrane were pronounced with propane and propylene at elevated pressure (100 psig). Activation energies of permeation (E_p) were determined. E_p of nitrogen is nearly constant and is the highest among gases tested in the pressure range. E_p shows a linear decreasing trend as pressure increases for hydrocarbons. Relatively high selectivities (12 to 26) were observed for the polar and non-polar gas pair CO₂/N₂. As temperature increased, the selectivity of CO₂/N₂ decreased. This study provides the groundwork for the use of PEO and PEBAX[®]2533 membranes for hydrocarbon separations.

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Chapter 1

Introduction

Gas separations have always been one of the key processes in the field of chemical engineering. With industry's demand on lowering operating costs and increasing separation efficiency, more research is being conducted on process improvements. Gas separation is usually achieved by physical or physicochemical phenomena. Over the past two decades, gas separation using polymeric membranes has drawn a great deal of interest from researchers due to many advantages such as low energy costs and high selectivities. This is especially true for hydrocarbon separations performed by the petrochemical industry.

In particular, olefin/paraffin separations incur a heavy cost to petrochemical companies. With a growing awareness of the importance of conserving natural resources, companies are enthusiastic about finding ways to reduce energy consumption and to recycle purge or waste streams. Traditionally, cryogenic distillation at elevated pressures in trayed fractionators is used to separate olefins and paraffins. This distillation system is expensive to build and operate, and is currently only economically attractive for streams containing high quality of olefins. Other available separation technologies include extractive distillation, physical or chemical adsorption, physical or chemical absorption, and more recently, membrane separation. A more thorough description of

different separation technologies can be found in the review written by Eldridge (1993).

1.1 Thesis Outline

The objective of this research is to develop an advanced membrane that exhibits high gas permeability and selectivity, particularly for olefins and paraffins. More specifically, it is to gain knowledge on both the preparation and the gas permeation properties of the new poly(ether-*b*-amide) copolymer membrane, PEBAX[®]2533.

To provide a basic understanding of the membrane separation process, an introduction to the transport mechanism through polymeric membranes used for gas separations is covered in Chapter 2. Transport models and equations are described and factors affecting gas permeation are discussed. Chapter 3 presents procedures for membrane preparation and permeability testing along with a description of the testing apparatus. Chapter 4 describes a screening study based on olefin/paraffin separation using poly(ethylene oxide) membranes containing silver nitrate. More background is given for this process that makes use of active facilitated transport via silver nitrate. Experimental methods are detailed and results from the study are presented and discussed. Our study of polyether-*b*-amide copolymer membrane, PEBAX[®] 2533 is covered in Chapter 5, and a brief review of recent investigations of PEBAX[®] membranes used for separation. Flat film membranes were made from PEBAX[®] resin and permeability tests were conducted to evaluate its gas separating performance against N₂, CO₂, and several hydrocarbon gases. Interactions between gas and membrane material over a range of temperatures and pressures were tested and discussed. Sample calculations from both PEO and PEBAX studies are included in Appendix C. Finally, based on the results from the experimental investigation of the two polymeric membranes, concluding remarks are presented in Chapter 6, along with recommendations for further work.

Chapter 2

Background and Literature Review

Membrane separation technology is currently one of the most innovative and rapidly growing fields across science and engineering. Many different separation processes are widely used in industry in liquid-liquid and liquid-solid systems. Several books have been published to detail the fundamental principles and applications of membrane technology (Bitter, 1991; Mulder, 1991; Noble and Stern, 1995), and some articles have provided overviews to membrane structure and formation (Kesting, 1985; Pinnau and Freeman, 2000).

The most attractive features of membrane separation systems are cost effectiveness, environmental friendliness, versatility, and simplicity. Membrane processes are classified according to the driving force by which they achieve separation. Table 2.1 lists commonly known means of separation along with their primary driving force and type of mechanism. Types of membranes used today include nonporous (dense) and porous polymers, ceramic and metal films with symmetric or asymmetric structures, liquid films with selective carrier components, and electrically charged barriers (Strathmann, 2001). The performance of a membrane is determined by several key properties: high selectivity and permeability; excellent chemical, thermal, and mechanical stability under the process operating conditions; low maintenance; good space efficiency; and

defect-free production.

Table 2.1: Various membrane separation processes and the corresponding driving forces

Process	Driving Force	Transport Mode
microfiltration	Δp	convection
ultrafiltration	Δp	convection
reverse osmosis	$\Delta C(\Delta \mu_i)$	diffusion
dialysis	$\Delta C(\Delta a)$	diffusion
gas separation	$\Delta p(\Delta f_i)$	diffusion
pervaporation	$\Delta p_i(\Delta f_i)$	diffusion
electrodialysis	$\Delta \varphi$	migration

(p -hydrostatic pressure, μ -chemical potential, C -concentration
 a -activity, p_i -partial pressure, f_i -fugacity, φ -electrical potential)

In the last two decades, the membrane industry has extended its interests to gas and vapor separations. Combined with advances in polymeric materials, membrane-based separations have become an important chemical unit operation which successfully competes with other well-established industrial gas separation processes such as cryogenic distillation, absorption, and pressure swing adsorption (Spillman, 1989).

Commercially, the most widely practiced separations using membranes include the separation of oxygen and nitrogen; the recovery of hydrogen from mixtures with larger components such as nitrogen, methane and carbon dioxide; and the removal of carbon dioxide from natural gas mixtures. For these separations, membranes with adequately high fluxes of the more permeable components (oxygen, hydrogen, and carbon dioxide, respectively) and sufficient selectivity have been developed. The membrane materials used in these separations are glassy polymers, which derive high selectivity from their ability to separate gases based on differences in penetrant size (Freeman and Pinnau, 1997).

Membranes can be categorized according to their geometry, bulk structure, production method,

separation regime, and application (Pinnau and Freeman, 2000). The basic scheme for membrane classification is shown in Figure 2.1. Hollow-fiber membranes are used commonly by industries due to their high surface area and compactness. Flat-sheet membranes are easy to produce and are used in laboratory experiments. In terms of structure, membranes can be separated into two groups; asymmetric and symmetric. This simply refers to the types of pores that can be found within the membrane. Symmetric membranes have pores which do not change in diameter significantly through the sheet. On the other hand, asymmetric membranes contain pores which increase in size from one side of the sheet to the other. The new membrane composites are good example of asymmetric membranes. They are made with a thin polymer film deposited onto a porous backing material. The separation is determined by the properties of the thin film while the mass transport or rate is dependent upon the porosity of the backing.

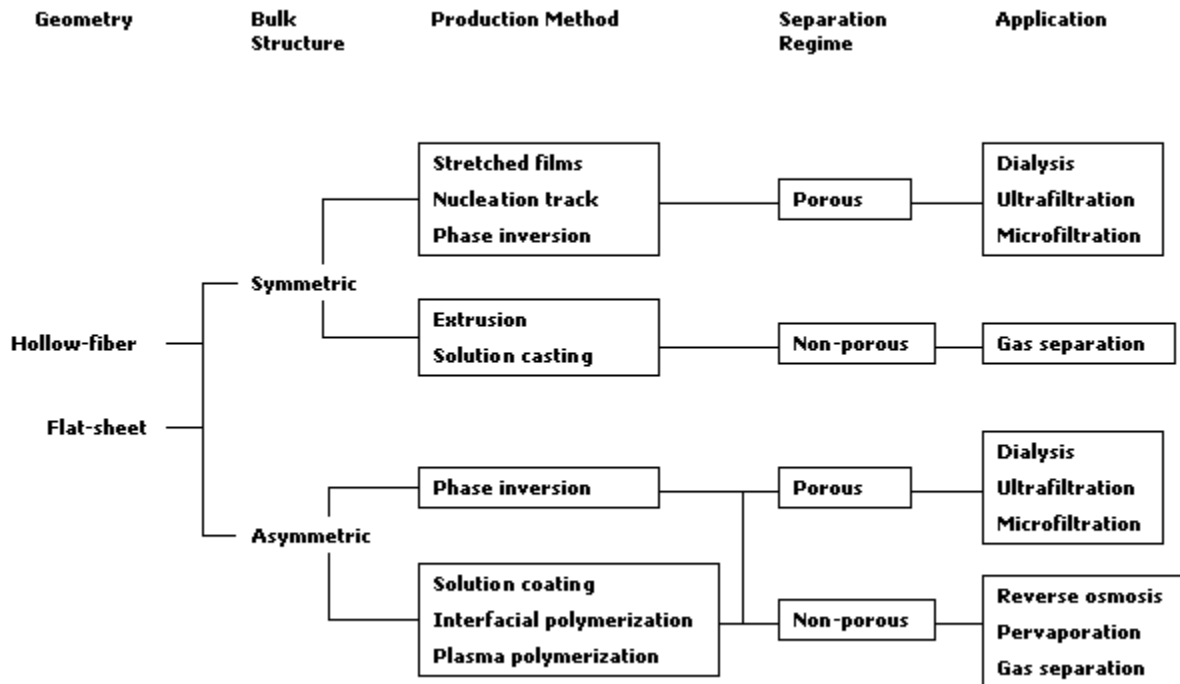


Figure 2.1: Classification scheme of synthetic membranes

Different production methods can result in membranes with unique characteristics. Membranes are the result of pressing a powder into a porous film and then sintering, stretching an extruded polymer into a sheet, irradiating a thin film with nuclear particles and then etching in a bath (nucleation track), dissolving a polymer in a solvent and spreading into a film followed by precipitation (solution casting), contacting two monomers in two immiscible liquids (interfacial polymerization), or condensing gaseous monomers on a substrate layer through a stimulated plasma (plasma polymerization).

2.1 Types of Gas Separation Membranes and Applications

Most gas separation membranes are made of amorphous (noncrystalline) polymers which are in either the glassy or the rubbery state. In the glassy state, polymers are rigid and often brittle. There is low level of molecular movement and the rate of diffusion of large molecules is small. In the rubbery state, polymers tend to be soft and more flexible. What separates the two states is the glass transition temperature, T_g , of the polymer. Properties that change around T_g include density, specific heat, dielectric coefficient, rates of gas/liquid diffusion through the polymer, and conductivity or charge mobility.

The majority of industrial membrane processes for gas separations utilize glassy polymeric membranes because of their high gas selectivity and good mechanical properties. Glassy polymers like polyimides are used for CO_2/CH_4 separation; polysulfones are used in H_2 separations, and cellulose acetate membranes are used for the removal of CO_2 and H_2S from natural gas. In the area of rubbery polymers, polyurethanes possess high permeability and are being applied in O_2/N_2 separation. Silicon polymers, particularly polydimethylsiloxanes (PDMS), are widely studied due to their large free volume, high permeability, and low selectivity. Stern (1994) has presented a thorough review on the structure/permeability/selectivity relationship on selected

rubbery and glassy polymers.

In view of their physical properties, including sorption and gas transport, rubbery polymers are considered equilibrium materials. Glassy polymers go through a physical aging process to attempt to reach equilibrium in the course of time. Details of the sorption and diffusion behaviours in both rubbery and glassy polymers can be found in reviews by Ghosal and Freeman (1993), and George and Thomas (2001). Through modifications, such as copolymerization and sol-gel process, polymer properties can be adjusted and enhanced to achieve desirable separation performance and mechanical strength.

2.2 Fundamentals

Three general transport mechanisms are commonly used to describe gas separations using membranes, as illustrated in Figure 2.2 (Koros and Fleming, 1993). They are Knudsen diffusion, molecular sieving, and solution-diffusion. As the name implies, the first type of separation is based on Knudsen diffusion and separation is achieved when the mean free paths of the molecules are large relative to the membrane pore radius. The separation factor from Knudsen diffusion is based on the inverse square root ratio of two molecular weights, assuming the gas mixture consists of only the two types of molecules. The process is limited to systems with large values for the molecular weight ratio, such as is found in H₂ separation. Due to their low selectivities, Knudsen diffusion membranes are not commercially attractive.

The molecular sieving mechanism describes the ideal condition for the separation of vapour compounds of different molecular sizes through a porous membrane. Smaller molecules have the highest diffusion rates. This process can happen only with sufficient driving force. In other words, the upstream partial pressure of the "faster" gas should be higher than the downstream

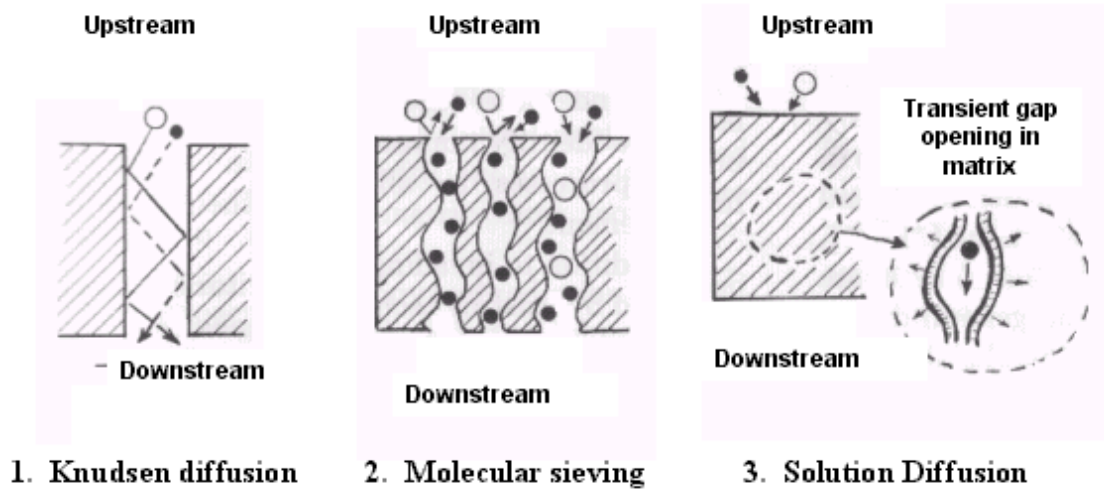


Figure 2.2: General transport mechanisms for gas separations using membranes

partial pressure. The main limitation is that condensible gases cause fouling, and alter the structure of the membrane; therefore, it is only feasible commercially in robust systems, such as those that use ultramicroporous carbon or hollow fibre glass membranes.

Solution-diffusion separation is based on both solubility and mobility factors. It is the most commonly used model in describing gas transport in non-porous membranes and it is applied in our studies. The details of this solution-diffusion model are given in the next section.

2.2.1 Solution-Diffusion Model and Permeability Equations

Gas permeation can be seen as a three-stage process in the solution-diffusion model:

1. adsorption and dissolution of gas at the polymer membrane interface.
2. diffusion of the gas in and through the bulk polymer.
3. desorption of gas into the external phase.

Permeation is used to describe the overall mass transport process, and diffusion refers only to the movement of gas molecules inside the polymer membrane. The model assumes that the pressure within a membrane is uniform and the chemical potential gradient across the membrane is expressed only as a concentration gradient. Koros et al. (1988) gave a thorough review on polymeric membranes for solution-diffusion based permeation separations. The review covered membranes for not only gas separations, but also for pervaporation, reverse osmosis, and liquid separation.

Koros and Fleming (1993) suggest that solution-diffusion is achieved via penetrant species undergoing random jumps in the polymer matrix due to a concentration difference between membrane upstream and downstream, resulting in a diffusion flux travelling downstream. Varying the chemical nature of the polymer allows control of the relative extent of solution and diffusion of different gases through the polymer matrix.

Figure 2.3 shows a schematic of gas transport across a membrane. The upstream gas, which has a pressure of p_1 , comes in contact with the membrane interface. With a driving force (e.g., chemical potential, concentration gradient, etc.), the permeate gas forms a concentration profile across the membrane with respect to membrane thickness, l . The normalized flux is gas flow rate divided by the membrane surface area and it is denoted as N_A . Separation of the gas mixture is achieved when one of the components interacts more strongly with the membrane material or, in other words, diffuses faster through the membrane.

Among the three solution-diffusion stages, the diffusion step is the slowest; hence, it is the rate-determining step in permeation. In general, the relationship between the linear flux, J and the driving force is:

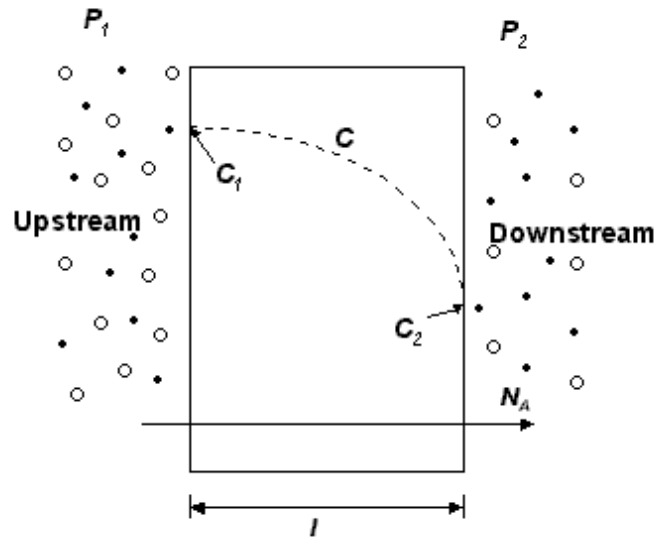


Figure 2.3: Gas transport across a membrane

$$J = -A \frac{dX}{dx} \quad (2.1)$$

where A is some phenomenological coefficient, X is a potential, and x denotes the space coordinate measured normal to the section. To describe gas diffusion in the membrane, Equation 2.1 can be written as:

$$J = -D \frac{dC}{dx} \quad (2.2)$$

where D is the diffusion coefficient, and X in Equation 2.1 now defines concentration and is denoted as C . Equation 2.2 is commonly known as Fick's first law.

When the solubility of a penetrant gas in a polymer is sufficiently low, the concentration of the penetrant is proportional to the vapor pressure of penetrant in polymer. This relationship is expressed as Henry's law, Equation 2.3. S is the solubility coefficient and p is the vapour

pressure of the penetrant.

$$C = S * p \quad (2.3)$$

At steady state, the permeation of a pure gas A through a membrane of thickness l is characterized by a permeability coefficient P_A . P_A is generally defined as:

$$P_A = \frac{N_A}{(p_1 - p_2)/l} = \frac{N_A}{(\Delta p/l)} \quad (2.4)$$

where N_A is the normalized flux, p_1 and p_2 are the upstream and downstream pressures, respectively, and Δp is $p_1 - p_2$. In a gas mixture, p_1 and p_2 refer to the partial pressures of penetrant A at the two sides of the membrane. The permeability coefficient of dense film materials is commonly expressed in units of Barrer.

$$1 \text{ Barrer} = 1 * 10^{-10} \frac{\text{cm}^3(\text{STP}) \text{ cm}}{\text{cm}^2 \text{ sec cmHg}} \quad (2.5)$$

If Henry's law applies, then S is constant at a given temperature and so is D . The permeability coefficient, P , can also be defined as:

$$P = D * S \quad (2.6)$$

The diffusion coefficient, D , is a kinetic term governed by the amount of energy necessary for a particular penetrant to execute a diffusive jump through the polymer and the intrinsic degree of segmental packing in the matrix. The solubility coefficient, S , is a thermodynamic term that depends on factors such as condensibility of the penetrant, interactions between the polymer and penetrant, and the amount of penetrant-scale non-equilibrium excess volume in glassy polymers.

For a binary gas mixture permeating through a polymer membrane, the selectivity of a polymer membrane towards two different penetrant gases, A and B, is commonly expressed in terms of the ideal selectivity or ideal permselectivity, α_{AB} . When the downstream pressure is negligible relative to the upstream pressure, α_{AB} can be written as the ratio of permeabilities:

$$\alpha_{AB} = \frac{P_A}{P_B} \quad (2.7)$$

Expanding the permeability into diffusivity and solubility terms, the ideal selectivity can be expressed by Equation 2.8.

$$\alpha_{AB} = \left(\frac{D_A}{D_B}\right)\left(\frac{S_A}{S_B}\right) \quad (2.8)$$

Here, D_A/D_B is the ratio of the concentration-averaged diffusion coefficients of penetrants A and B, and is referred to as the membrane's "diffusivity selectivity". S_A/S_B is the ratio of solubility coefficients of penetrants A and B, and is called the "solubility selectivity" (Ghosal and Freeman, 1993). In typical gas separation applications, the downstream pressure is not negligible; however, α_{AB} generally provides a convenient measure for assessing the relative ability of various polymers to separate gas mixtures. High permeability and high selectivity are the most important criteria in evaluating a membrane.

2.2.2 Facilitated Transport

The gas permeability of a membrane may be improved by facilitated transport. This is an active transport of permeant molecules across a membrane achieved by utilizing a carrier species. The carrier reacts with a permeant molecule to form a labile complex. Within the membrane, the carrier shuttles the permeant across the membrane boundaries, and hence the permeant is transported from the side with higher permeant concentration to the side with lower permeant

concentration. When a feed mixture only contains one species that the carrier will react with, only the transport of that species will be "facilitated" across the membrane. The process of facilitated transport is illustrated in Figure 2.4. The driving force in facilitated transport is a concentration gradient of permeant-carrier complexes across the membrane.

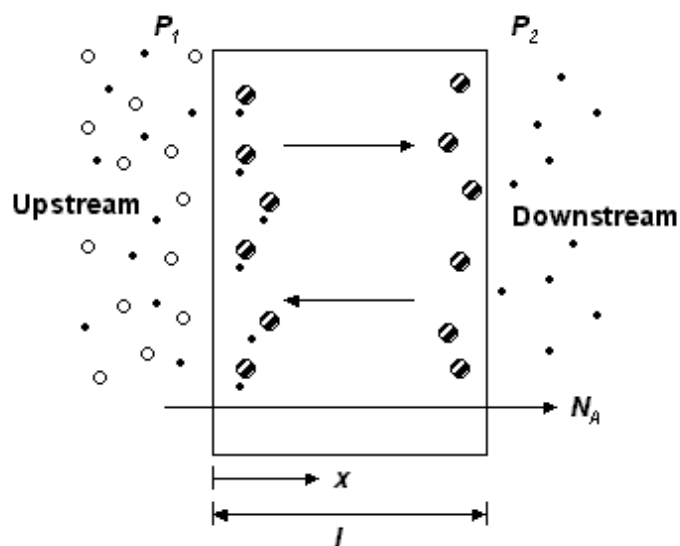


Figure 2.4: A schematic of facilitated transport mechanism across the membrane

It has been found that olefin transport can be facilitated by transition metals. Cuprous and silver ions are the mostly widely used in this type of research. The metal ions form a π -bond complexation with olefin molecules. More details will be given in Chapter 4.

Gas separation using facilitated transport is most commonly done with "immobilized liquid" membranes, prepared by dissolving the carrier in an appropriate solvent and using this solution to impregnate an electrically uncharged, rigid microporous matrix. Once formed, surface tension forces serve to hold the carrier molecules inside the membrane. Another technique is to swell a gel membrane, such as porous cellulose.

2.3 Factors Affecting Gas Permeation in Membranes

2.3.1 Temperature

As mentioned in Section 2.2.1, gas diffusion through polymers is related to an activation energy, thus, the temperature dependence of D , S , and P can be described by the following Arrhenius relationships:

$$D = D_0 e^{-E_d/RT} \quad (2.9)$$

$$S = S_0 e^{-\Delta H_s/RT} \quad (2.10)$$

$$P = P_0 e^{-E_p/RT} \quad (2.11)$$

where E_d is the activation energy of diffusion; ΔH_s is the heat of sorption; and E_p is the activation energy of permeation, which is simply:

$$E_p = E_d + \Delta H_s \quad (2.12)$$

Values of E_p , E_d , and ΔH_s for many polymer and gas pairs can be found in the Polymer Handbook (Pauly et al., 1989).

Gas diffusion coefficients typically increase appreciably with increasing temperature when the polymer does not undergo thermally induced morphological rearrangements such as crystallization over the temperature range of interest (Ghosal and Freeman, 1993). Since both diffusivity and solubility coefficients are temperature dependent, the selectivity described by Equation 2.8 is also sensitive to changes in temperature.

The increased segmental motion at higher temperatures undermines the ability of polymer to

discriminate between penetrants of different physical dimensions, thereby resulting in a diffusivity selectivity loss. The temperature changes also affect the solubility selectivity, which is governed primarily by the chemical nature of the penetrant and polymer-penetrant interactions. For most gases, as temperature increases, the solubilities increase. The solubility selectivity, therefore, will vary depending on the extent of the temperature effect on each component in the gas mixture (Costello and Koros, 1994).

2.3.2 Pressure

Change in the pressure of penetrant contacting with the polymer may cause large permeability variations. Four typical patterns of response are observed in permeability versus pressure relationships (Koros and Chern, 1987), as seen in Figure 2.5.

- (a) Linear, with slope close to 0. This represents the ideal case that satisfies the assumption of diffusion and solution being independent of gas pressure (i.e., low sorbing penetrants, such as He or N₂ in rubbery or glassy polymers).
- (b) Nearly linear increase of permeability with increasing pressure. This often describes the permeability of an organic vapor into a rubbery polymer.
- (c) A decreasing trend of permeability with increasing pressure. This is typically observed with highly soluble gases such as CO₂ in glassy polymers.
- (d) Concave upwards. This can be perceived as a combination of (b) and (c), and is typical of a plasticizing penetrant such as organic vapor in a glassy polymer.

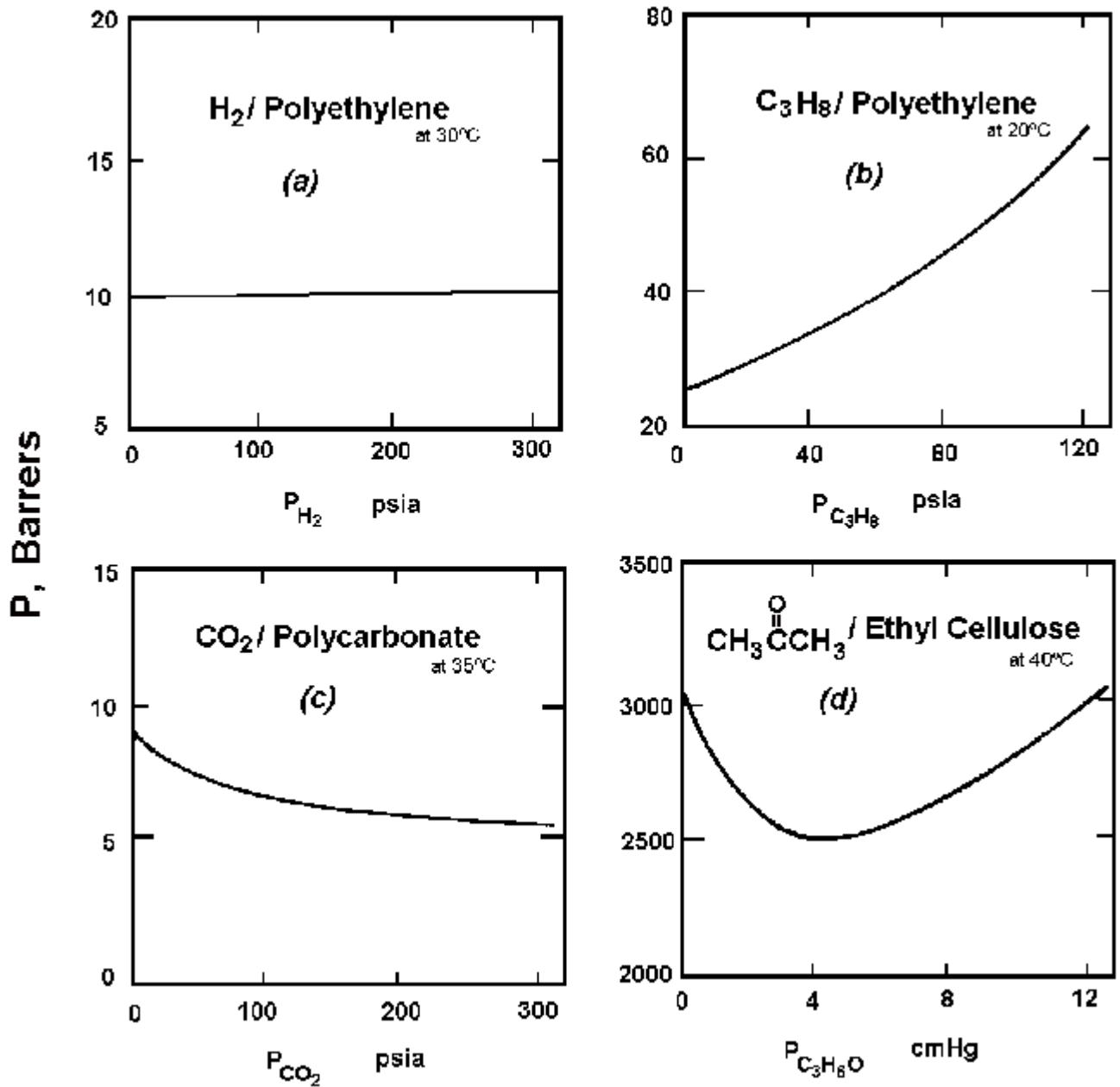


Figure 2.5: Pressure dependency of various penetrant-polymer systems

2.3.3 Plasticization

The pressure at which an increase in permeance occurs (i.e. the minimum in the permeance versus pressure plot, of a type (d) relationship mentioned in the previous section) is called the

plasticization pressure. At such feed pressure, the gas concentration in the polymer material disrupts the chain packing. The polymer matrix swells and the segmental mobility of the polymer chain increases. This results in an increase in gas diffusivity and induces permeability increases (Koros and Fleming, 1993). Therefore, when the polymer is highly plasticized by the penetrant, the diffusion coefficient may become a function of time and of history. This non-ideal behaviour is explained by free volume theory.

Free volume theory of diffusion suggests that molecules can only diffuse through free volume in a molecule matrix. Cohen and Turnbull (1959) have theorized that diffusion in a rubbery polymer is the result of redistribution of free volume within a matrix and migration of the penetrant among these volumes. Petropoulos (1994) has summarized the permeability equations derived based on the free volume approach to model the gas transport in plasticized polymer matrices. Studies have been done to suppress the plasticization effect on gas permeability and permselectivity by means of crosslinking, blending, or annealing of the polymer membranes (Ismail and Lorna, 2002; Krol et al., 2001; Bos et al., 2001; Petropoulos, 1992).

2.3.4 Other Factors

Apart from the operating conditions (i.e., temperature and pressure), factors such as composition in the gas mixture, penetrant condensibility, polymer-penetrant interactions, and polymer crystallinity may also affect the gas solubility. Furthermore, gas diffusivity is sensitive to properties such as penetrant size, polymer morphology, and polymer segmental dynamics.

In a binary or multi-component system, the case of $P = \sum P_i$, may be referred to as an ideal mixed gas transport system. It comes from the assumption that each single component behaves ideally, but the assumption will not hold when one of the permeants has a much higher perme-

ation flux than the other permeants. The non-ideality of this type of multi-component system must be accounted for to avoid invalid assumptions for permeability and permselectivity calculations. Models and descriptions of multi-component systems can be found in Petropoulos (1994), and Kamaruddin and Koros (1997).

In general, gas solubility in polymers increases with increasing gas condensibility. Condensibility can be measured as the gas critical temperature T_c , or the normal boiling point T_b . Diffusion coefficients of penetrants are found to decrease with increasing penetrant size. Diffusion coefficients in polymers are also sensitive to penetrant shape. Linear or oblong penetrant molecules like CO_2 exhibit higher diffusivities than those of spherical molecular shape of equivalent molecular volume such as CH_4 . Specific interactions between gas and polymer molecules (i.e., polarity) also affect gas solubility. Gases such as CO_2 , which has a quadrupole moment, are generally more soluble in polar polymers.

Crystallinity in polymers tends to reduce both penetrant solubility and diffusivity, thereby reducing permeability, which is generally undesirable. Polymer crosslinking reduces polymer segmental mobility; therefore, diffusion coefficients of the penetrant gas typically decrease with an increasing degree of crosslinking in the polymer. In lower molecular weight polymers, chains are more mobile and penetrant diffusivity decreases with increasing molecular weight. At higher molecular weights, when the concentration of chain ends is low, diffusivity is relatively independent of molecular weight as is solubility (Ghosal and Freeman, 1993).

Chapter 3

Experimental Apparatus and Methods

3.1 Membrane Preparation

Membranes are produced in various configurations including flat sheets, hollow fibres, capillaries, or tubes. Flat sheets are the most convenient for laboratory permeation tests. Dense flat sheet membranes are commonly made by melt extrusion or solution casting followed by solvent evaporation. Overviews of types of membrane formation have been done by Koros and Fleming (1993), and Pinnau and Freeman (2000).

In our studies, flat film membranes were prepared using the solution casting technique. The term "casting" indicates a laying down process of a polymer solution (often on a support) during preparation. A homogeneous polymer solution was first made by dissolving polymer powder or pellets in an appropriate solvent with continuous mixing. After pouring the polymer solution onto a thin glass plate, a casting knife was applied to obtain even thickness of the membrane. The glass plate was then set in a fume hood to allow the membrane to dry. The weight of glass plate was measured until it did not change over time, indicating that the solvent has evaporated completely. Dried membranes with support material were cut into desired configurations and

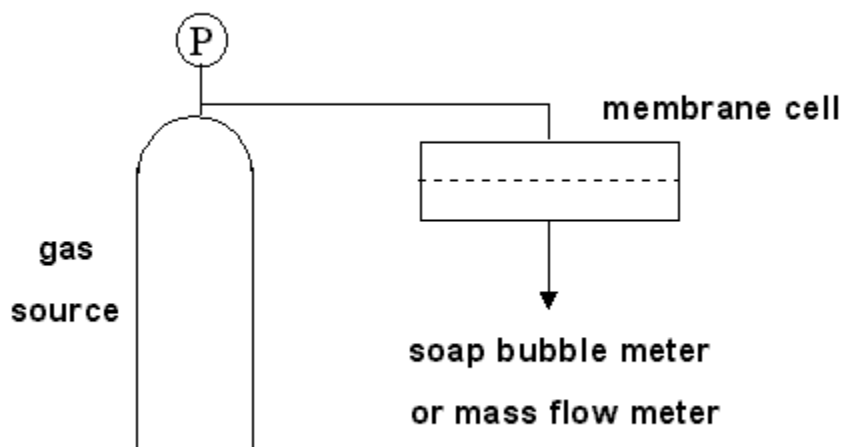


Figure 3.1: A schematic of gas permeation cell

placed in the membrane cell for permeation tests. Non-woven polyester fabric is used as our support material to obtain higher mechanical strength to the membranes during permeability tests. Gas permeation through the support fabric is neglected in our calculation since the gas resistance in the fabric is too small comparing to that in the membranes.

3.2 Membrane Module

Permeability measurements can be made using a simple experimental set-up. Figure 3.1 shows a schematic of a gas permeability testing apparatus (Mulder, 1991). It consists of an upstream gas source, a membrane cell, and a downstream device that measures the properties of the permeant. There are many types of apparatus used by researchers to measure permeabilities, but they are all based on two primary principles: constant pressure or constant volume. Constant volume/variable pressure and vacuum time-lag techniques are based on a constant volume principle whereas continuous flow techniques are based on a constant pressure principle.

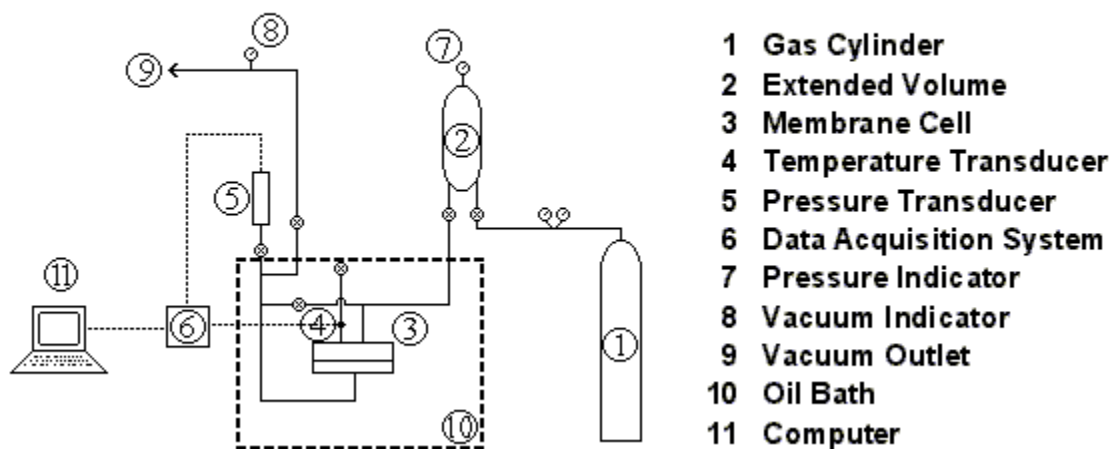


Figure 3.2: Gas permeation apparatus using constant volume/variable pressure method

The constant volume/variable pressure method has been described in detail by Pye et al. (1976). This method involved observing the pressure increase in a constant volume in which gas transport occurred, by employing a constant pressure difference between the two sides of a membrane. A schematic of a gas separation apparatus is shown in Figure 3.2. The membrane cell consists of two compartments separated by a membrane. A porous disk is placed in the bottom compartment of the cell to provide mechanical strength to the membrane such that the membrane can withstand the pressure difference employed during the experiments. The disk does not provide any resistance to the gas flow. An o-ring is placed in between the two compartments of the membrane cell to seal the cells.

Before experimentation takes place, the permeate side is kept under vacuum to remove residual air in the testing unit. During testing, the upstream pressure is kept constant, while an increase in downstream pressure of the permeate chamber is directly measured by the pressure transducer. Once steady state has been achieved, the pressure increase in the permeate chamber is

linear with time and the gas permeability coefficient can be calculated from the slope of the curve at steady state of pressure on the permeation side versus time.

In the continuous flow method, the permeant passes through the membrane under constant pressure differential, and into a flowing stream of inert carrier gas in the pressure compartment (Sridhar and Khan, 1999). Equipment setup from this method is very similar to that of the constant volume/variable pressure method, except that at the downstream side of the membrane cell, vacuum is replaced by a continuous gas carrier flow. By varying the carrier flow rate, the permeant gas partial pressure at the bottom membrane surface can be controlled, which also alters the driving force across the membrane. Helium or nitrogen are common carrier gases. This technique is advantageous in that the permeation rates can be easily adjusted by varying the carrier gas flow rate. This allows adjustment of the concentration of the permeant within the detectable range of the analyzer.

The vacuum time-lag method is currently a popular means to assess the permeability and diffusion coefficients of a gas through a polymer film for a given set of operating conditions (temperature and pressure). In this method, the permeate gas is allowed to accumulate in a pre-evacuated downstream volume. The mathematical analysis is based on the assumptions of a constant diffusion coefficient and constant membrane thickness (i.e. negligible swelling by permeant) throughout the entire permeation process.

Figure 3.3 illustrates a common plot obtained from time-lag method. The value of time-lag (θ) is determined from the x-intercept of the steady state tangent line. θ can be used to directly

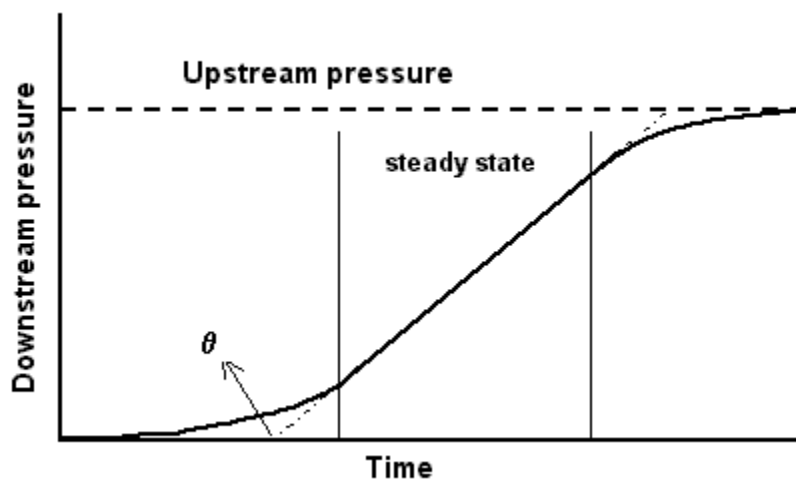


Figure 3.3: Determination of time-lag from a steady state permeation

calculate the permeate diffusion coefficient using the following expression:

$$\theta = \frac{L^2}{6D} \quad (3.1)$$

The variable L represents membrane thickness, and D is the diffusion coefficient. The framework and limitations of this technique, as well as some innovative attempts to apply to organic vapor, can be found in the recent studies of Yeom et al. (1999) and Favre et al. (2002).

In a recent review, Baker (2002) pointed out that data from the literature should be treated carefully. Some of the reported selectivities were based on the ratios from pure gas permeabilities, while others used a hard vacuum or sweep gas on the permeate side of the membrane. Both procedures yield high selectivities, but in an industrial plant, the feed gas will be at 100 to 150 psig and at a temperature sufficient to maintain the gas in the vapor phase. Furthermore, the permeate gas will be at a pressure of 10-20 psig. Under these operating conditions, plasticization and loss of selectivity occur with even the most rigid polymer membranes; therefore, under

industrial operating conditions, selectivities would usually be quite low.

Since the objective of this study could be achieved by collecting permeability data, a simple apparatus similar to that in Figure 3.1 was all that was required. A soap film bubble flow meter was connected at the downstream side of the membrane cell, and the permeate flow rate was determined using the bubble flow meter. Six readings were taken for each experiment to control for variability and ensure the flow had reached a steady state.

3.3 Permeation Tests

The experiments were performed at normal ambient lab temperature. Feed gas pressure came directly from a gas cylinder fitted with a pressure regulator and a test gauge. The downstream pressure was atmospheric, nominally assumed for all calculations to be 1 atm.

Stability of the membranes was determined by repeating tests over 24 hours, 72 hours, and a one week duration. These stability tests were performed at two or three times the normal testing pressure. This is referred to as "conditioning" of the membrane, and helps to increase gas flux once the membrane is stabilized. This stabilization is achieved when the interaction between the feed gas and the polymer chains reaches equilibrium.

Chapter 4

Poly(ethylene oxide) Membranes

Containing AgNO_3

4.1 Introduction

Olefin and paraffin gas mixtures are often found in petrochemical process streams. Some are a by-product of Liquefied Petroleum Gas production in crude oil refining. Olefins are a valuable feedstock for the production of commercial products such as polymers (polyesters, polyethylene, polypropylene, etc.), synthetic fluids, surfactants, additives, and specialty chemicals. Paraffins can be dehydrogenated to produce olefins of greater economic value.

Currently, the separation of ethylene and propylene from a light gas mixture is achieved by cryogenic distillation typical of the fractionation sequence used to recover olefins from ethylene reactor effluent streams and catalytic cracking reactors. The process is operated at a high pressure with a large number of trays and a high reflux ratio due to the close boiling points of the primary components. These systems are expensive to build and operate and are currently

only economically attractive for streams containing high quality olefins. Membrane technology may therefore be a very attractive alternative.

The objective of this section is to describe the development of an advanced membrane that exhibits high olefin permeability and olefin/paraffin selectivity. A further goal is to gain more knowledge regarding preparation and properties of poly(ethylene oxide) membranes containing a silver salt. The knowledge can then be further applied to advance the understanding of PEBAX[®] solid membranes (Chapter 5).

The basic transport mechanism of solution-diffusion has been illustrated in Chapter 2. Past studies of olefin/paraffin separation using facilitated transport membranes are reviewed in this chapter. An experimental design was used, and three main factors were considered. These factors are the weight-average molecular weight of PEO, the chemical form of silver salt, and the silver concentration in PEO.

4.2 Facilitated Transport

As described in Chapter 2, facilitated transport can dramatically improve membrane selectivity and permeability. In olefin/paraffin systems, it has been found that olefin transport can be facilitated by transition metal - most commonly cuprous and silver ions. Metal ions form a π -bond complexation with olefin molecules, which is described by the Dewar-Chatt model (see Figure 4.1 - Safarik and Eldridge 1998). The shaded areas in this diagram represent electron donor and acceptor interactions. Both the metal and alkene act as electron donors and acceptors in the complexation interaction. A sigma bond is formed between the overlap of the vacant outermost s atomic orbital of the metal and the full π molecular orbital of the olefin. A π component is formed by back-donation of electrons from the full outer d orbitals of the metal to the vacant

π^* (antibonding) molecular orbital of the olefin.

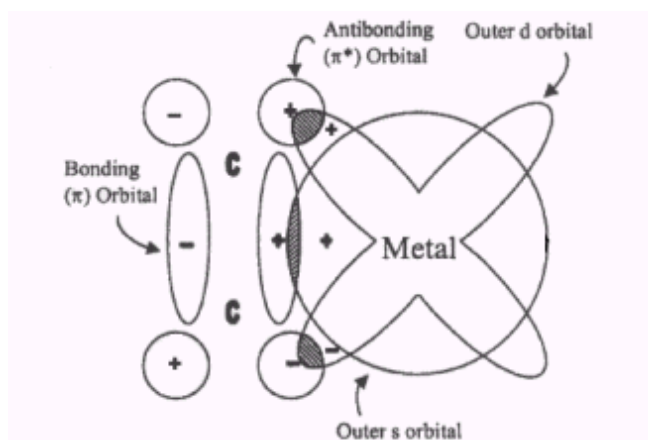


Figure 4.1: Dewar-Chatt model of π -bond complexation

The complexation reaction is fast enough to achieve high concentrations that drive the olefin fluxes. The reverse reaction should also be sufficiently fast to assure recovery of permeate molecules.

This separation process is based on the fact that complex-forming reactions enhance the permeation rate of olefin molecules. Paraffin molecules permeate through the membrane according to Fick's law of diffusion and at a lower rate than olefins, resulting in olefin/paraffin separations (Noble et al., 1989).

4.2.1 Background and Relevant Literature

Three configurations have been used to prepare membranes containing silver ions: supported liquid membranes, ion-exchange membranes, and salt/polymer membranes.

Gas separation using facilitated transport is most commonly carried out using "immobilized

liquid” membranes, prepared by dissolving the gas-carrier species in an appropriate solvent and using this solution to impregnate an electrically uncharged, rigid microporous matrix. The carrier species is then retained in the matrix by surface tension forces. Facilitated transport of gases via liquid membranes was first discussed in a review by Schultz et al. (1974). More work was done by Hughes et al. (1986) on silver-impregnated cellulose acetate membranes for both flat film and hollow fiber configurations. Teramoto et al. (1986; 1989) performed work on support and ”flowing” membranes for ethane and ethylene separation. Several limitations of this membrane type were pointed out by those investigations:

- * The tendency to degrade because the solution absorbed into the pores of the support membrane evaporates in the feed and sweep gas phase.
- * The inability to tolerate poisons to Ag^+ , such as acetylenes, H_2 , or H_2S .
- * A decline of performance due to water and/or Ag^+ loss.
- * Minimum pressure differential across the fiber wall is necessary to maintain optimum performance and maximize permeator lifetime.
- * The difficulty of making the membrane both thin and stable.

LeBlanc et al. (1980) introduced the ion-exchange type carrier membranes for olefin gas separations. With these membranes, silver ions are retained in the membrane by electrostatic interactions with the ion-exchange sites. They used a cation-exchange membrane of sulfonated polyphenylene oxide and obtained Ag^+ ions by soaking it in aqueous AgNO_3 . This type of membrane has a better ability to retain the carrier gas under operating conditions and there is no problem with solvent condensing on the high pressure side of the membrane to wash out the carrier. Hydrated Nafion cation exchange membranes containing Ag^+ ions and Na^+ ions for c-2-butene/t-2-butene separation were studied by Funke et al. (1993). Ho and Dalrymple

(1994) reported separations using poly(vinyl alcohol)-containing silver nitrate membranes in the thin film composite structure. The silver salt is trapped in the crosslinked poly(vinyl alcohol) matrix, yet ions are mobile in the hydrated polymer. Yamaguchi et al. (1996) compared an ion-exchange membrane (silver form Nafion) with a silver salt/polymer blend membrane (AgBF_4 /Nafion blend) on 1,3-butadiene/1-butene and 1,5-hexadiene/1-hexene systems.

Recent studies done by Yang and Hsiue (1998) reported gas transport properties of swollen complex membranes of linear low density polyethylene (LLDPE), silicone rubber (SR), and poly(1-trimethylsilyl-1-propyne) (PTMSP). The swollen complex membranes were constructed by dense matrix membranes, graft copolymers, metal ions, and the swelling agent. Low volatility glycerol impregnated in the membrane matrix served as the swelling agent of the film and as an activator of the Ag^+ complex.

The disadvantages of the above membranes include the need for addition of water, solvent, or swelling agent to the polymer matrix, and the need for some membranes to be operated with water-vapor-saturated feed and permeate streams. Downstream processing is still required to remove the extra component from the olefin-rich-permeate stream. Pinnau et al. (1997) was the first group to propose the use of solid polymeric membrane for olefin/paraffin separation. They report high pure-gas ethylene/ethane and propylene/propane selectivities using AgBF_4 in poly(ethylene oxide) or propylene oxide/allylglycidylether copolymer (PO-AGE) with a microporous poly(ether imide) membrane as the support material. With an increase in AgBF_4 loading, ethylene/ethane selectivity increases dramatically (from 160 to 2400 as AgBF_4 concentration increases from 50% to 80%). A similar increase is found for propylene/propane separation. The selectivities are significantly lower with mixed-gas permeation tests (2400 from pure-gas permeation vs. 120 from mixed-gas). The long term stability tests of this composite mem-

brane show a decrease in selectivity after 20 days. Pinnau and his group (Sunderrajan et al., 2001) recently compared four different silver salts (AgBF_4 , AgNO_3 , AgCF_3SO_3 , AgCF_3CO_2) in poly(ethylene oxide) (PEO) and found AgBF_4 to be the most soluble salt in PEO. Also, PEO membranes containing AgBF_4 showed a high ethylene/ethane selectivity of 240 (Pinnau and Toy, 2001). Other solid polymer materials such as poly(2,6-dimethyl-1,4-phenylene-oxide), poly(2-ethyl-2-oxazoline) (POZ), cellulose acetate, and poly(ether-*b*-amide) copolymer have also been studied for olefin/paraffin separation using silver salts as olefin facilitated transport carriers (Bai et al., 2000; Hong et al., 2001; Ryu et al., 2001; Morisato et al., 2001).

4.3 Experimental

Poly(ethylene oxide) (PEO) is a highly hydrophilic polymer. Three types of PEO with molecular weights of 1 million, 4 million, and 7 million g/mol, were purchased from Sigma-Aldrich Canada. The physical properties of PEO are summarized in Appendix A in Table A.1.

The structure of the PEO repeating unit is:



Flat films were prepared by the solution casting method as described in Chapter 3, and water was used as the solvent. Since high molecular weight PEO was used in the experiments, high solution viscosity could have resulted in uneven dispersion. To counteract this, the polymer solution was made with less than 2 % PEO solid by weight. For the samples with a molecular weight of 1 million and 4 million, 2% of polymer solution was prepared and for 7 million, the polymer solution only contained 1.5% PEO by weight. The polymer solutions were prepared at room temperature with vigorous stirring. After complete dissolution of the PEO in water, silver salt was added to the solution. In the mean time, the flask and rubber stopper was covered with foil to avoid light contact with the solution. The casting solution was then poured onto a glass

plate and left to air-dry for 3 days until the membrane was free of water.

AgNO_3 was selected as our source of silver salt in this study. Sunderrajan et al. (2001) suggested that silver salt ions can be solubilized by the polymer due to interaction of salt cations with electrons on a heteroatom in the polymer backbone such as the ether oxygens in PEO. The weight percentages of silver nitrate chosen are 50, 65, and 80, corresponding to 4:1, 2:1, and 1:1 molar ratios of oxygen atoms to silver atoms, respectively.

Due to difficulties in controlling the exact thickness of the membrane upon preparation, the thickness of the PEO membrane could not be pre-determined exactly. It was only possible to target a range of thickness. To control for this, thickness was measured after the membrane had been prepared.

4.4 Results and Discussion

Pure gas permeation tests were conducted using ethane and ethylene at room temperature, with a feed pressure of 100 psig. The thickness of the PEO membrane ranged from 70 to 90 μm . A full 2^3 factorial design with 3 centre point replications was set up for the experimental runs (see Appendix B Table B.1). Membrane thicknesses were represented as T1 (thickness 1) and T2 (thickness 2).

It was observed during the testing that membrane preparation was sensitive to light exposure. After adding silver salt to the polymer solution, the color of the solution gradually turned brown in color, indicating silver oxidation. The dried PEO membranes containing AgNO_3 became black and brittle after one day. Additionally, even when first formed/by this time, areas of uneven thickness could be seen on the surface of the membrane, which suggested membrane

defects. This was later confirmed by permeability tests.

Table 4.1 presents the result summary from the ethane and ethylene permeability tests. α_{AB} denotes pure gas selectivity of ethylene over ethane. Sample calculations on flux, permeability, and selectivity are included in Appendix C and raw data are in Appendix E. In some experimental runs, high selectivities of ethylene/ethane were observed; however, others showed almost no preferable selectivity over ethylene. Poor data reproducibility, even with the same membrane receipt, is apparent from the preliminary permeability results.

Table 4.1: Results from preliminary permeability tests of PEO membranes containing AgNO_3

no.	mol. wt.	Ag wt. %	permeability (Barrer)		selectivity
			ethane	ethylene	α_{AB}
1	1M	80	1562.48	1175.11	0.75
			21027.01	13602.94	0.65
			93.87	16272.78	173.35
2	1M	80	218784.28	184773.58	0.84
			164448.08	135412.52	0.82
3	4M	50	6945.50	65748.45	9.47
4	4M	50	209.07	6181.41	29.57
			3.64	6490.30	1782.39
			109.24	30.60	0.28
5	4M	50	553.06	327.83	0.59
6	7M	50	61.98	47.24	0.76
			19325.04	19706.40	1.02
			58.00	56.66	0.98
			1202.34	2152.18	0.56
			129.81	87.18	0.67

Pure PEO membranes were made during the course of experiments. Pinnau et al. (1997) reported in their study of PEO membranes containing AgBF_4 that pure PEO exhibits low ethylene/ethane selectivity of 1.2. However, our experiments were unable to obtain such a result from pure PEO membranes. All the pure PEO membranes, regardless of molecular weight,

showed extremely high gas flux, suggesting membrane defects. It is suspected that since PEO is a highly hydrophilic polymer, the relative humidity in the room may have affected the membrane structure during casting. This was verified by similar work which was later conducted by another member in the research group. A vacuum was installed to de-gas the dissolved air in the polymer solution, and the membranes were prepared in this vacuum rather than air-dried in a fume hood. The vacuum-dried PEO membranes were transparent, which stands in contrast to the translucent membrane the air-dried method produced. It is therefore likely that the membrane instability demonstrated in our trials was at least partly due to water and air trapped inside the polymer chain, which caused defects in the polymer structure.

Assuming that those of our membranes which did yield high ethylene/ethane selectivities were the ones that suffered the least from these defects, it is encouraging to note the relatively high selectivity that the PEO with AgNO_3 membrane showed. However, due to the fact that they appear to suffer structure damage from humidity and oxidation of silver salts, one must consider seriously the feasibility of employing this material in further testing. Since the preliminary results showed problems with membrane stability and inconsistent permeation data, the proposed experimental design was not carried out to completion. The experience and knowledge acquired from this investigation provided good groundwork in understanding membrane preparation and testing techniques, which we applied to the investigation of gas properties of PEBAX[®]2533 membranes (Chapter 5).

Chapter 5

Poly(ether-*b*-amide) Copolymer

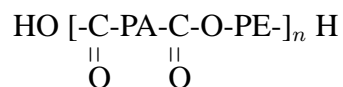
Membranes

5.1 Introduction

The history of polyether block amide (PEBA) resin can be dated to 1972 research initiatives by Atochem in which the goal was a "soft" nylon material. The actual polyether block amide polymer was commercialized in 1981 (Dennis and O'Brien, 2000).

Polyether block amide (PEBA) resin is best known under the trademark PEBA[®], and is a thermoplastic elastomer combining linear chains of rigid polyamide segments interspaced with flexible polyether segments. It is produced by polycondensation of a dicarboxylic polyamide and a polyether diol in the presence of heat, vacuum, and a catalyst (Cen et al., 2002).

The structure of the PEBA repeating unit is:



where PA is an aliphatic polyamide "hard segment" (i.e., Nylon-6 [PA6], or Nylon-12 [PA12]), and PE is an amorphous polyether "soft segment". The soft segment is either poly(ethylene oxide), or poly(tetramethylene oxide). This crystalline/amorphous structure creates a blend of properties of thermoplastics and rubbers. In application to permeation, the hard amide block provides the mechanical strength, whereas gas transport occurs primarily in the soft ether segments (Bondar et al., 2000).

Currently, the main commercial applications range from sporting goods (shoe soles), industrial equipment (conveyor belts), as well as functional films (breathable clothing, drying films) and various other materials.

5.2 Relevant Literature

Only in recent years have membranes based on PEBAX[®] polymer been investigated in separation processes. In the pulp and paper industry, recovery of methanol from water wet air streams is crucial to control hazardous air pollutant emissions. Rezac et al. (1997) evaluated the sorption and diffusion characteristics of water and methanol in a series of PEBAX[®] copolymers. Their results indicated that PEBAX[®] materials can be used to selectively separate methanol from air, but not methanol from water. The PEBAX[®] series in their study consist of Nylon-12 and polytetramethylene oxide of varying ratios. Among the four grades of PEBAX[®] (2533, 3533, 5533, and 6333), the 2533 grade was the most promising due to high permeation rates.

Djebbar et al. (1998) studied the pervaporation of three aqueous ethyl ester solutions with PEBAX[®] membranes of different polyamide composition ranging from 25 to 80 weight percent. PEBAX[®] was chosen as the material of interest due to its hydrophobicity and high se-

lectivity of aromatic organic compounds from water. The separation is considered to be an alternative for the extraction of volatile organic compounds (VOCs) from aqueous media. It was shown in this study that the use of PEBAX[®] membranes of high polyether content is most advantageous for VOCs extraction, as long as the polymer swelling from the penetrant is not excessive. PEBAX[®] grade 3533 was investigated for the pervaporation separation of isopropanol-water and ethyl butyrate-water mixtures (Sampranpiboon et al., 2000).

Bondar et al. (2000) found that in applications such as the removal of CO₂ from mixtures of hydrogen in syngas, PEBA was found to have high selectivity on polar or quadrupolar/nonpolar systems (e.g. CO₂/H₂ or CO₂/N₂). Bondar's group evaluated membranes made from four grades of PEBAX[®], which range from 80 to 53 weight percent of polyether (PE) in the block copolymer. The PEBAX[®] grades are 2533, 4011, 1074, 4033 in descending PE weight percent. Their sorption and permeation results suggest strong interaction between the polar gas CO₂ and the PE blocks in the copolymer. They found that PE composition and CO₂ permeability were directly correlated. Kim et al. (2001) reported the particular selectivity of CO₂ over N₂ is 61 and that of SO₂ over N₂ is 500. Strong affinity of polar species to the PE block is attributed to the high permeability and permselectivity of polarizable gases through PEBAX[®] copolymer.

Although PEBAX[®] copolymer has an excellent gas selectivity for organic gas separation in pervaporation and in polarizable/non polar gas mixture, there are almost no results regarding the permeation of hydrocarbons through PEBAX[®] membranes until a recent article by Morisato et al. (2001). This group utilized membranes based on PEBAX[®]2533 doped with AgBF₄ to separate ethylene and ethane. The group reported the value of mixed-gas ethylene/ethane selectivity to be less than 2 as the AgBF₄ concentration increased from 0 to 70%. The selectivity increased to 26 when the salt concentration was raised from 70 to 90%.

The objective of our study is to investigate the gas permeation process through a dry PEBAX[®] membrane from the view point of organic gas separation. Permeation experiments were conducted using pure gas feed. The effects of membrane preparation conditions and operating conditions on the separation performance of the PEBAX[®] membrane will be reported and compared with literature data.

5.3 Experimental

The hydrophobic PEBAX[®] (grade 2533) copolymer was supplied by ATOFINA Chemical, Inc. (Philadelphia, PA.). Physical property data for PEBAX[®]2533 are summarized in Table A.2 of Appendix A. PEBAX[®]2533 flat film was prepared by the solution casting method as previously mentioned in Section 3.1. Among choices of solvents, Kim et al. (2001) compared various solvents for the preparation of the PEBAX[®] polymer solution, and reported a 3:1 by weight mixture of 1-propanol and 1-butanol at 80°C gave best solubility to the copolymer. In this study, only 2533 grade of PEBAX[®] is used. It was found that either pure 1-propanol or 1-butanol can completely dissolve the polymer at 90°C while vigorously stirring over a 48-hour span. Therefore, 1-propanol, Certified ACS grade, was chosen to make a 3 weight percent PEBAX[®]2533 solution. The polymer solution was then poured into a Petri dish and dried at room temperature for 48 hours under the fume hood such that solvent can be completely removed.

Permeability tests of a single pure gas permeation through the membrane cells were performed in this study. The set-up of the permeation cell is shown in Figure 3.1. The permeation properties from six gases were studied. The six gases are nitrogen, carbon dioxide, ethane, ethylene, propane, and propylene. Gases were purchased from Praxair Inc., with at least 99% purity. The

studied pressures range from 25 psig to 200 psig and the temperatures of interest range from 25°C to 75°C. The permeation cell is placed in a 6-litre VWR circulation bath (Model 1167) with built-in temperature controller. Inside the bath, water was circulated to maintain constant temperature surrounding the permeation cell.

5.4 Results and Discussion

5.4.1 Effect of Permeation Time on Flux and Selectivity

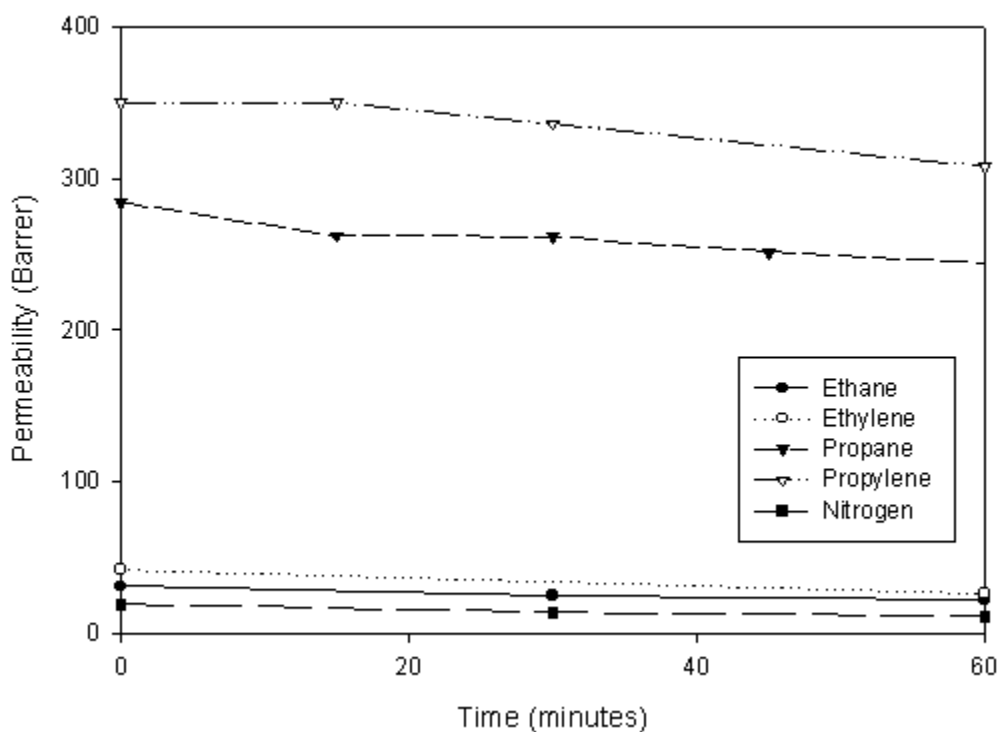


Figure 5.1: Time Dependency of permeability for PEBAx[®]2533(short term), P=75 psig.

The results of Figure 5.1 are from a series of short permeability tests, each lasting about one hour. A sample calculation is given in Appendix C, Section C.2 and raw data given in Ap-

pendix E. Each of the five gases (ethane, ethylene, propane, propylene, and nitrogen) was passed through a PEBAX membrane of 20 μm , with an upstream pressure of 75 psig. The results showed that C3 hydrocarbons (propane and propylene) have at least 7 times higher permeability than the C2 hydrocarbons (ethane and ethylene). Nitrogen was found to have the lowest permeability value of 10 Barrers after the first hour. These measurements reflect a fast check on the penetrant interaction with the membrane. It can be seen that the permeabilities of all five gases show a decreasing trend. This is an indication that interaction may occur between penetrant gas and the membrane material.

Permeability measurements were also taken for a much longer period of time to evaluate the time effect using another piece of 20 μm PEBAX membrane, as seen in Figure 5.2. Relative to other gases, permeabilities of propane and propylene took a longer time to stabilize. The results provide estimates for the conditioning period. It will take at least 24 hours of operation for ethane, ethylene or nitrogen and 72 hours for propane and propylene to give consistent results.

The extent of polymer-penetrant interaction can be seen in Figure 5.3. The values of the exponent in the power law model indicate that nitrogen has little interaction with PEBAX copolymer, whereas both ethylene and propylene have much stronger interaction with PEBAX. Similar trends are observed with ethane and propane permeation and the results are included in Appendix D, Figures D.1 and D.2.

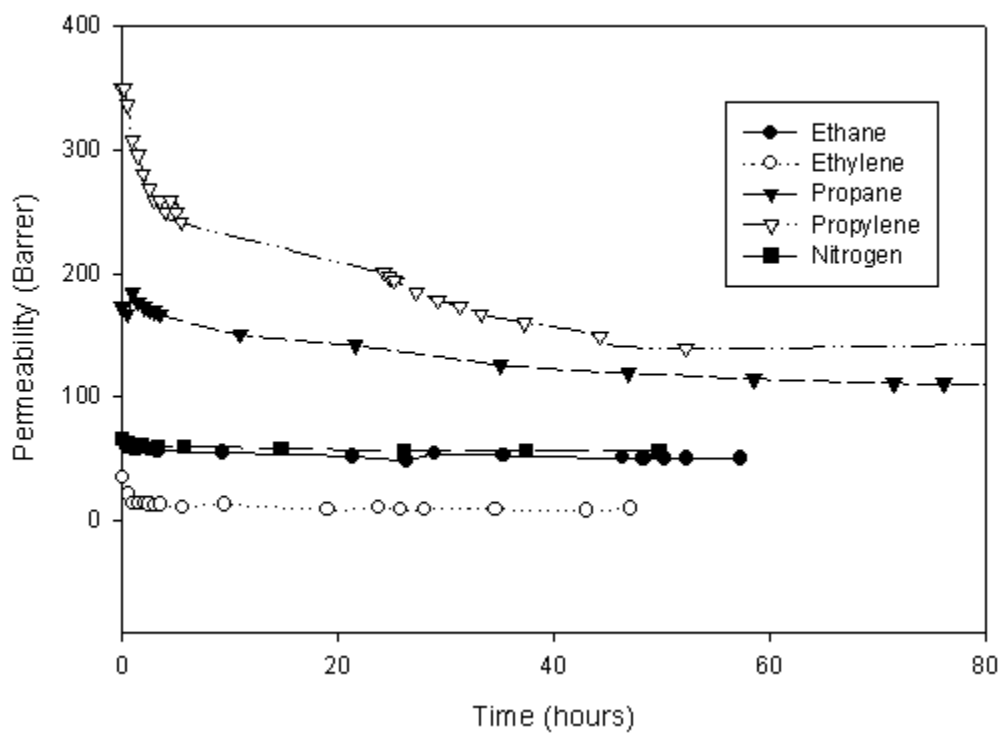


Figure 5.2: Time Dependency of permeability for PEBAx[®]2533 (long term)

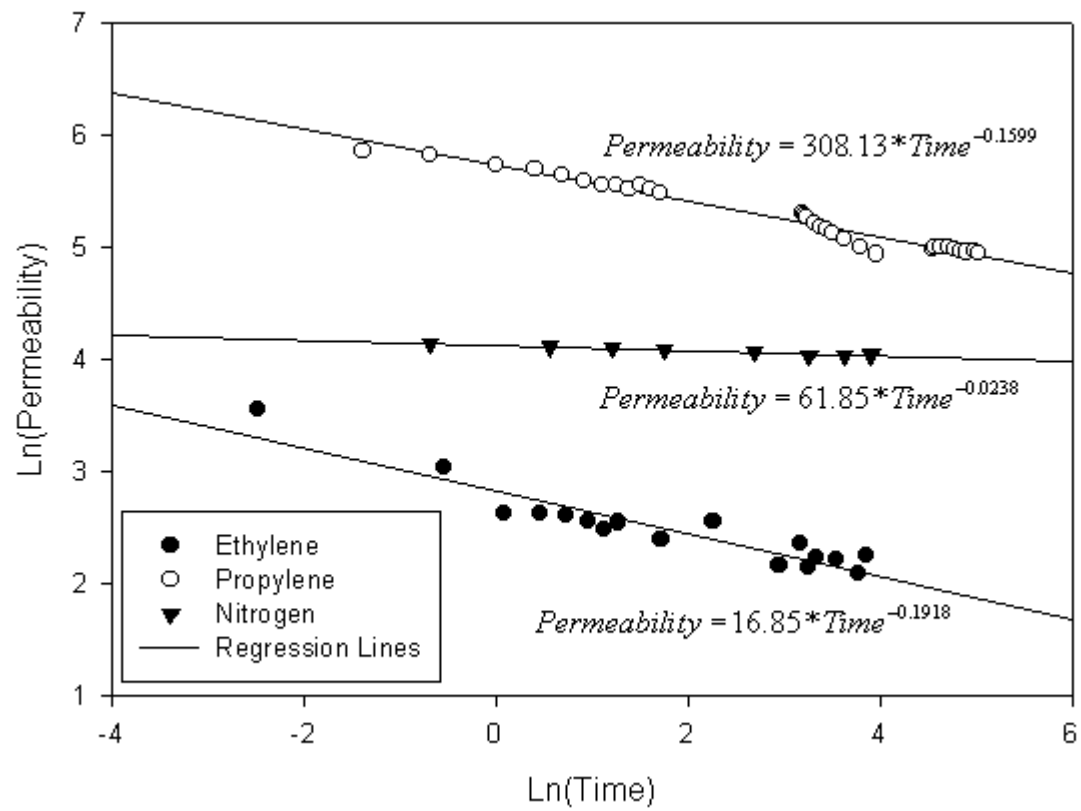


Figure 5.3: Log-log plot of permeability vs. time (Nitrogen, Ethylene, Propylene)

5.4.2 Effect of Pressure on Permeability and Selectivity

The permeabilities of PEBAX[®]2533 film were determined as a function of the feed pressure. The measurements were carried out at 25°C and pressures up to 100 psig. After the membrane had been conditioned with testing gas for three days under high pressure (200 psig) and room temperature, permeation measurements were taken while varying the feed pressure.

The permeabilities of ethane and ethylene have an almost linear relationship to feed pressures, as shown in Figure 5.4. This confirms the linear and positive response induced by an organic gas that permeates across a rubbery membrane (see Figure 2.5 (c), Section 2.3.2). Figure 5.5 presents the results from the propane and propylene permeability tests. The curved nature of the responses from propane and propylene indicates that plasticization was present in our testing pressure range. The plasticization pressure is defined by the lowest value on a permeability versus pressure curve, as shown in Figure 2.5 (d) (see Sections 2.3.2 and 2.3.3). The plasticization pressure for propane and propylene is estimated to be around 20 psig. Responses from ethane, propane and nitrogen were plotted together in Figure 5.6. The permeability of nitrogen is independent of gas pressure under the experimental conditions, representing an ideal case.

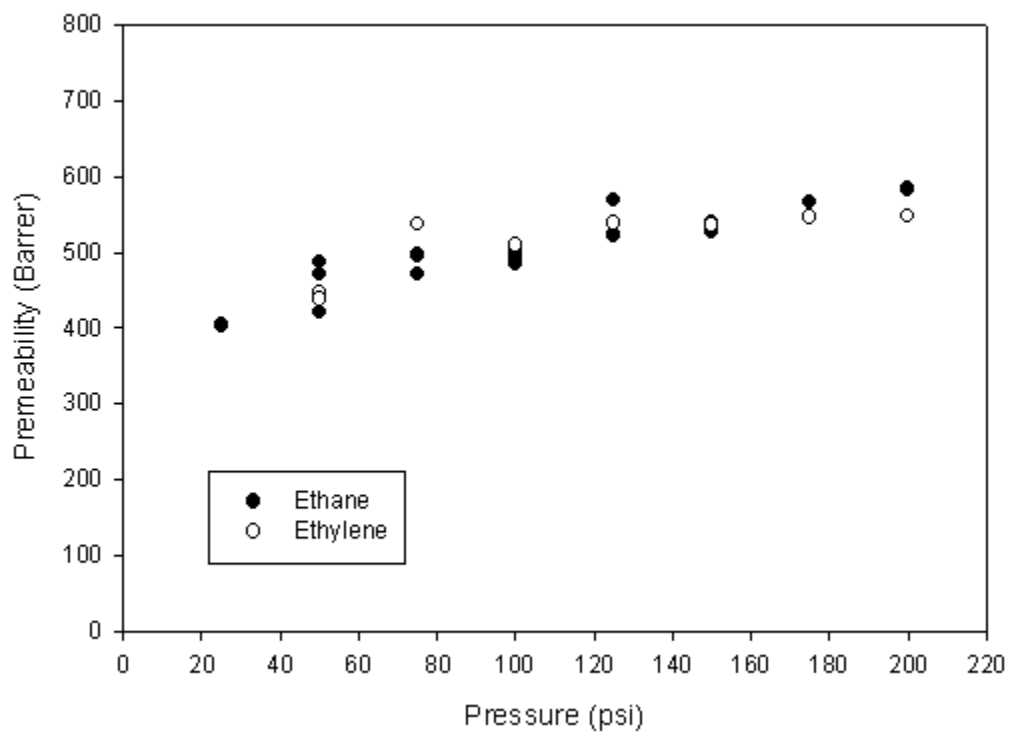


Figure 5.4: Permeability as a function of feed pressure (Ethane, Ethylene). Temperature: 25°C.

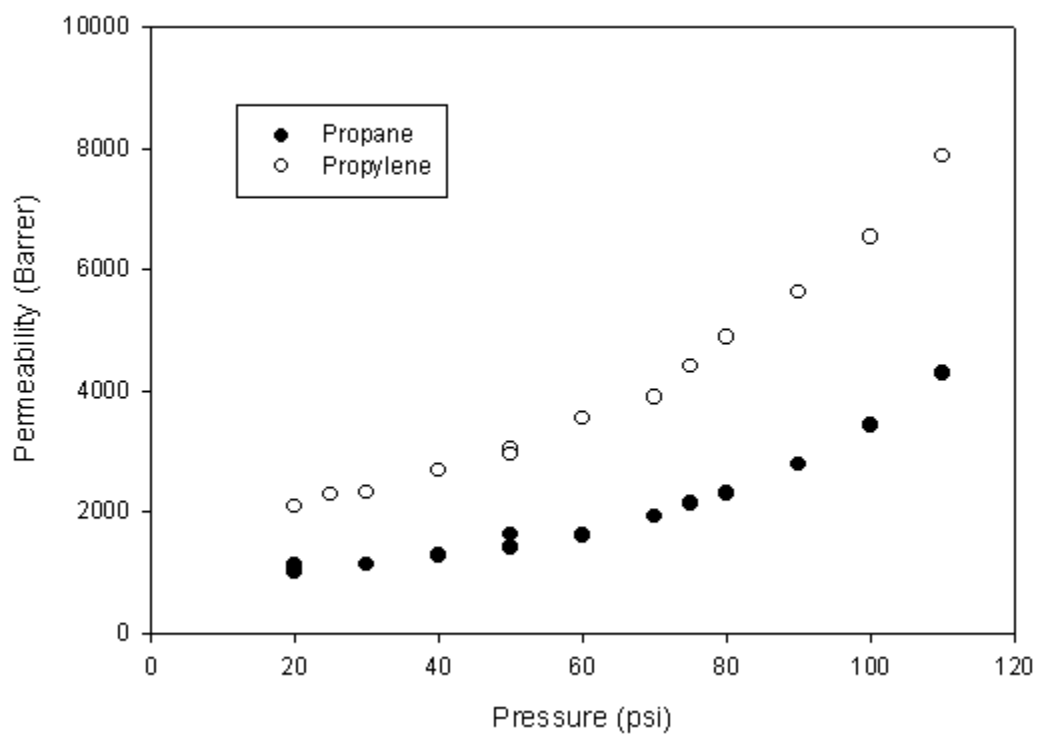


Figure 5.5: Permeability as a function of feed pressure (Propane, Propylene). Temperature: 25°C.

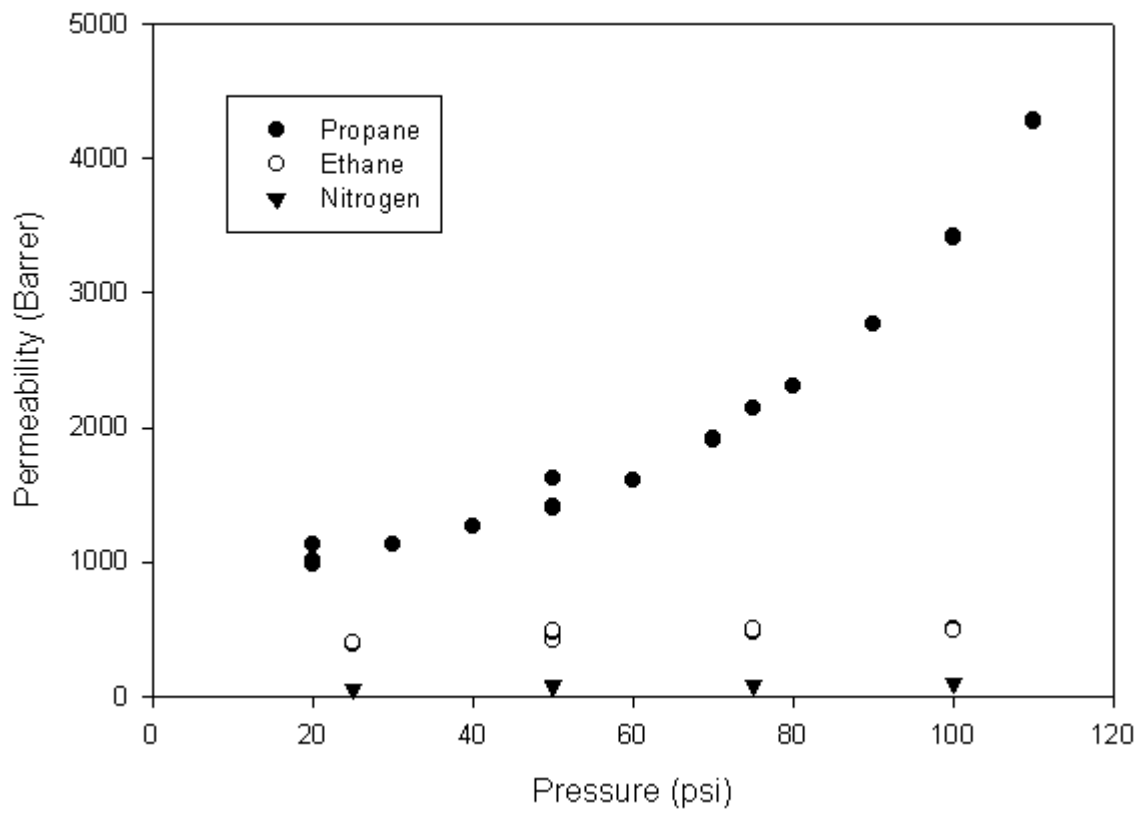


Figure 5.6: Permeability as a function of feed pressure (Nitrogen, Ethane, Propane). Temperature: 25°C.

At higher pressure, the permeabilities of propane and propylene strongly affect the selectivities for gas pairs involving propane and propylene. Table 5.1 presents the calculated selectivities of different gas pairs in relationship with pressure changes. Increasing trends in selectivity with pressure can be observed for the pairs of propylene/ethylene, propane/ethane, propane/nitrogen, and propylene/nitrogen. For the ethane/nitrogen and ethylene/nitrogen pairs, there was a slight decrease in selectivities when pressure was increased. This may be explained from Equation 2.8. Although gas diffusivity selectivity (D) increases as pressure (the driving force) increases, the solubility selectivity (S) of the gas into polymer decreases, causing a counter effect and thus reducing overall permselectivity. Selectivities remain constant for the ethane/ethylene and propane/propylene pairs, since pressure has similar effects on both components in the pairs.

Table 5.1: Pressure effect on selectivities of different gas pairs

pressure (psig)	selectivity			
	C_3H_8/C_3H_6	C_3H_8/C_2H_6	C_2H_6/C_2H_4	C_3H_6/C_2H_4
25	2.19	2.62	1.30	4.44
50	2.03	3.21	0.96	6.78
75	2.05	4.42	1.11	8.16
100	1.91	6.91	1.03	12.83
pressure (psig)	selectivity			
	C_3H_8/N_2	C_3H_6/N_2	C_2H_6/N_2	C_2H_4/N_2
25	20.89	45.85	7.96	10.32
50	19.40	39.46	6.05	5.82
75	24.74	50.78	5.59	6.22
100	36.31	69.45	5.25	5.41

5.4.3 "Memory" of PEBAX[®] 2533

To determine whether PEBAX has "memory" of prior permeations, after a set of pressure tests were run under various temperatures, another set of pressure tests were performed at 25°C. For propane gas, the second set of tests showed lower permeability than the first time, as seen in Figure 5.7. This indicates that with temperature and pressure changes, the PEBAX structures

are altered. Similar results were observed with ethane, as seen in Figure 5.8.

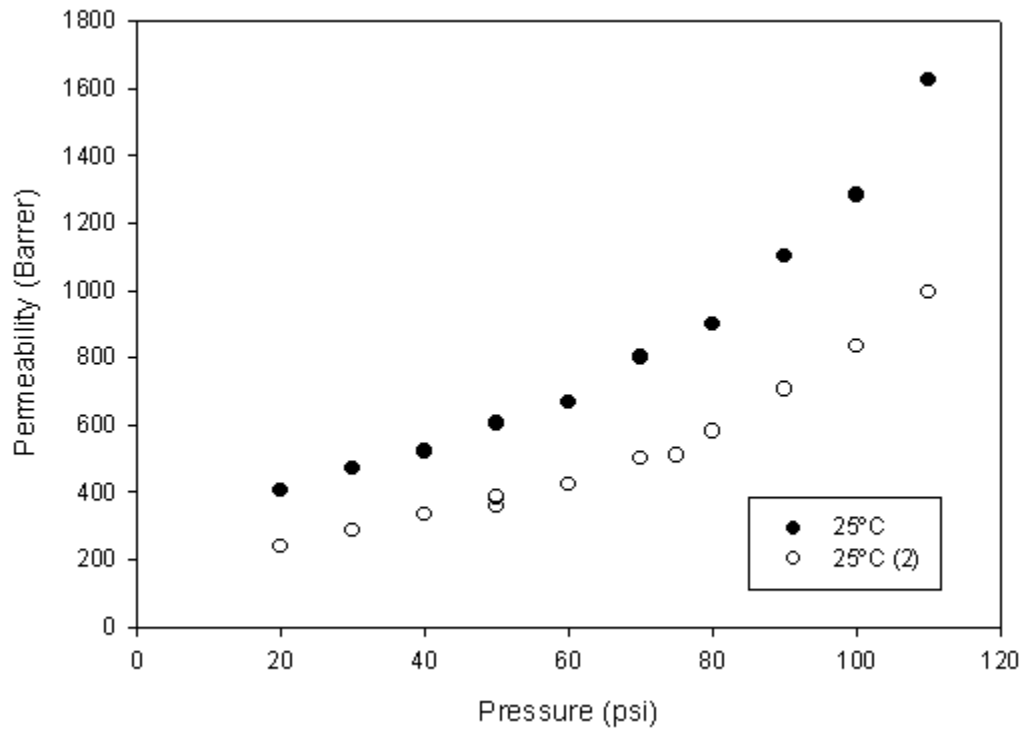


Figure 5.7: Permeability as a function of feed pressure. Propane through PEBAX[®] 2533

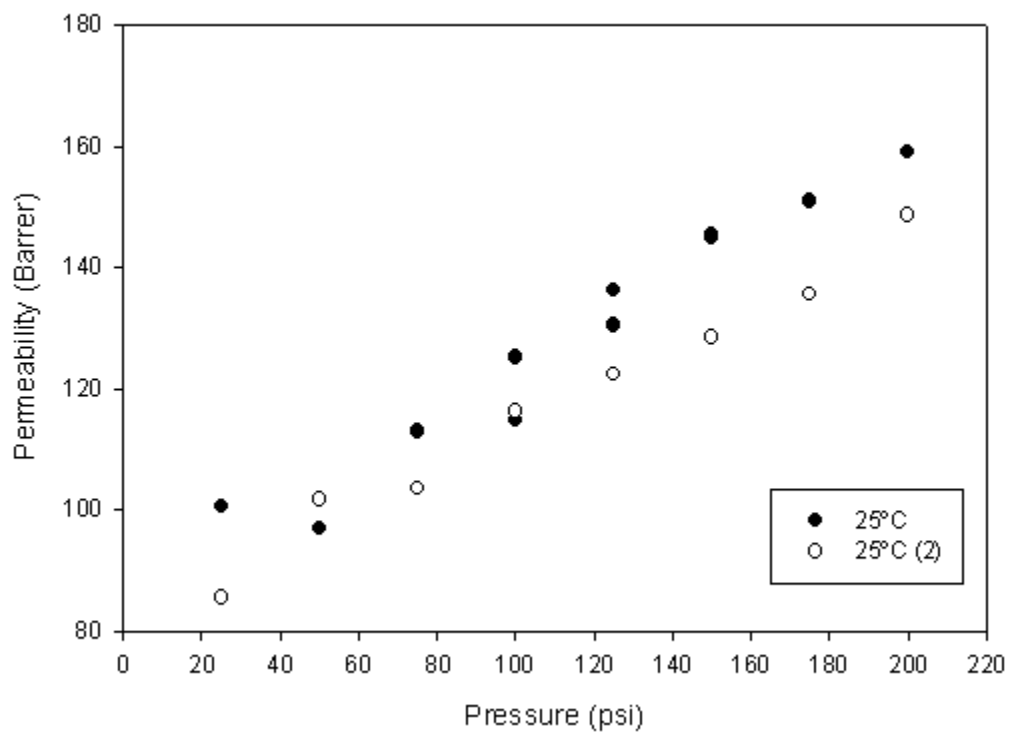


Figure 5.8: Permeability as a function of feed pressure. Ethane through PEBAX[®] 2533

5.4.4 Effect of Temperature

As discussed previously in Chapter 2, permeation is an activated process and the permeability coefficient can be approximated by an Arrhenius expression, as shown in Equation C.11. Figure 5.9 shows the temperature dependency of propane permeation. On a log-log graph, the relationship between permeability and inverse temperature is linear. Linear regression was applied to the permeability data and pre-exponential values and the activation energy of permeation were determined and are summarized in Table 5.2. Sample calculations on pre-exponential factor and activation energy values for permeation can be found in Appendix C. It can be seen clearly from Table 5.2 that as pressure increases, the activation energy of propane permeation decreases. Similar trends were observed for propylene, as seen in Figure 5.10.

Nitrogen shows a distinctly different trend from propane and propylene. Figure 5.11 shows that all regression lines are similar in slope and position. Comparing with results from the propane tests (same as in Table 5.2), nitrogen has both a higher pre-exponential value and activation energy (see Table 5.3). Ethane and ethylene exhibit similar behavior to nitrogen, but there is a slight decrease in activation energy as pressure increases (see Figure 5.12). This indicates that the permeability of nitrogen in PEBA-X is not affected by the temperature changes and that C3 hydrocarbons are more affected by temperature than C2 hydrocarbons are.

Plots of temperature dependency of ethane, and ethylene permeability are included in Appendix D, Figures D.3 and D.4. Table D.1 compares calculated values of pre-exponential factors and activation energy for ethane and ethylene.

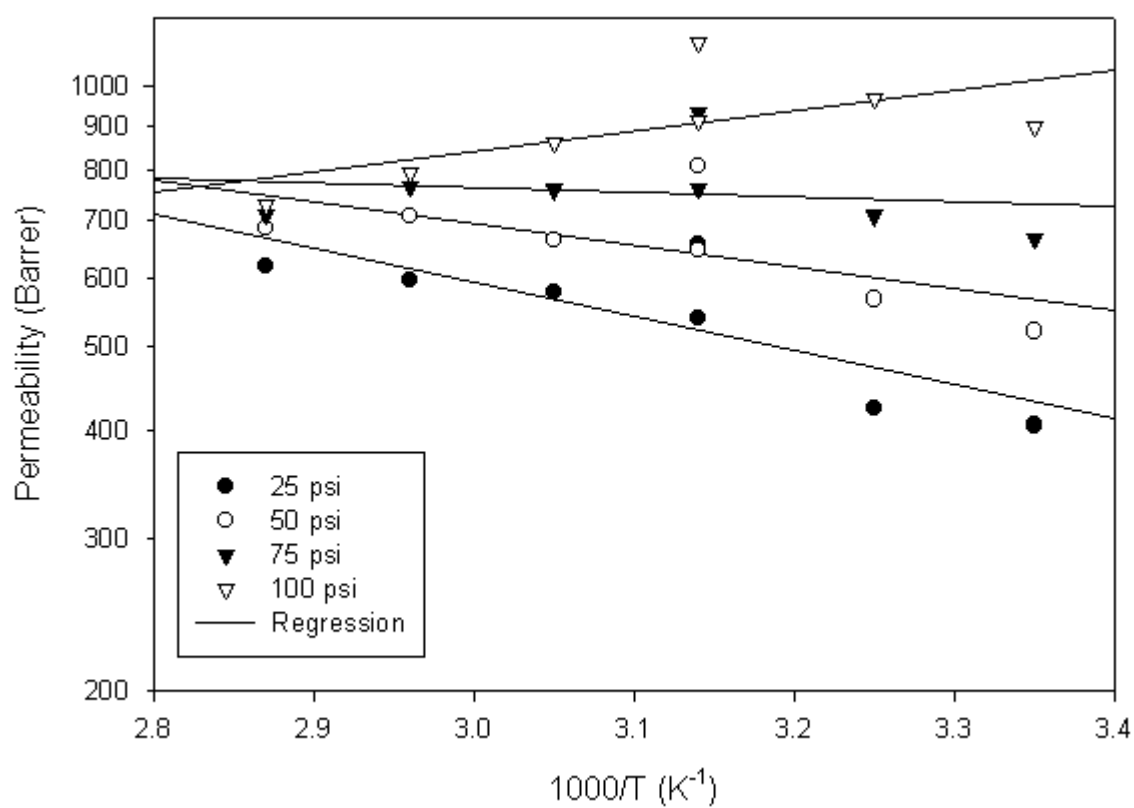


Figure 5.9: Temperature dependency of propane permeability in PEBAX[®] 2533

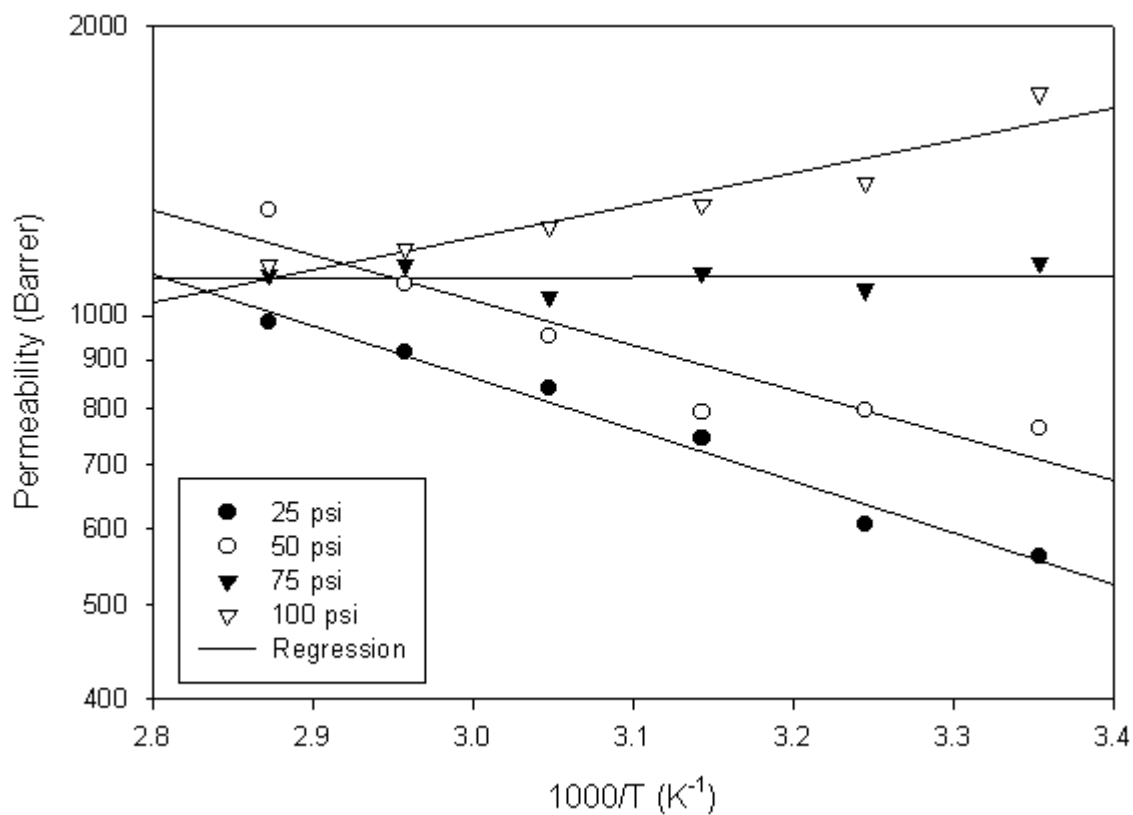
Figure 5.10: Temperature dependency of propylene permeability in PEBAX[®] 2533

Table 5.2: Calculated values of pre-exponential factors and activation energy for propane and propylene permeation

pressure (psig)	propane		propylene	
	P ₀ (Barrer)	E _p (KJ/mol.K)	P ₀ (Barrer)	E _p (KJ/mol.K)
25	10281.23	7.99	52950.46	11.39
50	4413.56	5.22	18960.75	8.08
75	1259.78	1.47	847.47	-0.66
100	187.63	-4.07	90.51	-7.09

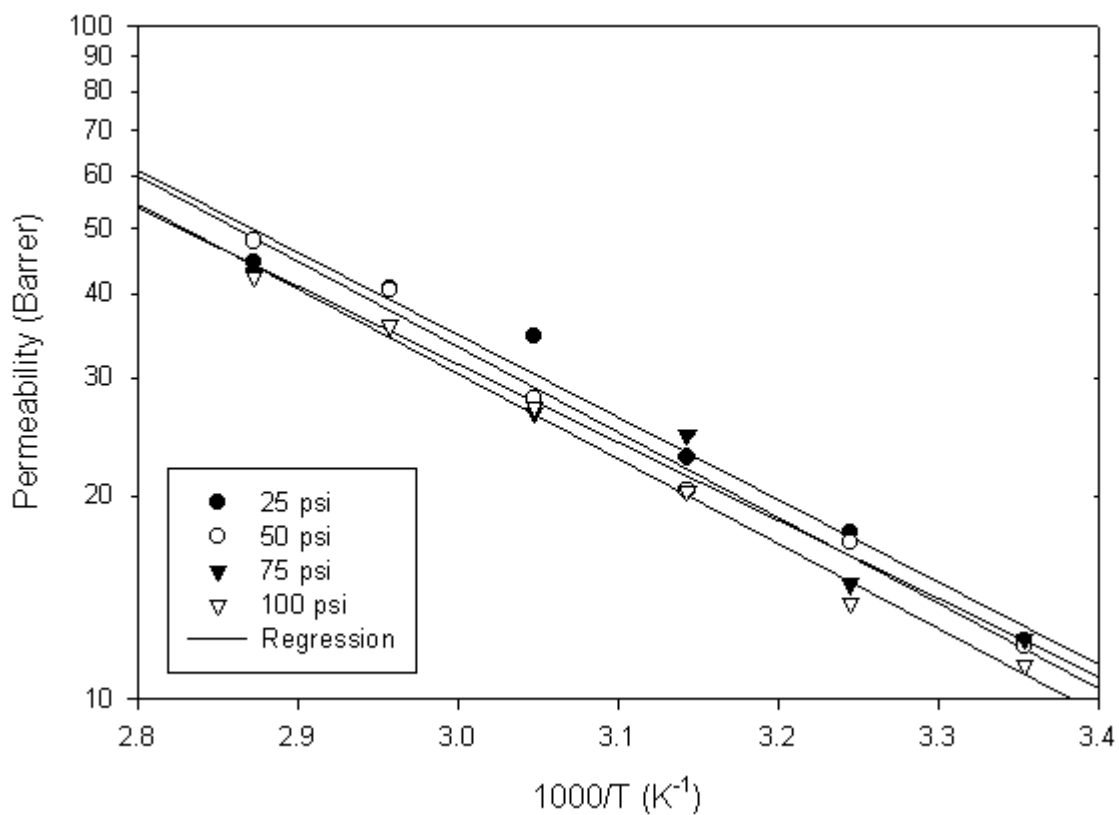
Figure 5.11: Temperature dependency of nitrogen permeability in PEBAX[®] 2533

Table 5.3: Calculated values of pre-exponential factors and activation energy for propane and nitrogen permeation

pressure (psig)	propane		nitrogen	
	P ₀ (Barrer)	E _p (KJ/mol.K)	P ₀ (Barrer)	E _p (KJ/mol.K)
25	10281.23	7.99	161337.91	23.40
50	4413.56	5.22	211336.77	24.26
75	1259.78	1.47	96566.12	22.26
100	187.63	-4.07	185817.33	24.16

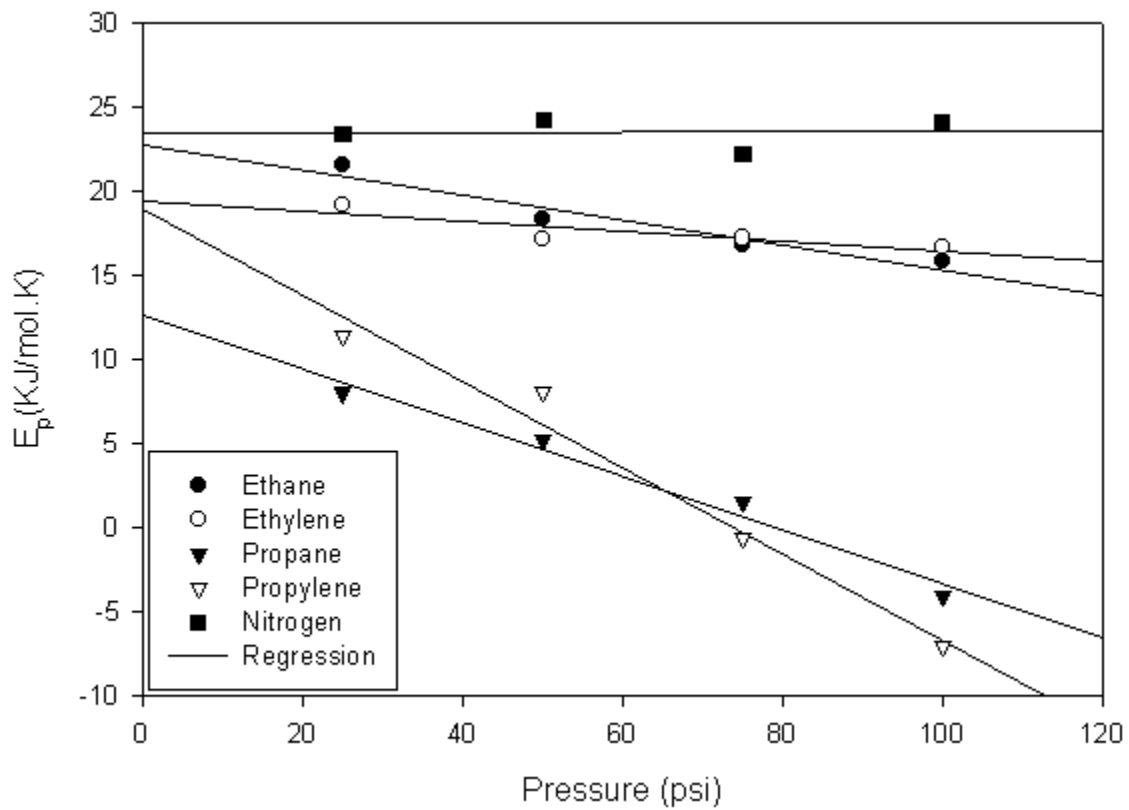


Figure 5.12: Pressure dependence of activation energy of permeation

5.4.5 Polar vs. Non-Polar Gases

In permeation studies done by Kim et al. (2001), Kim and Lee (2001), and Bondar et al. (2000), PEBAX[®] membranes have shown high selectivities for separations of CO₂/N₂. Kim et al. (2001) reported that as temperature increases, the selectivity of CO₂/N₂ decreases. To confirm the above findings, CO₂ and N₂ permeability tests were conducted at temperatures ranging from 25°C to 75°C at pressures of 25 and 50 psig. Selectivities of CO₂/N₂ were plotted against inverse temperature (1000/T), shown as Figure 5.13. Figure 5.14 is taken from Kim and Lee (2001), who used PEBAX[®] 1657 at a pressure of 3 atm. Although a different grade of PEBAX[®] was used in our experiments, a similar trend is observed for the temperature dependency of CO₂/N₂ separation using this type of copolymer. Our study verified that selectivity of polar and non-polar gas pairs using PEBAX[®] membranes is high and it has an inverse temperature dependency.

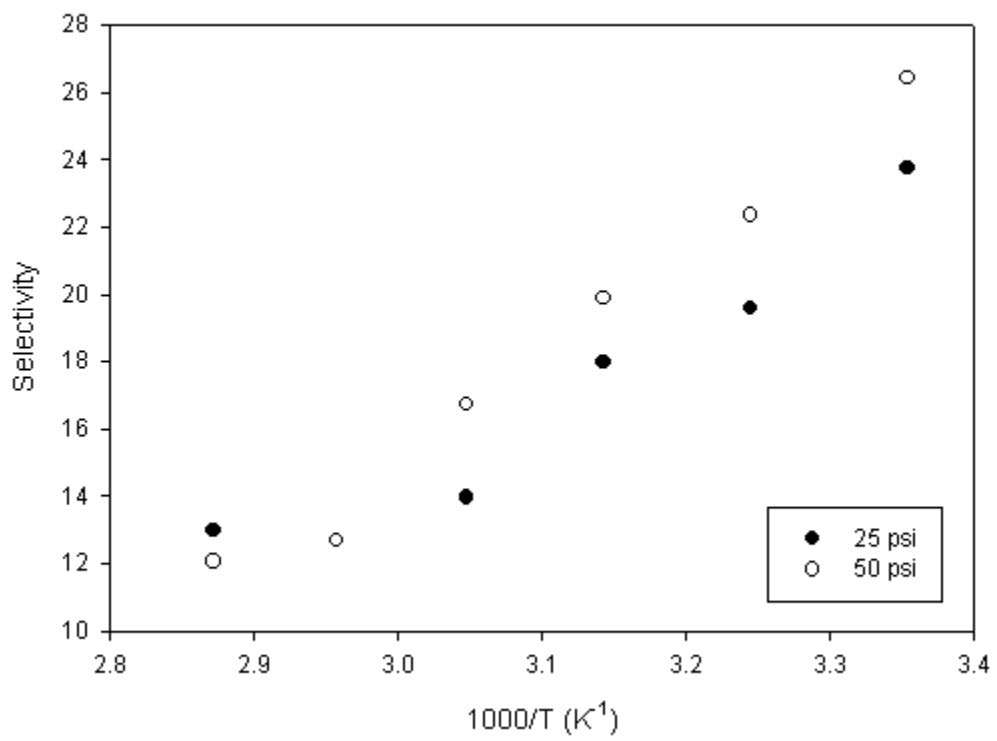


Figure 5.13: Temperature dependency of CO₂/N₂ selectivity for PEBAx[®]2533

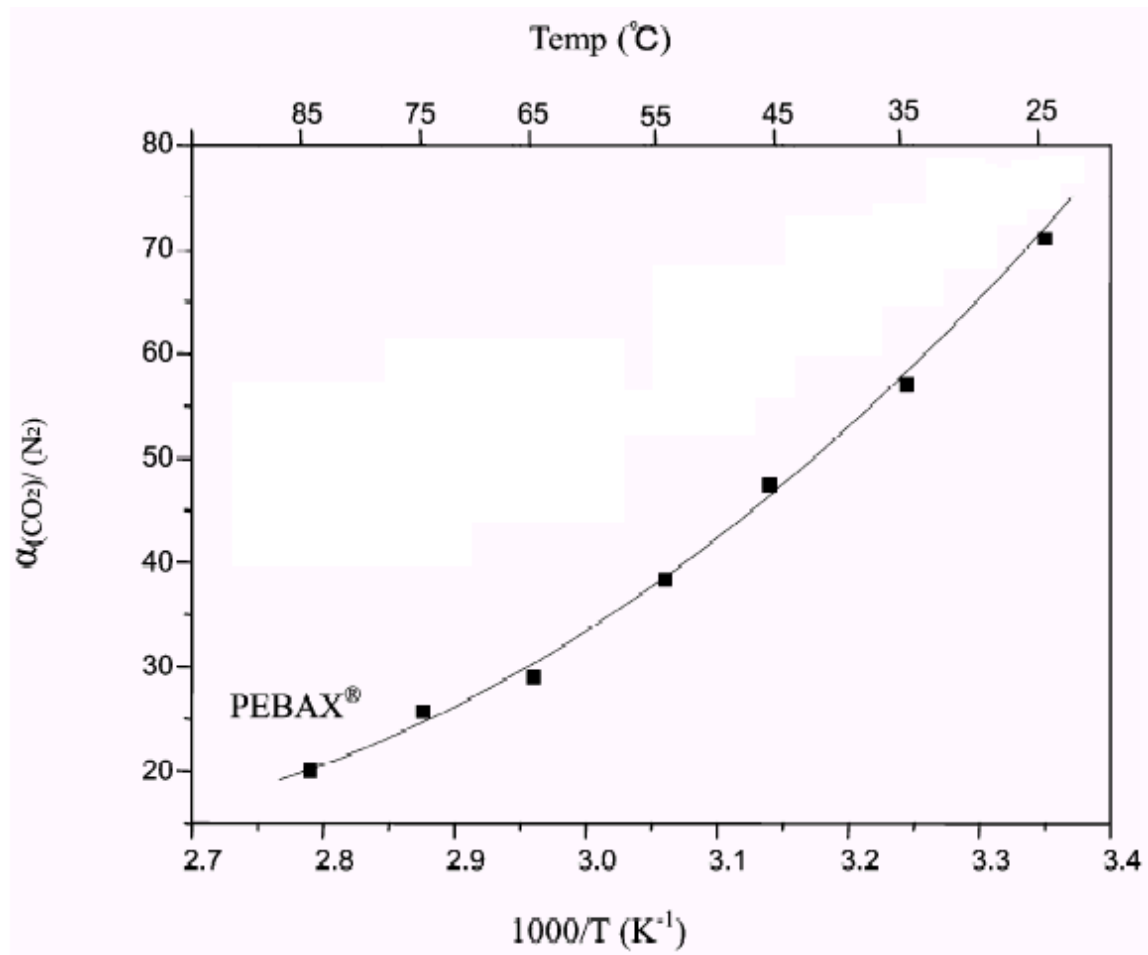


Figure 5.14: Selectivity of CO₂/N₂ versus Temperature from Kim and Lee (2001)

Chapter 6

Concluding Remarks and Recommendations

6.1 Concluding Remarks

The gas permeation properties on two types of polymeric membranes for hydrocarbon gas separations have been investigated. One is poly(ethylene oxide) containing AgNO_3 and the other is poly(ether-*b*-amide) PEBAX[®]2533 block copolymer.

The permeability results from PEO membranes containing AgNO_3 were compared with results from PEO membranes containing AgBF_4 from Pinnau et al. (1997). However, since the prepared PEO containing AgNO_3 membranes gave inconclusive permeability results for ethane and ethylene separations under operating conditions of 100 psig and room temperature, only pure PEO gas properties were discussed. The inconclusive results likely stem from membrane instability and defects due to flaws with the method of preparation and the oxidation of silver salts.

The second polymer material, PEBAX[®]2533 membranes showed high hydrocarbon permeation. The permeability of PEBAX[®]2533 film was determined as a function of feed pressures and operating temperatures. Permeation properties obtained from propane and propylene indicate plasticization effects on the PEBAX[®]2533 polymer matrix. Nitrogen showed no interaction with the membrane material, which is considered ideal. Permeabilities of propane and propylene are strongly affected by both temperature and pressure. This is consistent with observations in the literature. As pressure increases, the permeability of propane and propylene increases. Their temperature dependency of permeation can be approximated by Arrhenius expressions and it is found that the activation energy of permeation decreases as pressure increases. Due to the polar nature of this membrane material, it has been investigated for separating polar and non-polar gas pairs. CO₂/N₂ separation is temperature sensitive with PEBAX and higher selectivity is achieved at lower temperature.

6.2 Recommendations

Based on this work, some recommendations that may provide further insight into gas separation membranes are listed below.

First of all, systematic methods to investigate reasons for membrane defects should be pursued with PEO membranes containing silver salts. Different silver salts may be used for this investigation to validate literature data. In the literature, it has been noted that there is a lack of detailed preparation method. Since membrane preparation can greatly affect membrane properties, it is important to eliminate the possibility of causing defects due to improper membrane preparation.

Secondly, mixed gas permeability tests may be conducted using PEBAX[®]2533 membranes.

As mentioned in the background section, gas selectivities calculated from pure gas permeability can only give partial insight into the separation system. In order to account for effects of multicomponent cases, it is not sufficient to use pure gas permeation data only.

Thirdly, from collected permeation data on PEBAX membranes, optimal operating conditions can be determined for each gas pair to achieve highest permeability and selectivity.

Finally, silver-doped PEBAX may be prepared and tested, so the results can be compared against reported literature data by Morisato et al. (2001).

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Appendix A

Physical Properties of Polymers

All data are from manufacturer's information unless otherwise noted. T_g : Glass transition temperature; T_m : melting point.

A.1 Poly(ethylene oxide)

Table A.1: Selected Properties of Poly(ethylene oxide)

density	1.111 g/cm ³
T_m	60-63 °C
flash point	270 °C
percent volatile	0.15 %
T_g	-60 °C
Inhibitor	200 - 500 ppm BHT

A.2 PEBAX[®]2533

Results from characterization study done by Bondar et al. (2000) are based on elemental analysis, differential scanning calorimetry (DSC) and wide-angle X-ray diffraction spectroscopy (WAXD). PE: Poly(tetramethylene oxide); PA: Polyamide 12 (Nylon-12).

Table A.2: Selected Properties of PEBAX[®]2533

density	1.01 g/cm ³
melting point (ASTM D3418)	147.78 °C
hardness (D2240)	25 Shore D
ultimate tensile strength (D638)	4950 psi
ultimate elongation (D638)	640 %
weight percent PE	80
T_g	-77 °C
T_m (PE)	9 °C
T_m (PA)	126 °C
crystallinity in PA block	14 % by weight

Appendix B

Preliminary Design Data

Table B.1: Factorial design on PEO permeability tests

Trial	Coded Value			Operating Conditions		
	A	C	D	PEO Mwt	Ag (wt.%)	Thickness
1	1	1	1	7.00E+06	80	T1
2	1	1	-1	7.00E+06	80	T2
3	1	-1	1	7.00E+06	50	T1
4	1	-1	-1	7.00E+06	50	T2
5	-1	1	1	1.00E+06	80	T1
6	-1	1	-1	1.00E+06	80	T2
7	-1	-1	1	1.00E+06	50	T1
8	-1	-1	-1	1.00E+06	50	T2
center 1	0	0	1	4.00E+06	65	T1
center 2	0	0	1	4.00E+06	65	T1
center 3	0	0	1	4.00E+06	65	T1
center 4	0	0	-1	4.00E+06	65	T2
center 5	0	0	-1	4.00E+06	65	T2
center 6	0	0	-1	4.00E+06	65	T2

Appendix C

Sample Calculations

C.1 PEO Tests

Results in Table 4.1 were obtained from the calculations detailed below.

In experiment no. 1, PEO molecular weight of 1 million g/mol containing 80% silver, a flat film membrane with an average of 80 μm in thickness was prepared. The diameter of the membrane cross section was 3.5 cm. When pure ethane gas was fed at 100 psig, the measured downstream flow of 1 mL takes an average of 9.49 seconds. Assuming temperature of 23°C and pressure of 1 atm, the flow rate can be corrected to standard temperature and pressure (STP):

$$PV = nRT \quad (\text{C.1})$$

$$\frac{V_1}{V_2} = \frac{T_1}{T_2} * \frac{P_2}{P_1} \quad (\text{C.2})$$

$$P_1 = P_2 = 1\text{atm} \quad (\text{C.3})$$

$$\text{flow rate } (\dot{V}) = \frac{V}{\text{time}} \quad (\text{C.4})$$

$$\dot{V}_{STP} = \frac{T_{273K}}{T_{296K}} * \dot{V}_{296K} \quad (\text{C.5})$$

Ethane flux is, therefore,

$$\begin{aligned}
 \text{Flux} &= \frac{\dot{V}_{STP}}{\text{membrane area}} \\
 &= \frac{1 \text{ mL} \left| \begin{array}{c} 273.15 \text{ K} \\ 9.49 \text{ sec} \end{array} \right|}{1/4 * \pi * (3.5)^2 \text{ cm}^2} \left| \begin{array}{c} 1 \text{ cm}^3 \\ 1 \text{ mL} \end{array} \right| \\
 &= 0.0101 \text{ cm}^3 \text{ (STP) / cm}^2 \text{ sec}
 \end{aligned}$$

According to Equation 2.4, the ethane permeability can be calculated,

$$P_A = \frac{N_A}{(p_1 - p_2)/l} = \frac{N_A}{(\Delta p/l)} \quad (\text{C.6})$$

$$\begin{aligned}
 P_{ethane} &= \frac{0.0101 \text{ cm}^3 \left| \begin{array}{c} 80 \mu\text{m} \\ \text{cm}^2 \text{ sec} \end{array} \right|}{100 \text{ psi} \left| \begin{array}{c} 1 \text{ cm} \\ 10^4 \mu\text{m} \end{array} \right|} \left| \begin{array}{c} 14.696 \text{ psi} \\ 760 \text{ mmHg} \end{array} \right| \left| \begin{array}{c} 10 \text{ mmHg} \\ 1 \text{ cmHg} \end{array} \right| \\
 &= 1.562 * 10^{-7} \text{ cm}^3 \text{ cm / cm}^2 \text{ sec cmHg}
 \end{aligned}$$

Since 1 Barrer = $1 * 10^{-10} \text{ cm}^3 \text{ (STP) cm / cm}^2 \text{ sec cmHg}$,

$$P_{ethane} = 1562 \text{ Barrer}$$

Similarly, ethylene permeability can be calculated as 1175 Barrer. α_{AB} denotes the pure gas selectivity of ethylene over ethane and can be calculated as the ratio of ethylene permeability to ethane permeability.

$$\begin{aligned}
 \alpha_{AB} &= \frac{P_{ethylene}}{P_{ethane}} \\
 &= \frac{1175 \text{ Barrer}}{1562 \text{ Barrer}} \\
 &= 0.75
 \end{aligned} \quad (\text{C.7})$$

C.2 PEBAX Tests

Permeabilities were calculated in the same manner as in the previous section. For clarity, another example from PEBAX[®]2533 tests is taken to show the detailed calculation. The raw data for this section can be found in Appendix E.

Referring to Figure 5.1, the permeability for PEBAX[®]2533 at 30 minutes, using propane gas:

$$\begin{aligned}
 \text{membrane thickness} &= 20 \mu\text{m} \\
 \text{pressure} &= 75 \text{ psig} \\
 \text{membrane diameter} &= 3.5 \text{ cm} \\
 \text{temperature} &= 23^\circ\text{C} \\
 \text{pressure} &= 1 \text{ atm}
 \end{aligned}$$

The measured downstream propane flow of 1 mL takes an average of 18.88 seconds. The propane flux at standard temperature and pressure (STP) is:

$$\begin{aligned}
 \text{Flux} &= \frac{\dot{V}_{STP}}{\text{membrane area}} \\
 &= \frac{1 \text{ mL} \left| \begin{array}{c} 273.15 \text{ K} \\ 1 \text{ cm}^3 \end{array} \right.}{18.88 \text{ sec} \left| \begin{array}{c} 296.15 \text{ K} \\ 1/4 * \pi * (3.5)^2 \text{ cm}^2 \\ 1 \text{ mL} \end{array} \right.} \\
 &= 0.005 \text{ cm}^3 \text{ (STP) / cm}^2 \text{ sec}
 \end{aligned}$$

Propane permeability is:

$$\begin{aligned}
 P_{\text{propane}} &= \frac{0.005 \text{ cm}^3}{\text{cm}^2 \text{ sec}} \left| \frac{20 \text{ } \mu\text{m}}{100 \text{ psi}} \right| \left| \frac{1 \text{ cm}}{10^4 \text{ } \mu\text{m}} \right| \left| \frac{14.696 \text{ psi}}{760 \text{ mmHg}} \right| \left| \frac{10 \text{ mmHg}}{1 \text{ cmHg}} \right| \\
 &= 2.619 \cdot 10^{-8} \text{ cm}^3 \text{ cm} / \text{cm}^2 \text{ sec cmHg}
 \end{aligned}$$

$$1 \text{ Barrer} = 1 \cdot 10^{-10} \text{ cm}^3 \text{ (STP) cm} / \text{cm}^2 \text{ sec cmHg}$$

$$P_{\text{propane}} = 261.9 \text{ Barrer}$$

Permeability vs. Time, Figure 5.3

Relationship between permeabilities and the permeation time can be fitted to power law models. Using nitrogen permeability as an example, the coefficient and exponent of the model are calculated as follows:

time (hour)	N ₂ permeability (Barrer)	Ln(time)	Ln(permeability)
0.000	66.669	N/A	4.200
0.500	62.655	-0.693	4.138
1.750	60.943	0.560	4.110
3.333	60.304	1.204	4.099
5.750	59.663	1.749	4.089
14.750	58.630	2.691	4.071
26.083	56.112	3.261	4.027
37.417	56.661	3.622	4.037
49.750	56.711	3.907	4.038

$$Permeability = a * Time^b \quad (C.8)$$

$$Ln(permeability) = b * Ln(time) + Ln(a) \quad (C.9)$$

The slope and y-intercept of the regression line were estimated using least squares, and they are -0.0238 and 4.125, respectively.

$$\begin{aligned} exponent &= -0.0238 \\ coefficient &= e^{y-intercept} \\ &= 61.85 \end{aligned}$$

Thus, for nitrogen,

$$Permeability = 61.85 * Time^{-0.0238} \quad (C.10)$$

Temperature Dependency of Permeability

As mentioned in Chapter 2, Section 2.3.1, temperature dependence of permeability can be expressed by an Arrhenius relationship:

$$P_0 = P_0 * e^{-E_p/RT} \quad (C.11)$$

where P_0 is the pre-exponential factor and E_p is the activation energy of permeation. Conventionally, $1000/T$ is used in calculations instead of $1/T$ to simplify the unit conversion.

$$Ln(P) = \frac{-E_p}{R} * Ln \frac{1000}{T} + Ln(P_0) \quad (C.12)$$

Example: Propane at 25 psig

temperature T (°C)	1000/T (K ⁻¹)	permability P Barrer	Ln(P)
25	3.35	405.33	6.0047
35	3.25	424.90	6.0518
45	3.14	540.40	6.2923
55	3.05	577.18	6.3581
65	2.96	596.60	6.3912
75	2.87	620.00	6.4297

Results from linear regression:

Slope = -0.961

Intercept = 9.238

$$\begin{aligned}
 E_p &= -0.961 * -1 * R \\
 &= 0.961 * 8.314 \text{ (KJ/mol K)} \\
 &= 7.99 \text{ (KJ/mol K)}
 \end{aligned}$$

$$\begin{aligned}
 P_0 &= e^{9.238} \\
 &= 10281.23 \text{ (Barrer)}
 \end{aligned}$$

Appendix D

Experimental Data for PEBAX[®] 2533

Permeability Study

D.1 Relationship between Permeability and Time

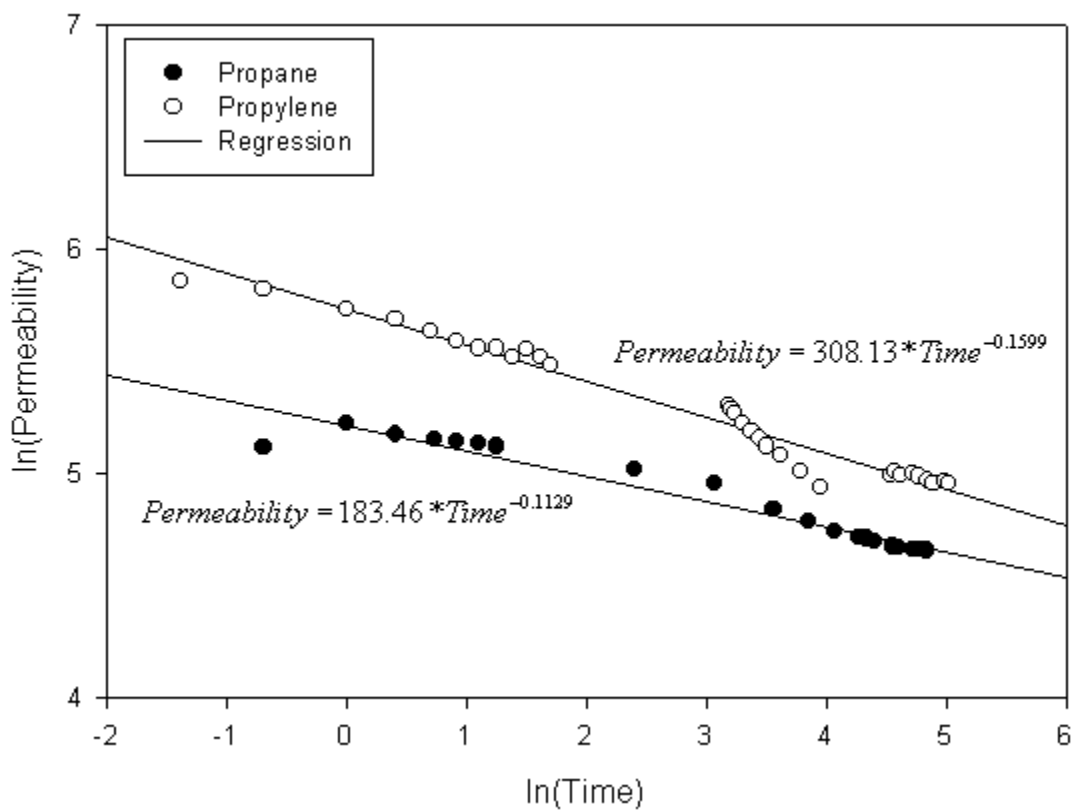


Figure D.1: Ln(Permeability) versus Ln(Time) - Propane and Propylene

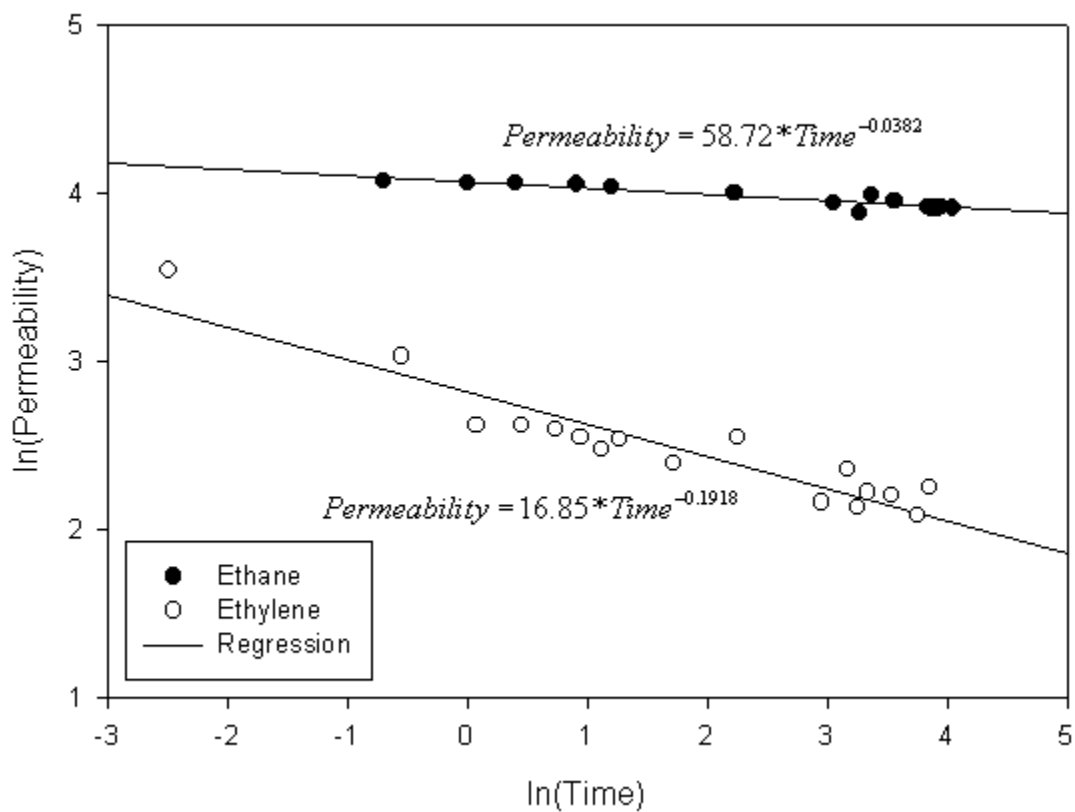


Figure D.2: Ln(Permeability) versus Ln(Time) - Ethane and Ethylene

D.2 Temperature Effects

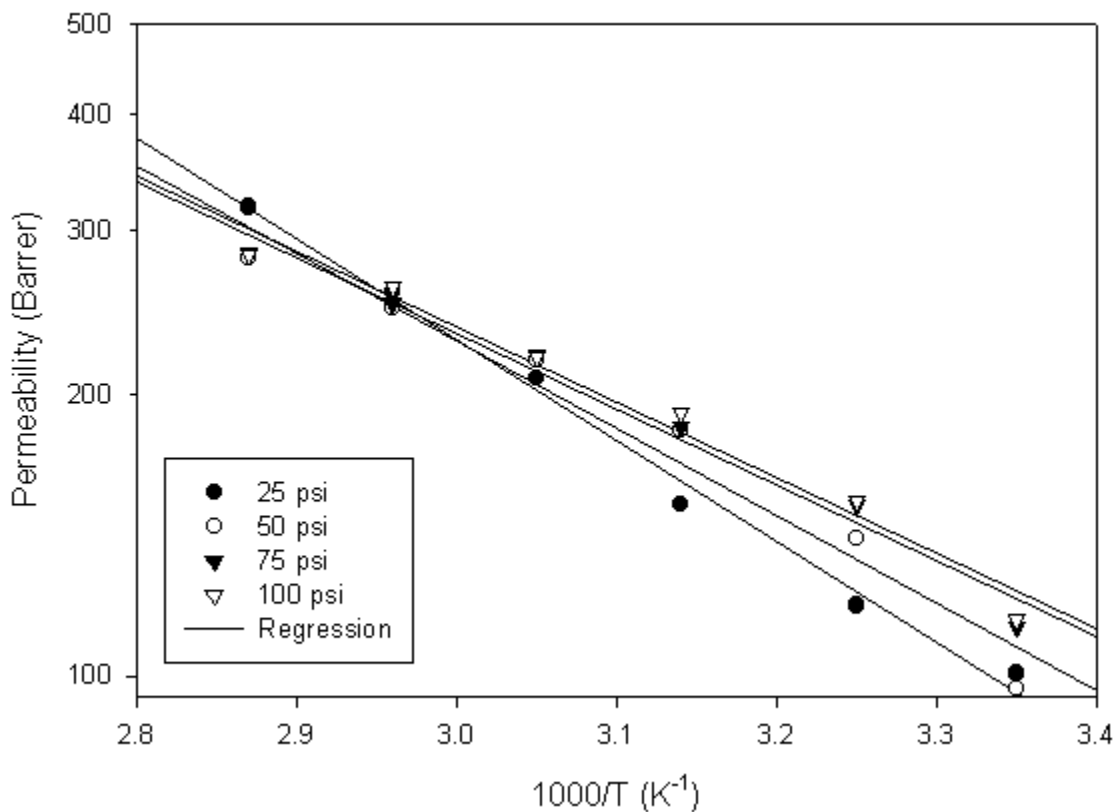


Figure D.3: Temperature dependency of ethane permeability in PEBAX[®] 2533

Table D.1: Calculated values of pre-exponential factors and activation energy for ethane and ethylene permeation

pressure (psig)	ethane		ethylene	
	P ₀ (Barrer)	E _p (KJ/mol.K)	P ₀ (Barrer)	E _p (KJ/mol.K)
25	435592.16	21.56	296013.09	19.16
50	18650.06	18.33	144837.80	17.17
75	19253.87	16.78	152724.93	17.19
100	15862.38	15.88	128378.85	16.72

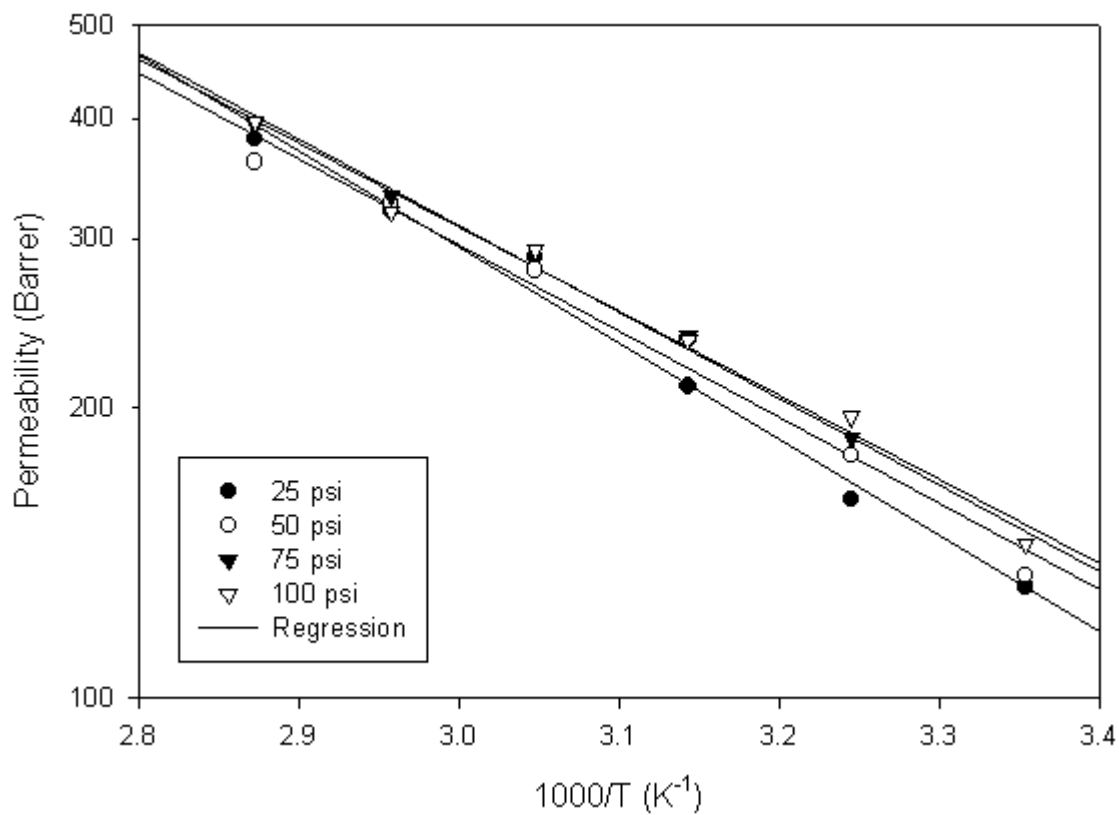


Figure D.4: Temperature dependency of ethylene permeability in PEBAX[®] 2533

Appendix E

Raw data

E.1 PEO Tests

No. 1 (This and subsequent numbers correspond to Table 4.1.)

Mol. Wt 1M
Silver AgNO3
Ag % 80
Membrane Thickness 8.00E-03 cm
Test Date Oct. 22, 2001

Gas	Ethane	Ethylene	Ethane	Ethylene	Ethane	Ethylene
Pressure (psi)	100	100	100	100	100	100
Volume (ml)	1	1	25	25	10	25
Average Time (sec)	9.491	12.620	17.632	27.255	1579.794	22.783
Flow rate (ml/s)	0.097	0.073	1.308	0.846	0.006	1.012
Flux (cm ³ /cm ² .s)	1.010E-02	7.596E-03	1.359E-01	8.793E-02	6.068E-04	1.052E-01
Permeability (cm ³ .cm/cm ² .s.cmHg)	1.562E-07	1.175E-07	2.103E-06	1.360E-06	9.387E-09	1.627E-06
Permeability (barrer)	1562.48	1175.11	21027.01	13602.94	93.87	16272.78
Ethylene/Ethane α_{AB}		0.752		0.647		173.350

No. 2

Mol. Wt 1M
 Silver AgNO₃
 Ag % 50
 Membrane Thickness 8.00E-03 cm
 Test Date Nov. 13, 2001

Gas	Ethane	Ethylene
Pressure (psi)	50	50
Volume (ml)	9	9
Average Time (sec)	38.433	4.060
Flow rate (ml/s)	0.216	2.045
Flux (cm ³ /cm ² .s)	2.245E-02	2.125E-01
Permeability (cm ³ .cm/cm ² .s.cmHg)	6.945E-07	6.575E-06
Permeability (barrer)	6,945.5	65,748.4
Ethylene/Ethane α_{AB}		9.466

No. 3

Mol. Wt 4M
 Silver AgNO₃
 Ag % 80
 Membrane Thickness 8.00E-03 cm
 Test Date Nov. 5, 2001

Gas	Ethane	Ethylene	Ethane	Ethylene
Pressure (psi)	30	28	24	23
Volume (ml)	9	9	1	1
Average Time (sec)	6.778	8.026	9.018	10.952
Flow rate (ml/s)	1.225	1.034	0.102	0.084
Flux (cm ³ /cm ² .s)	1.273E-01	1.075E-01	1.063E-02	8.754E-03
Permeability (cm ³ .cm/cm ² .s.cmHg)	2.188E-05	1.848E-05	1.644E-05	1.354E-05
Permeability (barrer)	218784.28	184773.58	164448.08	135412.52
Ethylene/Ethane α_{AB}		0.845		0.823

No. 4

Mol. Wt 7M
 Silver AgNO₃
 Ag % 50
 Membrane Thickness 8.00E-03 cm
 Test Date Nov. 18, 2001

Gas	Ethane	Ethylene	Ethane	Ethylene	Ethane	Ethylene
Pressure (psi)	98.5	102	49	51.5	98.5	98.5
Volume (ml)	1	1	9	9	1	1
Average Time (sec)	242.908	307.760	14.095	13.151	146.012	149.468
Flow rate (ml/s)	0.004	0.003	0.589	0.631	0.006	0.006
Flux (cm ³ /cm ² .s)	3.947E-04	3.115E-04	6.121E-02	6.561E-02	6.566E-04	6.414E-04
Permeability (cm ³ .cm/cm ² .s.cmHg)	6.198E-09	4.724E-09	1.933E-06	1.971E-06	5.800E-09	5.666E-09
Permeability (barrer)	61.98	47.24	19325.04	19706.40	58.00	56.66
Ethylene/Ethane α_{AB}		0.762		1.020		0.977

Gas	Ethane	Ethylene	Ethane	Ethylene
Pressure (psi)	95	100	100	97
Volume (ml)	1	1	1	1
Average Time (sec)	4.080	6.938	114.245	175.377
Flow rate (ml/s)	0.226	0.133	0.008	0.005
Flux (cm ³ /cm ² .s)	2.350E-02	1.382E-02	8.391E-04	5.466E-04
Permeability (cm ³ .cm/cm ² .s.cmHg)	2.152E-07	1.202E-07	1.298E-08	8.718E-09
Permeability (barrer)	2152.18	1202.34	129.81	87.18
Ethylene/Ethane α_{AB}		0.559		0.672

No. 5

Mol. Wt 4M
 Silver AgNO₃
 Ag % 50
 Membrane Thickness 7.00E-03 cm
 Test Date Nov. 21, 2001

Gas	Ethane	Ethylene	Ethane	Ethylene	Ethane	Ethylene
Pressure (psi)	101	101	151	101	150	145
Volume (ml)	1	9	1	9	1	1
Average Time (sec)	61.453	18.706	2359.980	17.816	79.188	292.480
Flow rate (ml/s)	0.015	0.444	0.000	0.466	0.012	0.003
Flux (cm ³ /cm ² .s)	1.560E-03	4.612E-02	4.062E-05	4.843E-02	1.211E-03	3.278E-04
Permeability (cm ³ .cm/cm ² .s.cmHg)	2.091E-08	6.181E-07	3.641E-10	6.490E-07	1.092E-08	3.060E-09
Permeability (barrer)	209.07	6181.41	3.64	6490.30	109.24	30.60
Ethylene/Ethane α_{AB}		29.567		1782.392		0.280

No. 6

Mol. Wt 4M
 Silver AgNO₃
 Ag % 50
 Membrane Thickness 5.00E-03 cm
 Test Date Nov. 14, 2001

Gas	Ethane	Ethylene
Pressure (psi)	54	126.5
Volume (ml)	1	1
Average Time (sec)	31.035	22.350
Flow rate (ml/s)	0.030	0.041
Flux (cm ³ /cm ² .s)	3.089E-03	4.289E-03
Permeability (cm ³ .cm/cm ² .s.cmHg)	5.531E-08	3.278E-08
Permeability (barrer)	553.06	327.83
Ethylene/Ethane α_{AB}		0.593

E.2 PEBAX Tests

Corresponds to Figure 5.1 to 5.3, Figure D.1 and D.2 in Appendix D

PEBAX(2533) membrane with support

0.002 cm

Nitrogen		75	30	60
Gas				
Pressure (psi)		75		
Volume (mL)		1		
Duration (min)		0	30	60
Average		259.84	364.655	452.02
Flow rate (mL/s)		0.003549633	0.00252934	0.002040478
Flux (cm ³ /cm ² .s)		0.000368941	0.00026289	0.000212083
Permeability (cm ³ .cm/cm ² .s.cmHg)		1.902E-09	1.356E-09	1.094E-09
Permeability (barrer)		19.02	13.56	10.94

Ethylene		75	60
Gas			
Pressure (psi)		75	
Volume (mL)		1	
Duration (min)		0	60
Average		119.44	192.23
Flow rate (mL/s)		0.007722176	0.00479809
Flux (cm ³ /cm ² .s)		0.000802627	0.0004987
Permeability (cm ³ .cm/cm ² .s.cmHg)		4.139E-09	2.572E-09
Permeability (barrer)		41.39	25.72

Ethane		75	30	60
Gas				
Pressure (psi)		75		
Volume (mL)		1		
Duration (min)		0	30	60
Average		161.935	201.88	224.21
Flow rate (mL/s)		0.005695721	0.00456874	0.004113718
Flux (cm ³ /cm ² .s)		0.000592001	0.00047487	0.000427571
Permeability (cm ³ .cm/cm ² .s.cmHg)		3.053E-09	2.449E-09	2.205E-09
Permeability (barrer)		30.53	24.49	22.05

Propane		75	15	30	45	70	80	95	110	125	140	155	190
Gas													
Pressure (psi)		75											
Volume (mL)		1											
Duration (min)		0.0	15	30	45	70	80	95	110	125	140	155	190
Duration (hr)			0.3	0.5	0.8	1.2	1.3	1.6	1.8	2.1	2.3	2.6	3.2
Average		17.37	18.8325	18.8775	19.635	20.615	21.4125	21.8925	22.3975	23.2125	23.45833333	23.45833333	25.072
Flow rate (mL/s)		0.053099404	0.04897579	0.048859047	0.04697411	0.04474105	0.04307468	0.042130257	0.04118034	0.03973448	0.04058687	0.039318081	0.036787518
Flux (cm ³ /cm ² .s)		0.005519042	0.00509044	0.005078308	0.004882391	0.00465029	0.00447709	0.004378931	0.0042802	0.00412992	0.00408664	0.00408664	0.003823618
Permeability (cm ³ .cm/cm ² .s.cmHg)		2.846E-08	2.625E-08	2.619E-08	2.518E-08	2.398E-08	2.309E-08	2.258E-08	2.207E-08	2.130E-08	2.175E-08	2.107E-08	1.972E-08
Permeability (barrer)		284.59	262.49	261.86	251.76	239.79	230.86	225.80	220.71	212.96	217.53	210.73	197.16

Propylene														
Gas	75													
Pressure (psi)	1	15	30	60	90	120	150	180	210	240	270	300		
Volume (mL)	0	0.25	0.5	1	1.5	2	2.5	3	3.5	4	4.5	5		
Duration (min)	0	14.12	14.68833333	16.02166667	16.71333333	17.61666667	18.40666667	19.065	19.05333333	19.81833333	19.10166667	19.80633333		
Average		0.065352148	0.06532129	0.065352148	0.05518568	0.05235591	0.050108837	0.04837853	0.04840815	0.04653957	0.048285664	0.046563062		
Flow rate (mL/s)		0.006792566	0.00678936	0.005983507	0.00573588	0.00544176	0.005208208	0.00502836	0.00503144	0.00483723	0.005018712	0.004838668		
Flux (cm ³ /cm ² .s)														
Permeability														
(cm ³ .cm/cm ² .s.cmHg)	3.503E-08	3.501E-08	3.365E-08	3.085E-08	2.958E-08	2.806E-08	2.688E-08	2.593E-08	2.594E-08	2.494E-08	2.588E-08	2.496E-08		
Permeability (barrer)	350.26	350.09	336.55	308.54	295.77	280.60	268.56	259.29	259.45	249.43	258.79	249.56		
Propylene														
Gas	75													
Pressure (psi)	1	605	1395	1425	1455	1485	1515	1635	1755	1875	1995	2235		
Volume (mL)	330	10.08333333	23.25	23.75	24.25	24.75	25.25	27.25	29.25	31.25	33.25	37.25		
Duration (min)	5.5	20.49	25.075	23.78666667	24.615	25.035	25.40166667	26.74333333	27.6516667	28.50333333	29.57	30.87166667		
Average		0.04501399	0.03678312	0.03776364	0.03747051	0.03684189	0.036310084	0.03448847	0.03333555	0.0323589	0.031191635	0.029876477		
Flow rate (mL/s)		0.004678661	0.00382316	0.004030231	0.00389461	0.00382927	0.003773995	0.00368466	0.00346691	0.00336332	0.003241994	0.003105299		
Flux (cm ³ /cm ² .s)														
Permeability														
(cm ³ .cm/cm ² .s.cmHg)	2.413E-08	1.971E-08	2.228E-08	2.078E-08	2.008E-08	1.975E-08	1.948E-08	1.848E-08	1.788E-08	1.734E-08	1.672E-08	1.601E-08		
Permeability (barrer)	241.25	197.14	222.59	207.82	200.83	197.46	194.61	184.84	178.77	173.43	167.17	160.12		
Propylene														
Gas	75													
Pressure (psi)	1	3135	3615	4185	4365	4545	4905	5625	5805	6105	6680	7085		
Volume (mL)	2655	44.25	60.25	69.75	72.75	75.75	81.75	93.75	96.75	101.75	111.3333333	118.0833333		
Duration (min)	44.25	33.1	37.06333333	27.88333333	28.97333333	29.66333333	30.46666667	33.72833333	33.065	33.515	33.48666667	33.76833333		
Average		0.027865156	0.02599108	0.033078422	0.03183398	0.03109349	0.030273632	0.02734605	0.02789465	0.02752011	0.027568098	0.027313656		
Flow rate (mL/s)		0.002896246	0.00270146	0.003438102	0.00330876	0.00323179	0.003146578	0.00284229	0.00289931	0.00286038	0.002865371	0.002838925		
Flux (cm ³ /cm ² .s)														
Permeability														
(cm ³ .cm/cm ² .s.cmHg)	1.493E-08	1.393E-08	1.334E-08	1.779E-08	1.706E-08	1.666E-08	1.623E-08	1.466E-08	1.495E-08	1.475E-08	1.478E-08	1.464E-08		
Permeability (barrer)	149.34	139.30	133.37	177.29	170.62	166.65	162.25	146.56	149.50	147.50	147.75	146.39		

Propylene				Ethylene			
Time	Permeability	lnP	lnx	Time	ln(T)	Permeability	lnP
0	350.2580957	5.8586703		0.083	-2.48490665	34.7069385	3.54693963
0.250	350.0927236	5.85819804	-1.386294361	0.583	-0.538996501	20.7763176	3.03381376
0.500	336.5466418	5.81873675	-0.693147181	1.083	0.080042708	13.7142718	2.61843703
1.000	308.5390153	5.7318483	0	1.583	0.459532329	13.726839	2.61935297
1.500	295.7703983	5.68958347	0.405465108	2.083	0.733969175	13.5039112	2.60297936
2.000	280.6041206	5.63694485	0.693147181	2.583	0.949080555	12.7752245	2.54750771
2.500	268.5608072	5.59307736	0.916290732	3.083	1.126011263	11.9942477	2.48442718
3.000	259.2871365	5.55793608	1.098612289	3.583	1.276293466	12.7046332	2.54196675
3.500	259.4459022	5.55854821	1.252762968	4.083	1.71978597	10.9918489	2.39715399
4.000	249.4311289	5.51918284	1.386294361	4.583	2.260025479	12.770769	2.54715889
4.500	258.789421	5.55601468	1.504077397	5.083	2.948815354	8.70921917	2.16438214
5.000	249.5570513	5.51968755	1.609437912	5.583	2.948815354	10.5450515	2.3556567
5.500	241.2547222	5.48585331	1.704748092	6.083	3.171085161	10.45718509	2.13501639
24.250	200.8250765	5.30243426	3.188416617	6.583	3.251665648	8.45718509	2.13501639
24.750	197.455932	5.28551543	3.208825489	7.083	3.335176281	9.2367227	2.22318714
25.250	194.6057053	5.27097549	3.228826156	7.583	3.54337187	9.09055832	2.20723633
27.250	184.8426745	5.21950505	3.305053521	8.083	3.763136225	8.08470047	2.08997345
29.250	178.7707525	5.18610427	3.375879574	8.583	3.851919081	9.49385762	2.25064502
31.250	173.4291635	5.15576924	3.442019376				
33.250	167.1731233	5.11902994	3.504054767				
37.250	160.1244698	5.07595145	3.617651945				
44.250	149.3446905	5.00625699	3.789855371				
52.250	139.3004675	4.93663324	3.956039891				
93.750	146.5625119	4.98745204	4.540631665				
96.750	149.5027751	5.00731495	4.572130332				
101.750	147.4954276	4.98379718	4.622518824				
111.333	147.7525931	4.99553921	4.712528704				
118.083	146.3889025	4.9862668	4.77139059				
126.667	143.7844461	4.96831528	4.841558964				
133.167	141.7097733	4.95378112	4.891601477				
145.083	143.0217742	4.96299689	4.97730829				
151.083	141.2979636	4.95087088	5.017831561				

$y = x^a \cdot \exp(b)$
 slope intercept exp(b)
 -0.1917719 2.824279433 16.8487999

$y = x^a \cdot \exp(b)$
 slope intercept exp(b)
 -0.15985617 5.730536341 308.134489

APPENDIX E. RAW DATA

PEBAX(2533) membrane with support		Second Set										0.002 cm									
Nitrogen																					
Gas	150																				
Pressure (psi)	1																				
Volume (mL)	0	30	105	200	345	885	1565	2245	2985												
Duration (min)	0.0	0.5	1.8	3.3	5.8	14.8	26.1	37.4	49.8												
Duration (hr)	37.07333333	39.44833333	40.55666667	40.98666667	41.42666667	42.15666667	44.04833333	43.62166667	43.58333333												
Average	0.024878709	0.023380878	0.022741925	0.022503334	0.022284322	0.021878785	0.020939195	0.021144003	0.0211626												
Flow rate (mL/s)	0.002585841	0.00243016	0.002363748	0.00233895	0.002314107	0.002274035	0.002176376	0.002197664	0.002199597												
Permeability	6.667E-09	6.266E-09	6.094E-09	6.030E-09	5.966E-09	5.863E-09	5.611E-09	5.666E-09	5.671E-09												
(cm3.cm/cm2.s.cmHg)	66.67	62.66	60.94	60.30	59.66	58.63	56.11	56.66	56.71												
Permeability (barrer)																					
Ethane																					
Gas	150																				
Pressure (psi)	1																				
Volume (mL)	30	60	90	150	200	560	1280	1580	1740												
Duration (min)	0.5	1.0	1.5	2.5	3.3	9.3	21.3	26.3	29.0												
Duration (hr)	41.95833333	42.26166667	42.6175	42.71333333	43.54833333	44.93833333	47.745	50.77	45.75333333												
Average	0.021982204	0.021824427	0.021642205	0.021593647	0.021179609	0.020524496	0.019317974	0.018166962	0.020158895												
Flow rate (mL/s)	0.002284785	0.002268386	0.002249446	0.002244399	0.002201365	0.002133273	0.00200787	0.001888236	0.002095274												
Permeability	5.891E-09	5.848E-09	5.800E-09	5.787E-09	5.676E-09	5.500E-09	5.177E-09	4.868E-09	5.402E-09												
(cm3.cm/cm2.s.cmHg)	58.91	58.48	58.00	57.87	56.76	55.00	51.77	48.68	54.02												
Permeability (barrer)																					
Ethane																					
Gas	150																				
Pressure (psi)	1																				
Volume (mL)	2780	2900	3020	3140	3440																
Duration (min)	46.3	48.3	50.3	52.3	57.3																
Duration (hr)	48.91666667	49.30833333	49.23666667	49.17666667	49.21166667																
Average	0.018855264	0.018705492	0.018732719	0.018755575	0.018742236																
Flow rate (mL/s)	0.001959777	0.00194421	0.00194704	0.001949415	0.001948029																
Permeability	5.053E-09	5.013E-09	5.020E-09	5.026E-09	5.022E-09																
(cm3.cm/cm2.s.cmHg)	50.53	50.13	50.20	50.26	50.22																
Permeability (barrer)																					
Propane																					
Gas	75																				
Pressure (psi)	1																				
Volume (mL)	0	30	60	90	125	150	180	210	660												
Duration (min)	0.0	0.5	1.0	1.5	2.1	2.5	3.0	3.5	11.0												
Duration (hr)	28.62333333	29.59	26.67333333	28.01333333	28.63	28.94333333	29.195	29.575	32.78833333												
Average	0.03223244	0.031170553	0.03457898	0.032924916	0.032215741	0.031866981	0.031592281	0.031186362	0.028130026												
Flow rate (mL/s)	0.003349217	0.003239802	0.003594067	0.003422147	0.0033348437	0.0033312188	0.003283636	0.003241446	0.002923776												
Permeability	1.727E-08	1.671E-08	1.853E-08	1.765E-08	1.727E-08	1.708E-08	1.693E-08	1.671E-08	1.508E-08												
(cm3.cm/cm2.s.cmHg)	172.70	167.06	185.33	176.46	172.66	170.79	169.32	167.14	150.76												
Permeability (barrer)																					

Propane										
Gas	Pressure (psi)	75								
	Volume (mL)	1								
	Duration (min)	2815	3510	4290	4565	4915	5640	5875	6000	6750
	Duration (hr)	46.9	58.5	71.5	76.1	81.9	94.0	97.9	100.0	112.5
	Average	41.36666667	43.175	44.48666667	44.59166667	45.08833333	46.195	46.37166667	46.44	46.955
	Flow rate (mL/s)	0.022296615	0.021362748	0.020732878	0.020684059	0.020458215	0.019986158	0.019890091	0.019860824	0.019642991
	Flux (cm ³ /cm ² .s)	0.002317464	0.00222204	0.002154932	0.002149858	0.002126177	0.002075241	0.0020267395	0.002047539	0.002041652
	Permeability									
(cm ³ .cm/cm ² .s.cmHg)	1.195E-08	1.145E-08	1.111E-08	1.109E-08	1.096E-08	1.096E-08	1.070E-08	1.066E-08	1.064E-08	1.053E-08
Permeability (barrier)	119.50	114.49	111.12	110.86	109.64	109.64	107.01	106.60	106.45	105.28

Ethylene										
Gas	Pressure (psi)	150								
	Volume (mL)	1								
	Duration (min)	25	55	85	115	145	190	235	280	325
	Duration (hr)	0.4	0.9	1.4	1.9	2.4	3.2	3.9	4.7	5.4
	Average	56.08	57.26166667	59.55166667	60.54833333	61.66833333	60.15	60.24166667	60.265	60.36666667
	Flow rate (mL/s)	0.016446802	0.016107401	0.015488007	0.015233064	0.014956406	0.015333943	0.01531061	0.015304682	0.015278906
	Flux (cm ³ /cm ² .s)	0.001709446	0.00167417	0.001609791	0.001583293	0.001554638	0.001593778	0.001591353	0.001590737	0.001588058
	Permeability									
(cm ³ .cm/cm ² .s.cmHg)	4.407E-09	4.318E-09	4.150E-09	4.082E-09	4.008E-09	4.008E-09	4.109E-09	4.103E-09	4.101E-09	4.094E-09
Permeability (barrier)	44.07	43.16	41.50	40.82	40.08	40.08	41.09	41.03	41.01	40.94

Ethylene										
Gas	Pressure (psi)	150								
	Volume (mL)	1								
	Duration (min)	610	985	1525	1810	2185	2605	3415	4170	5105
	Duration (hr)	10.2	16.4	25.4	30.2	36.4	43.4	56.9	69.5	85.1
	Average	61.52166667	63.43833333	64.60333333	64.46666667	66.38	65.06	67.52333333	65.81	64.15833333
	Flow rate (mL/s)	0.014992062	0.014539106	0.01427892	0.014307187	0.013894797	0.014176708	0.013669825	0.014015144	0.014375945
	Flux (cm ³ /cm ² .s)	0.001558244	0.001511164	0.001483913	0.001487059	0.001444196	0.001473498	0.001419743	0.001456705	0.001494206
	Permeability									
(cm ³ .cm/cm ² .s.cmHg)	4.018E-09	3.896E-09	3.826E-09	3.834E-09	3.723E-09	3.799E-09	3.799E-09	3.660E-09	3.756E-09	3.852E-09
Permeability (barrier)	40.18	38.96	38.26	38.34	37.23	37.99	37.99	36.60	37.56	38.52

Ethylene										
Gas	Pressure (psi)	150								
	Volume (mL)	1								
	Duration (min)	610	985	1525	1810	2185	2605	3415	4170	5105
	Duration (hr)	10.2	16.4	25.4	30.2	36.4	43.4	56.9	69.5	85.1
	Average	61.52166667	63.43833333	64.60333333	64.46666667	66.38	65.06	67.52333333	65.81	64.15833333
	Flow rate (mL/s)	0.014992062	0.014539106	0.01427892	0.014307187	0.013894797	0.014176708	0.013669825	0.014015144	0.014375945
	Flux (cm ³ /cm ² .s)	0.001558244	0.001511164	0.001483913	0.001487059	0.001444196	0.001473498	0.001419743	0.001456705	0.001494206
	Permeability									
(cm ³ .cm/cm ² .s.cmHg)	4.018E-09	3.896E-09	3.826E-09	3.834E-09	3.723E-09	3.799E-09	3.799E-09	3.660E-09	3.756E-09	3.852E-09
Permeability (barrier)	40.18	38.96	38.26	38.34	37.23	37.99	37.99	36.60	37.56	38.52

Propylene													
Gas													
Pressure (psi)	75												
Volume (mL)	1												
Duration (min)	10												
Duration (hr)	0.2												
Average	19.77	19.30166667	40	0.7	70	100	145	190	285	585	1260	10	130
Flow rate (mL/s)	0.046653346	0.047785337	0.047575825	0.047339777	0.046563062	0.045875984	0.044632792	0.044632792	0.042254103	21.82833333	32.10833333	0.2	2.2
Flux (cm ³ /cm ² .s)	0.004849052	0.004966709	0.004944932	0.004920398	0.004839668	0.004768254	0.00463904	0.00463904	0.004391804	0.028725772	0.02985697	18.5	22.29166667
Permeability													
(cm ³ .cm/cm ² .s.cmHg)	2.500E-08	2.561E-08	2.550E-08	2.537E-08	2.498E-08	2.459E-08	2.392E-08	2.392E-08	2.265E-08	2.265E-08	1.540E-08	2.672E-08	2.218E-08
Permeability (barrer)	250.04	256.11	254.99	253.72	249.56	245.87	239.21	239.21	226.46	226.46	153.96	267.21	221.76
Propylene													
Gas													
Pressure (psi)	75												
Volume (mL)	1												
Duration (min)	250												
Duration (hr)	4.2												
Average	23.77166667	24.53833333	370	6.2	550	640	1145	1350	1540	2045	2610	2765	2765
Flow rate (mL/s)	0.038799831	0.037587584	0.036136998	0.035474487	0.034644473	0.033319405	0.033373668	0.033319405	0.032295585	28.55833333	29.99666667	46.1	46.1
Flux (cm ³ /cm ² .s)	0.004032774	0.003906775	0.003756005	0.003687144	0.003478228	0.003463315	0.003468789	0.003463315	0.00335684	0.030747972	0.030747972	0.030787315	0.030787315
Permeability													
(cm ³ .cm/cm ² .s.cmHg)	2.079E-08	2.015E-08	1.937E-08	1.901E-08	1.794E-08	1.786E-08	1.789E-08	1.786E-08	1.731E-08	1.731E-08	1.648E-08	1.650E-08	1.650E-08
Permeability (barrer)	207.95	201.45	193.68	190.13	179.35	178.58	178.87	178.58	173.10	173.10	164.80	165.01	165.01

Nitrogen				Ethane			
Time	Permeability	ln(Time)	ln(P)	Time	Permeability	ln(Time)	ln(P)
0.0	66.6693	#NUM!	4.1997	0.5	58.9074	-0.6931	4.0760
0.5	62.6555	-0.6931	4.1377	1.0	58.4846	0.0000	4.0688
1.8	60.9432	0.5596	4.1099	1.5	57.9962	0.4055	4.0604
3.3	60.3039	1.2040	4.0994	2.5	57.8661	0.9163	4.0581
5.8	59.6634	1.7492	4.0887	3.3	56.7566	1.2040	4.0388
14.8	58.6302	2.6912	4.0713	9.3	55.0010	2.2336	4.0074
26.1	56.1123	3.2613	4.0274	21.3	51.7678	3.0603	3.9468
37.4	56.6612	3.6221	4.0371	26.3	48.6834	3.2708	3.8853
49.8	56.7110	3.9070	4.0380	29.0	54.0213	3.3673	3.9894
				35.3	52.5567	3.5648	3.9619
				46.3	50.5279	3.8359	3.9225
				48.3	50.1265	3.8781	3.9145
				50.3	50.1995	3.9187	3.9160
				52.3	50.2607	3.9576	3.9172
				57.3	50.2250	4.0489	3.9165

$y = x^a \cdot \exp(b)$
 slope intercept exp(b)
 -0.023819352 4.124707328 61.84970495

$y = x^a \cdot \exp(b)$
 slope intercept exp(b)
 -0.038200318 4.072784437 58.72023799

Propane				Ethylene				Propylene			
Time	Permeability	ln(TTime)	ln(P)	Time	Permeability	ln(TTime)	ln(P)	Time	Permeability	ln(TTime)	ln(P)
0.0	172.7021	#NUM!	5.1516	0.4	44.0737	-0.8755	3.7859	0.2	250.0409	-1.7918	5.5216
0.5	167.0601	-0.6931	5.1184	0.9	43.1642	-0.0870	3.7650	0.7	256.1079	-0.4055	5.5456
1.0	185.3278	0.0000	5.2221	1.4	41.5044	0.3483	3.7258	1.2	254.9850	0.1542	5.5412
1.5	176.4627	0.4055	5.1731	1.9	40.8212	0.6506	3.7092	1.7	253.7199	0.5108	5.5362
2.1	172.6619	0.7340	5.1513	2.4	40.0798	0.8824	3.6909	2.4	249.5571	0.8824	5.5197
2.5	170.7927	0.9163	5.1405	3.2	41.0915	1.1527	3.7158	3.2	245.8746	1.1527	5.5048
3.0	169.3204	1.0986	5.1318	3.9	41.0290	1.3652	3.7143	4.8	239.2117	1.5681	5.4773
3.5	167.1449	1.2528	5.1189	4.7	41.0131	1.5404	3.7139	9.8	226.4630	2.2773	5.4226
11.0	150.7643	2.3979	5.0157	5.4	40.9440	1.6895	3.7122	21.0	153.9572	3.0445	5.0367
21.6	141.7098	3.0719	4.9538	6.2	40.8482	1.8192	3.7099	0.2	267.2059	-1.7918	5.5880
35.1	126.1048	3.5577	4.8371	10.2	40.1754	2.3191	3.6933	2.2	221.7559	0.7732	5.4016
46.9	119.4998	3.8484	4.7833	16.4	38.9615	2.7983	3.6626	4.2	207.9496	1.4271	5.3373
58.5	114.4947	4.0690	4.7405	25.4	38.2589	3.2354	3.6444	6.2	201.4525	1.8192	5.3056
71.5	111.1189	4.2897	4.7106	30.2	38.3400	3.4067	3.6465	9.2	193.6780	2.2156	5.2662
76.1	110.8572	4.3318	4.7082	36.4	37.2349	3.5950	3.6172	10.7	190.1273	2.3671	5.2477
81.9	109.6361	4.4057	4.6972	43.4	37.9904	3.7708	3.6573	19.1	179.3545	2.9488	5.1894
94.0	107.0096	4.5433	4.6729	56.9	36.6045	4.0416	3.6002	22.5	178.5770	3.1135	5.1850
97.9	106.6019	4.5841	4.6691	69.5	37.5574	4.2413	3.6259	25.7	178.8678	3.2452	5.1866
100.0	106.4451	4.6052	4.6676	85.1	38.5243	4.4436	3.6513	34.1	173.0952	3.5288	5.1538
112.5	105.5811	4.7230	4.6585					43.5	164.7953	3.7728	5.1047
119.0	105.2776	4.7791	4.6566					46.1	165.0062	3.8305	5.1060
125.8	105.1917	4.8350	4.6558								

$y=x^a \cdot \exp(b)$ intercept exp(b)
 slope -0.112872531 5.212013282 183.4630495

$y=x^a \cdot \exp(b)$ intercept exp(b)
 slope -0.029886645 3.748791621 42.46873144

$y=x^a \cdot \exp(b)$ intercept exp(b)
 slope -0.094147058 5.497056816 243.97333

Propane		cell 1		65C		75C		50		75		100	
Gas	Pressure (psi)	100	20	50	75	100	20	50	75	100	20	50	75
Gas	Pressure (psi)	100	20	50	75	100	20	50	75	100	20	50	75
	Volume (ml)	0.5	0.1	0.2	0.2	0.5	0.1	0.2	0.2	0.5	0.1	0.2	0.2
	Average Time (sec)	1.506E+01	2.108E+01	1.419E+01	8.763E+00	1.580E+01	1.970E+01	1.423E+01	9.172E+00	1.676E+01	1.423E+01	9.172E+00	1.676E+01
	Flow rate (ml/s)	2.783E-02	3.832E-03	1.139E-02	1.844E-02	2.556E-02	3.982E-03	1.103E-02	1.711E-02	2.341E-02	1.103E-02	1.711E-02	2.341E-02
	Flux (cm ³ /cm ² .s)	2.872E-03	3.983E-04	1.184E-03	1.916E-03	2.657E-03	4.139E-04	1.146E-03	1.778E-03	2.433E-03	1.146E-03	1.778E-03	2.433E-03
	Permeability (cm ³ .cm/cm ² .s.cmHg)	8.604E-08	5.966E-08	7.092E-08	7.654E-08	7.960E-08	6.200E-08	6.868E-08	7.103E-08	7.288E-08	6.200E-08	6.868E-08	7.103E-08
	Permeability (barrer)	860.43	596.60	709.19	765.39	795.97	620.00	686.80	710.31	728.82	620.00	686.80	710.31
Gas	Pressure (psi)	25	50	75	100	110	90	70	50	50	90	70	50
	Volume (ml)	0.1	0.1	0.1	0.5	0.5	0.5	0.2	0.1	0.1	0.5	0.2	0.1
	Average Time (sec)	6.027E+01	1.597E+01	7.460E+00	1.710E+01	1.304E+01	2.243E+01	1.628E+01	1.499E+01	1.471E+01	2.243E+01	1.628E+01	1.471E+01
	Flow rate (ml/s)	1.520E-03	5.737E-03	1.228E-02	2.679E-02	3.512E-02	2.042E-02	1.125E-02	6.112E-03	6.229E-03	2.042E-02	1.125E-02	6.112E-03
	Flux (cm ³ /cm ² .s)	1.580E-04	5.963E-04	1.276E-03	2.785E-03	3.651E-03	2.123E-03	1.170E-03	6.353E-04	6.475E-04	2.123E-03	1.170E-03	6.353E-04
	Permeability (cm ³ .cm/cm ² .s.cmHg)	2.367E-08	3.573E-08	5.099E-08	8.342E-08	9.943E-08	7.066E-08	5.007E-08	3.807E-08	3.879E-08	7.066E-08	5.007E-08	3.807E-08
	Permeability (barrer)	236.67	357.26	509.87	834.21	994.26	706.57	500.65	380.66	387.95	706.57	500.65	380.66
Gas	Pressure (psi)	30	40	60	80	80	80	80	80	80	80	80	80
	Volume (ml)	0.1	0.1	0.1	0.2	0.2	0.2	0.2	0.2	0.2	0.2	0.2	0.2
	Average Time (sec)	3.307E+01	2.132E+01	1.122E+01	1.226E+01	1.226E+01	1.226E+01	1.226E+01	1.226E+01	1.226E+01	1.226E+01	1.226E+01	1.226E+01
	Flow rate (ml/s)	2.771E-03	4.297E-03	8.168E-03	1.494E-02	1.494E-02	1.494E-02	1.494E-02	1.494E-02	1.494E-02	1.494E-02	1.494E-02	1.494E-02
	Flux (cm ³ /cm ² .s)	2.880E-04	4.466E-04	8.489E-04	1.553E-03	1.553E-03	1.553E-03	1.553E-03	1.553E-03	1.553E-03	1.553E-03	1.553E-03	1.553E-03
	Permeability (cm ³ .cm/cm ² .s.cmHg)	2.876E-08	3.345E-08	4.239E-08	5.816E-08	5.816E-08	5.816E-08	5.816E-08	5.816E-08	5.816E-08	5.816E-08	5.816E-08	5.816E-08
	Permeability (barrer)	287.59	334.51	423.88	581.63	581.63	581.63	581.63	581.63	581.63	581.63	581.63	581.63
Pressure	Temperature (°C)	25	25	50	75	100	75	50	75	100	75	50	75
	1000/T (K)	3.35	405.33	520.76	665.28	898.51	665.28	520.76	665.28	898.51	665.28	520.76	665.28
	P	3.14	540.40	645.09	760.70	912.31	760.70	645.09	760.70	912.31	760.70	645.09	760.70
	P	3.25	424.90	567.20	708.29	967.00	708.29	567.20	708.29	967.00	708.29	567.20	708.29
	P	3.14	657.11	810.12	933.25	1123.53	933.25	810.12	933.25	1123.53	933.25	810.12	933.25
	P	3.05	577.18	665.23	759.67	860.43	759.67	665.23	759.67	860.43	759.67	665.23	759.67
	P	2.96	596.60	709.19	765.39	795.97	765.39	709.19	765.39	795.97	765.39	709.19	765.39
	P	2.87	620.00	686.80	710.31	728.82	710.31	686.80	710.31	728.82	710.31	686.80	710.31
	P	3.35	236.67	357.26	509.87	834.21	509.87	357.26	509.87	834.21	509.87	357.26	509.87
Slope	Intercept	25	50	75	100	10281.23	10281.23	7.99	7.99	7.99	10281.23	10281.23	7.99
	Po	-0.961391354	9.238075637	8.392436723	4413.56	5.22	4413.56	5.22	4413.56	5.22	4413.56	5.22	4413.56
	Po	-0.627998784	8.392436723	7.138690169	1259.78	1.47	1259.78	1.47	1259.78	1.47	1259.78	1.47	1259.78
	Po	-0.177013283	7.138690169	5.234467369	187.63	-4.07	187.63	-4.07	187.63	-4.07	187.63	-4.07	187.63
	Po	0.489412449	5.234467369										

$$\ln P = \ln P_o + (-E_p/R) \cdot (1/T)$$

1-Jun-02 Cell 1		0.015492857 cm									
		25°C					35°C				
Propylene		117.5	117.5	50	75	20	40	60	80	100	
Gas Pressure (psi)	117.5	117.5	50	75	20	40	60	80	100		
Volume (ml)	1	2	0.5	0.5	0.1	0.1	0.5	0.5	0.5		
Average Time (sec)	1,118E+01	2,211E+01	3,731E+01	1,673E+01	2,852E+01	1,055E+01	2,552E+01	1,425E+01	8,387E+00		
Flow rate (ml/s)	8.197E-02	8.286E-02	1.228E-02	2.737E-02	3.213E-03	8.688E-03	1.795E-02	3.214E-02	5.462E-02		
Flux (cm3/cm2.s)	8.520E-03	8.612E-03	1.276E-03	2.845E-03	3.339E-04	9.030E-04	1.866E-03	3.341E-03	5.677E-03		
Permeability (cm ³ .cm/cm ² .s.cmHg)	2.172E-07	2.196E-07	7.647E-08	1.137E-07	5.002E-08	6.763E-08	9.316E-08	1.251E-07	1.701E-07		
Permeability (barrer)	2172.24	2195.81	764.66	1136.54	500.18	676.32	931.59	1251.04	1700.74		
25C		35°C					55°C				
Gas Pressure (psi)	110	90	50	30	25	50	75	100	100		
Volume (ml)	1	0.5	0.1	0.1	0.1	0.1	0.5	0.5	0.5		
Average Time (sec)	1,292E+01	1,079E+01	7,642E+00	1,645E+01	1,817E+01	6,918E+00	1,729E+01	1,003E+01	1,650E+01		
Flow rate (ml/s)	7.091E-02	4.245E-02	1.199E-02	5.568E-03	4.880E-03	1.281E-02	2.564E-02	4.417E-02	2.523E-02		
Flux (cm3/cm2.s)	7.370E-03	4.412E-03	1.246E-03	5.787E-04	5.072E-04	1.332E-03	2.665E-03	4.591E-03	2.822E-03		
Permeability (cm ³ .cm/cm ² .s.cmHg)	2.007E-07	1.469E-07	7.466E-08	5.779E-08	6.078E-08	7.979E-08	1.064E-07	1.375E-07	1.049E+01		
Permeability (barrer)	2007.25	1468.58	746.62	577.94	607.79	797.92	1064.46	1375.48	1049.01		
45°C		55°C					75°C				
Gas Pressure (psi)	25	50	100	75	50	25	25	50	75	100	
Volume (ml)	0.1	0.5	0.5	0.5	0.5	0.1	0.1	0.5	0.5	0.5	
Average Time (sec)	1,437E+01	3,364E+01	1,025E+01	1,640E+01	3,144E+01	1,403E+01	1,232E+01	2,725E+01	1,650E+01	1,049E+01	
Flow rate (ml/s)	5.973E-03	1,276E-02	4.187E-02	2.617E-02	1.365E-02	6.122E-03	6.757E-03	1.528E-02	2.523E-02	3.966E-02	
Flux (cm3/cm2.s)	6.208E-04	1.326E-03	4.352E-03	2.720E-03	1.419E-03	6.363E-04	7.023E-04	1.588E-03	2.822E-03	4.122E-03	
Permeability (cm ³ .cm/cm ² .s.cmHg)	7.440E-08	7.947E-08	1.304E-07	1.087E-07	8.502E-08	7.625E-08	8.416E-08	9.513E-08	1.047E-07	1.235E-07	
Permeability (barrer)	743.98	794.70	1303.66	1086.63	850.22	762.46	841.64	951.28	1047.34	1235.03	
65°C		75°C					100				
Gas Pressure (psi)	25	50	100	25	50	75	100	100	100		
Volume (ml)	0.1	0.5	1	0.1	0.5	0.5	1	1	1		
Average Time (sec)	1,099E+01	2,337E+01	2,142E+01	9,942E+00	2,418E+01	1,478E+01	2,169E+01	2,169E+01	2,169E+01		
Flow rate (ml/s)	7.352E-03	1,728E-02	3,771E-02	7.892E-03	2.068E-02	2.654E-02	3.618E-02	3.618E-02	3.618E-02		
Flux (cm3/cm2.s)	7.642E-04	1.796E-03	3.920E-03	8.203E-04	2.149E-03	2.759E-03	3.761E-03	3.761E-03	3.761E-03		
Permeability (cm ³ .cm/cm ² .s.cmHg)	9.158E-08	1.076E-07	1.174E-07	9.829E-08	1.288E-07	1.102E-07	1.127E-07	1.127E-07	1.127E-07		
Permeability (barrer)	915.75	1076.28	1174.26	982.94	1287.76	1102.07	1126.59	1126.59	1126.59		

Pressure Temperature (°C)	1000/T (K)	P	25	50	75	100
25	3.354016435	562.16	P	P	P	P
35	3.245172805	607.79	764.66	1136.54	1700.74	7.4388
45	3.14317146	743.98	797.92	1064.46	1375.48	7.2266
55	3.047368686	841.64	794.70	1106.30	1303.66	7.1729
65	2.957267485	915.75	951.28	1047.34	1235.03	7.1188
75	2.872325147	982.94	1076.28	1131.34	1174.26	7.0684
45	3.14317146	762.46	1287.76	1102.07	1126.59	7.0270
25	3.354016435	486.33	841.64	951.28	1047.34	6.9540
			788.77	1181.25	1720.23	7.4502

Pressure	Slope	Intercept	Po	Ep (KJ/mol.K)
25	-1.369384663	10.87711199	52950.45767	11.38506409
50	-0.371314385	9.850126379	18960.7509	8.075507795
75	0.079585373	6.742259669	847.4735835	-0.661672788
100	0.852554923	4.505438242	90.50799973	-7.088141626

Pressure	ln(P)	25	50	75	100
25	6.3318	1.39	1.47	1.71	1.89
35	6.4098	1.43	1.41	1.50	1.42
45	6.6120	1.13	0.98	1.19	1.16
55	6.7354	1.46	1.43	1.38	1.44
65	6.8197	1.53	1.52	1.48	1.48
75	6.8905	1.59	1.88	1.55	1.55
85	6.6366				
95	6.1889				

$\ln P = \ln P_0 + (-E_p/R) \cdot (1/T)$

7-May-02 Cell 1		0.01549286 cm									
Ethane		200	200	200	200	200	200	200	200	200	200
Gas	Pressure (psi)	200	0.2	0.2	0.2	0.2	0.2	0.2	0.2	0.2	200
	Volume (ml)	0.2	0.2	0.2	0.2	0.2	0.2	0.2	0.2	0.2	200
	Duration	15	45	75	105	150	180	2470	2625	2925	3220
	hr	0.250	0.750	1.250	1.750	19.833	30.333	41.167	43.750	48.750	53.667
	Average Time (sec)	1.810E+01	1.832E+01	1.824E+01	1.774E+01	2.098E+01	2.175E+01	2.168E+01	2.159E+01	2.163E+01	2.214E+01
	Flow rate (ml/s)	1.019E-02	1.007E-02	1.011E-02	1.040E-02	8.795E-03	8.481E-03	8.509E-03	8.543E-03	8.530E-03	8.331E-03
	Flux (cm ³ /cm ² .s)	1.059E-03	1.047E-03	1.051E-03	1.081E-03	9.141E-04	8.815E-04	8.844E-04	8.880E-04	8.866E-04	8.659E-04
	Permeability										
	(cm ³ .cm/cm ² .s.cmHg)	1.587E-08	1.568E-08	1.575E-08	1.619E-08	1.369E-08	1.320E-08	1.325E-08	1.330E-08	1.328E-08	1.297E-08
	Permeability (barrer)	158.69	156.81	157.47	161.92	136.92	132.04	132.47	133.01	132.81	129.71
25C											
Gas	Pressure (psi)	25	50	75	100	125	150	175	200	200	100
	Volume (ml)	0.01	0.05	0.05	0.05	0.1	0.1	0.1	0.1	0.1	125
	Average Time (sec)	1.136E+01	2.942E+01	1.685E+01	1.243E+01	1.676E+01	1.313E+01	1.080E+01	8.972E+00	1.140E+01	8.745E+00
	Flow rate (ml/s)	8.068E-04	1.557E-03	2.719E-03	3.687E-03	5.466E-03	6.976E-03	8.487E-03	1.021E-02	7.011E-03	5.238E-03
	Flux (cm ³ /cm ² .s)	8.386E-05	1.618E-04	2.826E-04	3.832E-04	5.681E-04	7.250E-04	8.821E-04	1.061E-03	7.287E-04	5.444E-04
	Permeability										
	(cm ³ .cm/cm ² .s.cmHg)	1.005E-08	9.695E-09	1.129E-08	1.148E-08	1.362E-08	1.448E-08	1.510E-08	1.590E-08	1.455E-08	1.305E-08
	Permeability (barrer)	100.49	96.95	112.87	114.80	136.15	144.81	151.01	158.98	145.55	130.48
35C											
Gas	Pressure (psi)	25	50	75	100	25	50	75	100	25	50
	Volume (ml)	0.05	0.05	0.05	0.1	0.05	0.05	0.05	0.1	0.05	75
	Average Time (sec)	4.645E+01	1.970E+01	1.205E+01	1.791E+01	3.497E+01	1.456E+01	9.643E+00	1.397E+01	2.489E+01	7.818E+00
	Flow rate (ml/s)	9.543E-04	2.249E-03	3.679E-03	4.950E-03	1.228E-03	2.948E-03	4.452E-03	6.147E-03	1.672E-03	5.323E-03
	Flux (cm ³ /cm ² .s)	9.918E-05	2.338E-04	3.824E-04	5.145E-04	1.276E-04	3.064E-04	4.627E-04	6.389E-04	1.738E-04	5.533E-04
	Permeability										
	(cm ³ .cm/cm ² .s.cmHg)	1.189E-08	1.401E-08	1.527E-08	1.541E-08	1.529E-08	1.836E-08	1.848E-08	1.914E-08	2.083E-08	2.210E-08
	Permeability (barrer)	118.86	140.08	152.75	154.73	152.90	183.59	184.82	191.41	208.30	221.01
55C											
Gas	Pressure (psi)	25	50	75	100	25	50	75	100	25	50
	Volume (ml)	0.05	0.05	0.05	0.1	0.05	0.05	0.05	0.1	0.05	75
	Average Time (sec)	1.950E+01	1.012E+01	6.693E+00	9.632E+00	1.535E+01	8.708E+00	1.149E+01	8.643E+00	1.854E+01	2.808E+01
	Flow rate (ml/s)	2.071E-03	3.990E-03	6.034E-03	8.387E-03	2.555E-03	4.505E-03	6.830E-03	9.077E-03	2.116E-03	1.632E-03
	Flux (cm ³ /cm ² .s)	2.153E-04	4.147E-04	6.272E-04	8.717E-04	2.656E-04	4.682E-04	7.099E-04	9.435E-04	2.199E-04	1.696E-04
	Permeability										
	(cm ³ .cm/cm ² .s.cmHg)	2.580E-08	2.485E-08	2.505E-08	2.611E-08	3.182E-08	2.805E-08	2.836E-08	2.826E-08	2.635E-08	1.016E-08
	Permeability (barrer)	257.95	248.46	250.52	261.14	318.24	280.54	283.58	282.65	263.54	101.61
65C											
Gas	Pressure (psi)	25	50	75	100	25	50	75	100	25	50
	Volume (ml)	0.05	0.05	0.05	0.1	0.05	0.05	0.1	0.1	0.05	75
	Average Time (sec)	1.950E+01	1.012E+01	6.693E+00	9.632E+00	1.535E+01	8.708E+00	1.149E+01	8.643E+00	1.854E+01	2.808E+01
	Flow rate (ml/s)	2.071E-03	3.990E-03	6.034E-03	8.387E-03	2.555E-03	4.505E-03	6.830E-03	9.077E-03	2.116E-03	1.632E-03
	Flux (cm ³ /cm ² .s)	2.153E-04	4.147E-04	6.272E-04	8.717E-04	2.656E-04	4.682E-04	7.099E-04	9.435E-04	2.199E-04	1.696E-04
	Permeability										
	(cm ³ .cm/cm ² .s.cmHg)	2.580E-08	2.485E-08	2.505E-08	2.611E-08	3.182E-08	2.805E-08	2.836E-08	2.826E-08	2.635E-08	1.016E-08
	Permeability (barrer)	257.95	248.46	250.52	261.14	318.24	280.54	283.58	282.65	263.54	101.61
75C											
Gas	Pressure (psi)	25	50	75	100	25	50	75	100	25	50
	Volume (ml)	0.05	0.05	0.05	0.1	0.05	0.05	0.1	0.1	0.05	75
	Average Time (sec)	1.950E+01	1.012E+01	6.693E+00	9.632E+00	1.535E+01	8.708E+00	1.149E+01	8.643E+00	1.854E+01	2.808E+01
	Flow rate (ml/s)	2.071E-03	3.990E-03	6.034E-03	8.387E-03	2.555E-03	4.505E-03	6.830E-03	9.077E-03	2.116E-03	1.632E-03
	Flux (cm ³ /cm ² .s)	2.153E-04	4.147E-04	6.272E-04	8.717E-04	2.656E-04	4.682E-04	7.099E-04	9.435E-04	2.199E-04	1.696E-04
	Permeability										
	(cm ³ .cm/cm ² .s.cmHg)	2.580E-08	2.485E-08	2.505E-08	2.611E-08	3.182E-08	2.805E-08	2.836E-08	2.826E-08	2.635E-08	1.016E-08
	Permeability (barrer)	257.95	248.46	250.52	261.14	318.24	280.54	283.58	282.65	263.54	101.61

25C		125	150	175	200
Gas Pressure (psi)		0.1	0.1	0.1	0.1
Volume (ml)		1.865E+01	1.480E+01	1.202E+01	9.593E+00
Average Time (sec)		4.914E-03	6.190E-03	7.622E-03	9.550E-03
Flow rate (ml/s)		5.107E-04	6.434E-04	7.922E-04	9.926E-04
Flux (cm ³ /cm ² .s)		1.224E-08	1.285E-08	1.356E-08	1.487E-08
Permeability (cm ³ .cm/cm ² .s.cmHg)		122.40	128.50	135.62	148.68
Permeability (barre)					

Pressure Temperature (°C)	1000/T (K)	P	25	P	50	P	75	P	100
25	3.354016435	1.005E+02	9.695E+01	1.129E+02	1.148E+02	1.148E+02	1.148E+02	1.148E+02	1.148E+02
35	3.245172805	1.189E+02	1.401E+02	1.527E+02	1.541E+02	1.541E+02	1.541E+02	1.541E+02	1.541E+02
45	3.14317146	1.529E+02	1.836E+02	1.848E+02	1.914E+02	1.914E+02	1.914E+02	1.914E+02	1.914E+02
55	3.047386866	2.083E+02	2.180E+02	2.210E+02	2.197E+02	2.197E+02	2.197E+02	2.197E+02	2.197E+02
65	2.957267485	2.580E+02	2.485E+02	2.505E+02	2.611E+02	2.611E+02	2.611E+02	2.611E+02	2.611E+02
75	2.872325147	318.24	280.54	283.58	282.65	282.65	282.65	282.65	282.65
25	3.354016435	8.547E+01	1.016E+02	1.036E+02	1.162E+02	1.162E+02	1.162E+02	1.162E+02	1.162E+02
75	2.872325147	2.635E+02							

Pressure	ln(P)	25	50	75	100
25	4.6101	4.6101	4.5742	4.7262	4.7432
35	4.7779	4.7779	4.9422	5.0288	5.0378
45	5.0298	5.0298	5.2127	5.2194	5.2544
55	5.3390	5.3390	5.3843	5.3982	5.3922
65	5.5528	5.5528	5.5153	5.5236	5.5651
75	5.7628	5.7628	5.6367	5.6475	5.6442
25	4.4481	4.4481	4.6211	4.6402	4.7553

Pressure	Slope	Intercept	Po	Ep (KJ/mol.K)
25	-2.59334189	12.9844617	435592.16	21.56
50	-2.20511352	9.83360473	18650.06	18.33
75	-2.0186716	9.86546732	19253.87	16.78
100	-1.91063106	9.6717055	15862.38	15.88

$\ln P = \ln P_o + (E_p/R) \cdot (1/T)$

15-May-02 Cell 1		0.01549286 cm												
Ethylene		25°C				35°C				55°C				
Gas		200	25	50	75	100	125	150	175	200	250	50	75	100
Pressure (psi)		2.00	0.05	0.05	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.05	0.1	0.1
Volume (ml)		8.547E+00	4.374E+01	2.127E+01	1.877E+01	1.877E+01	1.442E+01	1.165E+01	9.739E+00	7.957E+00	1.982E+01	0.05	0.05	0.1
Average Time (sec)		1.072E-02	1.047E-03	2.154E-03	3.483E-03	4.635E-03	6.353E-03	7.867E-03	9.412E-03	1.151E-02	2.311E-03	1.291E-03	6.865E+00	1.545E+01
Flow rate (ml/s)		1.114E-03	1.089E-04	2.238E-04	3.620E-04	4.817E-04	6.603E-04	8.177E-04	9.793E-04	1.197E-03	2.402E-04	1.342E-04	2.868E-03	4.477E-03
Flux (cm3/cm2.s)		1.669E-08	1.304E-08	1.341E-08	1.446E-08	1.443E-08	1.582E-08	1.633E-08	1.675E-08	1.793E-08	1.439E-08	1.608E-08	1.786E-08	1.859E-08
Permeability	(cm ³ .cm/cm ² .s.cmHg)	166.89	130.44	134.12	144.60	144.32	158.25	163.32	167.48	179.27	143.92	160.82	178.63	188.87
Permeability (barrier)		1.29806044	1.3833255	1.28112526	1.25716695	1.25716695	1.16225587	1.12780879	1.10907534	1.12756598	0.98881695			
Selectivity (Ethylene/Ethane)														
Gas		45°C				55°C				75°C				
Pressure (psi)		25	50	75	100	100	50	75	100	100	50	25	50	75
Volume (ml)		0.05	0.05	0.1	0.1	0.05	0.05	0.1	0.1	0.1	0.05	0.05	0.05	0.1
Average Time (sec)		2.539E+01	1.133E+01	1.502E+01	1.134E+01	1.807E+01	9.322E+00	1.188E+01	8.858E+00	9.017E+00	1.712E+01	1.291E-03	2.868E-03	4.477E-03
Flow rate (ml/s)		1.691E-03	3.789E-03	5.716E-03	7.569E-03	2.303E-03	4.465E-03	7.023E-03	9.397E-03	4.616E-03	2.431E-03	1.291E-03	2.868E-03	4.477E-03
Flux (cm3/cm2.s)		1.757E-04	3.939E-04	5.941E-04	7.867E-04	2.394E-04	4.641E-04	7.300E-04	9.767E-04	4.798E-04	2.527E-04	1.342E-04	2.868E-03	4.477E-03
Permeability		2.106E-08	2.360E-08	2.373E-08	2.357E-08	2.868E-08	2.781E-08	2.916E-08	2.926E-08	2.875E-08	3.028E-08	1.608E-08	1.786E-08	1.859E-08
Permeability (barrier)		210.60	235.99	237.32	235.68	286.85	278.05	291.59	292.60	287.46	302.76			
Gas		65°C				75°C				95°C				
Pressure (psi)		25	50	75	100	100	50	75	100	100	50	25	50	75
Volume (ml)		0.05	0.1	0.1	0.5	0.1	0.1	0.5	0.5	0.5	0.1	0.05	0.05	0.1
Average Time (sec)		1.567E+01	1.542E+01	1.010E+01	3.938E+01	2.563E+01	1.357E+01	4.148E+01	3.074E+01	3.074E+01	1.712E+01	1.291E-03	2.868E-03	4.477E-03
Flow rate (ml/s)		2.578E-03	5.240E-03	7.998E-03	1.026E-02	3.061E-03	5.783E-03	9.457E-03	1.276E-02	1.276E-02	2.431E-03	1.291E-03	2.868E-03	4.477E-03
Flux (cm3/cm2.s)		2.679E-04	5.447E-04	8.313E-04	1.066E-03	3.182E-04	6.011E-04	9.830E-04	1.326E-03	1.326E-03	2.527E-04	1.342E-04	2.868E-03	4.477E-03
Permeability		3.211E-08	3.263E-08	3.320E-08	3.194E-08	3.812E-08	3.601E-08	3.926E-08	3.974E-08	3.974E-08	3.028E-08	1.608E-08	1.786E-08	1.859E-08
Permeability (barrier)		321.06	326.34	332.05	319.36	381.25	360.15	392.64	397.39	397.39	302.76			

APPENDIX E. RAW DATA

21-May-02 Cell 1		0.015492857 cm											
Nitrogen		25°C			35°C			45°C			65°C		
Gas	Pressure (psi)	25	50	75	100	25	50	75	100	25	50	75	100
Volume (ml)		0.01	0.01	0.01	0.01	0.01	0.01	0.01	0.01	0.01	0.01	0.01	0.01
Average Time (sec)		9.379E+01	5.216E+01	3.391E+01	2.777E+01	6.279E+01	3.229E+01	2.486E+01	1.994E+01	4.684E+01	2.617E+01	1.443E+01	1.316E+01
Flow rate (ml/s)		9.768E-05	1.917E-04	2.949E-04	3.601E-04	1.413E-04	2.745E-04	3.565E-04	4.445E-04	1.833E-04	3.280E-04	5.949E-04	6.524E-04
Flux (cm ³ /cm ² .s)		1.015E-05	1.993E-05	3.065E-05	3.743E-05	1.469E-05	2.853E-05	3.706E-05	4.620E-05	1.905E-05	3.410E-05	6.183E-05	6.781E-05
Permeability (cm ³ .cm/cm ² .s.cmHg)		1.217E-09	1.194E-09	1.224E-09	1.121E-09	1.760E-09	1.710E-09	1.480E-09	1.384E-09	2.283E-09	2.043E-09	2.470E-09	2.031E-09
Permeability (barrier)		12.17	11.94	12.24	11.21	17.60	17.10	14.80	13.84	22.83	20.43	24.70	20.31
45C													
Gas	Pressure (psi)	50	75	100	25	50	75	100	25	50	75	100	25
Volume (ml)		0.01	0.01	0.01	0.01	0.01	0.01	0.01	0.01	0.01	0.01	0.01	0.01
Average Time (sec)		2.547E+01	1.945E+01	1.341E+01	3.007E+01	1.862E+01	1.297E+01	9.542E+00	2.465E+01	1.241E+01	4.673E+01	3.510E+01	3.510E+01
Flow rate (ml/s)		3.370E-04	4.414E-04	6.403E-04	2.768E-04	4.471E-04	6.419E-04	8.724E-04	3.277E-04	6.510E-04	8.642E-04	1.151E-03	1.151E-03
Flux (cm ³ /cm ² .s)		3.503E-05	4.588E-05	6.655E-05	2.877E-05	4.647E-05	6.672E-05	9.067E-05	3.406E-05	6.766E-05	8.983E-05	1.196E-04	1.196E-04
Permeability (cm ³ .cm/cm ² .s.cmHg)		2.099E-09	1.832E-09	1.994E-09	3.448E-09	2.784E-09	2.665E-09	2.716E-09	4.082E-09	4.054E-09	3.588E-09	3.583E-09	3.583E-09
Permeability (barrier)		20.99	18.32	19.94	34.48	27.84	26.65	27.16	40.82	40.54	35.88	35.83	35.83
75C													
Gas	Pressure (psi)	25	50	75	100	25	50	75	100	25	50	75	100
Volume (ml)		0.02	0.05	0.05	0.05	0.05	0.05	0.05	0.05	0.05	0.05	0.05	0.05
Average Time (sec)		4.386E+01	5.105E+01	3.801E+01	2.887E+01	3.801E+01	2.887E+01	3.801E+01	2.887E+01	3.801E+01	2.887E+01	3.801E+01	2.887E+01
Flow rate (ml/s)		3.578E-04	7.684E-04	1.032E-03	1.359E-03	1.032E-03	7.684E-04	1.032E-03	1.359E-03	1.032E-03	7.684E-04	1.032E-03	1.359E-03
Flux (cm ³ /cm ² .s)		3.719E-05	7.987E-05	1.073E-04	1.412E-04	1.073E-04	7.987E-05	1.073E-04	1.412E-04	1.073E-04	7.987E-05	1.073E-04	1.412E-04
Permeability (cm ³ .cm/cm ² .s.cmHg)		4.456E-09	4.786E-09	4.285E-09	4.231E-09	4.285E-09	4.456E-09	4.786E-09	4.231E-09	4.285E-09	4.456E-09	4.786E-09	4.231E-09
Permeability (barrier)		44.56	47.86	42.85	42.31	42.85	44.56	47.86	42.31	42.85	44.56	47.86	42.31
Temperature (°C)													
Pressure	1000/T (K)	25	50	75	100	25	50	75	100	25	50	75	100
Temperature (°C)		3.354016435	1.217E+01	1.194E+01	1.224E+01	1.121E+01	1.121E+01	1.121E+01	1.121E+01	1.121E+01	1.121E+01	1.121E+01	1.121E+01
Pressure	P	3.245172805	1.760E+01	1.710E+01	1.480E+01	1.384E+01	1.384E+01	1.384E+01	1.384E+01	1.384E+01	1.384E+01	1.384E+01	1.384E+01
Temperature (°C)	P	3.143171146	2.283E+01	2.043E+01	2.470E+01	2.031E+01	2.031E+01	2.031E+01	2.031E+01	2.031E+01	2.031E+01	2.031E+01	2.031E+01
Pressure	P	3.047386866	3.448E+01	2.784E+01	2.665E+01	2.716E+01	2.716E+01	2.716E+01	2.716E+01	2.716E+01	2.716E+01	2.716E+01	2.716E+01
Temperature (°C)	P	2.957267485	4.082E+01	4.054E+01	3.588E+01	3.588E+01	3.588E+01	3.588E+01	3.588E+01	3.588E+01	3.588E+01	3.588E+01	3.588E+01
Pressure	P	2.872325147	4.456E+01	4.786E+01	4.285E+01	4.231E+01	4.231E+01	4.231E+01	4.231E+01	4.231E+01	4.231E+01	4.231E+01	4.231E+01
Slope													
Pressure	Intercept	25	50	75	100	25	50	75	100	25	50	75	100
Pressure	Po	-2.814634019	11.99125626	161337.91	23.40	-2.918174106	12.26120823	211336.77	24.26	-2.676818599	11.47798328	96566.12	22.26
Pressure	Po	-2.918174106	12.26120823	211336.77	24.26	-2.676818599	11.47798328	96566.12	22.26	-2.906303299	12.13251938	185817.33	24.16
Pressure	Po	-2.676818599	11.47798328	96566.12	22.26	-2.906303299	12.13251938	185817.33	24.16				

ln P = ln Po + (-Ep/R)*(1/T)

22-May-02 Cell 1		0.015492857 cm									
CO2											
Gas		50	50	50	50	50	50	50	50	50	50
Pressure (psi)		0.01	0.01	0.01	0.05	0.05	0.1	0.1	0.1	0.1	0.1
Volume (ml)		10	40	310	235	310	1430	1820	2995	2995	5010
Duration		0.167	0.667	3.917	3.917	5.167	23.833	49.917	49.917	83.500	83.500
Average Time (sec)		1.069E+01	7.903E+00	1.927E+01	1.458E+01	1.458E+01	2.481E+01	2.079E+01	2.385E+01	2.385E+01	1.955E+01
Flow rate (ml/s)		8.625E-04	1.167E-03	2.393E-03	3.164E-03	3.164E-03	4.437E-03	4.437E-03	3.868E-03	3.868E-03	4.719E-03
Flux (cm3/cm2.s)		8.965E-05	1.213E-04	2.487E-04	3.289E-04	3.289E-04	3.865E-04	4.612E-04	4.020E-04	4.020E-04	4.905E-04
Permeability											
(cm ³ .cm/cm ² .s.cmHg)		5.372E-09	7.268E-09	1.490E-08	1.970E-08	1.970E-08	2.387E-08	2.849E-08	2.849E-08	2.849E-08	3.030E-08
Permeability (barrer)		53.7152	72.6775	149.0257	197.0480	197.0480	238.7099	284.8519	284.8519	284.8519	302.9725
Gas		35°C									
Pressure (psi)		25	45	15	35	35	25	25	45	25	45
Volume (ml)		0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1
Average Time (sec)		3.949E+01	2.009E+01	2.686E+01	5.896E+01	5.896E+01	3.203E+01	3.203E+01	1.605E+01	2.602E+01	1.462E+01
Flow rate (ml/s)		2.320E-03	4.560E-03	3.411E-03	1.554E-03	1.554E-03	2.767E-03	2.767E-03	5.522E-03	3.300E-03	5.874E-03
Flux (cm3/cm2.s)		2.411E-04	4.739E-04	3.546E-04	1.615E-04	1.615E-04	2.876E-04	2.876E-04	5.739E-04	3.430E-04	6.105E-04
Permeability											
(cm ³ .cm/cm ² .s.cmHg)		2.890E-08	3.155E-08	3.035E-08	3.226E-08	3.226E-08	3.447E-08	3.447E-08	3.821E-08	4.110E-08	4.064E-08
Permeability (barrer)		288.9673	315.5215	303.4851	322.5678	322.5678	344.6936	344.6936	382.0783	410.9728	406.4429
Gas		75°C									
Pressure (psi)		25	45	45	25	25	25	25	45	25	45
Volume (ml)		0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1
Average Time (sec)		2.156E+01	1.238E+01	1.947E+01	1.086E+01	1.086E+01	1.690E+01	1.690E+01	9.412E+00	9.412E+00	9.412E+00
Flow rate (ml/s)		3.861E-03	6.724E-03	4.149E-03	7.442E-03	7.442E-03	4.643E-03	4.643E-03	8.336E-03	8.336E-03	8.336E-03
Flux (cm3/cm2.s)		4.013E-04	6.988E-04	4.312E-04	7.735E-04	7.735E-04	4.826E-04	4.826E-04	8.664E-04	8.664E-04	8.664E-04
Permeability											
(cm ³ .cm/cm ² .s.cmHg)		4.809E-08	4.653E-08	5.167E-08	5.149E-08	5.149E-08	5.783E-08	5.783E-08	5.768E-08	5.768E-08	5.768E-08
Permeability (barrer)		480.9110	465.2504	516.7458	514.9210	514.9210	578.3422	578.3422	576.8287	576.8287	576.8287
Pressure		25 psi									
Temperature (°C)		25	25	45	45	45	25	25	45	25	45
1000/T (K)		3.354016435	2.890E+02	3.155E+02	3.155E+02	3.155E+02	5.6663	5.6663	5.7542	5.6663	5.7542
P		3.245172805	3.447E+02	3.821E+02	3.821E+02	3.821E+02	5.8427	5.8427	5.9456	5.8427	5.9456
Po		3.14317146	4.110E+02	4.064E+02	4.064E+02	4.064E+02	6.0185	6.0185	6.0074	6.0185	6.0074
Intercept		3.047388666	4.809E+02	4.653E+02	4.653E+02	4.653E+02	6.1757	6.1757	6.1426	6.1757	6.1426
Slope		2.957267485	516.7458	514.9210	514.9210	514.9210	6.2476	6.2476	6.2440	6.2476	6.2440
Ep (KJ/mol.K)		2.872325147	578.3422	576.8287	576.8287	576.8287	6.3602	6.3602	6.3575	6.3602	6.3575
Pressure		25 psi									
Temperature (°C)		25	25	45	45	45	25	25	45	25	45
Slope		-1.44344951	10.53116212	37464.98807	37464.98807	37464.98807	12.00083923	12.00083923	12.00083923	12.00083923	12.00083923
Intercept		-1.202087532	9.805584517	18134.73641	18134.73641	18134.73641	9.994155743	9.994155743	9.994155743	9.994155743	9.994155743
Ep (KJ/mol.K)											

In P = ln Po + (-Ep/R)*(1/T)